

# Common Mode Board Simulation

Simulation of the mode cleaner board and the common mode board.

## Setup

```
In[*]:= Needs["Controls`LinearControl`"]
```

```
In[*]:= $TextStyle = {FontFamily -> "Helvetica", FontSize -> 13};
```

```
In[*]:= plotopt =
  Sequence @@ {GridLines -> Automatic, Frame -> True, FrameStyle -> Thickness[0.0025],
    PlotStyle -> {Darker[Green], Blue, Red}, BaseStyle -> {FontSize -> 13}};
```

```
In[*]:= plotoptn[n_Integer? (# > 0 & # < 8 &)] :=
  Sequence @@ {GridLines -> Automatic, Frame -> True, FrameStyle -> Thickness[0.0025],
    PlotStyle -> Take[{Gray, Orange, Purple, Brown, Darker[Green], Blue, Red}, -n],
    BaseStyle -> {FontSize -> 13}};
plotoptn[n_Integer? (# ≤ 0 ∨ # ≥ 8 &)] := plotopt
```

```
In[*]:= mylegend[labels_List, pos_ : Right] :=
  {Placed[LineLegend[labels, LabelStyle -> {FontSize -> 11}, LegendMargins -> 2,
    LegendFunction -> (Framed[#, Background -> White] &)], pos]}
```

## Free Running Laser Noise

```
In[*]:= npro[f_] :=  $\frac{1 \cdot 10^4}{f}$  (*Hz/√Hz*)
```

## Import

```
In[*]:= path = NotebookDirectory[] <> "/MCbaseline/";
mcbaseline = ReadList[path <> "MC_BASELINE.TXT", {Number, Number}];
cmbaseline = ReadList[path <> "CM_BASELINE.TXT", {Number, Number}];
mcslewbaseline = ReadList[path <> "MCSLEW_BASELINE.TXT", {Number, Number}];
cmslewbaseline = ReadList[path <> "CMSLEW_BASELINE.TXT", {Number, Number}];
```

## Equations

### Parallel and Serial Impedance

```

In[*]:= par[r1_, r2_] :=  $\frac{1}{\frac{1}{r1} + \frac{1}{r2}}$ 

par[r1_, r2_, r3_] :=  $\frac{1}{\frac{1}{r1} + \frac{1}{r2} + \frac{1}{r3}}$ 

par[r1_, r2_, r3_, r4_] :=  $\frac{1}{\frac{1}{r1} + \frac{1}{r2} + \frac{1}{r3} + \text{Plus}@@\left(\frac{1}{\text{List}[r4]}\right)}$ 

ser[r1_, r2_] := r1 + r2
ser[r1_, r2_, r3_] := r1 + r2 + r3
ser[r1_, r2_, r3_, r4_] := r1 + r2 + r3 + Plus@@List[r4]

```

### Pole/zero

```

In[*]:= pole[s_, s0_] :=  $\frac{1}{1 + \frac{s}{s0}}$ 

zero[s_, s0_] :=  $1 + \frac{s}{s0}$ 

pole[s_, s0_, Q_] :=  $\frac{1}{1 + \frac{1}{Q} \frac{s}{s0} + (s / s0)^2}$ 

zero[s_, s0_, Q_] :=  $1 + \frac{1}{Q} \frac{s}{s0} + (s / s0)^2$ 

```

### Transfer Function of an OpAmp

This function computes the transfer function of an idealized OpAmp circuit

g: +1 for non-inverting configuration or -1 for inverting configuration, 0 for differential configuration

z2: Impedance in feedback path [Ohm]

z1: Impedance of input path (inverting) or impedance to ground (non-inverting) [Ohm]

```

In[*]:= OpAmp[g_, z1_, z2_] :=
  Which[g > 0, 1 +  $\frac{z2}{z1}$ , g < 0,  $\frac{z2}{z1}$ , True,  $\frac{z2}{z1}$ ]

```

### Noise of an OpAmp

This function computes the equivalent input noise of an OpAmp circuit

g: +1 for non-inverting configuration or -1 for inverting configuration, 0 for differential configuration

z1: Impedance of input path (inverting) or impedance to ground (non-inverting) [Ohm]

z2: Impedance over feedback path [Ohm]

en: voltage noise [Volt]

in: current noise [Ampere]

```
In[*]:= FourKT = 1.62*^-20; (* V^2/Hz/Ohm; room temperature 20C*)
OpAmpNoise[g_, z1_, z2_, en_, in_] :=
  Which[g > 0, If[z1 == Infinity,  $\sqrt{en^2 + FourKT Abs[z2] + (in Abs[z2])^2}$ ,
     $\sqrt{en^2 + FourKT Abs[par[z1, z2]] + (in Abs[par[z1, z2]])^2}$ ],
  g < 0,  $\sqrt{\left(Abs\left[1 + \frac{z1}{z2}\right]^2 en^2 + Abs[z1]^2 \left(in^2 + Abs\left[\frac{FourKT}{z1}\right] + Abs\left[\frac{FourKT}{z2}\right]\right)\right)}$ ,
  True,  $\sqrt{\left(Abs\left[1 + \frac{z1}{z2}\right]^2 en^2 + 2 Abs[z1]^2 \left(in^2 + Abs\left[\frac{FourKT}{z1}\right] + Abs\left[\frac{FourKT}{z2}\right]\right)\right)}$ ]
```

Flicker Noise: The variable \$Flicker determines if flicker noise is added or not. It can also be explicitly specified with the option Flicker.

```
In[*]:= $Flicker = True;
Clear[OpAmpNoiseFlicker];
Options[OpAmpNoiseFlicker] = {Flicker -> $Flicker};
OpAmpNoiseFlicker[f_, fknee_, opts___] :=
  If[Flicker /. {opts} /. Options[OpAmpNoiseFlicker],  $\sqrt{\frac{fknee}{f} + 1}$ , 1]
OpAmpNoiseFlicker[f_, fknee_, floor_, opts___] := floor OpAmpNoiseFlicker[f, fknee, opts]
```

