

Nanolayers Re-Thought

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- Coating Materials – the Titania Paradigm
- Goal and Background
- A QWL HR-Coating
- Modeling
- Questions
- Selecting Nanocomposite Materials
- Simulation Algorithm
- Selecting Nanocomposite Designs
- Selection Winners
- Deposition Accuracy and Robustness
- Conclusions

Coating Materials (Amorphous)

	n @ 1064nm	k @ 1064nm	Y [Gpa]	ϕ	ν
SiO ₂	1.4496 (1)	uncertain	72 (2)	$5.0 \cdot 10^{-5}$ (2,3)	0.17 (2)
Al ₂ O ₃	1.7545 (1)	uncertain	210 (2)	$2.4 \cdot 10^{-4}$ (2)	0.22 (2)
Ta ₂ O ₅	2.0760 (1)	uncertain	140 (2)	$4.72 \cdot 10^{-4}$ (3)	0.23 (2)
HfO ₂	2.0813 (1)	uncertain	380 (2)	$5.9 \cdot 10^{-4}$ (2)	0.2 (2)
ZrO ₂	2.1224 (1)	uncertain	200 (2)	$2.3 \cdot 10^{-4}$ (2)	0.27 (2)
Nb ₂ O ₅	2.2537 (1)	uncertain	68 (2)	$4.6 \cdot 10^{-4}$ (2)	0.20 (2)
TiO ₂	2.4789 (1)	uncertain	165 (3)	$1.4 \cdot 10^{-4}$ (3)	0.28 (2)

(1) <https://refractiveindex.info/>

(2) Franc et al., ET-021-09 (2009), [arxiv/papers/0912/0912.0107.pdf](https://arxiv.org/abs/0912.0107);
Flaminio et al., CQG 27 (2010) 083030

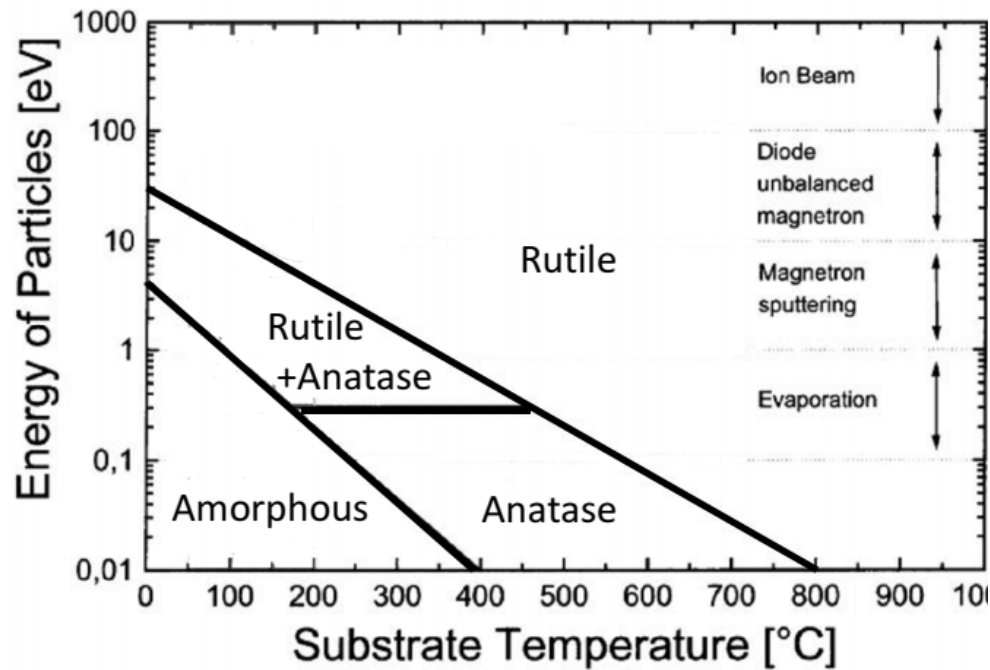
(3) Principe et al., Phys. Rev. D81 (2015) 022005
(consistent with Scott and MacKrone, Rev. Sci. Instr. 39 (1968) 821)

See also:

