


Making LIGO Possible: A Technical History

A bronze relief sculpture of a face, possibly a commemorative piece. The face is stylized with large, almond-shaped eyes and a prominent nose. The text is engraved into the surface of the sculpture.

they ask me to remember
but they want me to remember
their memories
and i keep on remembering
mine.

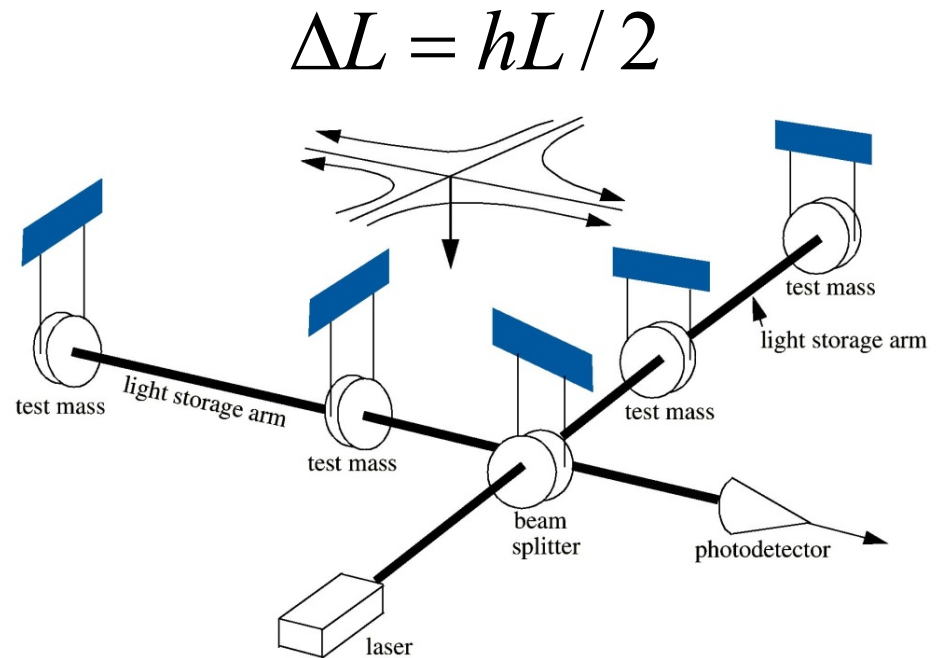
- Lucille Clifton (1936-), "why some
people be mad at me sometimes"