## OpAmp Parameters

```

In[*]:= Clear[AD829, OP27]
AD829[f_] := {s → 2 π i f, en → enAD829, in → inAD829,
  enfloor → enfloorAD829, infloor → infloorAD829} //.
{enAD829 → OpAmpNoiseFlicker[f, ekneeAD829, enfloorAD829],
 inAD829 → OpAmpNoiseFlicker[f, ikneeAD829, infloorAD829],
 ekneeAD829 → 50, ikneeAD829 → 100, (*guess*)
 enfloorAD829 → 1.7*^-9, infloorAD829 → 1.5*^-12};
OP27[f_] := {s → 2 π i f, en → enOP27, in → inOP27,
  enfloor → enfloorOP27, infloor → infloorOP27} //.
{enOP27 → OpAmpNoiseFlicker[f, ekneeOP27, enfloorOP27],
 inOP27 → OpAmpNoiseFlicker[f, ikneeOP27, infloorOP27],
 ekneeOP27 → 2.7, ikneeOP27 → 140,
 enfloorOP27 → 3.0*^-9, infloorOP27 → 0.4*^-12};
LT1028[f_] := {s → 2 π i f, en → enLT1028, in → inLT1028,
  enfloor → enfloorLT1028, infloor → infloorLT1028} //.
{enLT1028 → OpAmpNoiseFlicker[f, ekneeLT1028, enfloorLT1028],
 inLT1028 → OpAmpNoiseFlicker[f, ikneeLT1028, infloorLT1028],
 ekneeLT1028 → 3.5, ikneeLT1028 → 250,
 enfloorLT1028 → 0.85*^-9, infloorLT1028 → 1*^-12};
LT1128[f_] := {s → 2 π i f, en → enLT1128, in → inLT1128,
  enfloor → enfloorLT1128, infloor → infloorLT1128} //.
{enLT1128 → OpAmpNoiseFlicker[f, ekneeLT1128, enfloorLT1128],
 inLT1128 → OpAmpNoiseFlicker[f, ikneeLT1128, infloorLT1128],
 ekneeLT1128 → 3.5, ikneeLT1128 → 250,
 enfloorLT1128 → 0.85*^-9, infloorLT1128 → 1*^-12};
AD797[f_] := {s → 2 π i f, en → enAD797, in → inAD797,
  enfloor → enfloorAD797, infloor → infloorAD797} //.
{enAD797 → OpAmpNoiseFlicker[f, ekneeAD797, enfloorAD797],
 inAD797 → OpAmpNoiseFlicker[f, ikneeAD797, infloorAD797],
 ekneeAD797 → 50, ikneeAD797 → 100, (*guess*)
 enfloorAD797 → 0.9*^-9, infloorAD797 → 2*^-12};
LT1012[f_] := {s → 2 π i f, en → enLT1012, in → inLT1012,
  enfloor → enfloorLT1012, infloor → infloorLT1012} //.
{enLT1012 → OpAmpNoiseFlicker[f, ekneeLT1012, enfloorLT1012],
 inLT1012 → OpAmpNoiseFlicker[f, ikneeLT1012, infloorLT1012],
 ekneeLT1012 → 2.5, ikneeLT1012 → 120, (*guess*)
 enfloorLT1012 → 14*^-9, infloorLT1012 → 6*^-15};
PA98A[f_] := {s → 2 π i f, en → enPA98A, in → inPA98A,
  enfloor → enfloorPA98A, infloor → infloorPA98A} //.
{enPA98A → OpAmpNoiseFlicker[f, ekneePA98A, enfloorPA98A],
 inPA98A → OpAmpNoiseFlicker[f, ikneePA98A, infloorPA98A],
 ekneePA98A → 100(*guess*), ikneePA98A → 120, (*guess*)
 enfloorPA98A → 4*^-9, infloorPA98A → 1*^-12 (*guess*)};

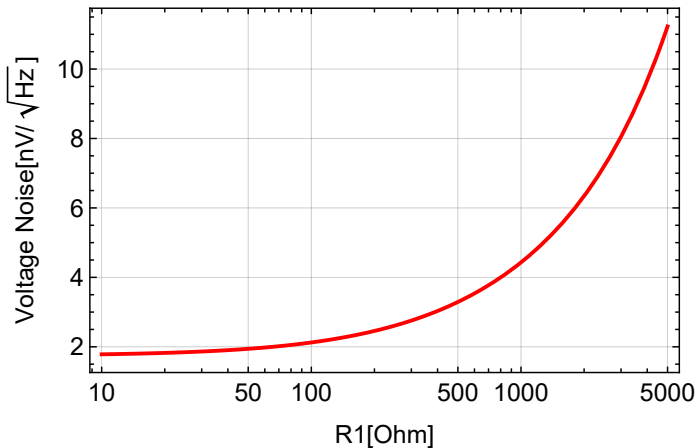
```

## Examples (AD829)

Non-Inverting configuration: input noise w/ gain of 10 as function of r1

```
In[ ]:= LogLinearPlot[1*^9 OpAmpNoise[+1, r, 9 r, en, in] /. AD829[1000],
  {r, 10, 5000}, FrameLabel -> {"R1[Ohm]", "Voltage Noise[nV/√Hz]"},
  Frame -> True, GridLines -> Automatic, Evaluate[plotopt] ]
```

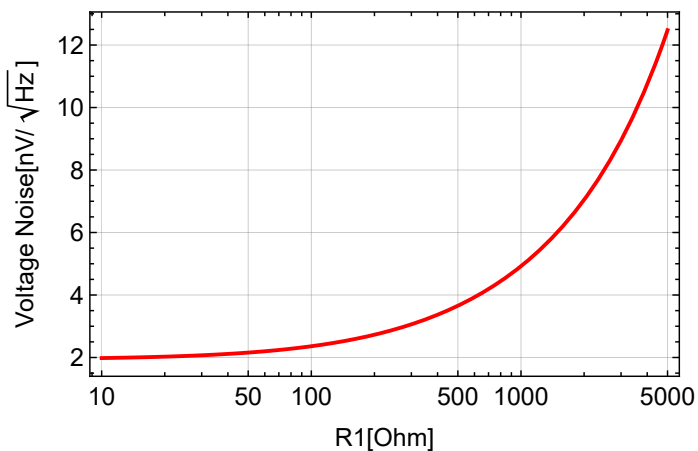
Out[ ]:=



Inverting configuration: input noise w/ gain of 10 as function of r1

```
In[ ]:= LogLinearPlot[1*^9 OpAmpNoise[-1, r, 9 r, en, in] /. AD829[1000],
  {r, 10, 5000}, FrameLabel -> {"R1[Ohm]", "Voltage Noise[nV/√Hz]"},
  Frame -> True, GridLines -> Automatic, Evaluate[plotopt] ]
```

Out[ ]:=



## Series Product of OpAmps

Computes the transfer function of several OpAmps circuits in series.

```
In[*]:= OpAmpProduct[t_, m_] := Product[t[[i]], {i, m}]
OpAmpProduct[t_List] := Product @@ t
```

Computes the equivalent input noise of several OpAmps circuits in series.

```
In[*]:= NoiseSum[prev_, {t_, n_}] :=  $\sqrt{\text{prev}^2 + n^2}$  Abs[t]
OpAmpNoiseProduct[t_, n_, m_] :=  $\frac{\text{Fold}[\text{NoiseSum}, \theta, \text{Table}[\{t[[i]], n[[i]]\}, \{i, m\}]]}{\text{Abs}[\text{OpAmpProduct}[t, m]]}$ 
OpAmpNoiseProduct[t_List, n_List] :=  $\frac{\text{Fold}[\text{NoiseSum}, \theta, \text{Transpose}[t, n]]}{\text{Abs}[\text{OpAmpProduct}[t]]}$ 
```

## Spectrum Math

Propagate noise spectrum

```
In[*]:= SpecProp[prev_, t_] := {#[[1]], Abs[t /. s -> 2.  $\pi$  #[[1]] #[[2]]} & /@ prev
SpecProp[noise_, t_List] := FoldList[SpecProp, noise, t]
SpecProp[noise_, t_, m_] := FoldList[SpecProp, noise, Table[t[[i]], {i, m}]]
```

RMS of spectrum

```
In[*]:= Clear[SpecRMS];
SpecRMS[l_List?(MatrixQ[#, NumberQ] &)] := Block[{i, sqr = 0},
  For[i = 1, i < Length[l], ++i,
    sqr += (l[[i + 1, 1]] - l[[i, 1]])  $\left(\frac{l[[i, 2]] + l[[i + 1, 2]]}{2}\right)^2$ ];
   $\sqrt{\text{sqr}}$ ]
```

Integrated RMS spectrum

```
In[*]:= Clear[RMSSpec];
RMSSpec[l_List?(MatrixQ[#, NumberQ] &), dir_ : (-1)] := Block[{i, sqr = 0, r = N[l]},
  If[dir  $\geq$  0,
    For[i = 2, i  $\leq$  Length[l], ++i,
      r[[i, 2]] =  $\sqrt{r[[i - 1, 2]]^2 + r[[i, 2]]^2 (r[[i, 1]] - r[[i - 1, 1]])}$ ],
    For[i = Length[l] - 2, i  $\geq$  1, --i,
      r[[i, 2]] =  $\sqrt{r[[i + 1, 2]]^2 + r[[i, 2]]^2 (r[[i + 1, 1]] - r[[i, 1]])}$ ];
  r]
```