Granata et al., Phys. Rev. D93 (2016) 012007

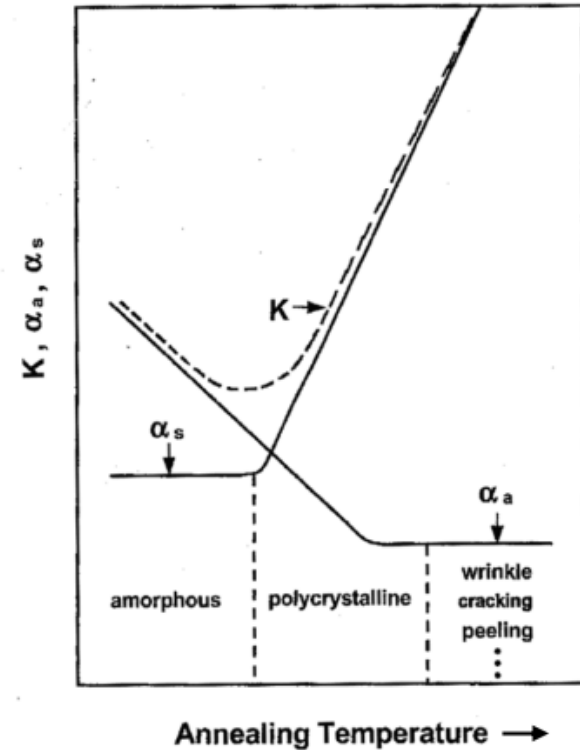
Vajente, LIGO-G1900400

Crystallization – the Titania Paradigm



J. Szczyrbowski, Surf. Coat. Technol. 112 (1999) 261–266.

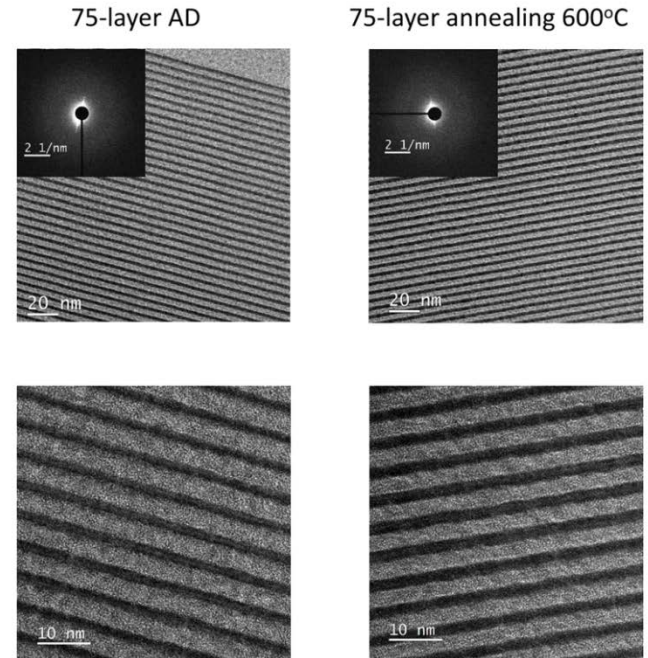
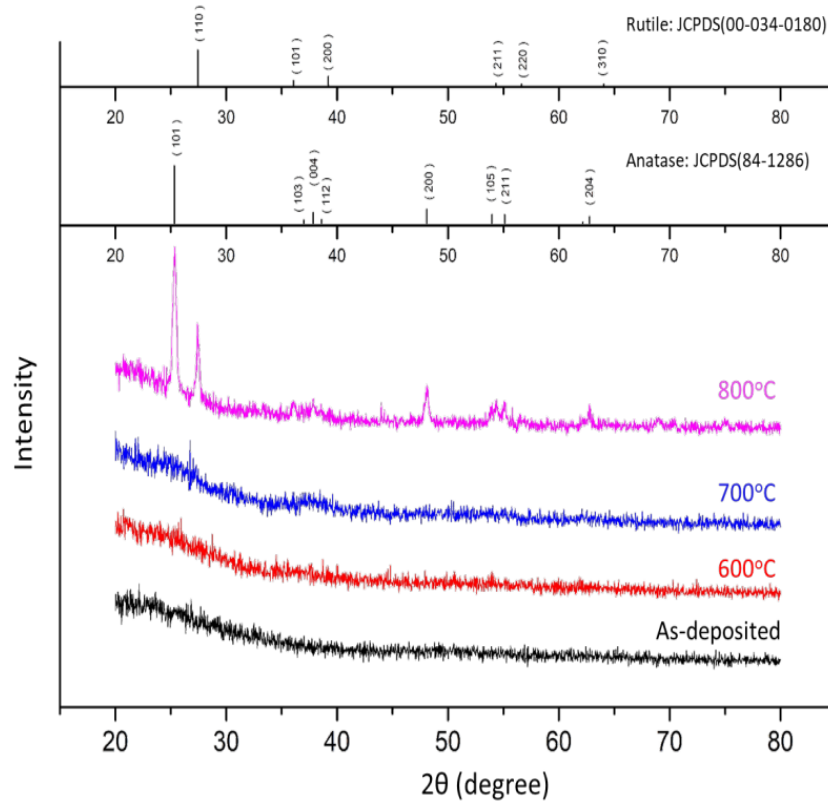
Extinction coefficient, and its absorption and scattering components, vs $T_{\text{annealing}}$.



W.H. Wang & S. Chao, Opt. Lett., 23 (1998) 1417

Silica/Titania Nanocomposite – Nanolayering hinders crystallization

[Chao et al., LIGO-G1900356]

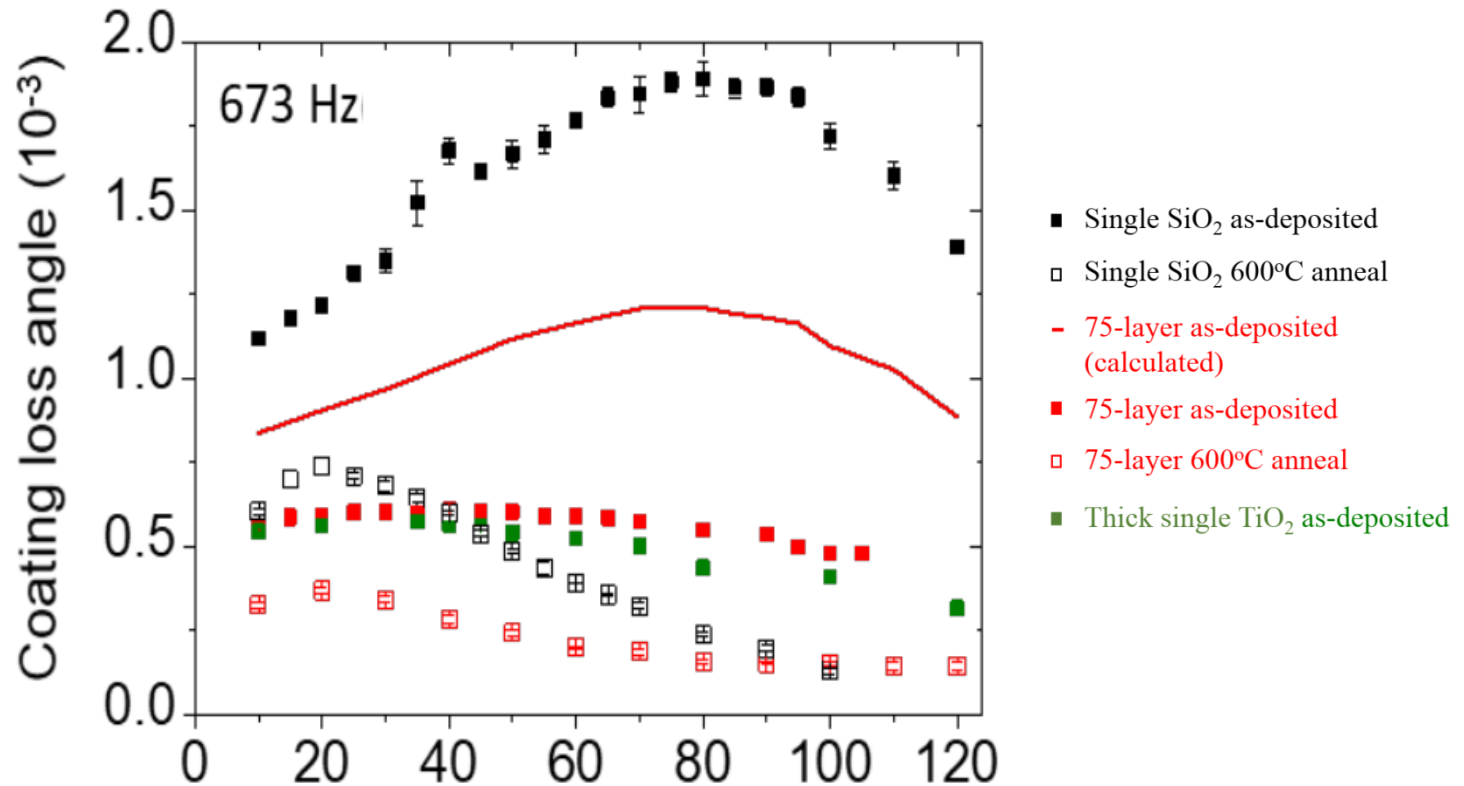


75-layer (TiO₂=1.8nmx38, SiO₂=3.6nmx37)
The film remain amorphous and the morphology is intact

➔ 1.8nm TiO₂ sustained to 700°C~800°C without crystallization. 75-layer (TiO₂=1.8nmx38, SiO₂=3.6nmx37)

