



Detectability of Nonlinear Gravitational Wave Memory (August 21, 2020)

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Introduction

- I. **Background:** gravitational wave (GW) memory form and types
- II. **Problem:** can we detect GW memory?
- III. **Approach:** Bayesian parameter estimation
- IV. **Results:** posterior samples...and a lot of 'em!
- V. **Future work:** where can we go next?

Background

What is Memory?

What is GW Memory?

Time Domain Waveform

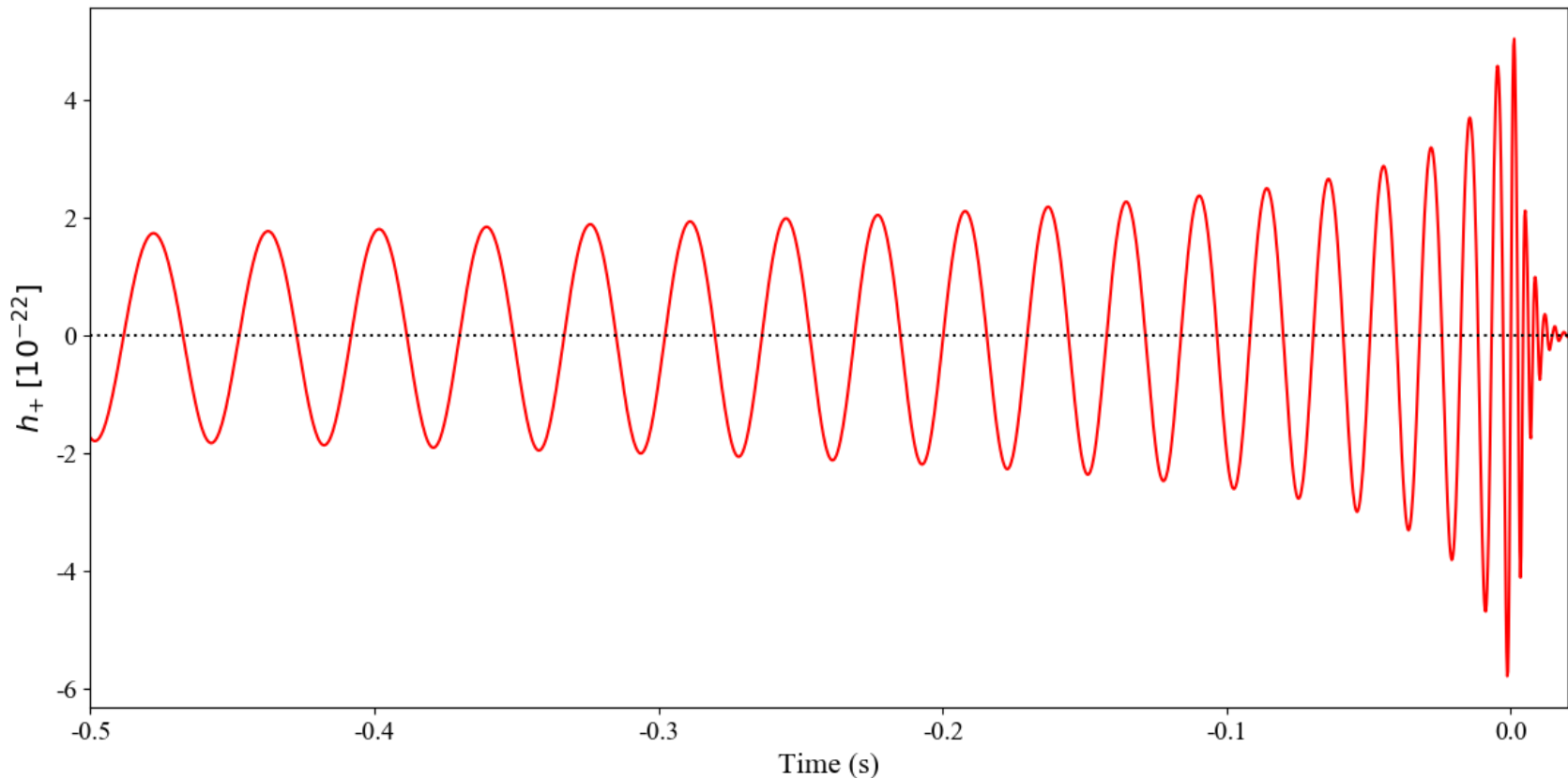
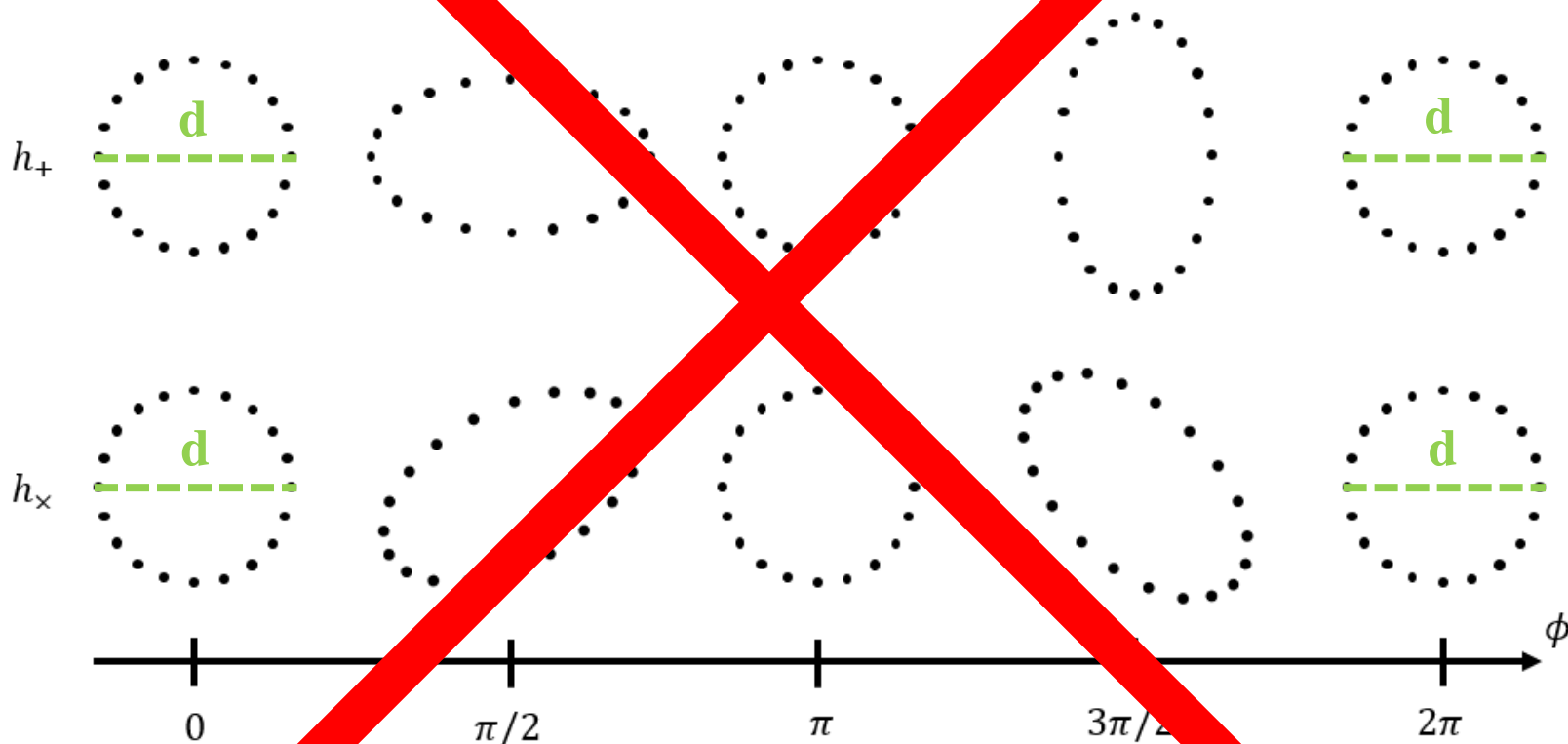


Figure 1. Sourced from a binary black hole (BBH) merger with non-spinning components, $M = 60M_{\odot}$, $q = 1$ and $d_L = 600\text{Mpc}$.