## IFO Common Mode Transfer Functions & Noise

```
In[*]:= ugf = 20*^3;
```

### First Stage: Differential Input Amplifier

```
In[*]:= n = 1;
z1[n] = 2000.;
z2[n] = par[2000,  $\frac{1}{s 10*^{-12}}$ ];
opamp[n] = OpAmp[0, z1[n], z2[n]];
opampnoise[n] = OpAmpNoise[0, z1[n], z2[n], 1.7*^{-9}, 1.5*^{-12}];

In[*]:= {dB[opamp[1]], Phase[opamp[1]]} /. s -> 2 pi i ugf
BodePlotEx[opamp[1] /. s -> 2 pi i 1000 f, {f, 0.01, 10*^3}, XAxisLabel -> "kHz", plotopt];

Out[*]=
{-0.0000274323, -0.144}
```

### Second Stage: Gain Stage (+12dB)

```
In[*]:= n += 1;
z1[n] = Infinity;
z2[n] = 100.;
opamp[n] = 4 OpAmp[1, z1[n], z2[n]];
opampnoise[n] = OpAmpNoise[1, z1[n], z2[n], 1.7*^{-9}, 1.5*^{-12}];
```

### Third Stage: Summing Node

```
In[*]:= n += 1;
z1[n] = 2000.;
z2[n] = par[2000.,  $\frac{1}{s 10*^{-12}}$ ];
opamp[n] = OpAmp[-1, z1[n], z2[n]];
opampnoise[n] = OpAmpNoise[-1, z1[n], z2[n], 1.7*^{-9}, 1.5*^{-12}];
```

### Forth Stage: Pole/Zero Pair

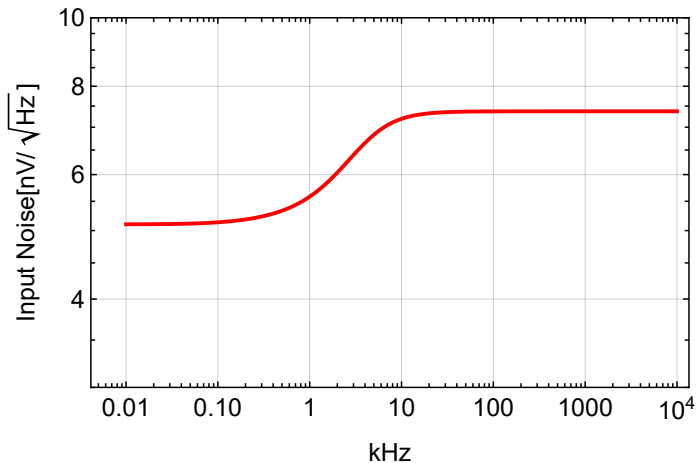
```
In[*]:= n += 1;
z1[n] = 1210.;
z2[n] = par[121.*^3, ser[1210.,  $\frac{1}{s 33*^{-9}}$ ]]];
opamp[n] = OpAmp[-1, z1[n], z2[n]];
opampnoise[n] = OpAmpNoise[-1, z1[n], z2[n], 1.7*^{-9}, 1.5*^{-12}];
```

```
In[*]:= {dB[opamp[4]], Phase[opamp[4]]} /. s -> 2 π i ugf
BodePlotEx[opamp[4] /. s -> 2 π i 1000 f, {f, 0.01, 10*^3}, XAxisLabel -> "kHz", plotopt];
```

```
Out[*]=
{0.0827091, -11.1579}
```

```
In[*]:= ListLogLogPlot[Table[{10i, 1*^9 opampnoise[4] /. s -> 2 π i 1000 × 10i}, {i, -2, 4, 0.01}],
Joined -> True, FrameLabel -> {"kHz", "Input Noise[nV/√Hz]"},
PlotRange -> {3, 10}, plotoptn[1]]
```

```
Out[*]=
```



## Fifth Stage: Boosts

```
In[*]:= n += 1;
z1A[n] = Infinity;
z2A[n] = par[1580.,  $\frac{1}{s 100*^{-9}}$ ];
z1B[n] = Infinity;
z2B[n] = par[1580.,  $\frac{1}{s 100*^{-9}}$ ];
z1C[n] = Infinity;
z2C[n] = par[3160.,  $\frac{1}{s 100*^{-9}}$ ];

opamp[n] =
OpAmp[+1, z1A[n], z2A[n]] × OpAmp[+1, z1B[n], z2B[n]] × OpAmp[+1, z1C[n], z2C[n]];
opampnoise[n] = Sqrt[OpAmpNoise[+1, z1A[n], z2A[n], 1.7*^{-9}, 1.5*^{-12}]2 +
OpAmpNoise[+1, z1B[n], z2B[n], 1.7*^{-9}, 1.5*^{-12}]2 +
OpAmpNoise[+1, z1C[n], z2C[n], 1.7*^{-9}, 1.5*^{-12}]2];
```

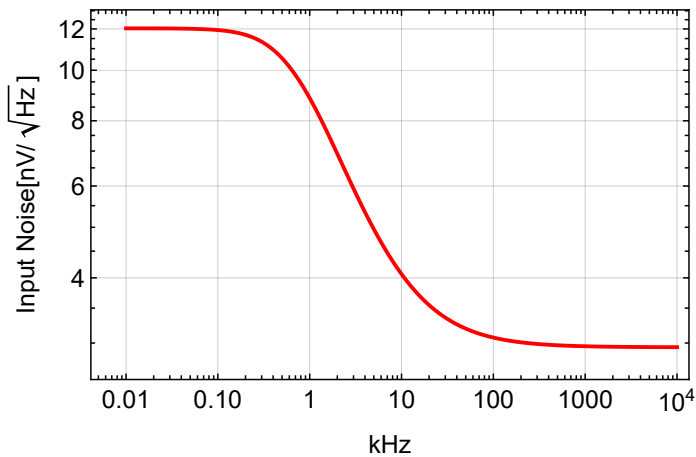


```

In[ ]:= ListLogLogPlot[Table[{10i, 1*9 opampnoise[5] /. s → 2 π i 1000 × 10i}, {i, -2, 4, 0.01}],
  Joined → True, FrameLabel → {"kHz", "Input Noise[nV/√Hz]"},
  PlotRange → All, PlotOptn[1]]

```

Out[ ]:=



## Sixth Stage: Exc1

```

In[ ]:= n += 1;
  z1[n] = 2000.;
  z2[n] = par[2000., s  $\frac{1}{s 10*^{-12}}$ ];
  opamp[n] = OpAmp[-1, z1[n], z2[n]];
  opampnoise[n] = OpAmpNoise[-1, z1[n], z2[n], 1.7*-9, 1.5*-12];

```

## Seventh Stage: Generic

```

In[ ]:= n += 1;
  z1[n] = Infinity;
  z2[n] = 100;
  opamp[n] = OpAmp[+1, z1[n], z2[n]];
  opampnoise[n] = OpAmpNoise[+1, z1[n], z2[n], 1.7*-9, 1.5*-12];

```

## Eighth Stage: Polarity

```

In[ ]:= n += 1;
  z1[n] = 3300;
  z2[n] = 3300;
  opamp[n] = OpAmp[-1, z1[n], z2[n]];
  opampnoise[n] = OpAmpNoise[-1, z1[n], z2[n], 1.7*-9, 1.5*-12];

