

LASER INTERFEROMETER GRAVITATIONAL WAVE OBSERVATORY  
- LIGO -  
CALIFORNIA INSTITUTE OF TECHNOLOGY  
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<b>Active Reduction of Residual Amplitude Modulation in Free Space EOMs</b>		
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# 1 Introduction

## 1.1 LIGO

The Laser Interferometer Gravitational-wave Observatory, also known as LIGO, is an earth-based network of two gravitational wave detectors located in the United States. The design is similar to a Michelson Interferometer, but with the addition of Fabry-Perot cavities along both arms. Due to the high finesse cavities in LIGO, it requires ultra-stable frequency lasers to make the precise measurements needed for gravitational wave detections. Utilizing an array of detectors, it is possible to better find the location of an event in the sky and study it.

## 1.2 EOMs

An Electro-Optic Modulator (or EOM for short) is one type of optical component used within LIGO. For our purpose, we use it as a phase modulator in a Pound-Drever-Hall (PDH) set-up for laser frequency stabilization. An EOM consists of an electro-optic crystal, which means the crystal's birefringence depends on an applied electric field, and a set of electrodes on the top and bottom of the crystal. This crystal has two principal axes which can have different refractive indices dependent on the electric field in that direction. The voltage difference of the electrodes creates an electric field across that axis of the crystal which then changes the index of refraction for the crystal in the respective axis. With two different indices of refraction for the principal axes, we essentially have a tunable waveplate. As we change the birefringence of the crystal, the light's phase is shifted in turn. Due to polarization misalignments, etalons, and other factors, EOM's in use as phase modulators also introduce residual amplitude modulation (RAM).

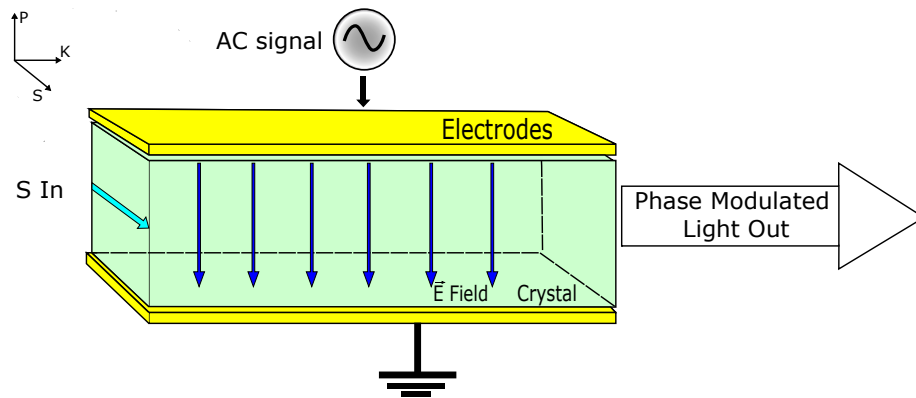


Figure 1: Experimental Set-up

## 1.3 Pound-Drever-Hall and Frequency Stabilization

The purpose of PDH is to lock the frequency of a laser to a cavity, or vice versa. This is usually done by measuring the power being reflected from the cavity and generating a

feedback signal to control the frequency of the laser or the length of the cavity. For light to resonate in the cavity its frequency must be an integer multiple of the cavity's free spectral range  $\Delta\nu_{fsr} = c/2L$ , where  $c$  is the speed of light and  $L$  is the length of the cavity. When the laser frequency is near resonance, the amount of light being reflected can be approximated as a linear function of the laser's frequency[1]. Phase modulation creates upper and lower sidebands, which when far from resonance can be treated as seeing the maximum reflection from the cavity. The photodetector sees the power from the superposition of these sidebands and the reflected carrier from the cavity. This power is converted to a voltage and then used as an error signal for locking.

Any RAM introduced by an EOM is fed through the experiment and is picked up on the photodetector. After the photodetector and the local oscillator's signals are mixed, this RAM introduces an offset on the signal being fed to the locking servo. This unwanted offset means the system is not at the frequency it expects. So instead of locking the laser's frequency to resonance, we unintentionally lock off-resonance reducing the effectiveness of the system. Any changes in RAM over time would change this offset uncontrollably leading to unpredictable behavior from the system.