Stan Whitcomb
APS April Meeting
15 April 2019

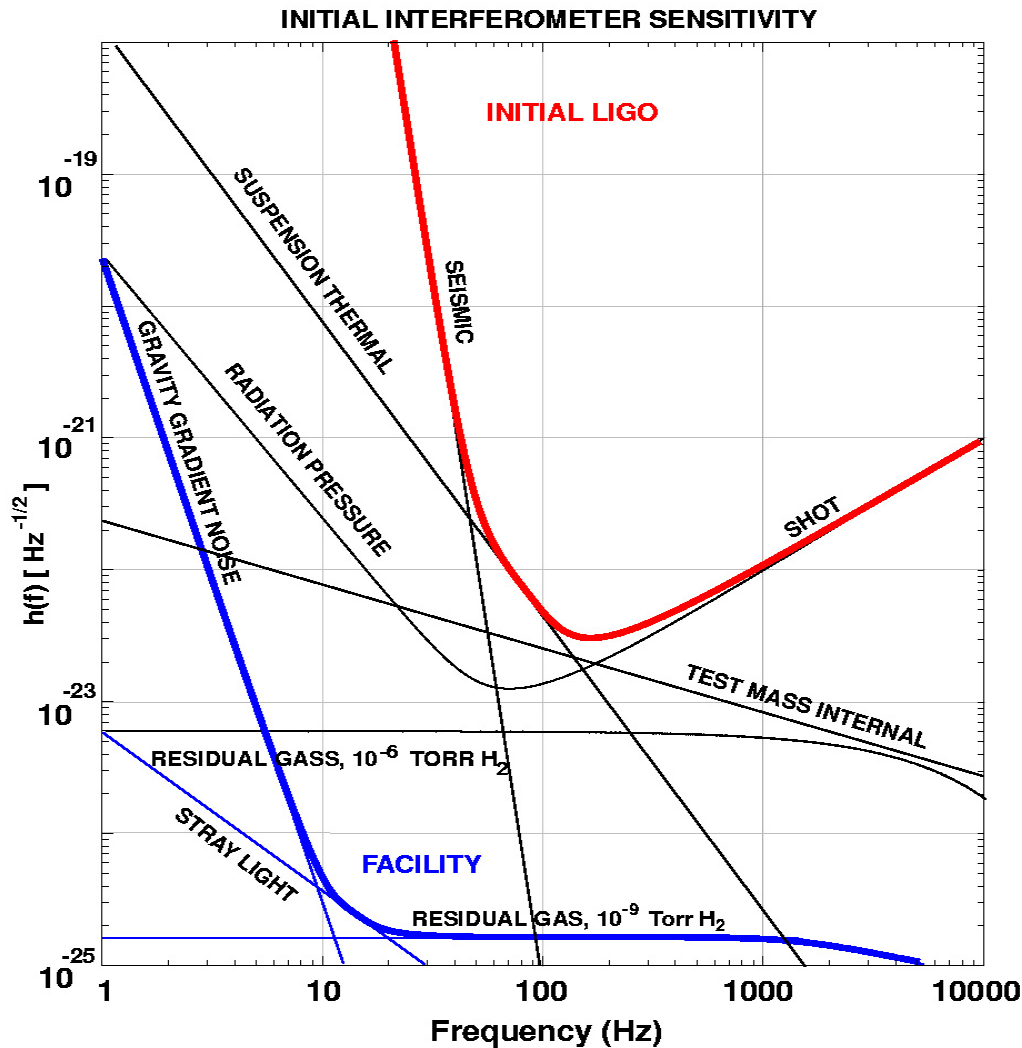
- Review a few of the technical developments that enabled LIGO, with emphasis on pre-construction era
 - » “Invention” of laser interferometry for GW detection
 - » Residual gas noise (Vacuum requirement)
 - » Thermal noise
 - » Mirror figure requirements
 - » Mirror orientation noise
- Disclaimer: LIGO has an equally “rich” socio-political history—NOT covered in this talk
 - » See e.g., Janna Levin, *Black Hole Blues*
 - » Caltech Archives--search for “LIGO Oral Histories” at <http://archives.caltech.edu/search/index.html>

Suspended mirrors act as “freely-falling” test masses in horizontal plane for frequencies $f \gg f_{\text{pend}}$

For a LIGO detector,
 $L \sim 4 \text{ km}$, $h \sim 10^{-21}$
 $\Delta L \sim 10^{-18} \text{ m}$



The Core Principle Driving LIGO: Noise Reduction



- Sensing Noise
 - » Photon Shot Noise
 - » Residual Gas
- Displacement Noise
 - » Seismic motion
 - » Thermal Noise
 - » Radiation Pressure
- Noise sources add
 - » All noise sources have to be identified, understood and controlled

Three documents so central to the technical history of LIGO that they must be introduced immediately

- “Rai’s RLE paper”
 - » “Electromagnetically Coupled Broadband Gravitational Antenna”
R. Weiss, Quarterly Reports of the Research Laboratory of Electronics MIT **105**, p. 54 (1973).
 - » Paper “... grew out of an undergraduate seminar that I ran at M.I.T. several years ago...”
- The “Blue Book”
 - » “A Study of a Long Baseline Gravitational Wave Antenna System”
 - » Authors: Paul Linsay, Peter Saulson, Rai Weiss
 - » Dated October 1983, but not really published
- NSF Proposal for LIGO Construction (’89 proposal)
 - » Proposal team: Robbie Vogt, Ron Drever, Rai Weiss, Kip Thorne, Fred Raab, but with contributions from many others