What is Memory?

GW \otimes



Time Domain Memory

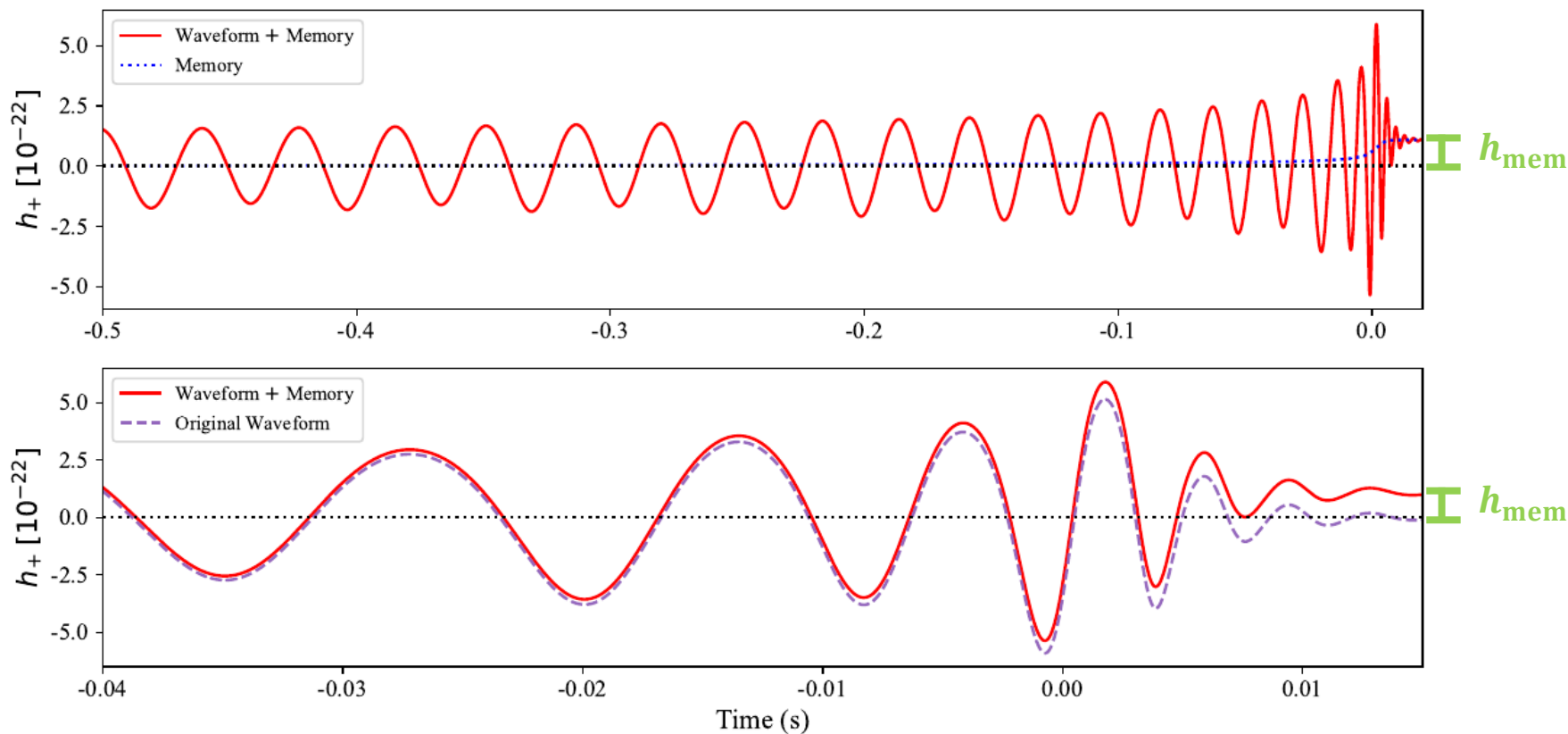
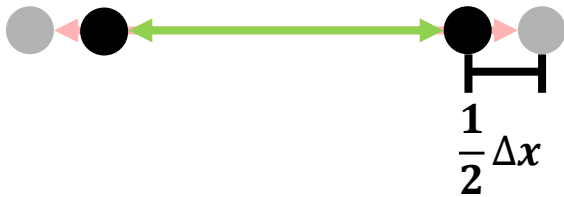
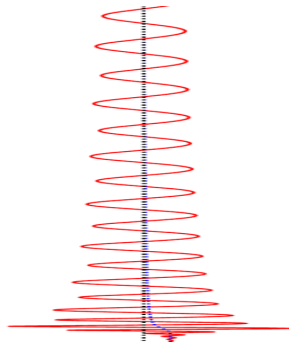


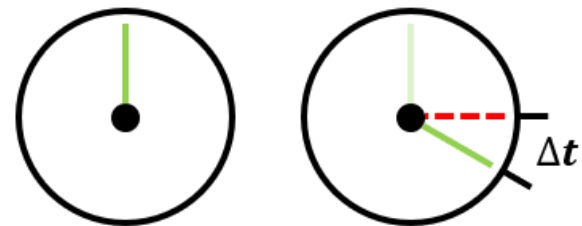
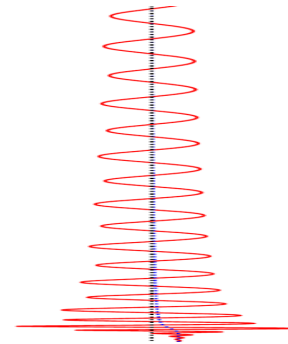
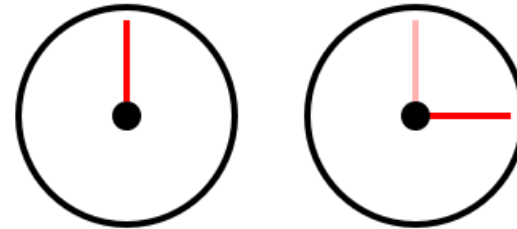
Figure 2. (Top) Superposed memory and full waveform. (Bottom) Superposed oscillatory and full waveform over the LIGO band only. All waveforms were sourced from a BBH merger with non-spinning components, $M = 60M_{\odot}$, $q = 1$ and $d_L = 600\text{Mpc}$.

What is Memory?