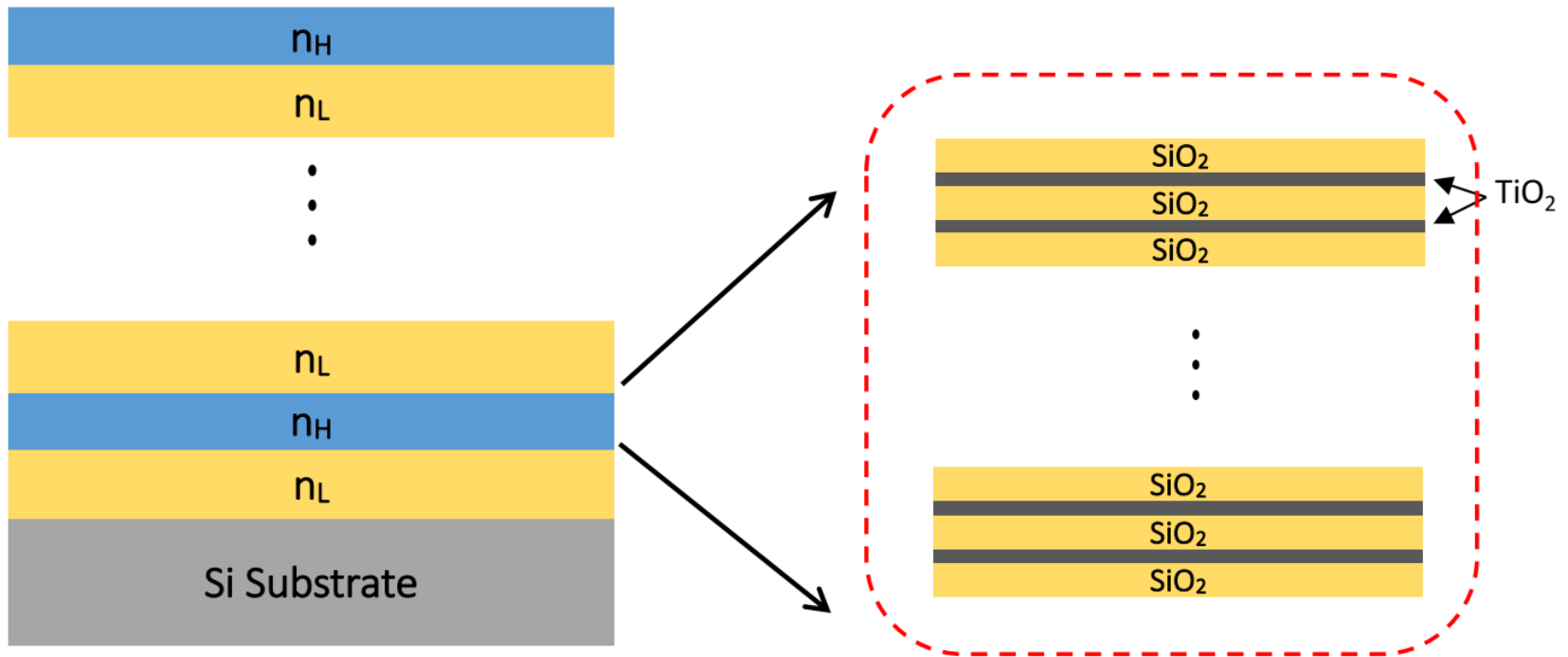
Nanolayers : Background, contd.

[Chao et al., LIGO-G1900356]



- The cryogenic loss of the 75-layer nano-layer (TiO₂=1.8nm x 38, SiO₂=3.6 nm x 37) was reduced after 600°C anneal to below that of the single SiO₂ annealed at 600°C and the as-deposited single TiO₂.
- The room temperature loss of the 75-layer nano-layer was reduced after 600°C anneal from 9×10^{-4} down to 1×10^{-4} at ~ 100 Hz.

Goal : a Nanolayer Based HR Coating



Rationale: nice properties of nanolayered materials :

- Suppression of Silica cryopeak in mechanical loss [Kuo et al. Opt. Lett. 44 (2019) 247]
- Inhibition of crystallization at increasing annealing-T [Pan et al. Opt. Exp. 22 (2014) 29847]

In the following we stick to the case where the coating low-index material is Silica.
For cryogenic operation Silica/Alumina nanocomposites could be a nice alternative ...

Nanolayers are *routinely deposited* to make X-Ray Mirrors

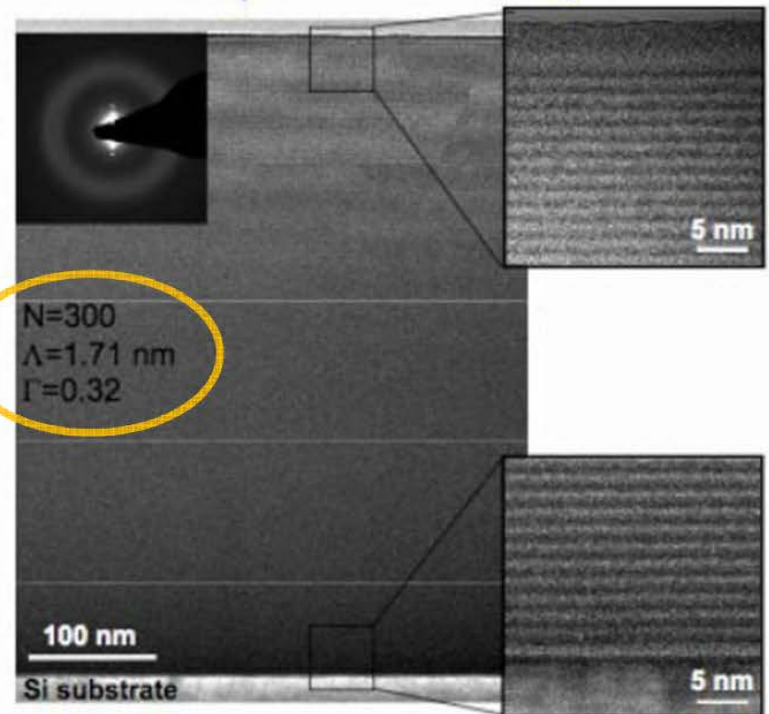
Interference mirrors consisting of hundreds/thousands of nm scale layers, with sub - nm precision [see, e.g., Proc . 10th PXRMS Conf. (2008)] , using

- Interleaved nm-scale “buffering” layers to prevent crystallization & maintain flatness [E. Gullikson, Proc. 8th PXRMS (2006)]
- Ion assisted (modulated) magnetron sputtering [N. Ghafoor et al., Thin Sol. Films 516 (2008) 982]



Control of stress, crystallite size, and roughness [D.L. Windt, Proc. SPIE (2007) vol 6688]

Interleaved B₄C- Cr/Sc multilayer



See also [R. DeSalvo, LIGO-G080106] for a survey.

Modeling : HR Multilayers

Simplest Option: QWL :

- Requires *minimum number* of LH doublets for a given transmittance.
- QWL is conservative (can be improved) in terms of noise.

Transmittance

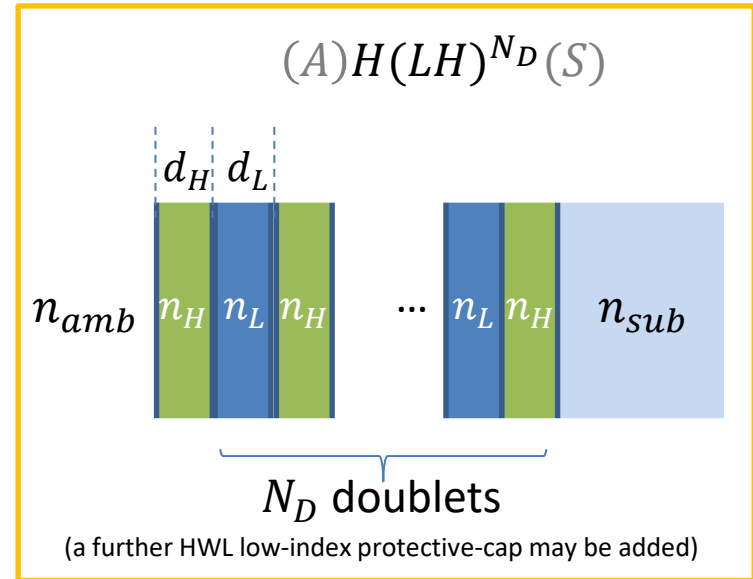
$$\Gamma = \frac{1 - \left(\frac{n_H}{n_L}\right)^{2N_D+2} \frac{n_L^2}{n_{amb}n_{sub}}}{1 + \left(\frac{n_H}{n_L}\right)^{2N_D+2} \frac{n_L^2}{n_{amb}n_{sub}}}, \quad \tau_P = 1 - |\Gamma|^2$$