## 2 Objective

Our goal is to use an EOM as a phase modulator and create an ultra-fast feedback mechanism by controlling the temperature and DC bias of the EOM to actively suppress RAM to the level of  $1 \times 10^{-5}$ . This will be done by using a free space EOM to phase modulate a beam, which will be partially picked off and sampled by a photodetector for use as our feedback signal to the temperature and DC bias control. The DC bias component influences the in-phase response 20 times more than the quadrature response, but the temperature control influences the quadrature response 5 times more than the in-phase response[2]. Working together, it should be feasible to have good suppression of both components over an extended period of time.

## 3 Approach

### 3.1 Mathematical Motivation

From our photodetector the amplitude modulated current for a given modulation frequency  $\omega$  is given by

$$I(\omega_m) = -\sin(2\beta)\sin(2\gamma)|\epsilon_0|^2 J_1(M) \times \sin(\omega t) \sin(\Delta\phi + \Delta\phi_{DC}) [2].$$

Where  $\beta$  and  $\gamma$  represent polarization misalignments of the half-wave plates from the crystal's axes,  $\epsilon_0$  is the amplitude of the incoming laser field,  $J_1(M)$  is the first order Bessel function with  $M$  being the difference in modulation depth between the ordinary and extraordinary axis, and  $\Delta\phi + \Delta\phi_{DC}$  represents the crystals natural phase shift summed with the phase shift induced by the bias voltage. We can see that when this sum is zero or an integer multiple of  $\pi$  the  $\sin$  term will become zero yielding no RAM.

### 3.2 Experimental Set-Up

The set-up involves using feedback mechanisms for temperature and  $DC_{bias}$  suppression of RAM in an EOM being used as a phase modulator. As reported by [2] the in-phase RAM is much more effective at suppressing through the  $DC_{bias}$  voltage, and the quadrature component is better suppressed by the temperature control. The PD acts as our RAM signal which we then decompose into the in-phase component to feedback to the  $DC_{bias}$  port of the EOM, as well as a quadrature component which is used to control a heater in thermal contact with the EOM. The DC Servo's output is fed through a high voltage amplifier in order to reach the DC bias needed for RAM suppression in free space EOM's, which is usually a couple of hundred volts.

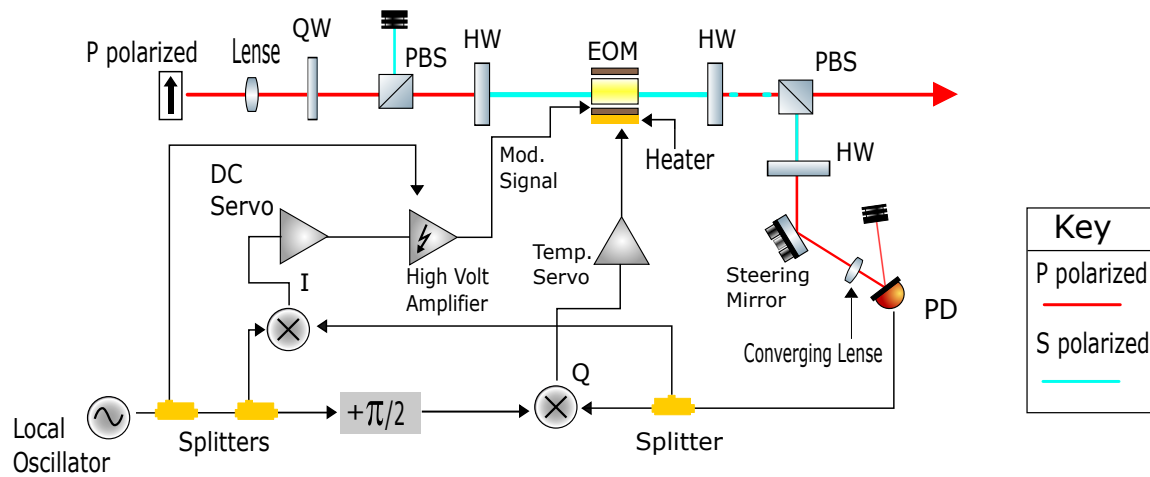


Figure 2: Experimental Set-up

## 4 Timeline

### 4.1 Week 1-2

The first two weeks we should be able to place optics on the table and achieve good alignment onto the photodetectors. Once we have the optical set-up in place, we can measure the signal strength from the PD to inform us on the requirements of the servos.