Space

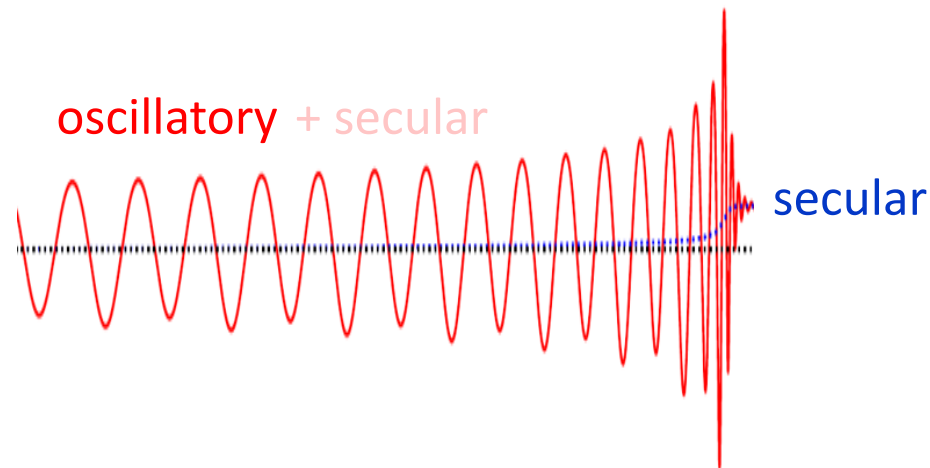


Time



What is Memory?

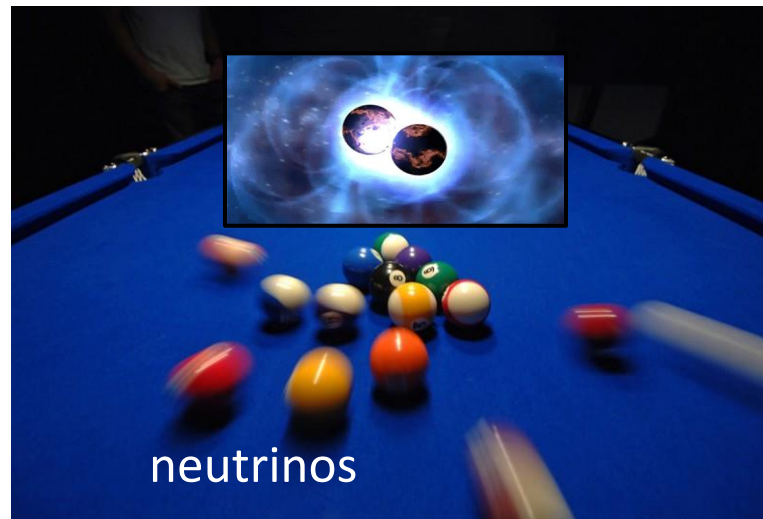
- Every gravitational waveform has two components: *oscillatory* and *secular* [1]



- Two kinds of secular components: *linear* and *nonlinear*

Linear Memory

- Independent of source's past motion (i.e. integrable or conservative)
- Only exists alongside mass emission (e.g. neutrinos)
- Too small to detect in BBH mergers [2, 3]

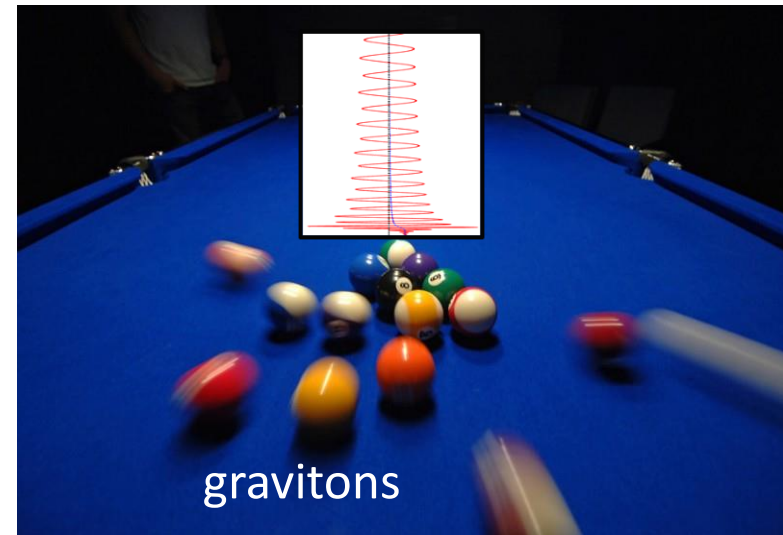


(Courtesy of Lea [4] and LIGO Caltech [5])

Nonlinear Memory

1. accelerating masses \Rightarrow GWs
 2. mass \propto energy
 3. GWs = energy
-

\therefore GWs \Rightarrow GWs!!! [3]





Nonlinear Memory

- Depends on entire past motion of source
(i.e. hereditary, nonintegrable, or nonconservative)
- More prominent than linear memory in BBHs [1, 2]
- Typically 10 times weaker than oscillatory component [3]