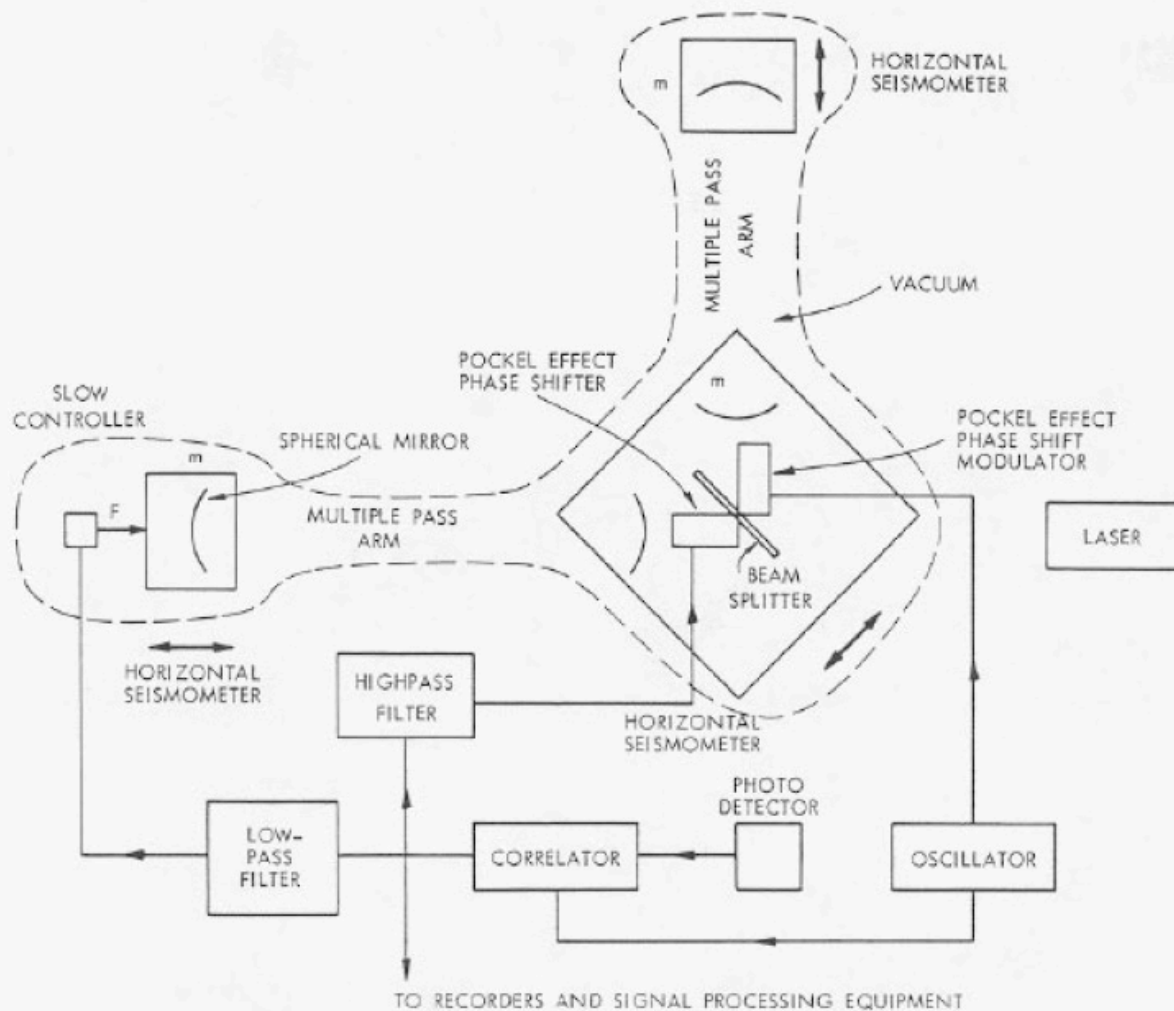
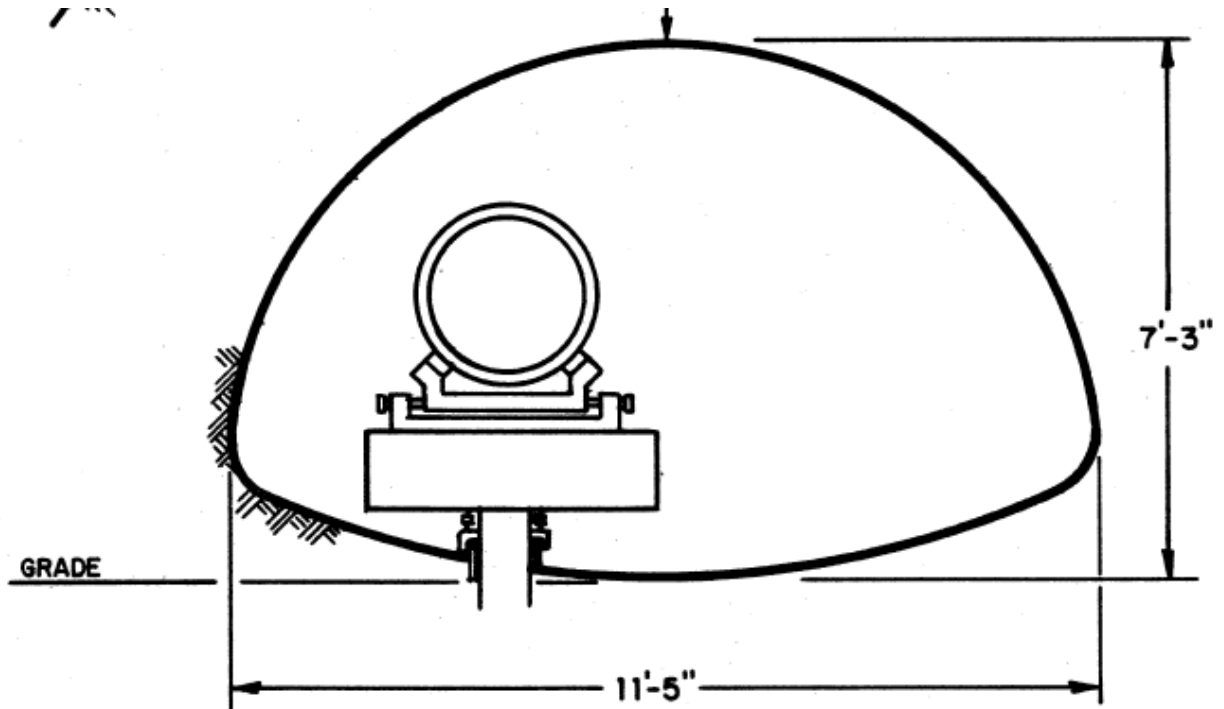