### 4.2 Week 3-4

Knowing the strength of signal to the servos, we can then investigate what form of servos we will use for feedback. These may be digital PID code, or analog circuits with amplification.

### 4.3 Week 5-6

After we know what form of servo we desire, we can either build the circuit or get/make the software we need. Once we have all the components for the electrical side of the feedback loop, we can fully construct the experiment.

### 4.4 Week 7-8

The next step will be to take the data analyzing the stabilization of RAM suppression over a set period of time. This hopefully will be actively kept under the level of  $1 \times 10^{-5}$  which is the level of suppression desired. If the RAM is above this threshold level, we will have to re-evaluate the components of our feedback loop and try to achieve the indicated level of RAM suppression.

### 4.5 Week 9-10

Here we will finish up the data acquisition and analysis. After which we will work for the remainder of our time on writing the final paper and working on a presentation of our findings.

## 5 Interim Report 1

### 5.1 Bias Tee Characterization

The first step in being able to introduce DC bias feedback was to characterize the bias tee used to see the attenuation of the DC and RF signals into each port of the device. This was done by using the network analyzer to measure the S matrix for the device. Because the DC port of the device did not have any connector attached, I soldered a female BNC connector to attached to the network analyzer as shown in the picture.



Figure 3: Bias Tee with Soldered BNC connector

## 5.2 Fitting to Simplified Model

I made 4 plots from this data, three showing the data for each port individually and one showing the transfer functions that will apply when using the bias as expected. The first three plots gave the signals read from the two alternate ports when the signal is injected into the respective port. The last plot, shown below, is the coupling between the RF and RF+DC ports as well as between the DC and RF+DC ports, which characterizes the transfer functions we expect to see in practice. While the device has multiple capacitors and inductors to perform the biasing, I used the S32 and S31 transfer functions to fit the electrical schematic as one capacitor and one inductor.

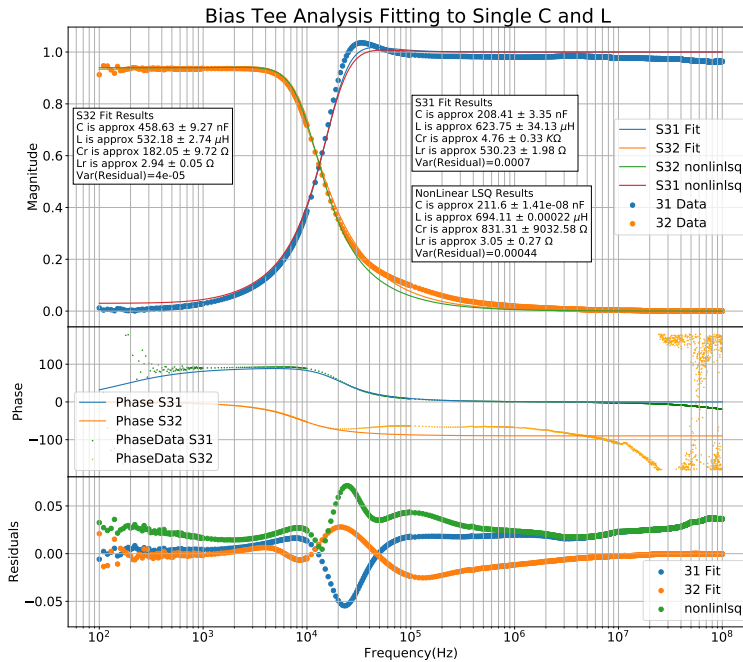


Figure 4: Fit of Data to Single Capacitor and Inductor

## 5.3 Modeling

Once we had realistic values for the capacitor and inductor, I used LTspice to add a model of the bias tee to the EOM driver and see what value of a tunable inductor was needed to maintain the resonant circuit at 37 MHz and 36 MHz for two different drivers. After confirming we had the correct inductor I soldered a new EOM driver board for this purpose. Here we see the left driver is complete, while the right one has no inductor or connectors.