index ratio
(contrast)

number of doublets

$\cong n_L$, typically

→ yields N_D from prescribed τ_P and given contrast



Coating Loss Angle (Thermal (Brownian) Noise PSD) can be written

$$\phi_c = \frac{1}{4\pi^{1/2}} \frac{\lambda_0 \phi_L}{w n_L} \left(\frac{Y_L}{Y_S} + \frac{Y_S}{Y_L} \right) \left[N_d + \frac{n_L \phi_H \left(\frac{Y_H}{Y_S} + \frac{Y_S}{Y_H} \right)}{n_H \phi_L \left(\frac{Y_L}{Y_S} + \frac{Y_S}{Y_L} \right)} (1 + N_d) \right]$$

blows up linearly with N_d

depends on choice of L-material only

key quantity, depends on choice of H-material

Modeling : Nanolayered Composites

- For simplicity, restrict to *binary* nanolayered composites using two materials with parameters $\{\tilde{n}_{L,H}, \tilde{Y}_{L,H}, \tilde{\phi}_{L,H}\}$.

▶
$$n_{eff} = [r_H \tilde{n}_H^2 + (1 - r_H) \tilde{n}_L^2]^{1/2}$$

 Drude's formula

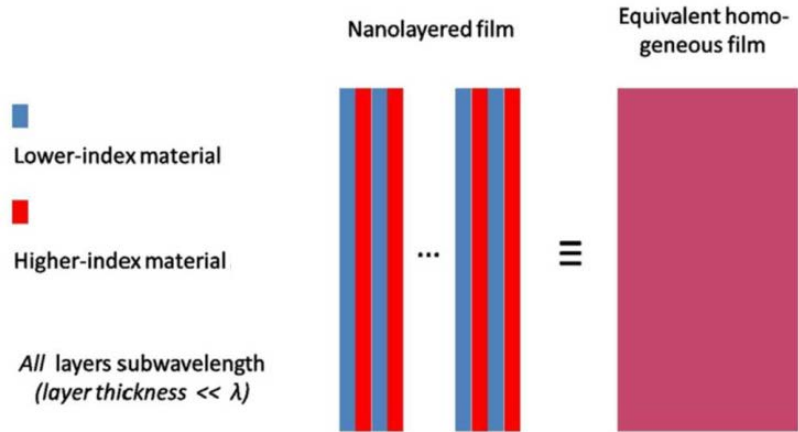
(normal incidence, $\delta_{L,H} \ll \lambda$)

$$Y_{eff}^\perp = [r_H / \tilde{Y}_H + (1 - r_H) / \tilde{Y}_L]^{-1}$$

 Reuss formula

$$Y_{eff}^\parallel = r_H \tilde{Y}_H + (1 - r_H) \tilde{Y}_L$$

 Voigt formula



Let :

$$r_H = \frac{\delta_H}{\delta_L + \delta_H}$$

thickness fraction

total metric thicknesses of high (δ_H) and low (δ_L) index nanocomposite constituents

▶
$$\phi_{eff} \left(\frac{Y_{eff}}{Y_s} + \frac{Y_s}{Y_{eff}} \right) = \left(\frac{\tilde{Y}_H}{Y_s} + \frac{Y_s}{\tilde{Y}_H} \right) r_H \tilde{\phi}_H + \left(\frac{\tilde{Y}_L}{Y_s} + \frac{Y_s}{\tilde{Y}_L} \right) (1 - r_H) \tilde{\phi}_L$$

(mere consequence of (simple) coating noise formula)

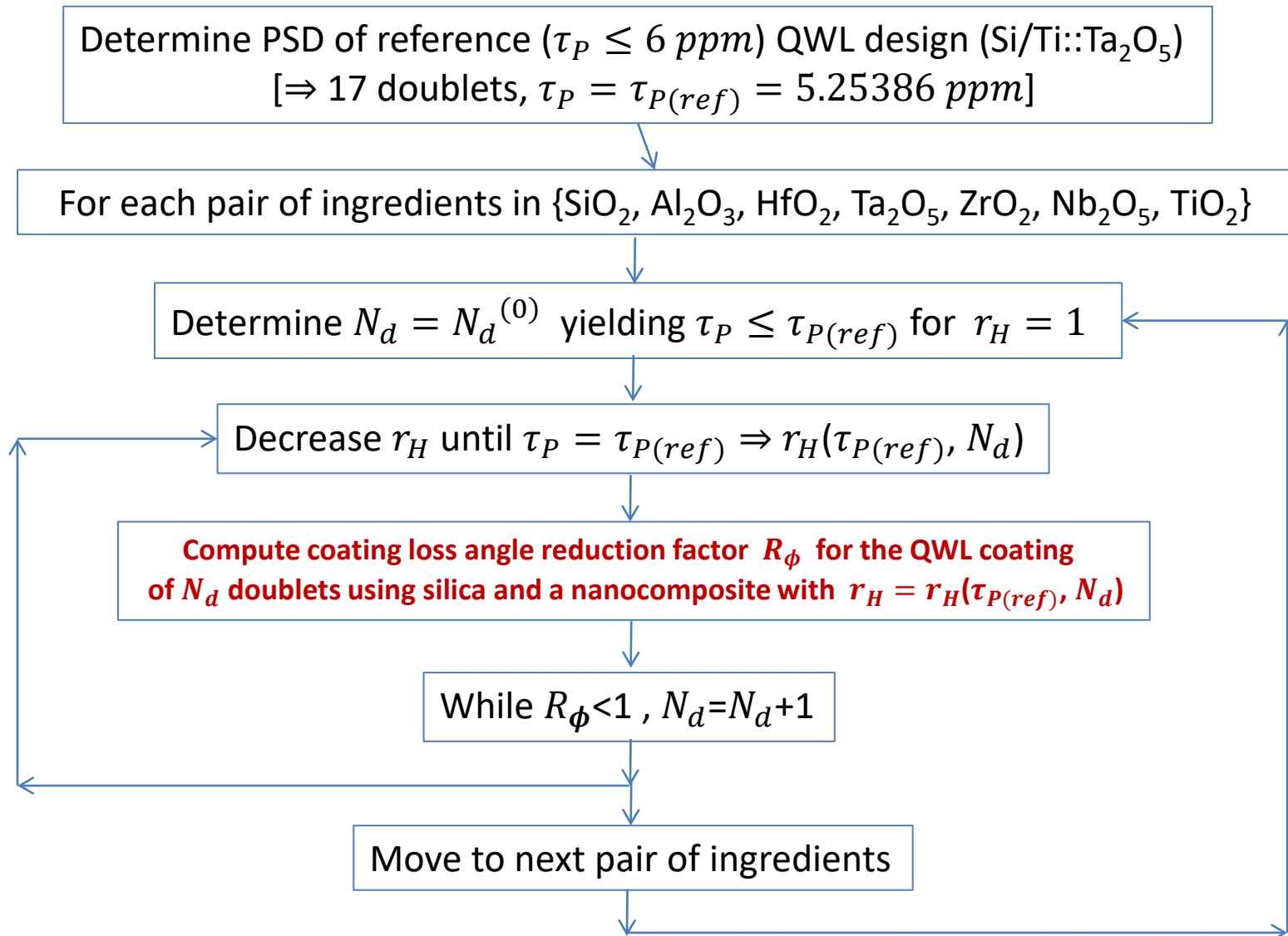
Questions – Nanolayers Rethought

- Which materials are *more promising* in terms of noise reduction when used to produce (binary) high-index nanolayered films ?
- Which nanolayer *designs* are *more feasible* for a given material pair ?
- Blind trial-and-error would be *impractically time (and money) consuming*. Preliminary simulations may/should be used to provide guidelines and priorities.