```

## Ninth Stage: Exc2

```

In[*]:= n += 1;
z1[n] = 2000.;
z2[n] = par[2000., s  $\frac{1}{s \cdot 10^{-12}}$ ];
opamp[n] = OpAmp[-1, z1[n], z2[n]];
opampnoise[n] = OpAmpNoise[-1, z1[n], z2[n], 1.7*^-9, 1.5*^-12];

```

## Tenth Stage: Differential Input Amplifier

```

In[*]:= n += 1;
z1[n] = 2000.;
z2[n] = par[2000,  $\frac{1}{s \cdot 10^{-12}}$ ];
opamp[n] = OpAmp[0, z1[n], z2[n]];
opampnoise[n] = OpAmpNoise[0, z1[n], z2[n], 1.7*^-9, 1.5*^-12];

```

## Eleventh Stage: Gain Stage (8dB)

```

In[*]:= n += 1;
z1[n] = Infinity;
z2[n] = 100.;
opamp[n] = 2.5 OpAmp[1, z1[n], z2[n]];
opampnoise[n] = OpAmpNoise[1, z1[n], z2[n], 1.7*^-9, 1.5*^-12];

```

## Twelfth Stage: Low Pass

```

In[*]:= n += 1;
z1[n] = Infinity;
z2[n] = 100;

div[n] =  $\frac{1600.}{\text{ser}[1600, \frac{1}{s \cdot 20^{-6}}]}$ ;
opamp[n] = div[n] × OpAmp[+1, z1[n], z2[n]];
opampnoise[n] = OpAmpNoise[+1, z1[n], z2[n], 1.7*^-9, 1.5*^-12] / Abs[div[n]];

```

### Thirteenth Stage: Low Pass

```

In[*]:= n += 1;
z1[n] = Infinity;
z2[n] = 100;

div[n] =  $\frac{1600.}{\text{ser}\left[1600, \frac{1}{s 20 \cdot 10^{-6}}\right]}$ ;

opamp[n] = OpAmp[+1, z1[n], z2[n]];
opampnoise[n] = OpAmpNoise[+1, z1[n], z2[n], 1.7*10-9, 1.5*10-13] / Abs[div[n]];

```

### Fourteenth Stage: Limiter

```

In[*]:= n += 1;
z1[n] = Infinity;
z2[n] = 100;

opamp[n] = OpAmp[+1, z1[n], z2[n]];
opampnoise[n] = OpAmpNoise[+1, z1[n], z2[n], 1.7*10-9, 1.5*10-13];

```

### Fifteenth Stage: Output Driver

```

In[*]:= n += 1;
z1[n] = 3300.;
z2[n] = par[3300.,  $\frac{1}{s 10 \cdot 10^{-12}}$ ];

opamp[n] = OpAmp[-1, z1[n], z2[n]];
opampnoise[n] = OpAmpNoise[-1, z1[n], z2[n], 1.7*10-9, 1.5*10-13];

```

### IFO Common Mode Overall Transfer Functions & Noise

```

In[*]:= stages = n
opamp[0] = OpAmpProduct[opamp, stages];
opampnoise[0] = OpAmpNoiseProduct[opamp, opampnoise, stages];

```

```
Out[*]=
```

```
15
```

## Plots

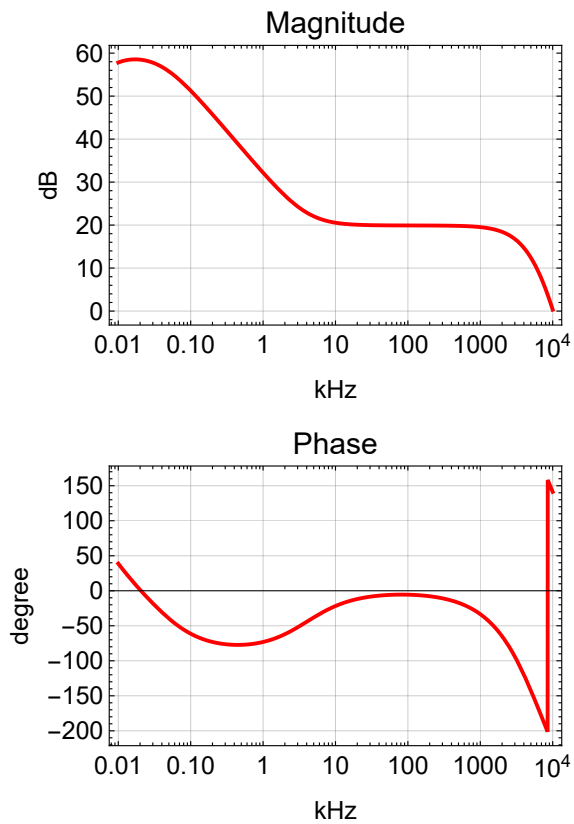
### Transfer function

```
In[*]:= {dB[opamp[0]], Phase[opamp[0]]} /. s -> 2  $\pi$  i ugf  
BodePlotEx[opamp[0] /. s -> 2  $\pi$  i 1000 f, {f, 0.01, 10*^3}, XAxisLabel -> "kHz", plotoptn[1]]
```

```
Out[*]=
```

```
{20.0826, -11.799}
```

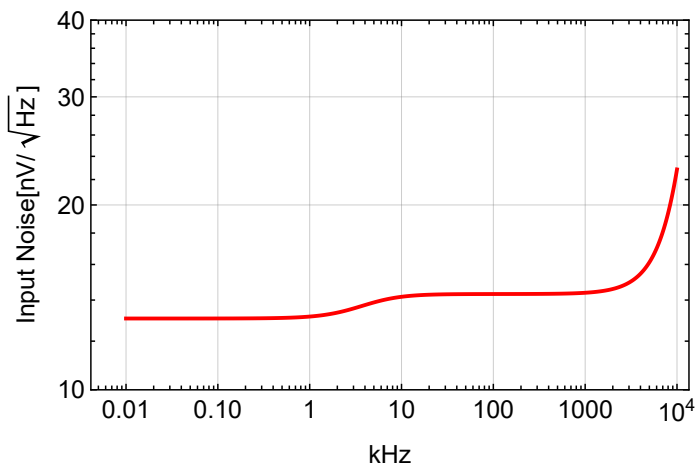
```
Out[*]=
```



## Equivalent Input Noise

```
In[ ]:= ListLogLogPlot[Table[{10i, 1*9 opampnoise[0] /. s → 2 π i 1000 × 10i}, {i, -2, 4, 0.01}],
  Joined → True, FrameLabel → {"kHz", "Input Noise[nV/√Hz]"},
  PlotRange → {9.999, 40}, plotoptn[1]]
```

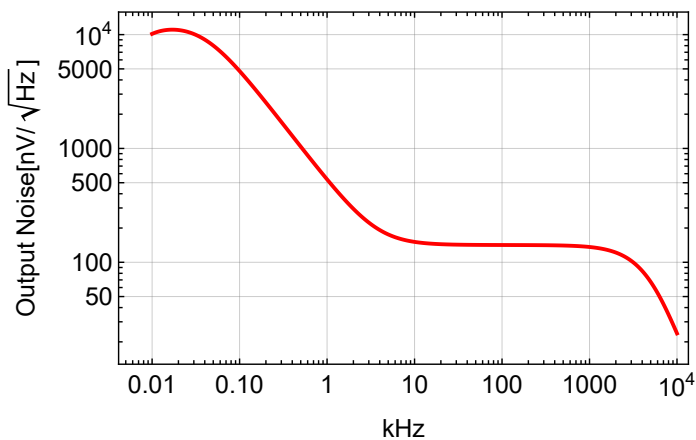
Out[ ]=



## Output Noise w/ Input Terminated

```
In[ ]:= ListLogLogPlot[
  Table[{10i, 1*9 opampnoise[0] Abs[opamp[0]] /. s → 2 π i 1000 × 10i}, {i, -2, 4, 0.01}],
  Joined → True, FrameLabel → {"kHz", "Output Noise[nV/√Hz]"},
  PlotRange → All, plotoptn[1]]
```