Frequency Domain Memory

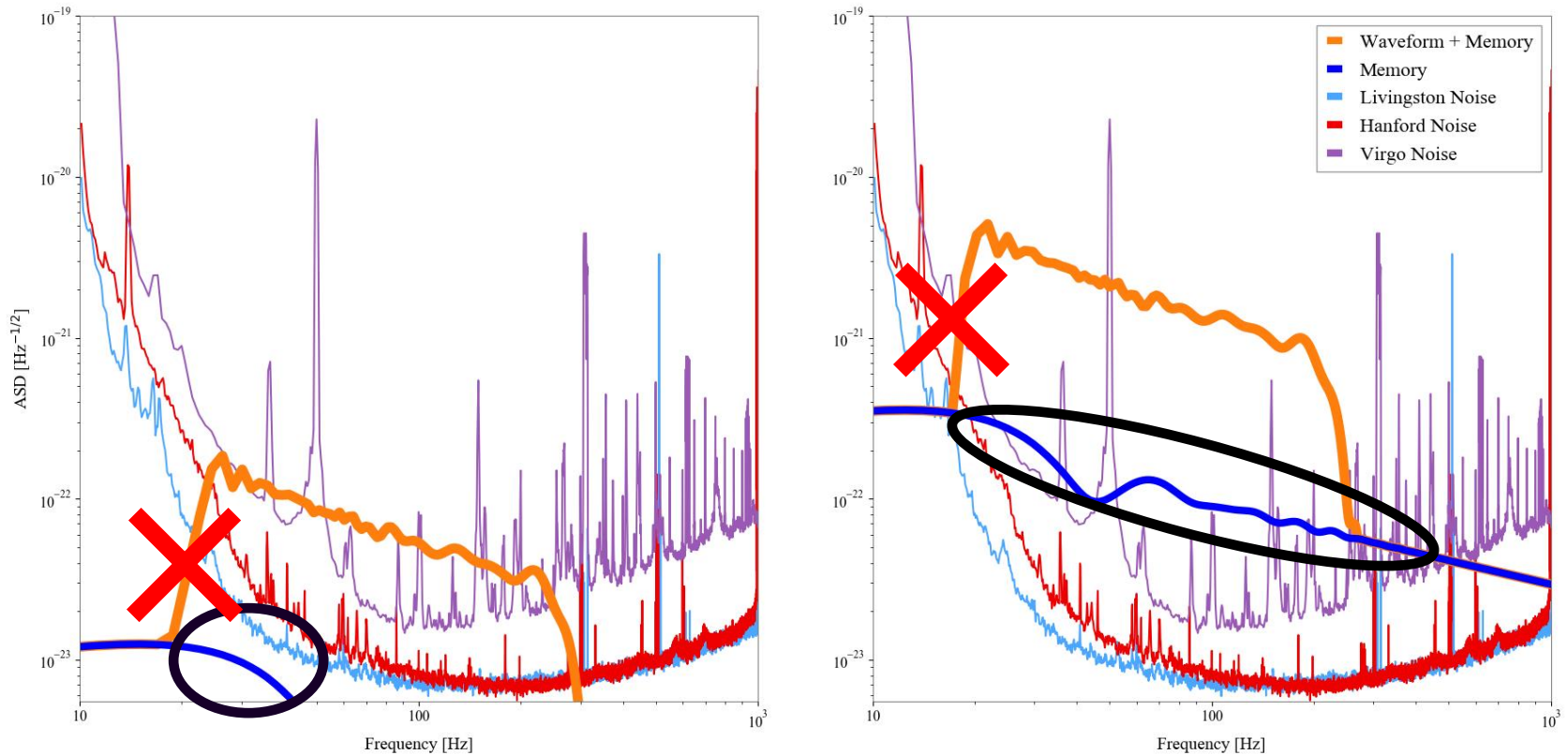


Figure 3. (Left) Undetectable memory: $M = 60M_{\odot}$, $q = 1$ and $d_L = 600\text{Mpc}$. (Right) Detectable memory: $M = 80M_{\odot}$, $q = 1$ and $d_L = 20\text{Mpc}$. All sub-20-Hz power from the total waveform is incorrect due to windowing.

Estimating Memory

- Nonlinear GW memory is given by:

$$h_{\text{mem}} \approx \frac{5}{14c^2} \frac{E}{r} \sin^2 \iota \quad (1)$$

where $E \equiv$ total radiated energy of GW source,
 $c \equiv$ vacuum speed of light
 $r \equiv$ distance between source and detector,
 $\iota \equiv$ inclination angle \equiv angle between \vec{L} and \vec{r} .

- Let's use GW150914 as an example:

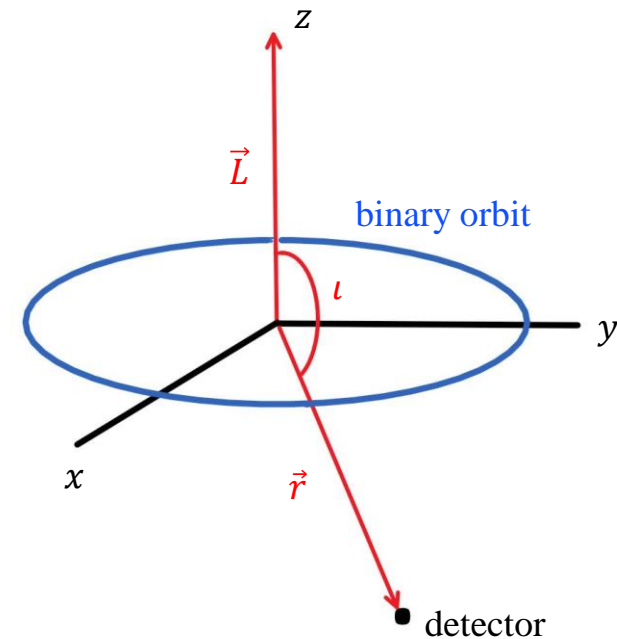
$$E = 3.0M_{\odot} \cdot c^2, r = 410\text{Mpc}, \text{ and } \iota = 150^{\circ}.$$

Thus,

$$h_{\text{mem}} \approx 3.0 \times 10^{-23}. \quad (2)$$

- For reference,

$$h_{\text{max}} \approx 1.0 \times 10^{-21}.$$



(Courtesy of Garfinkle [6])

Problem

Can we detect memory?

Under what circumstances can we detect memory?

Importance

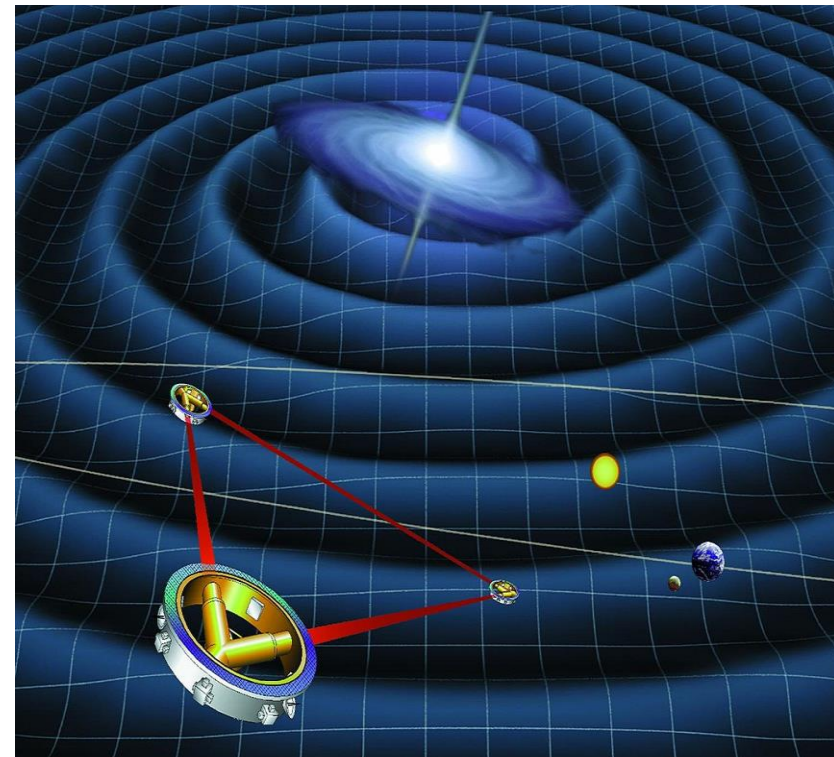
- Verification of General Relativity

But, why now?

- MANY new and exciting events [7]
- More detectors than ever
- Higher sensitivity per detector

Later...

- LISA [1]



(Courtesy of NASA [8])