Selecting Nanocomposite Materials

Simulation Algorithm



Selecting Nanocomposite Materials

Simulation Results

Noise PSD (and Coating Loss Angle) Reduction Factor compared to Reference (Si/Ti::Ta, 5.32ppm@1064nm)							
	SiO ₂	Al ₂ O ₃	HfO ₂	Ta ₂ O ₅	ZrO ₂	Nb ₂ O ₅	TiO ₂
SiO ₂	x	>1	>1	>1	>0.794	>0.792	>0.309
Al ₂ O ₃		x	>1	>1	>0.833	>0.796	>0.352
HfO ₂			x	>1	>1	>0.849	>0.663
Ta ₂ O ₅				x	>1	>0.802	>0.415
ZrO ₂					x	>0.791	>0.369
Nb ₂ O ₅						x	>0.433
TiO ₂							x

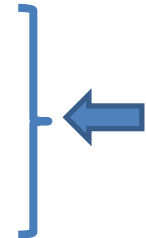
Note: Changing the noise PSD by a factor ρ yields an event rate boost by $\rho^{-3/2}$

Simulation Results

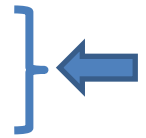
a Closer Look

using glass formers

QWL HR Coating – Silica (L) / Silica-Titania nanolayered composite (H)				
#of doublets in Coating	Silica Fraction in nanocomposite	Effective index of nanocomposite	Coating power transmittance	Noise PSD Reduction
12	0.0882959	2.40581	5.25386	0.308983
13	0.188226	2.32031	5.25386	0.322875
14	0.269172	2.24867	5.25386	0.337020
15	0.335952	2.1878	5.25386	0.351363
16	0.391907	2.13547	5.25386	0.365862
17	0.439421	2.09	5.25386	0.380487



QWL HR Coating – Silica (L) / Alumina-Titania nanolayered composite (H)				
#of doublets in Coating	Alumina Fraction in nanocomposite	Effective index of nanocomposite	Coating power transmittance	Noise PSD Reduction
12	0.116424	2.40581	5.25386	0.352285
13	0.248188	2.32031	5.25386	0.425948
14	0.35492	2.24867	5.25386	0.499978
15	0.442974	2.1878	5.25386	0.574344
16	0.516755	2.13547	5.25386	0.649013
17	0.579404	2.09	5.25386	0.723955



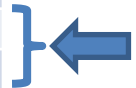
Arrows point to nanocomposites with noise $PSD \leq 0.5 PSD_{REF}$

Simulation Results

a Closer Look, contd.

not using glass formers

QWL HR Coating – Silica (L) / Zirconia-Titania nanolayered composite (H)				
#of doublets in Coating	Zirconia Fraction in nanocomposite	Effective index of nanocomposite	Coating power transmittance	Noise PSD Reduction
12	0.217655	2.40581	5.25386	0.368841
13	0.463991	2.32031	5.25386	0.465358
14	0.663526	2.24867	5.25386	0.562285
15	0.828143	2.1878	5.25386	0.659601
16	0.966077	2.13547	5.25386	0.757277



QWL HR Coating – Silica (L) / Tantalum-Titania nanolayered composite (H)				
#of doublets in Coating	Tantalum Fraction in nanocomposite	Effective index of nanocomposite	Coating power transmittance	Noise PSD Reduction
12	0.194551	2.40581	5.25386	0.415789
13	0.414737	2.32031	5.25386	0.577109
14	0.593092	2.24867	5.25386	0.738964
15	0.740235	2.1878	5.25386	0.901357



QWL HR Coating – Silica (L) / Niobia-Titania nanolayered composite (H)				
#of doublets in Coating	Niobia Fraction in nanocomposite	Effective index of nanocomposite	Coating power transmittance	Noise PSD Reduction
12	0.334997	2.40581	5.25386	0.433520
13	0.714136	2.32031	5.25386	0.619317

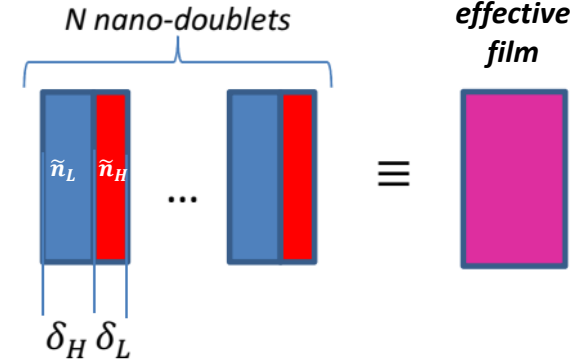


Arrows point to nanocomposites with noise $PSD \leq 0.5 PSD_{REF}$

Selecting Nanocomposite Design

- For simplicity, restrict to composites made of identical nanoscale-doublets. These are entirely specified by a triplet (δ_L, δ_H, N) .
- To any given value of the effective index $n_{eff} \in (\tilde{n}_L, \tilde{n}_H)$ corresponds the ratio

$$\frac{\delta_L}{\delta_H} = \left(\frac{\tilde{n}_H^2 - n_{eff}^2}{n_{eff}^2 - \tilde{n}_L^2} \right) \quad (1)$$



- Prescribing the optical thickness z of the nanolayered film (in units of the local wavelength) enforces the further condition

$$N(\delta_H + \delta_L) = z \frac{\lambda_0}{n_{eff}} \quad (2)$$

Equations (1) and (2) determine *an infinite set* of nanolayer designs (δ_L, δ_H, N) yielding *the same* effective index n_{eff} and optical thickness z . Larger N correspond to *thinner* nano layers. The set of feasible designs is determined by the machine-dependent minimum deposition thickness and the maximum thickness of the material(s) prone to crystallization.

Note: inaccuracies in the individual nanolayer thicknesses *have no effect*, insofar as the total thickness fraction is preserved, and all individual nanolayers are much thinner than the (local) wavelength.

Selecting a Nanodesign: Silica/Titania

➔ Select annealing-tolerant design featuring smallest R_{PSD} and minimum N , subject to $\delta_L \geq 0.9nm$, $\delta_H \leq 2nm$ (highlighted in yellow); select *easiest* one (circled in red)