Out[ ]=



## IFO Common Mode Noise Propagation and Slew Rate Limit

```
In[*]:= signal = SpecProp[cmbaseline, opamp, stages];
slew = SpecProp[cmslewbaseline, opamp, stages];
```

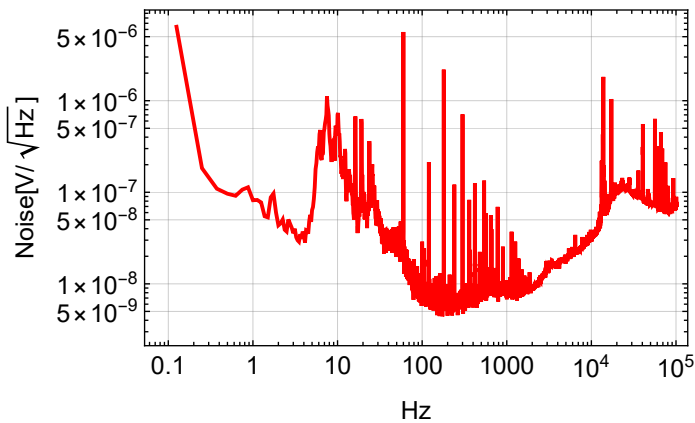
```
In[*]:= SpecRMS /@ (Drop[#, 7] & /@ signal)
SpecRMS /@ (Drop[#, 7] & /@ slew)
```

```
Out[*]=
{0.0000329826, 0.0000328078, 0.000131231, 0.000130539, 0.000575068,
 0.000575068, 0.000575068, 0.000575068, 0.000575068, 0.000575068,
 0.000574882, 0.00143721, 0.00115498, 0.000991745, 0.000991745, 0.000990664}
```

```
Out[*]=
{10.2981, 10.2101, 40.8405, 40.4923, 42.8589, 42.8589, 42.8589, 42.8589,
 42.8589, 42.8589, 42.5016, 106.254, 106.244, 106.234, 106.234, 104.785}
```

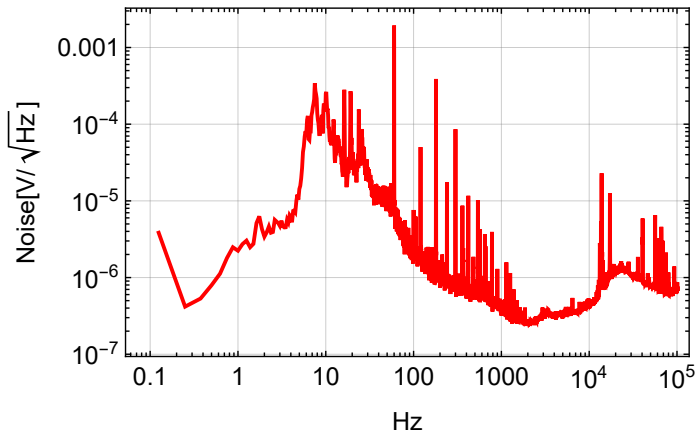
```
In[*]:= ListLogLogPlot[signal[[1]], Joined → True,
  FrameLabel → {"Hz", "Noise[V/√Hz]"}, PlotRange → All, plotoptn[1]]
```

```
Out[*]=
```



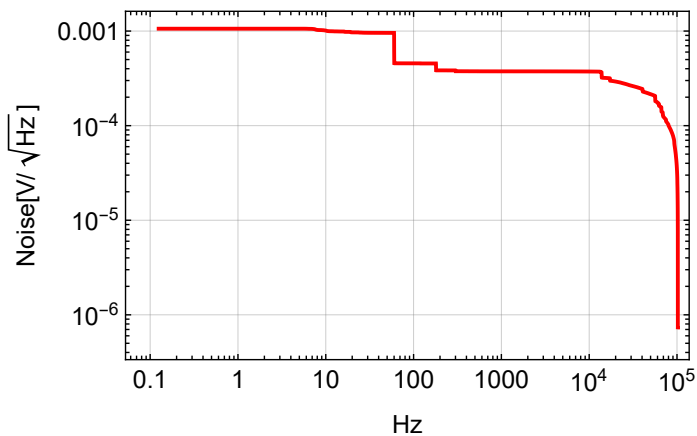
```
In[*]:= ListLogLogPlot[signal[[16]], Joined → True,
  FrameLabel → {"Hz", "Noise[V/√Hz]"}, PlotRange → All, plotoptn[1]]
```

Out[\*]=



```
In[*]:= ListLogLogPlot[RMSSpec[signal[[16]], -1], Joined → True,
  FrameLabel → {"Hz", "Noise[V/√Hz]"}, PlotRange → All, plotoptn[1]]
```

Out[\*]=




---

## Mode Cleaner Board Transfer Functions & Noise

```
In[*]:= ugf = 100*^3;
```

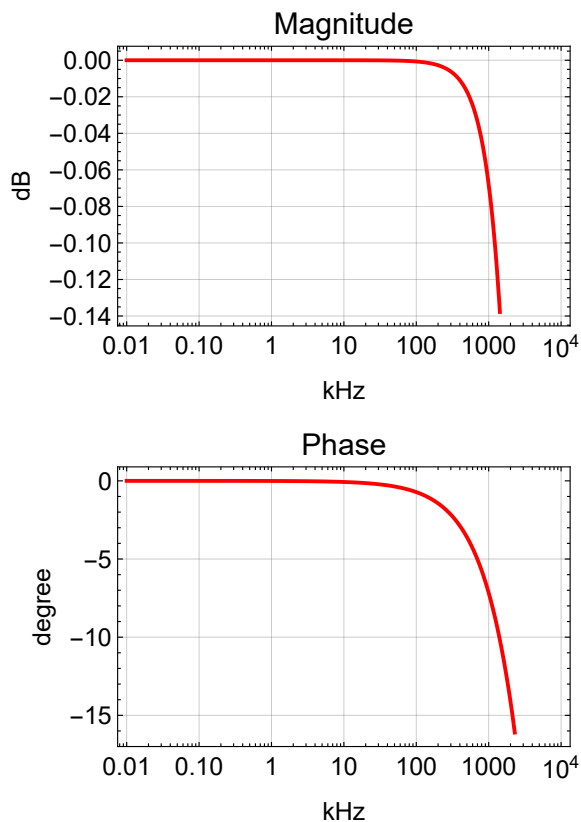
## First Stage: Differential Input Amplifier

```
In[ ]:= n = 1;
z1[n] = 2000.;
z2[n] = par[2000,  $\frac{1}{s \cdot 10^{-12}}$ ];
opamp[n] = OpAmp[0, z1[n], z2[n]];
opampnoise[n] = OpAmpNoise[0, z1[n], z2[n], 1.7*10^-9, 1.5*10^-12];
```

```
In[ ]:= {dB[opamp[1]], Phase[opamp[1]]} /. s -> 2 Pi i ug f
BodePlotEx[opamp[1] /. s -> 2 Pi i 1000 f, {f, 0.01, 10*10^3}, XAxisLabel -> "kHz", plotopt]
```

```
Out[ ]:= {-0.000685756, -0.719962}
```

```
Out[ ]:=
```