Approach

Model with Memory

memory constant

$$h_{\text{tot}} = h + \lambda h_{\text{mem}}$$

Bayes' Theorem

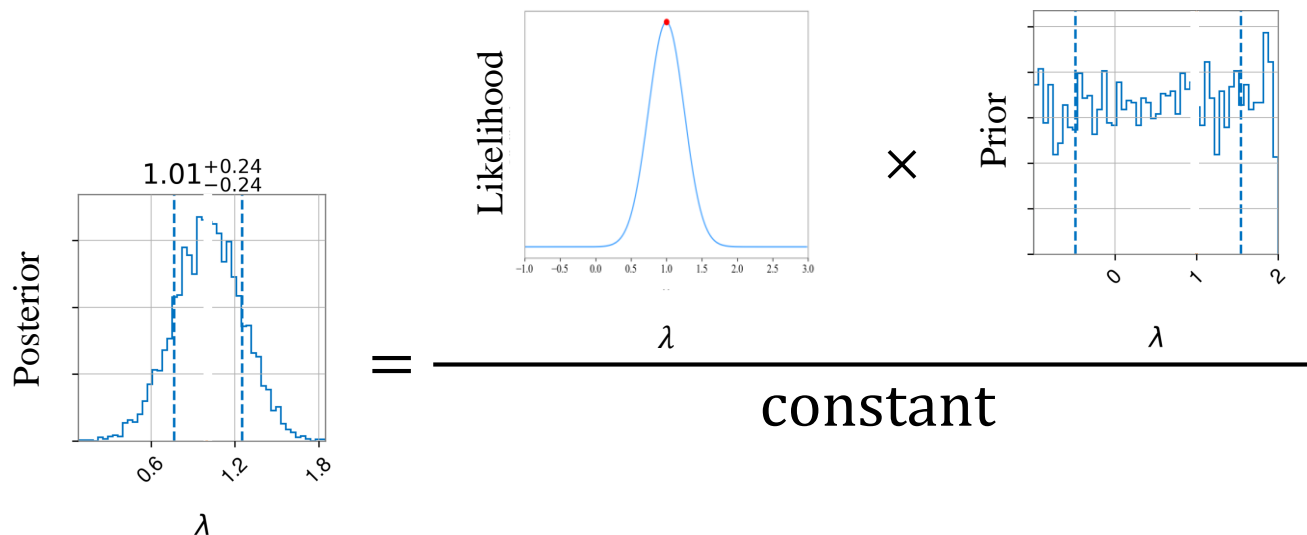
FOR MATHEMATICIANS

$$P(H | D) = \frac{P(D | H) P(H)}{P(D)}$$

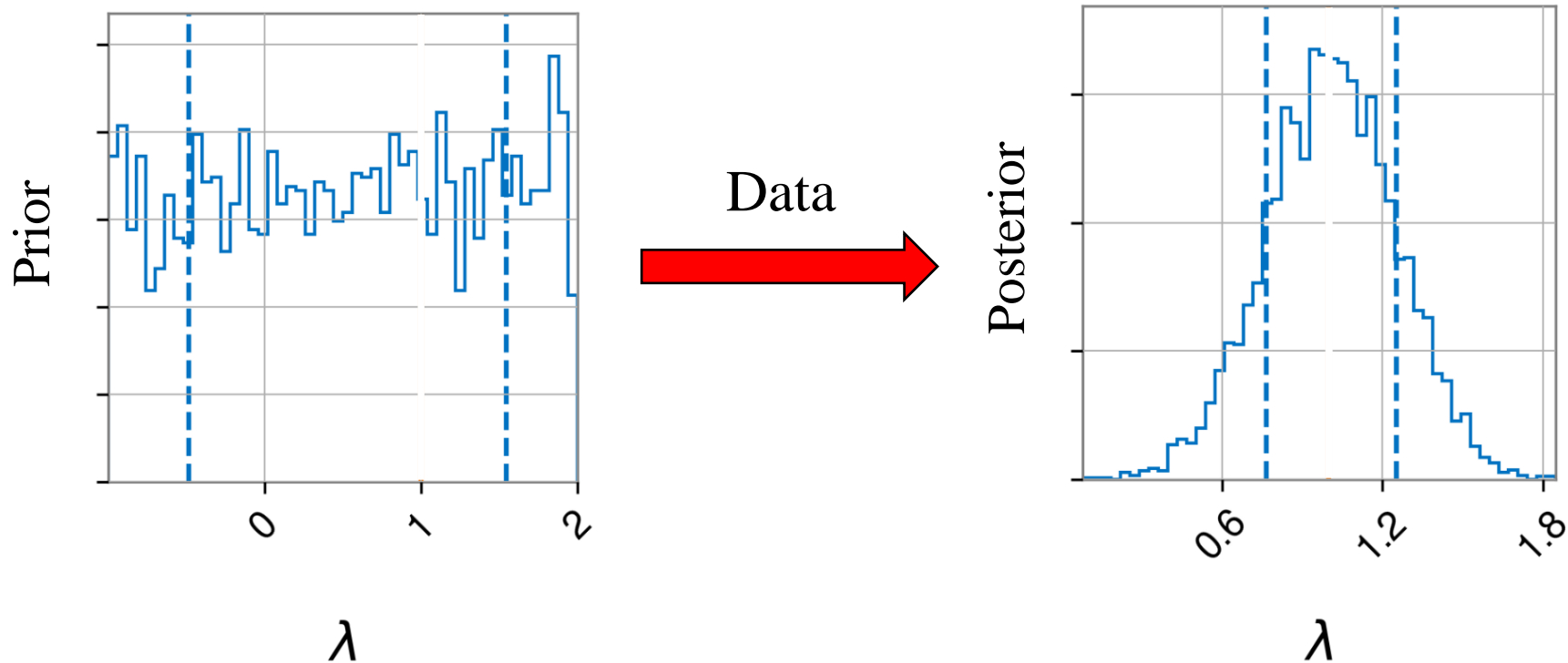
FOR THEORISTS

$$\text{posterior} = \frac{\text{likelihood} \times \text{prior}}{\text{evidence}}$$