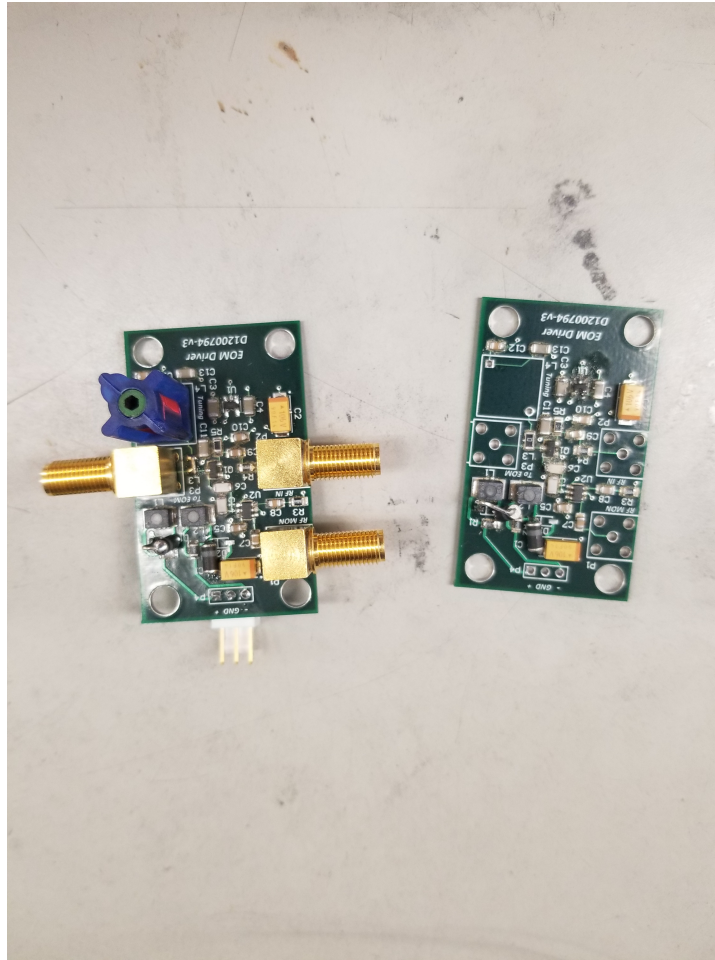


Figure 5: EOM Drivers

#### 5.4 Reflow Soldering

While soldering I learned of a new form called reflow soldering. This involves using a paste that has solder beads suspended in a flux, which when heated evaporates and fuses the solder together. In order to spread awareness of how this process is done, I made a little step by step tutorial within the ELOG and linked a youtube video of the fusing process. After learning reflow soldering I used this technique to solder 3 channels to the AD590 temperature sensor board below, changing one resistor to bring it more in the room temperature range.