## Second Stage: Gain Stage (0dB)

```
In[ ]:= n += 1;
z1[n] = Infinity;
z2[n] = 100.;
opamp[n] = OpAmp[1, z1[n], z2[n]];
opampnoise[n] = OpAmpNoise[1, z1[n], z2[n], 1.7*10^-9, 1.5*10^-12];
```



### Third Stage: Summing Node

```

In[*]:= n += 1;
z1[n] = 2000.;
z2[n] = par[2000.,  $\frac{1}{s \cdot 10^{-12}}$ ];
opamp[n] = OpAmp[-1, z1[n], z2[n]];
opampnoise[n] = OpAmpNoise[-1, z1[n], z2[n], 1.7*10-9, 1.5*10-12];

```

### Forth Stage: Pole/Zero Pair

```

In[*]:= n += 1;
z1[n] = 1210.;
z2[n] = par[121.*103, ser[1210.,  $\frac{1}{s \cdot 33 \cdot 10^{-9}}$ ]];
opamp[n] = OpAmp[-1, z1[n], z2[n]];
opampnoise[n] = OpAmpNoise[-1, z1[n], z2[n], 1.7*10-9, 1.5*10-12];

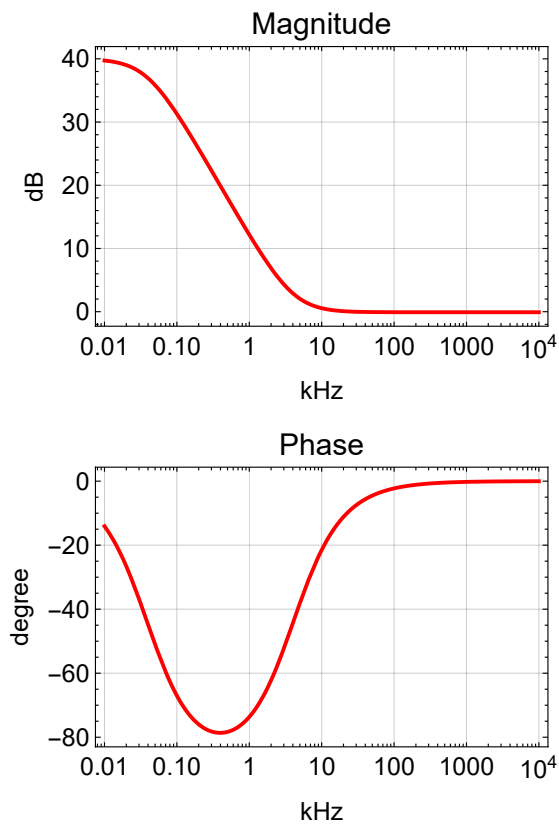
In[*]:= {dB[opamp[4]], Phase[opamp[4]]} /. s -> 2 Pi i ug f
BodePlotEx[opamp[4] /. s -> 2 Pi i 1000 f, {f, 0.01, 10*103}, XAxisLabel -> "kHz", plotopt]

```

Out[\*]=

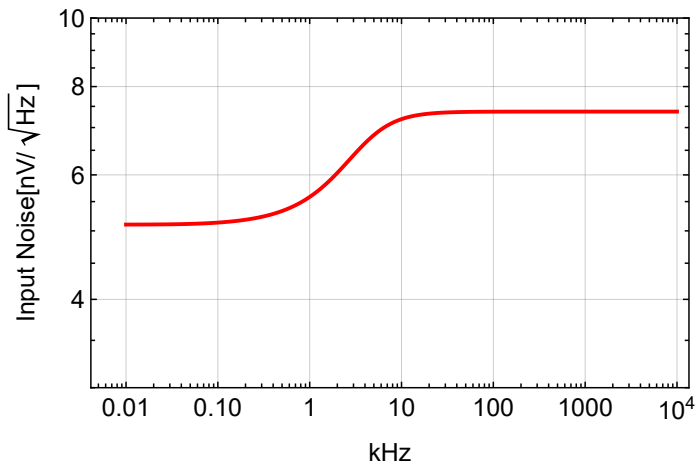
```
{-0.079534, -2.2599}
```

Out[\*]=



```
In[ ]:= ListLogLogPlot[Table[{10^i, 1*^9 opampnoise[4] /. s -> 2 π i 1000 × 10^i}, {i, -2, 4, 0.01}],
  Joined -> True, FrameLabel -> {"kHz", "Input Noise[nV/√Hz]"},
  PlotRange -> {3, 10}, plotoptn[1]]
```

Out[ ]:=



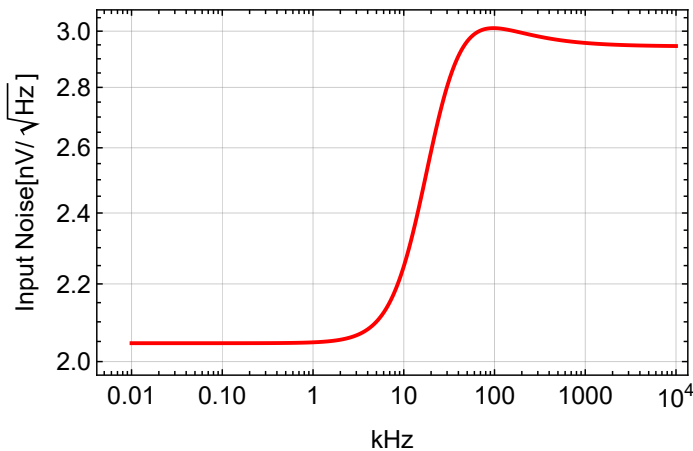
## Fifth Stage: Boosts

```
In[ ]:= n += 1;
z1A[n] = 82.5;
z2A[n] = par[1580., 1 / (s 100*^-9)];
z1B[n] = 82.5;
z2B[n] = par[1580., 1 / (s 100*^-9)];
z1C[n] = Infinity;
z2C[n] = par[3160., 1 / (s 100*^-9)];

opamp[n] =
  OpAmp[+1, z1A[n], z2A[n]] × OpAmp[+1, z1B[n], z2B[n]] × OpAmp[+1, z1C[n], z2C[n]];
opampnoise[n] = Sqrt[OpAmpNoise[+1, z1A[n], z2A[n], 1.7*^-9, 1.5*^-12]^2 +
  OpAmpNoise[+1, z1B[n], z2B[n], 1.7*^-9, 1.5*^-12]^2 +
  Abs[OpAmp[+1, z1A[n], z2A[n]]]^2 +
  OpAmpNoise[+1, z1C[n], z2C[n], 1.7*^-9, 1.5*^-12]^2 /
  Abs[OpAmp[+1, z1A[n], z2A[n]] × OpAmp[+1, z1B[n], z2B[n]]]^2];
```

```
In[*]:= ListLogLogPlot[Table[{10i, 1*9 opampnoise[5] /. s → 2 π i 1000 × 10i}, {i, -2, 4, 0.01}],
  Joined → True, FrameLabel → {"kHz", "Input Noise[nV/√Hz]"},
  PlotRange → All, PlotOptn[1]]
```

Out[\*]=



## Sixth Stage: Exc1

```
In[*]:= n += 1;
z1[n] = 2000.;
z2[n] = par[2000., s  $\frac{1}{s 10*^{-12}}$ ];
opamp[n] = OpAmp[-1, z1[n], z2[n]];
opampnoise[n] = OpAmpNoise[-1, z1[n], z2[n], 1.7*-9, 1.5*-12];
```