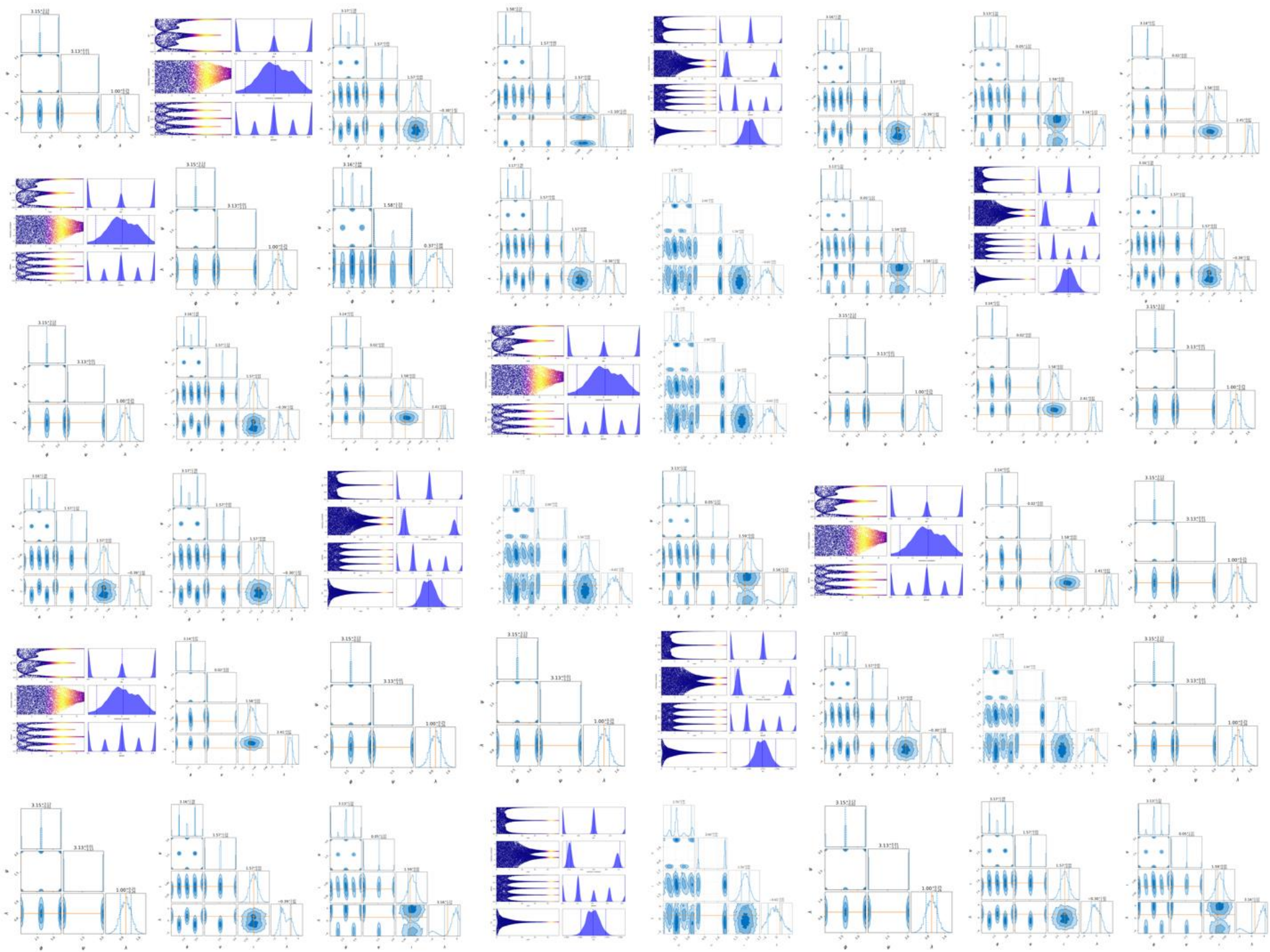
FOR LIGO SCIENTISTS



Bayes' Theorem



Results





Questions?

Under the transformation
 $(\psi \rightarrow \psi + \pi/2, \phi_c \rightarrow \phi_c + \pi/2)$...

- Oscillatory part remains the same
- Memory swaps sign

...but only if we are looking at the
 (2, 2)-mode alone.

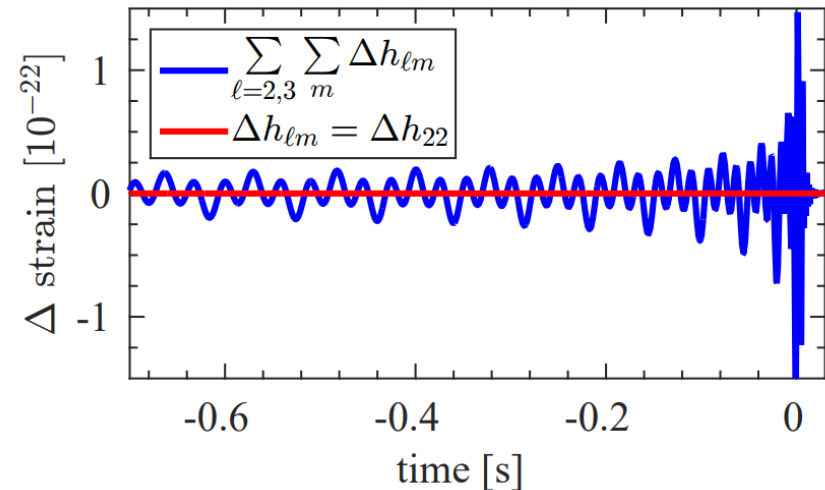


Figure 4. Time series plot of the difference between $h_{lm}(\psi, \phi_c)$ and $h_{lm}(\psi + \pi/2, \phi_c + \pi/2)$. (Red) (2, 2)-mode only and (Blue) higher-order modes only. The injected waveform used to generate these posterior distributions is sourced by a system with the following parameters: $M = 70.4$ solar masses, $q = 1.1$, $d_L = 342.2$ Mpc, $\iota = 2.5$, $\alpha = \delta = 1.2$ (Courtesy of Lasky et al. [])

(2, 2)-mode only

Higher-order modes

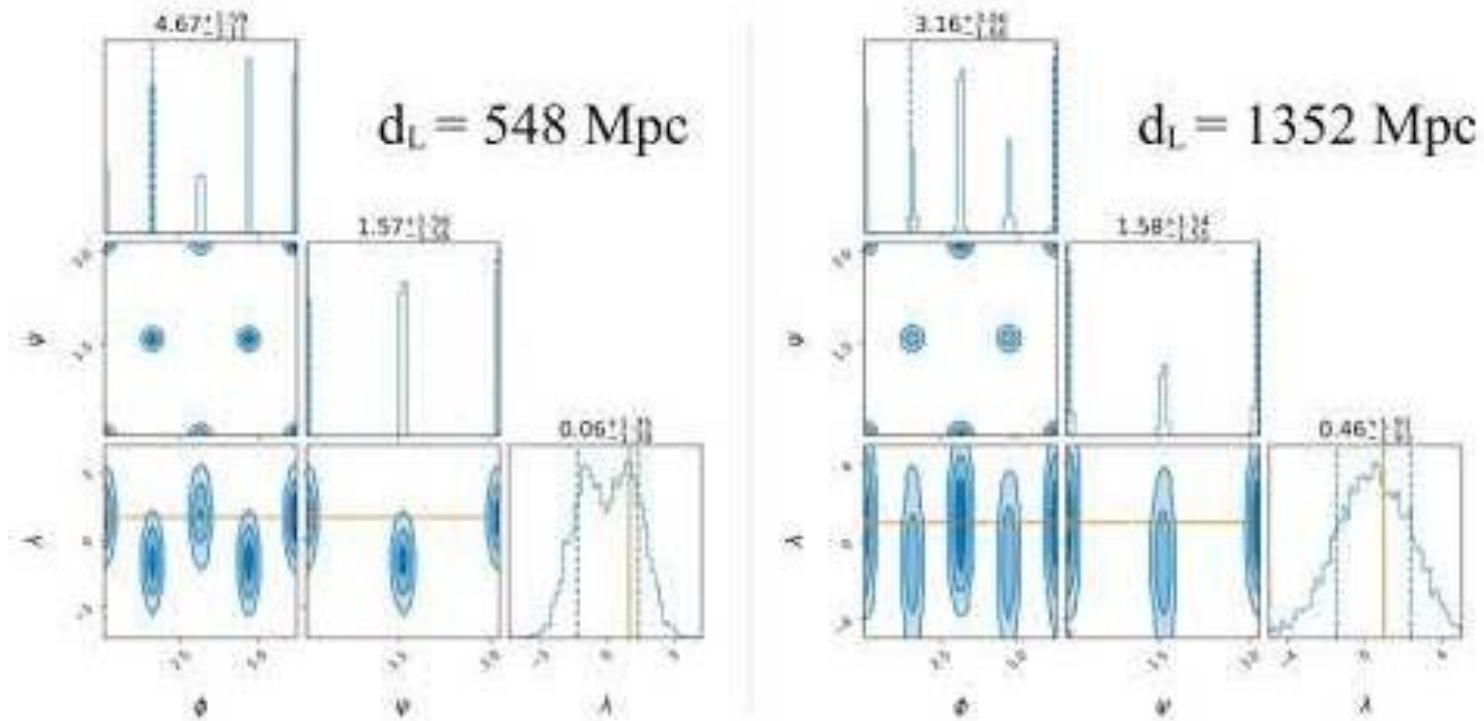


Figure 5. (Left) (2, 2) mode only and (Right) all modes included. The injected waveform used to generate these posterior distributions is sourced by non-spinning components with $M_{\text{tot}} = 60$ solar masses, $q = 1$, $\iota = \pi/2$, $\psi = 0$, $\phi_c = 0$, $\alpha = 0$, $\delta = 0$.