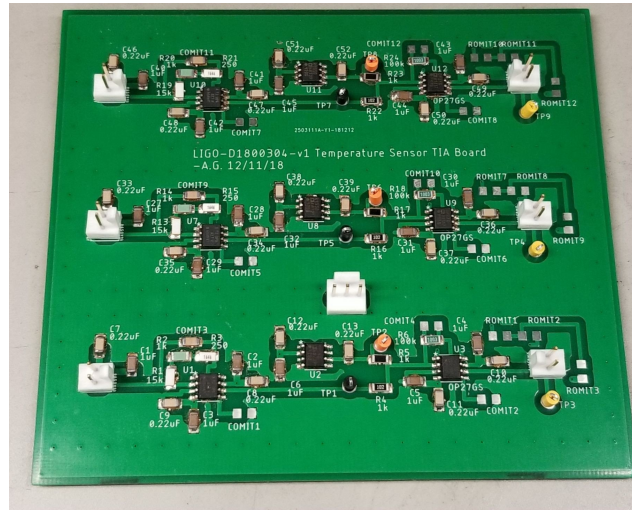


Figure 6: AD590 Temperature Sensing Board

## 5.5 Next Up

Our next step will be to characterize the AD590 temperature sensor. We will determine the noise of the device by using two of them over the same course of time and subtract their values from one another. Any change on both sensors will be interpreted as real temperature readings, but any non-coupled components of their signals will indicate noise. Using this technique we hope to see a noise level below the resolution of the sensor or around 1 millikelvin.

## 5.6 Anticipated Challenges

The model of a single inductor and capacitor is very simplified. Therefore the EOM drivers inductor values I calculated to maintain the resonant circuits for each frequency is only approximate. We may have to resolder a different tuneable inductor to better fit the reality of what is happening outside of the simulation.

# 6 Interim Report 2

## 6.1 AD590 Temperature Sensing Results

The first step in understanding the noise from AD590 temperature sensors was to use Zero to model all the known noise contributions present at the output. I was able to estimate the noise in terms of the input-referred current noise density by dividing the output noise by the overall transfer function. Then knowing the AD590s conversion from temperature change to current output, I found the input-referred temperature noise density of the circuit as a whole from the sensor to computer acquisition.

From there I set up an experiment that measures the time series of three AD590's in thermal

contact with a large metal block. The large metal block has a high heat capacity so it should be insensitive to small local temperature fluctuations, yielding the lowest noise power spectral density as possible due to the environment. I measured the input-referred noise of the ADC I was using by shorting the input and measuring the output. Because the ADC has a gain of one this output noise is the input-referred noise. I also measured the noise due to the 15V regulated power supply used to power the circuit. I used the power noise times the power supply rejection ratio of the op-amps in the circuit to estimate the input-referred noise of the power supply as well. I took the difference of the time series for each pair of AD590 sensors to get differential data, which should not contain any common temperature-induced fluctuations.

I assumed all channels have the same transfer function but different offsets, so each PSD of the difference channels has the sum of the noise of both devices in quadrature. The difference PSDs, for instance the difference between channels 0 and 1, then takes the form

$$N_{01} = n_0^2 + n_1^2$$

By adding difference PSDs with the channel we want and subtracting the other we get the noise of a single device squared. Taking the square root we can pull out the individual noise spectral density for each channel, this is also known as the three corner hat method. By plotting the estimated noise sum and the measured individual noise of each device on one graph we were able to directly compare our expected noise with reality. I found the measured noise was below the simulated noise for all frequencies between a millihertz and ten hertz. By integrating this real noise over the bandwidth of a millihertz to ten hertz, we found the total noise of the device is always under one millikelvin. This means the circuit is sensitive enough to resolve this level of temperature change up to ten times per second, which matches our goal for the circuit.