## Seventh Stage: Generic

```
In[*]:= n += 1;
z1[n] = Infinity;
z2[n] = 100;
opamp[n] = OpAmp[+1, z1[n], z2[n]];
opampnoise[n] = OpAmpNoise[+1, z1[n], z2[n], 1.7*-9, 1.5*-12];
```

## Eighth Stage: Polarity

```
In[*]:= n += 1;
z1[n] = 3300;
z2[n] = 3300;
opamp[n] = OpAmp[-1, z1[n], z2[n]];
opampnoise[n] = OpAmpNoise[-1, z1[n], z2[n], 1.7*-9, 1.5*-12];
```

## Ninth Stage: Exc2

```

In[*]:= n += 1;
z1[n] = 2000.;
z2[n] = par[2000., s  $\frac{1}{s \cdot 10^{-12}}$ ];
opamp[n] = OpAmp[-1, z1[n], z2[n]];
opampnoise[n] = OpAmpNoise[-1, z1[n], z2[n], 1.7* $10^{-9}$ , 1.5* $10^{-12}$ ];

```

## Tenth Stage: Differential Input Amplifier

```

In[*]:= n += 1;
z1[n] = 2000.;
z2[n] = par[2000.,  $\frac{1}{s \cdot 10^{-12}}$ ];
opamp[n] = OpAmp[0, z1[n], z2[n]];
opampnoise[n] = OpAmpNoise[0, z1[n], z2[n], 1.7* $10^{-9}$ , 1.5* $10^{-12}$ ];

```

## Eleventh Stage: Gain Stage

```

In[*]:= n += 1;
z1[n] = Infinity;
z2[n] = 100.;
opamp[n] = OpAmp[1, z1[n], z2[n]];
opampnoise[n] = OpAmpNoise[1, z1[n], z2[n], 1.7* $10^{-9}$ , 1.5* $10^{-12}$ ];

```

## Twelfth Stage: Lead Compensation

```

In[*]:= n += 1;
z1[n] = par[1130.,  $1130. + \frac{1}{s \cdot 10^{-9}}$ ];
z2[n] = par[1130.,  $\frac{1}{s \cdot 10^{-12}}$ ];
opamp[n] = OpAmp[-1, z1[n], z2[n]];
opampnoise[n] = OpAmpNoise[-1, z1[n], z2[n], 1.7* $10^{-9}$ , 1.5* $10^{-12}$ ];

```

## Thirteenth Stage: Identity

```

In[*]:= n += 1;
z1[n] = Infinity;
z2[n] = 100;
opamp[n] = OpAmp[+1, z1[n], z2[n]];
opampnoise[n] = OpAmpNoise[+1, z1[n], z2[n], 1.7* $10^{-9}$ , 1.5* $10^{-13}$ ];

```

## Fourteenth Stage: Limiter

```
In[*]:= n += 1;
z1[n] = Infinity;
z2[n] = 100;
opamp[n] = OpAmp[+1, z1[n], z2[n]];
opampnoise[n] = OpAmpNoise[+1, z1[n], z2[n], 1.7*^-9, 1.5*^-13];
```

## Fifteenth Stage: Output Driver

```
In[*]:= n += 1;
z1[n] = 3300.;
z2[n] = par[3300.,  $\frac{1}{s \cdot 10*^-12}$ ];
opamp[n] = OpAmp[-1, z1[n], z2[n]];
opampnoise[n] = OpAmpNoise[-1, z1[n], z2[n], 1.7*^-9, 1.5*^-13];
```

## Mode Cleaner Overall Transfer Functions & Noise

```
In[*]:= stages = n
opamp[0] = OpAmpProduct[opamp, stages];
opampnoise[0] = OpAmpNoiseProduct[opamp, opampnoise, stages];

Out[*]=
15
```

## Plots

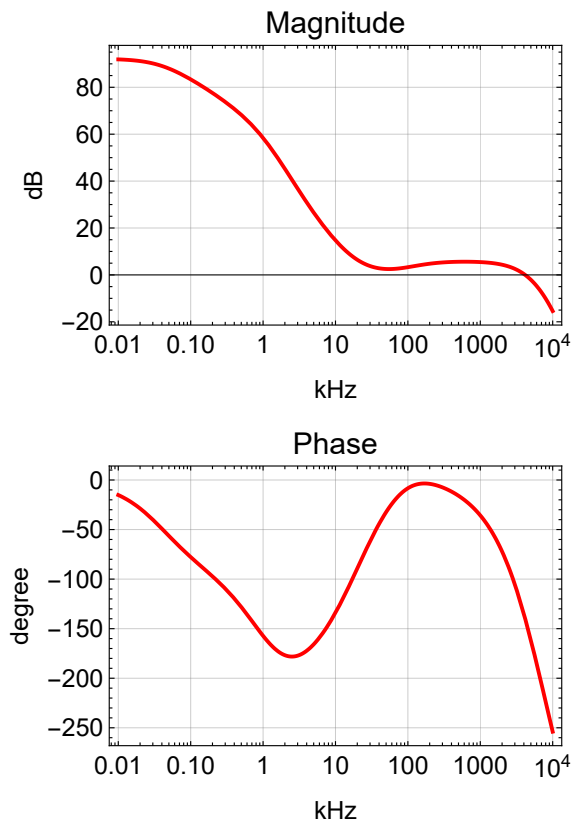
### Transfer function

```
In[*]:= {dB[opamp[0]], Phase[opamp[0]]} /. s -> 2  $\pi$  i ug f  
BodePlotEx[opamp[0] /. s -> 2  $\pi$  i 1000 f, {f, 0.01, 10*^3}, XAxisLabel -> "kHz", plotopt]
```

Out[\*]=

```
{3.28828, -8.33801}
```

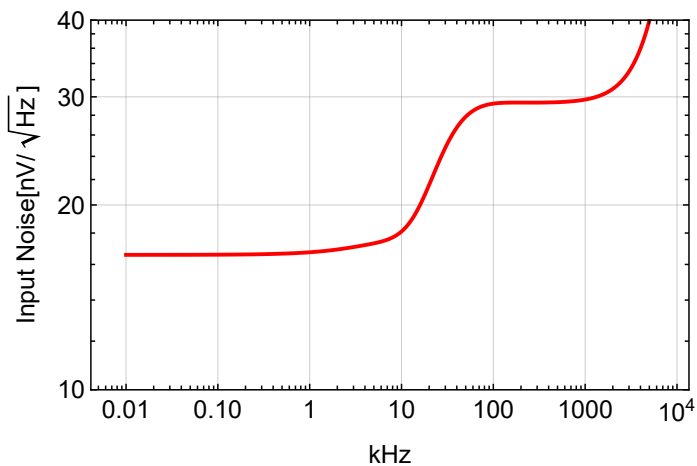
Out[\*]=



## Equivalent Input Noise

```
In[ ]:= ListLogLogPlot[Table[{10i, 1*9 opampnoise[0] /. s → 2 π i 1000 × 10i}, {i, -2, 4, 0.01}],
  Joined → True, FrameLabel → {"kHz", "Input Noise[nV/√Hz]"},
  PlotRange → {9.999, 40}, plotoptn[1]]
```