Noiseless

Noisy

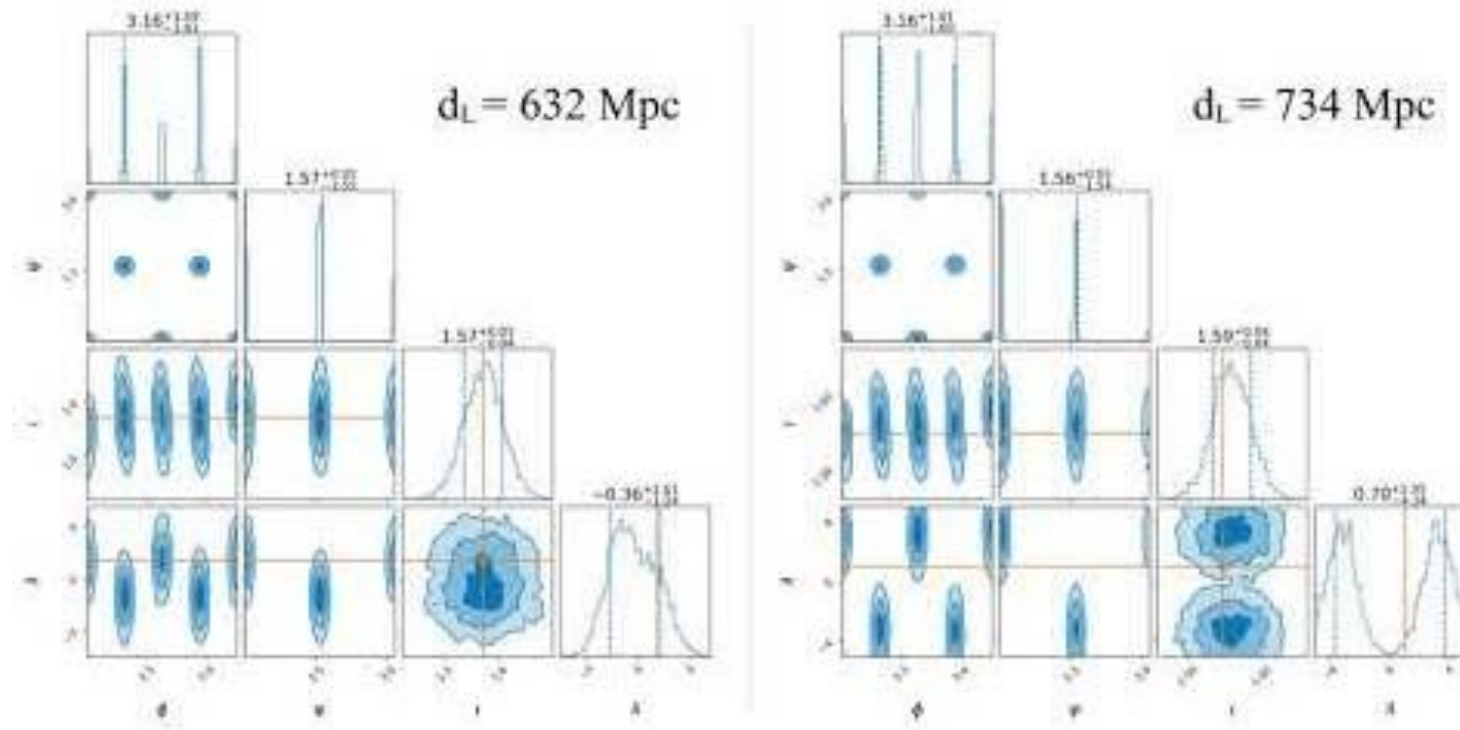


Figure 6. $(2, 2)$ -mode degeneracy. (*Left*) noiseless and (*Right*) with noise. The injected waveform used to generate these posterior distributions is sourced by non-spinning components with $M_{\text{tot}} = 60$ solar masses, $q = 1$, $\iota = \pi/2$, $\psi = 0$, $\phi_c = 0$, $\alpha = 0$, $\delta = 0$.

Noiseless

Noisy

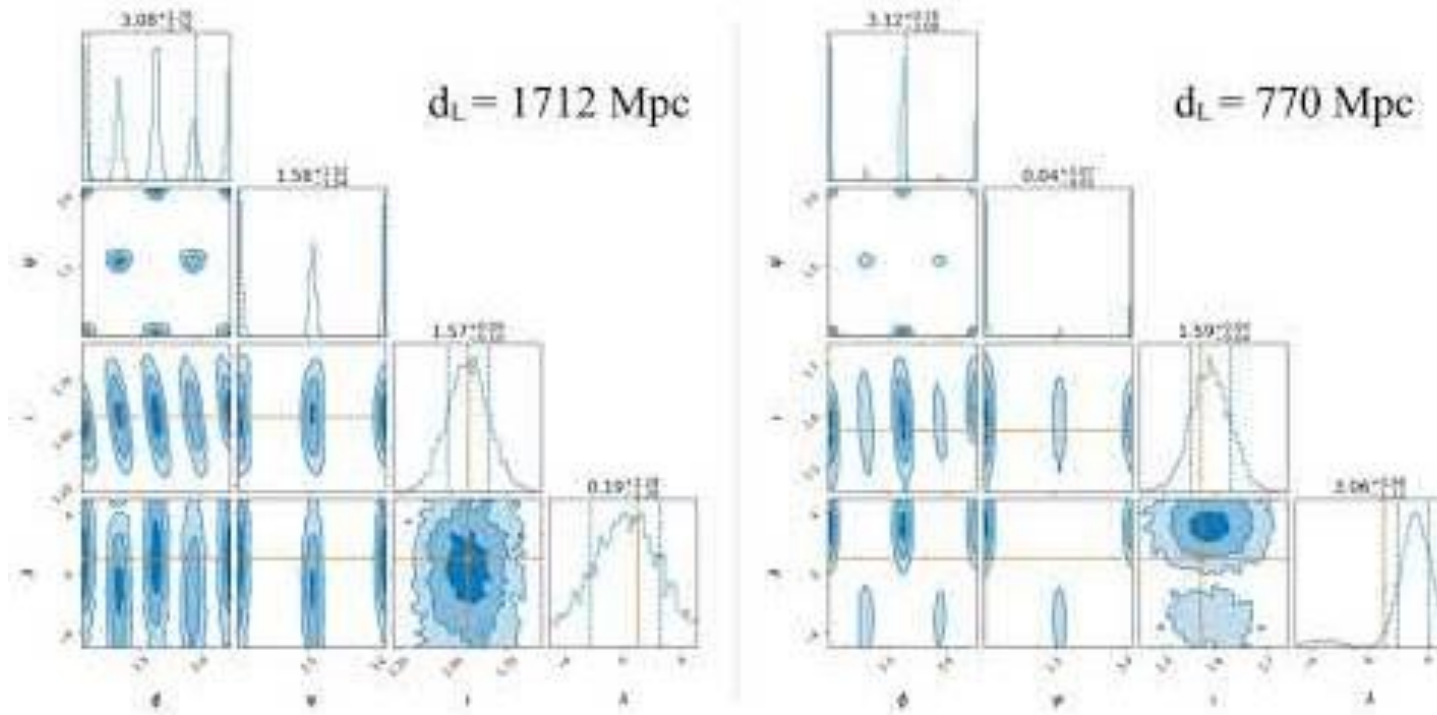


Figure 7. (Left) Noiseless signal with all modes included and (Right) noisy signal with all modes included. The injected waveform used to generate these posterior distributions is sourced by non-spinning components with $M_{\text{tot}} = 60$ solar masses, $q = 1$, $\iota = \pi/2$, $\psi = 0$, $\phi_c = 0$, $\alpha = 0$, $\delta = 0$.