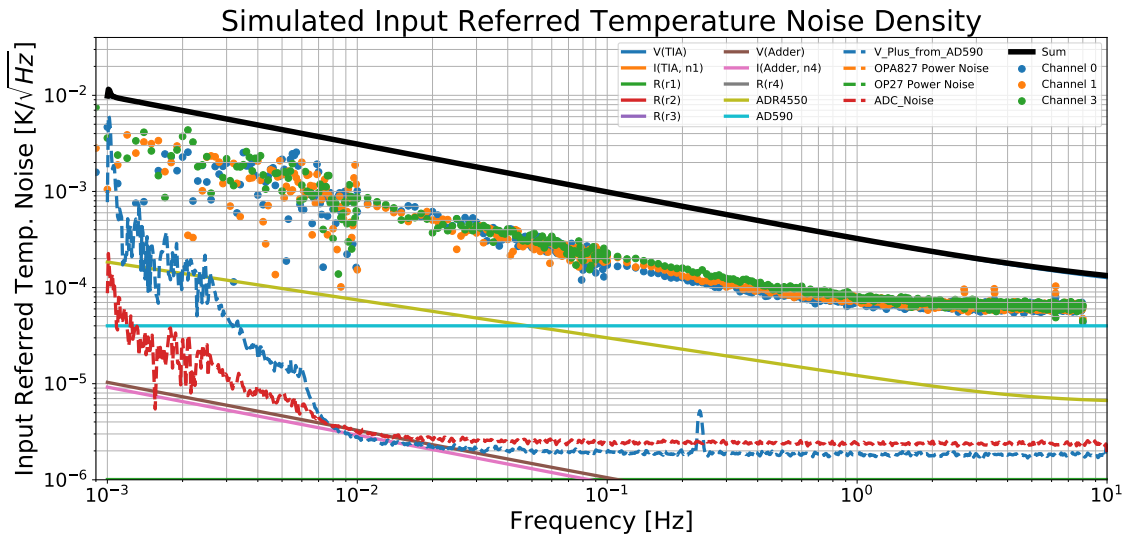


Figure 7: AD590 Input Referred Temperature Noise Density

## 6.2 Optimal Op-amp for Temperature Sensing

To determine what would be the best op-amp to use in the transimpedance amplifier of the AD590 temperature sensing circuit I ran a Zero simulation which calculated the noise sum of the circuit as a whole for different op-amp choices. A major consideration is we do not want the circuit's response to change with temperature in a temperature sensing circuit. Also since this is the location where the current information of the temperature given by the AD590 is converted into a voltage response, we want any noise introduced after this transimpedance stage to be much less than this stage. After the analysis, I found the Op-amp we were using (OPA827) had the lowest temperature drift, but AD8671 or LT1128 had an all-around lower noise density. Because we found the noise level of the circuit was a millikelvin sensitive, I thought OPA827 was a good choice to reduce the temperature dependence as much as possible.

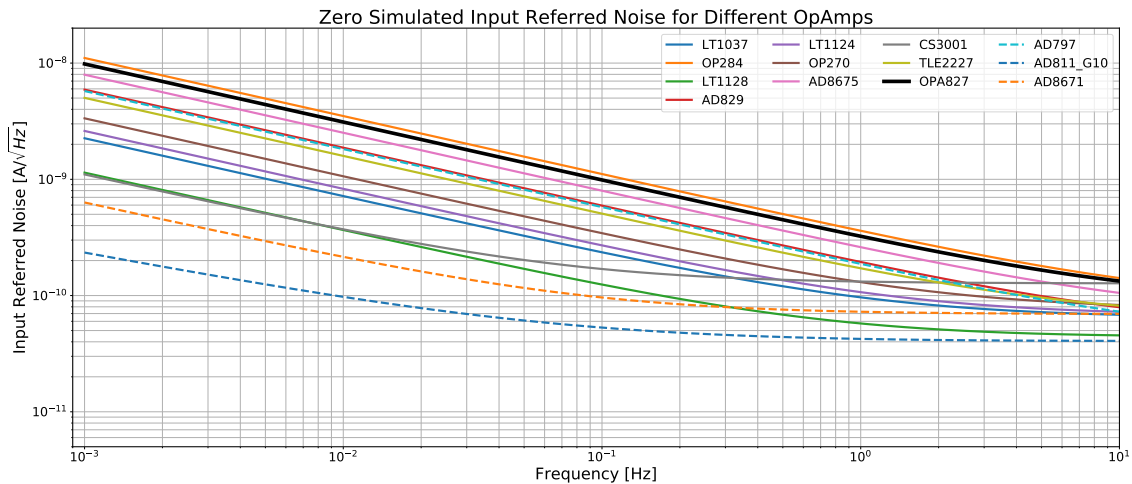


Figure 8: Noise Density of Different Op-Amps

## 6.3 EOM Driver Resonant Circuit Update

From Report 1 we saw there was a good possibility the tunable inductor I found would not be in the correct range to have a resonant circuit around 37 MHz. This turned out to be correct, as a replaced the 891nH - 1270nH inductor with a 460nH-788nH inductor to finally achieve the correct peak location. To take the measurement I attached a 50-ohm termination to the bias tee's DC port, and directly connected a 20pF 'Dummy EOM' to the RF+DC port which matches the EOM expected capacitance. I used a network analyzer to measure the transfer function through the bias tee and EOM system while tuning the inductor to move the peak to 37MHz. This resonant circuit will ensure no higher-order harmonics of our modulation frequency will create unwanted modulation at higher frequencies. The transfer function from the RF Input of the EOM Driver to the EOM has a max gain of around 10, this gain will be enough to get a 40 Vpp signal which equates to a 0.3 modulation depth.