$r_L = 0.0882959$ ($R_{PSD} = 0.30983$)			$r_L = 0.188226$ ($R_{PSD} = 0.322875$)			$r_L = 0.269172$ ($R_{PSD} = 0.33702$)			$r_L = 0.335952$ ($R_{PSD} = 0.351363$)			$r_L = 0.391907$ ($R_{PSD} = 0.365862$)			$r_L = 0.439421$ ($R_{PSD} = 0.3808437$)		
N	$\delta_L[nm]$	$\delta_H[nm]$	N	$\delta_L[nm]$	$\delta_H[nm]$	N	$\delta_L[nm]$	$\delta_H[nm]$	N	$\delta_L[nm]$	$\delta_H[nm]$	N	$\delta_L[nm]$	$\delta_H[nm]$	N	$\delta_L[nm]$	$\delta_H[nm]$
7	1.39464	14.4005	18	1.19879	5.17009	28	1.13717	3.08754	27	1.51282	2.99026	25	1.95268	3.02983	23	2.43158	3.10202
8	1.22031	12.6004	19	1.13570	4.89798	29	1.09796	2.98108	28	1.45879	2.88347	26	1.87758	2.91330	24	2.33026	2.97277
9	1.08472	11.2004	20	1.07891	4.65308	30	1.06136	2.88171	29	1.40848	2.78404	27	1.80804	2.80540	25	2.23705	2.85386
10	0.97625	10.0803	21	1.02754	4.43151	31	1.02713	2.78875	30	1.36153	2.69123	28	1.74347	2.70521	26	2.15101	2.74409
			22	0.98083	4.23008	32	0.99503	2.70160	31	1.31761	2.60442	29	1.68335	2.61192	27	2.07135	2.64246
									32	1.27644	2.52303	30	1.62724	2.52486	28	1.99737	2.54809
									33	1.23776	2.44658	31	1.57474	2.44341	29	1.92849	2.46022
									34	1.20135	2.37462	32	1.52553	2.36705	30	1.86421	2.37821
									35	1.16703	2.30677	33	1.47930	2.29533	31	1.80407	2.30150
									36	1.13461	2.24270	34	1.43580	2.22782	32	1.74770	2.22958
									37	1.10395	2.18208	35	1.39477	2.16416	33	1.69474	2.16201
									38	1.07490	2.12466	36	1.35603	2.10405	34	1.64489	2.09842
									39	1.04733	2.07018	37	1.31938	2.04718	35	1.59789	2.03847
									40	1.02115	2.01843	38	1.28466	1.99331	36	1.55351	1.98184
									41	0.996245	1.96920	39	1.25172	1.94220	37	1.51152	1.92828
												40	1.22043	1.89364	38	1.47175	1.87754
												41	1.19066	1.84746	39	1.43401	1.82940
												42	1.16231	1.80347	40	1.39816	1.78366
												43	1.13528	1.76153	41	1.36406	1.74016
												44	1.10948	1.72149	42	1.33158	1.69872
												45	1.08482	1.68324	43	1.30061	1.65922
												46	1.06124	1.64665	44	1.27105	1.62151
												47	1.03866	1.61161	45	1.24281	1.58548
												48	1.01702	1.57804	46	1.21579	1.55101
												49	0.996267	1.54583	47	1.18992	1.51801
												48	1.16513	1.48638	48	1.16513	1.48638
												49	1.14135	1.45605	49	1.14135	1.45605
												50	1.11853	1.42693	50	1.11853	1.42693
												51	1.09659	1.39895	51	1.09659	1.39895
												52	1.07551	1.37205	52	1.07551	1.37205
												53	1.05521	1.34616	53	1.05521	1.34616
												54	1.03567	1.32123	54	1.03567	1.32123
												55	1.01684	1.29721	55	1.01684	1.29721
												56	0.99868	1.27404	56	0.99868	1.27404

QWL HR Coating – Silica (L) / Silica-Titania nanolayered composite (H)				
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Expected to crystallize before reaching $T_{ann} = 650C$

Expected to remain amorphous at $T_{ann} = 650C$



Selecting a Nanodesign : Alumina/Titania

$r_L = 0.116424 (R_{PSD} = 0.35492)$			$r_L = 0.248188 (R_{PSD} = 0.425948)$			$r_L = 0.354920 (R_{PSD} = 0.499978)$		
N	$\delta_L [nm]$	$\delta_H [nm]$	N	$\delta_L [nm]$	$\delta_H [nm]$	N	$\delta_L [nm]$	$\delta_H [nm]$
9	1.43028	10.8548	25	1.13809	3.44750	25	1.67937	3.05231
10	1.28725	9.76933	26	1.09432	3.31491	26	1.61478	2.93492
11	1.17023	8.88121	27	1.05379	3.19213	27	1.55497	2.82622
12	1.07271	8.14111	28	1.01615	3.07813	28	1.49944	2.72528
13	0.99019	7.51487	29	0.98111	2.97199	29	1.44773	2.63131
						30	1.39947	2.54360
						31	1.35433	2.46154
						32	1.31201	2.38462
						33	1.27225	2.31236
						34	1.23483	2.24435
						35	1.19955	2.18022
						36	1.16623	2.11966
						37	1.13471	2.06237
						38	1.10485	2.00810
						39	1.07652	1.95661
						40	1.04961	1.90770
						41	1.02401	1.86117
						42	0.99962	1.81685

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Selecting a Nanodesign : Zirconia/Titania

$r_L = 0.217655$ ($R_{PSD} = 0.368841$)			$r_L = 0.463991$ ($R_{PSD} = 0.464358$)		
N	$\delta_L [nm]$	$\delta_H [nm]$	N	$\delta_L [nm]$	$\delta_H [nm]$
21	1.14596	4.11907	24	2.21633	2.56034
22	1.09387	3.93184	25	2.12767	2.45792
23	1.04631	3.76089	26	2.04584	2.36339
24	1.00272	3.60419	27	1.97007	2.27585
25	0.96261	3.46002	28	1.89971	2.19457
			29	1.83420	2.11890
			30	1.77306	2.04827
			31	1.71587	1.98220
			32	1.66225	1.92025
			33	1.61187	1.86206
			34	1.56447	1.80730
			35	1.51977	1.75566
			36	1.47755	1.70689
			37	1.43762	1.66076
			38	1.39979	1.61705
			39	1.36389	1.57559
			40	1.32980	1.53620
			41	1.29736	1.49873
			42	1.26647	1.46305
			43	1.23702	1.42902
			44	1.20891	1.39655
			45	1.18204	1.36551
			46	1.15634	1.33583
			47	1.13174	1.30741
			48	1.10816	1.28017
			49	1.08555	1.25404
			50	1.06384	1.22896
			51	1.04298	1.20486
			52	1.02292	1.18169
			53	1.00362	1.15940
			54	0.98503	1.13793

Expected to crystallize before reaching $T_{ann} = 650C$

Expected to remain amorphous at $T_{ann} = 650C$

QWL HR Coating – Silica (L) / Zirconia-Titania nanolayered composite (H)				
#of doublets in Coating	Zirconia Fraction in nanocomposite	Effective index of nanocomposite	Coating power transmittance	Noise PSD Reduction
12	0.217655	2.40581	5.25386	0.368841
13	0.463991	2.32031	5.25386	0.465358
14	0.663526	2.24867	5.25386	0.562285
15	0.828143	2.1878	5.25386	0.659601
16	0.966077	2.13547	5.25386	0.757277

➔ Select annealing-tolerant design featuring smallest R_{PSD} and minimum N , subject to $\delta_L \geq 0.9nm$, $\delta_H \leq 2nm$ (highlighted in yellow); select *easiest* one (circled in red)

Selecting a Nanodesign : Tantalum/Titania

$r_L = 0.194551$ ($R_{PSD} = 0.415788$)

N	δ_L [nm]	δ_H [nm]
18	1.19504	4.94751
19	1.13214	4.68711
20	1.07553	4.45276
21	1.02432	4.24072
22	0.97775	4.04796

$r_L = 0.414737$ ($R_{PSD} = 0.577109$)

N	δ_L [nm]	δ_H [nm]
29	1.63950	2.3136
30	1.58485	2.23648
31	1.53372	2.16434
32	1.48580	2.09670
33	1.44077	2.03317
34	1.39840	1.97337
35	1.35844	1.91698
36	1.32071	1.86373
37	1.28501	1.81336
38	1.25120	1.76564
39	1.21911	1.72037
40	1.18864	1.67736
41	1.15965	1.63645
42	1.13203	1.59749
43	1.10571	1.56034
44	1.08058	1.52487
45	1.05657	1.49099
46	1.03360	1.45858
47	1.01161	1.42754
48	0.99053	1.39780