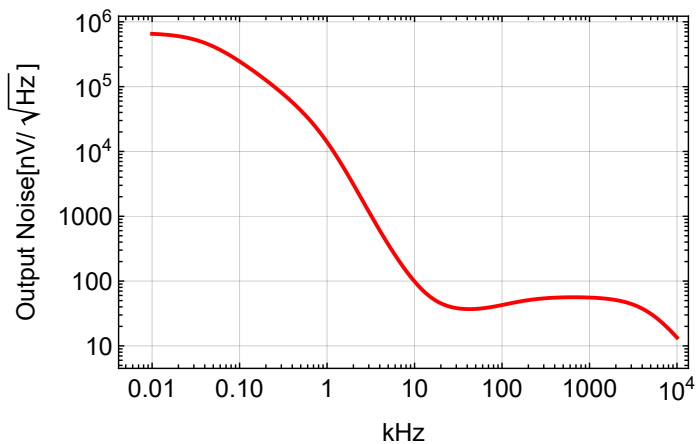
Out[ ]=



## Output Noise w/ Input Terminated

```
In[ ]:= ListLogLogPlot[
  Table[{10i, 1*9 opampnoise[0] Abs[opamp[0]] /. s → 2 π i 1000 × 10i}, {i, -2, 4, 0.01}],
  Joined → True, FrameLabel → {"kHz", "Output Noise[nV/√Hz]"},
  PlotRange → All, plotoptn[1]]
```

Out[ ]=



## Mode Cleaner Noise Propagation and Slew Rate Limit

```
In[ ]:= signal = SpecProp[mcbaseline, opamp, stages];
slew = SpecProp[mcslewbaseline, opamp, stages];
```

```
In[ ]:= signal[[1, 2100]]
slew[[1, 2100]]
```

```
Out[ ]:=
{1000, 1.22563 × 10-6}
```

```
Out[ ]:=
{1000, 0.00770086}
```

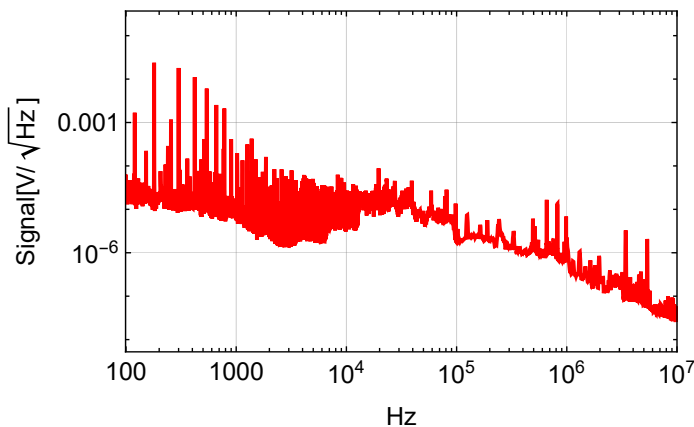
```
In[ ]:= SpecRMS /@ (Drop[#, 2100] & /@ signal)
SpecRMS /@ (Drop[#, 2100] & /@ slew)
```

```
Out[ ]:=
{0.00436962, 0.00407199, 0.00407199, 0.00389906,
0.00448875, 0.0982917, 0.0982917, 0.0982917, 0.0982917, 0.0982917,
0.0982654, 0.0982654, 0.099494, 0.099494, 0.099494, 0.0994429}
```

```
Out[ ]:=
{51276.2, 32248.3, 32248.3, 21135.9, 20961.7, 21379.2, 21379.2, 21379.2,
21379.2, 21379.2, 14839.1, 14839.1, 23225.5, 23225.5, 23225.5, 15395.8}
```

```
In[ ]:= ListLogLogPlot[signal[[5]], Joined → True,
FrameLabel → {"Hz", "Signal[V/√Hz]"}, PlotRange → {{99, 1*^7}, All}, plotoptn[1]]
```

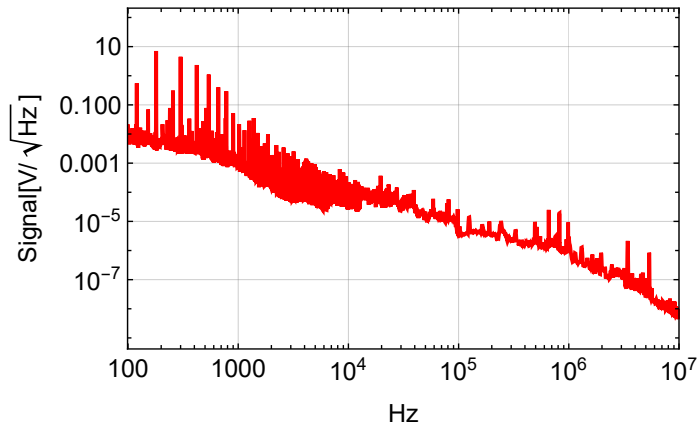
```
Out[ ]:=
```





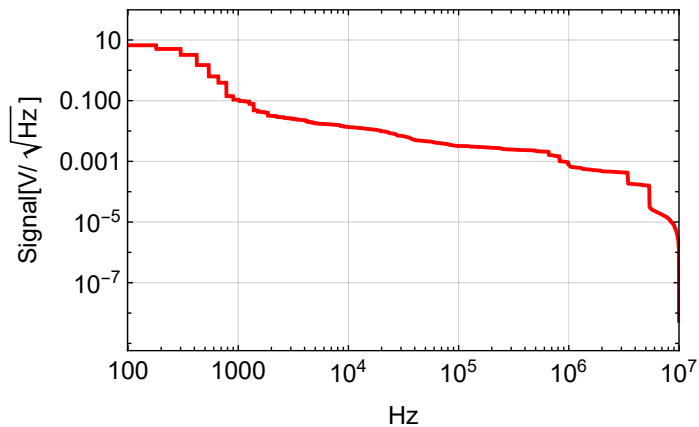
```
In[ ]:= ListLogLogPlot[signal[[16]], Joined → True,  
  FrameLabel → {"Hz", "Signal[V/√Hz]"}, PlotRange → {{99, 1*^7}, All}, plotoptn[1]
```

Out[ ]=



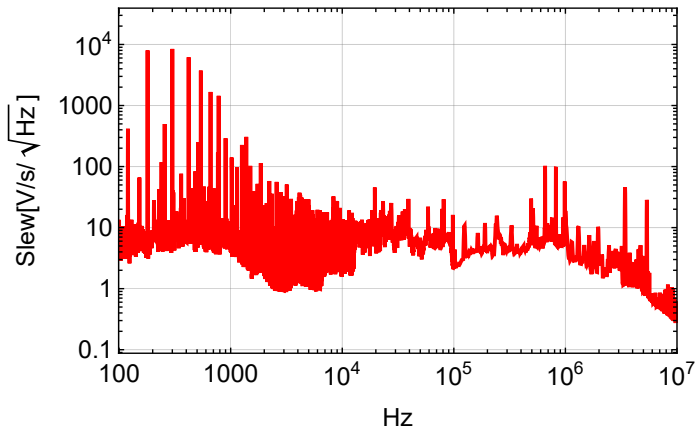
```
In[ ]:= ListLogLogPlot[RMSpec[signal[[16]], -1], Joined → True,  
  FrameLabel → {"Hz", "Signal[V/√Hz]"}, PlotRange → {{99, 1*^7}, All}, plotoptn[1]
```

Out[ ]=



```
In[ ]:= ListLogLogPlot[slew[[16]], Joined → True,
  FrameLabel → {"Hz", "Slew[V/s/√Hz]"}, PlotRange → {{99, 1*^7}, All}, plotoptn[1]
```

Out[ ]=



```
In[ ]:= ListLogLogPlot[RMSSpec[Drop[slew[[16]], 2100], 1],
  Joined → True, FrameLabel → {"Hz", "Slew[V/s/√Hz]"},
  PlotRange → {{999, 1*^7}, {1*^2, 1*^5}}, plotoptn[1]
```

Out[ ]=