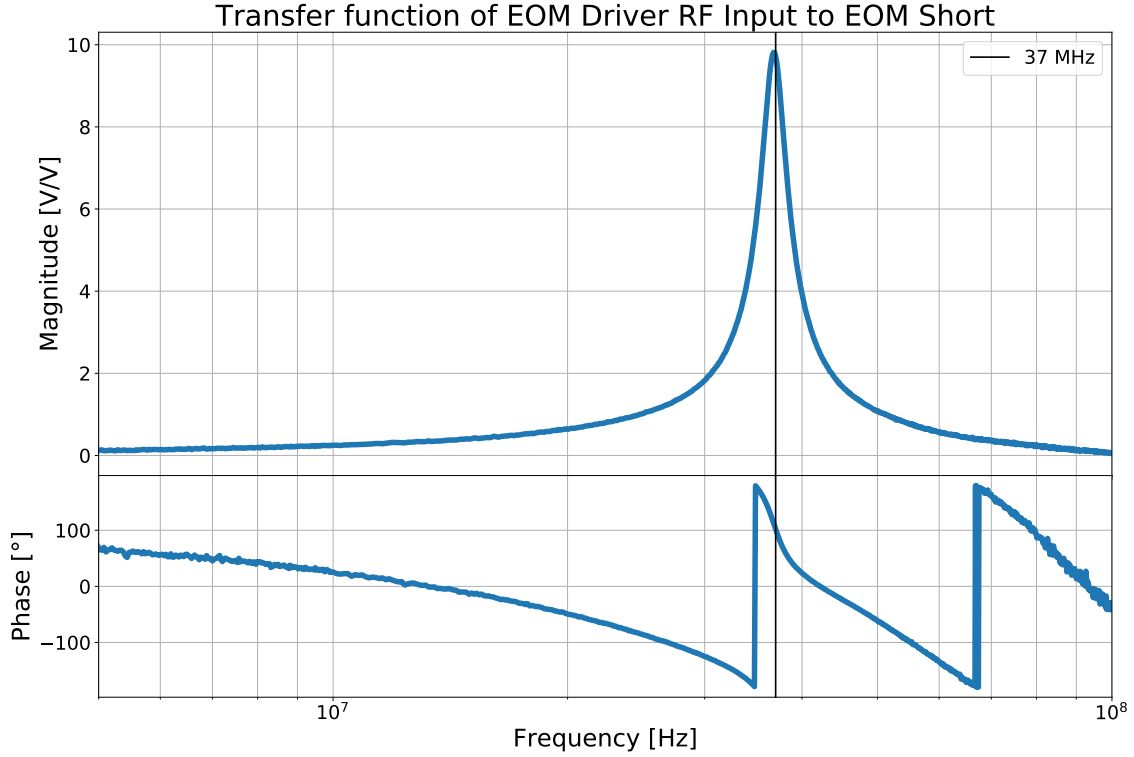


Figure 9: Resonant Circuit Transfer Function

#### 6.4 RAM Measurement Set-up

The eventual goal of the project to actively suppress the RAM in EOM's. The first step in this process on the optical table is to set up some sort of pick-off by which we can measure and correct for the RAM present. We used the PBS within the faraday isolator (FI) as a pickoff, and rotate the HW plate at the input to control the power reflected. I then used a mirror and a focusing lens to steer the picked-off beam onto the active area of an 1811 new focus photodetector. Using the DC coupled output I maximized the output on an o-scope to get the best possible alignment. I then used the AC output port to measure the spectrum of the signal. I saw a peak at 14.75 MHz from a previous EOM, as well as its second harmonic at 29.5 MHz. The third peak is the RAM due to the 37 MHz EOM which we focus on.