Expected to crystallize before reaching $T_{ann} = 650C$

Expected to remain amorphous at $T_{ann} = 650C$

QWL HR Coating – Silica (L) / Tantalum-Titania nanolayered composite (H)				
#of doublets in Coating	Tantala Fraction in nanocomposite	Effective index of nanocomposite	Coating power transmittance	Noise PSD Reduction
12	0.194551	2.40581	5.25386	0.415789
13	0.414737	2.32031	5.25386	0.577109
14	0.593092	2.24867	5.25386	0.738964
15	0.740235	2.1878	5.25386	0.901357

➡ Select annealing-tolerant design featuring smallest R_{PSD} and minimum N , subject to $\delta_L \geq 0.9nm$, $\delta_H \leq 2nm$ (highlighted in yellow); select *easiest* one (circled in red)

Note: for Tantalum /Titania $R_{PSD} \cong 0.58 > 0.5$.

Selecting a Nanodesign: Niobia/Titania

$r_L = 0.334997$ ($R_{PSD} = 0.433520$)				$r_L = 0.714136$ ($R_{PSD} = 0.619317$)			
N	δ_L [nm]	δ_H [nm]		N	δ_L [nm]	δ_H [nm]	
32	1.15748	2.29771		15	5.45790	2.18476	
33	1.12240	2.22808		16	5.11678	2.04821	
34	1.08939	2.16255		17	4.81580	1.92773	
35	1.05826	2.10076		18	4.54825	1.82063	
36	1.02887	2.04240		19	4.30887	1.72481	
37	1.00106	1.98720		20	4.09343	1.63857	
38	0.97472	1.93491		21	3.89850	1.56054	
				22	3.72130	1.48961	
				23	3.55950	1.42484	
				24	3.41119	1.36547	
				25	3.27474	1.31086	
				26	3.14879	1.26044	
				27	3.03217	1.21376	
				28	2.92388	1.17041	
				29	2.82305	1.13005	
				30	2.72895	1.09238	
				31	2.64092	1.05714	
				32	2.55839	1.02411	
				33	2.48086	0.99307	

Expected to remain amorphous at $T_{ann} = 650C$

QWL HR Coating – Silica (L) / Niobia-Titania nanolayered composite (H)				
#of doublets in Coating	Niobia Fraction in nanocomposite	Effective index of nanocomposite	Coating power transmittance	Noise PSD Reduction
12	0.334997	2.40581	5.25386	0.433520
13	0.714136	2.32031	5.25386	0.619317

➔ Select annealing-tolerant design featuring smallest R_{PSD} and minimum N , subject to $\delta_L \geq 0.9nm$, $\delta_H \leq 2nm$ (highlighted in yellow); select *easiest* one (circled in red)

Selection Winners

$$(\delta_L, \delta_H)^{N_N} [\delta_{SiO_2}, (\delta_L, \delta_H)^{N_N}]^{N_D}$$

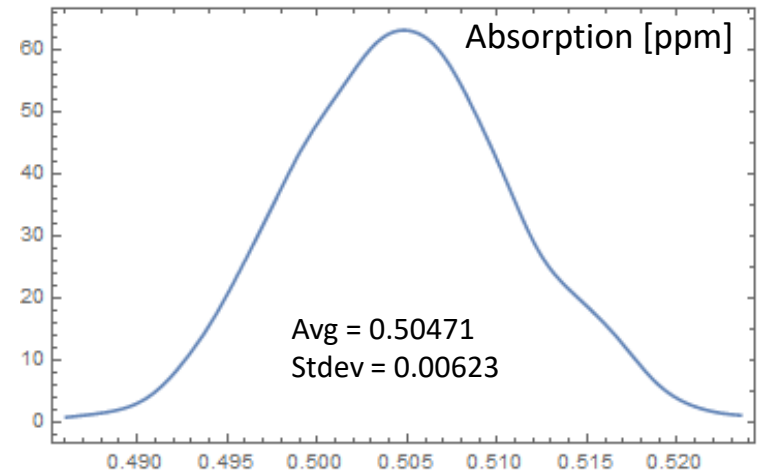
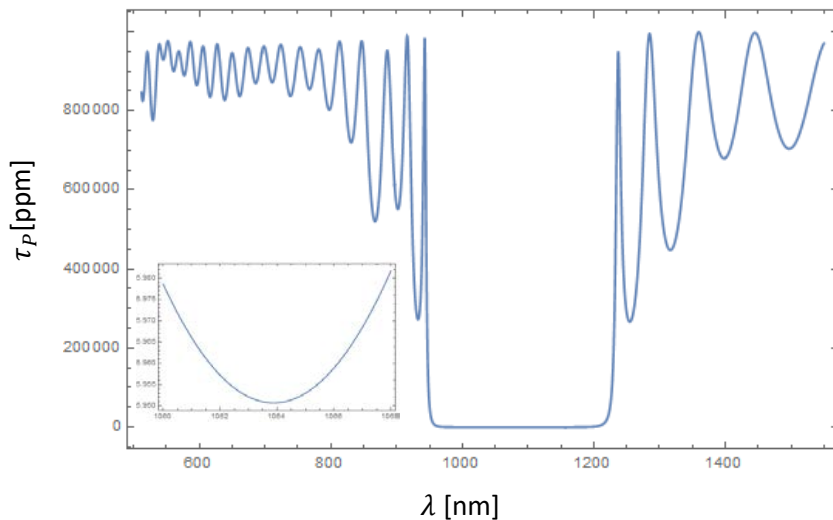
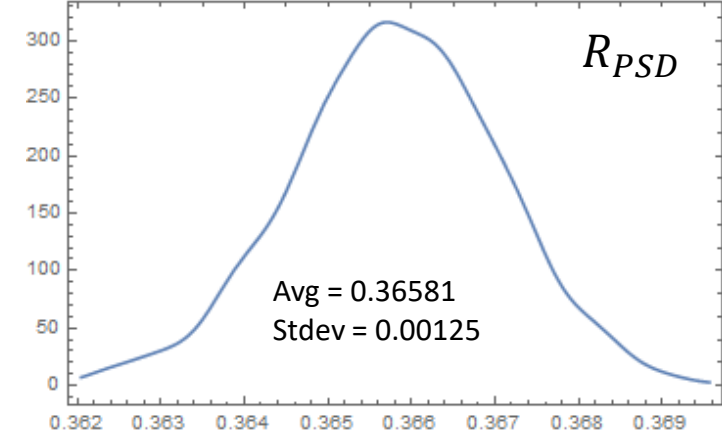
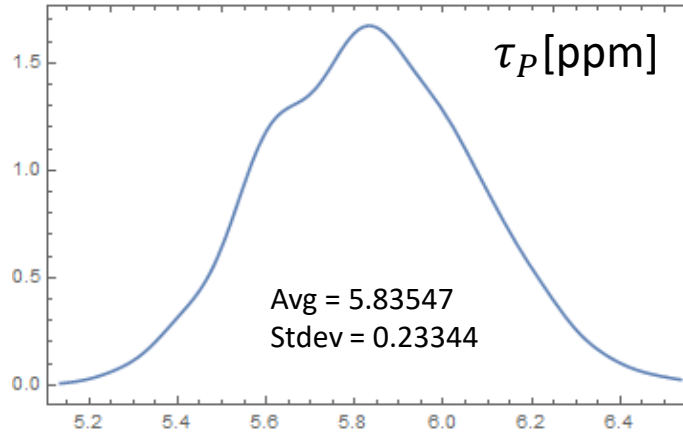
	Silica-Titania	Niobia-Titania	Zirconia-Titania	Alumina-Titania	Tantala-Titania
τ_P [ppm]	5.25386	5.25386	5.25386	5.25386	5.25386
R_{PSD}	0.36586	0.43352	0.464358	0.49998	0.57711
N_D	16	12	13	14	13
N_N	38	37	31	39	34
δ_L [nm]	1.28466	1.00106	1.71587	1.07652	1.39840
δ_H [nm]	1.99331	1.98720	1.98220	1.95661	1.97337
δ_{SiO_2} [nm]	183.499	183.499	183.499	183.499	183.499