The Real Deal!!!

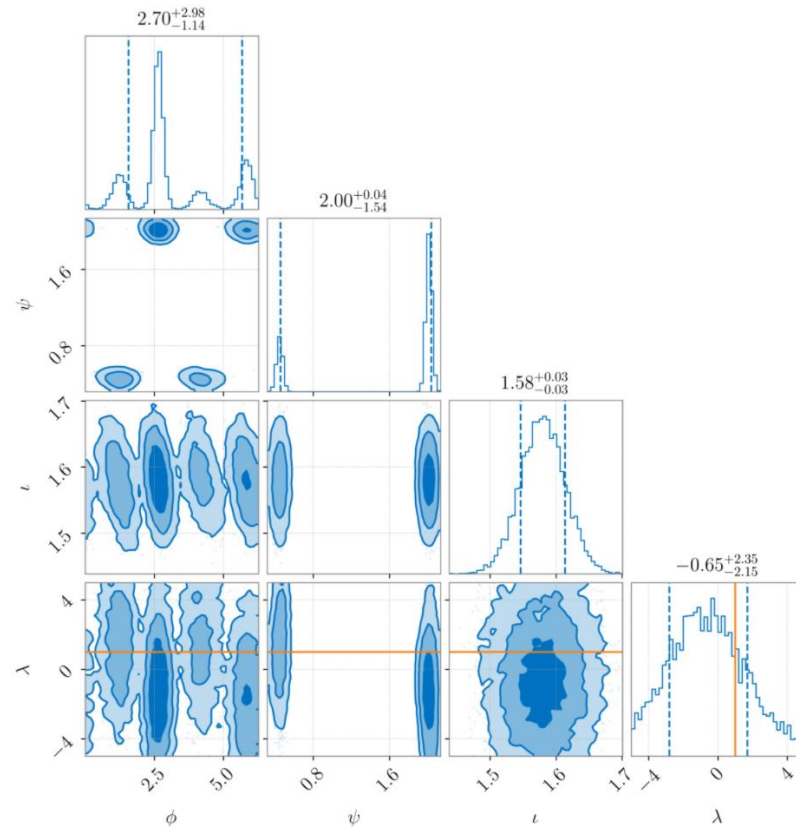


Figure 8. Strain data comes from GW150914. Non-inferred priors were retrieved from posterior samples obtained by memoryless parameter estimation. These values correspond to the maximum likelihood and are $M = 70.4$ solar masses, $q = 1.1$, $d_L = 342.2\text{Mpc}$, $\iota = 2.5$, $\psi = 0$, $\phi_c = 0$, $\alpha = \delta = 1.2$ (*Parameter values courtesy of Abbott et al. [10]*)

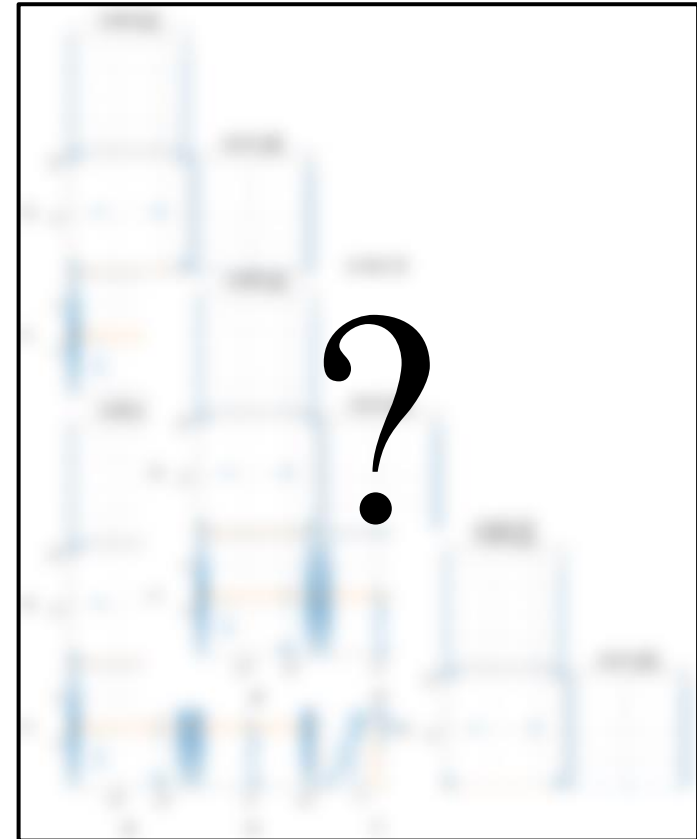
Future Work

Future Work

- Analyze remaining events
- Explore higher dimensional parameter spaces
- Incorporate full posterior samples for physical events

Later...

- Event stacking





Acknowledgements

Mentors

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Caltech





References

- [1] M. Favata. “The gravitational-wave memory effect.” *Classical Quantum Gravity*, 27(8): 2010.
- [2] C. Talbot et al. “Gravitational-wave memory: waveforms and phenomenology.” *Phys. Rev. D*, 98(6): 2018.
- [3] K. Thorne. “Gravitational-wave bursts with memory: The Christodoulou effect.” *Phys. Rev. D*, 45(2): 520-24: 1992.
- [4] R. Lea. DOI: <https://sciscomedia.co.uk/reverse-time>.
- [5] LIGO Caltech. DOI: <https://www.ligo.caltech.edu/video/BNS-merge>.
- [6] D. Garfinkle. “A Simple Estimate of Gravitational Wave Memory in Binary Black Hole Systems.” *Classical Quantum Gravity*, 33(17): 2016.
- [7] B. P. Abbott et al. *Astrophys. J. Lett.*, 892(L3): 2020.
- [8] NASA. DOI: lisa.jpl.nasa.gov/gallery/lisa-waves.
- [9] P. D. Lasky et al. “Detecting Gravitational-Wave Memory with LIGO: Implications of GW150914.” *Phys. Rev. Lett.*, 117(6): 2016.
- [10] B. P. Abbott et al. “GWTC-1: A Gravitational-Wave Transient Catalog of Compact Binary Mergers Observed by LIGO and Virgo During the First and Second Observing Runs.” *Phys. Rev. X*, 9(3): 2019.
- [11] C. M. Biwer et al. “PyCBC Inference: A Python-based parameter estimation toolkit for compact binary coalescence signals.” *PASP*, 131(996): 2019.
- [12] C. Talbot. “GWMemory.” DOI: github.com/colmtalbot/gwmemory.
- [13] G. Ashton. “BILBY.” DOI: lscsoft.docs.ligo.org/bilby/index.

Questions?