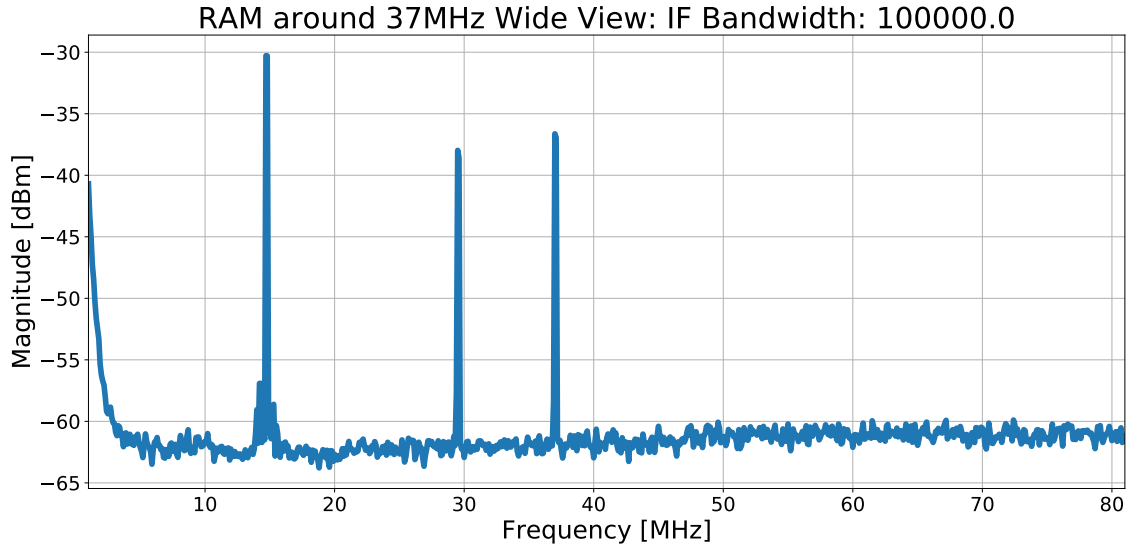


Figure 10: Spectral Density of signal from Photo-Detector

## 6.5 DC Bias Servo/Next Steps

The next step is to create a DC bias servo which will take the signal from the photodetector, downmix it with a local oscillator at the modulation frequency and then low pass filter it to yield a dc signal which is proportional to the amount of RAM seen. This dc value will then be fed through a high voltage amplifier to get into the value of hundreds of volts, which is the order of the  $V_\pi$  of the EOM. Here we will have to choose a corner frequency for the low pass filter, as well as the gain value of the high voltage amp. As quoted from [2] their servo bandwidth is typically 200kHz, so we will start with this value. For the high voltage amplifier, the plan is to begin at a gain of 10 and investigate the open-loop gain to determine stability in feedback. After the DC Servo is complete the plan is to build the temperature servo, which will require a much lower bandwidth, [2] had 0.1 Hz.

## 6.6 Research Goals

The goal is to get as far as the servo creation as possible until the end of the summer. Once the servos are ready there will be the need to take data to see the effectiveness of the locking. Our final goal is still to maintain RAM down to the level of  $1 \times 10^{-5}$ . While it is very unlikely we will get to build the temperature servo during the duration of the summer, the main goal is to get as far as possible with the DC Bias servo.

## References

- [1] Black, E. D. An introduction to Pound-Drever-Hall laser frequency stabilization. Am. J. Phys. 69, 79 - 87 (2001).

- [2] W. Zhang, M. J. Martin, C. Benko, J. L. Hall, J. Ye, C. Hagemann, T. Legero, U. Sterr, F. Riehle, G. D. Cole, and M. Aspelmeyer, "Reduction of residual amplitude modulation to  $1 \times 10^{-6}$  for frequency modulation and laser stabilization," *Opt. Lett.* 39, 1980-1983 (2014)