Note: Changing the noise PSD by a factor ρ yields an event rate boost by $\rho^{-3/2}$

Deposition Accuracy and Robustness

Assumption: i.i.d. Gaussian thickness errors with 0 avg. and .3nm std. deviation on each layer. 1000 trial-depositions.

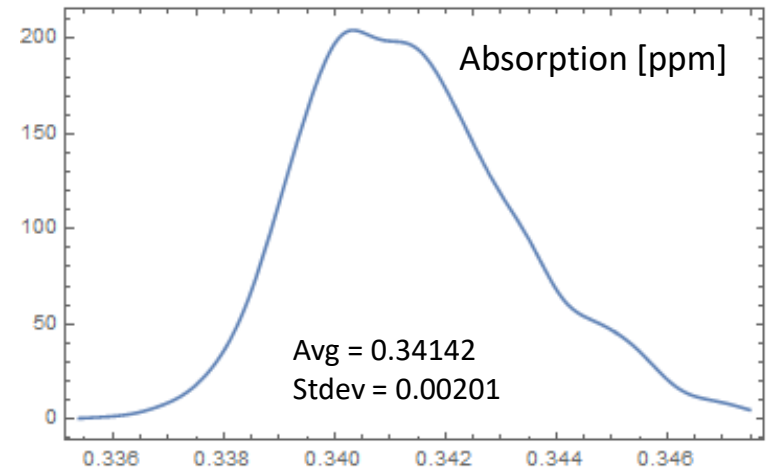
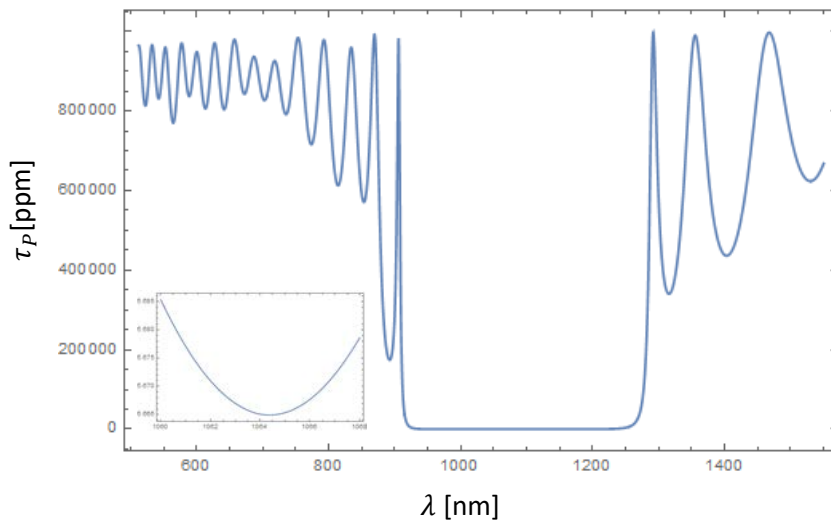
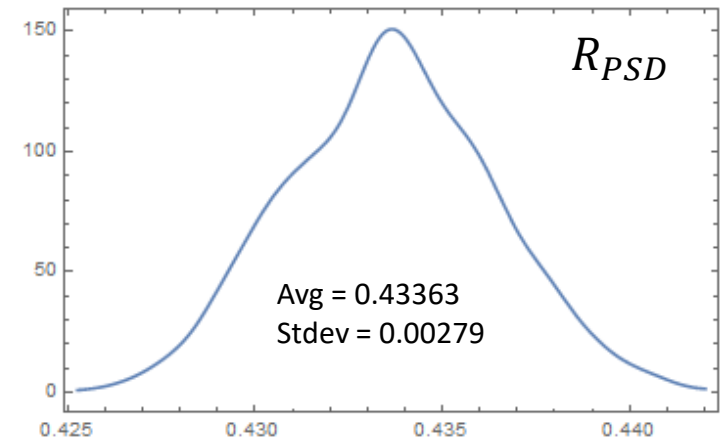
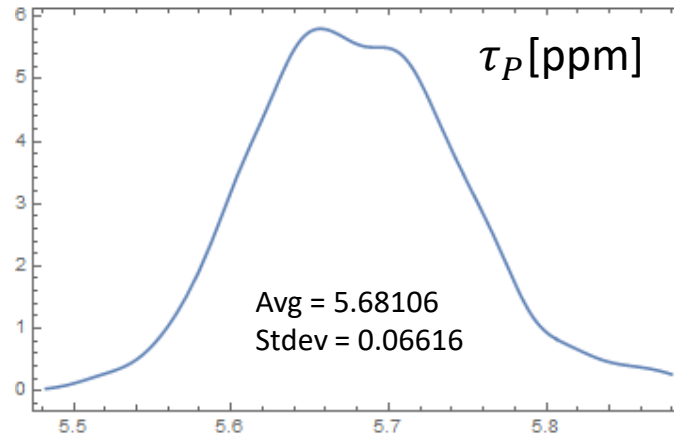
	Silica-Titania
τ_P [ppm]	5.25386
R_{PSD}	0.36586
N_D	16
N_N	38
δ_L [nm]	1.28466
δ_H [nm]	1.99331
δ_{SiO_2} [nm]	183.499



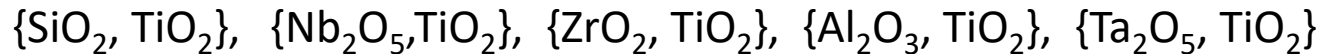
Deposition Accuracy and Robustness, contd.

Assumption: i.i.d. Gaussian thickness errors with 0 avg. and .3nm std. deviation on each layer. 1000 trial-depositions

	Niobia-Titania
τ_P [ppm]	5.25386
R_{PSD}	0.43352
N_D	12
N_N	37
δ_L [nm]	1.00106
δ_L [nm]	1.98720
δ_{SiO_2} [nm]	183.499



- The nanolayered (binary) composites that may be used in place of the high index material in a QWL coating with the same τ_P as the reference Si/Ti::Ta2O5 design, to obtain $PSD \leq 0.5 PSD_{REF}$ are (best to worst)



- For each of these material-pairs there's at least one design that (fiducially) should be both free from crystallization upon annealing up to 650C, and feasible/easy to deposit (sufficiently thick nanolayers, including several atomic layers, reasonably small number of nanolayers)
- The number of *promising/easy* nanolayered prototypes (and QWL HR coatings) is basically 5 for the considered pool of material constituents.
These 5 prototypes are scheduled for deposition in our Lab.
- Thickness optimization of the above coatings is expected to provide some extra noise reduction (to be calculated soon – stay tuned...)