Fig. V-20. Proposed antenna.

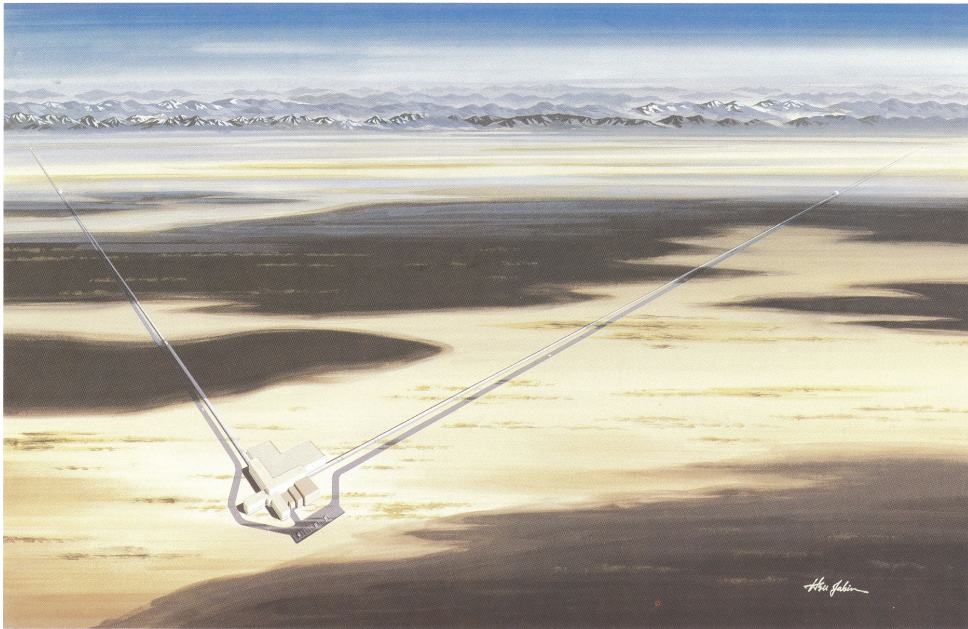
Not first suggestion of a laser interferometer to measure GWs, but first detailed noise/sensitivity analysis

- » Shot noise/
radiation pressure
- » Thermal noise
- » Seismic noise
- » Gravity gradient
- » ...

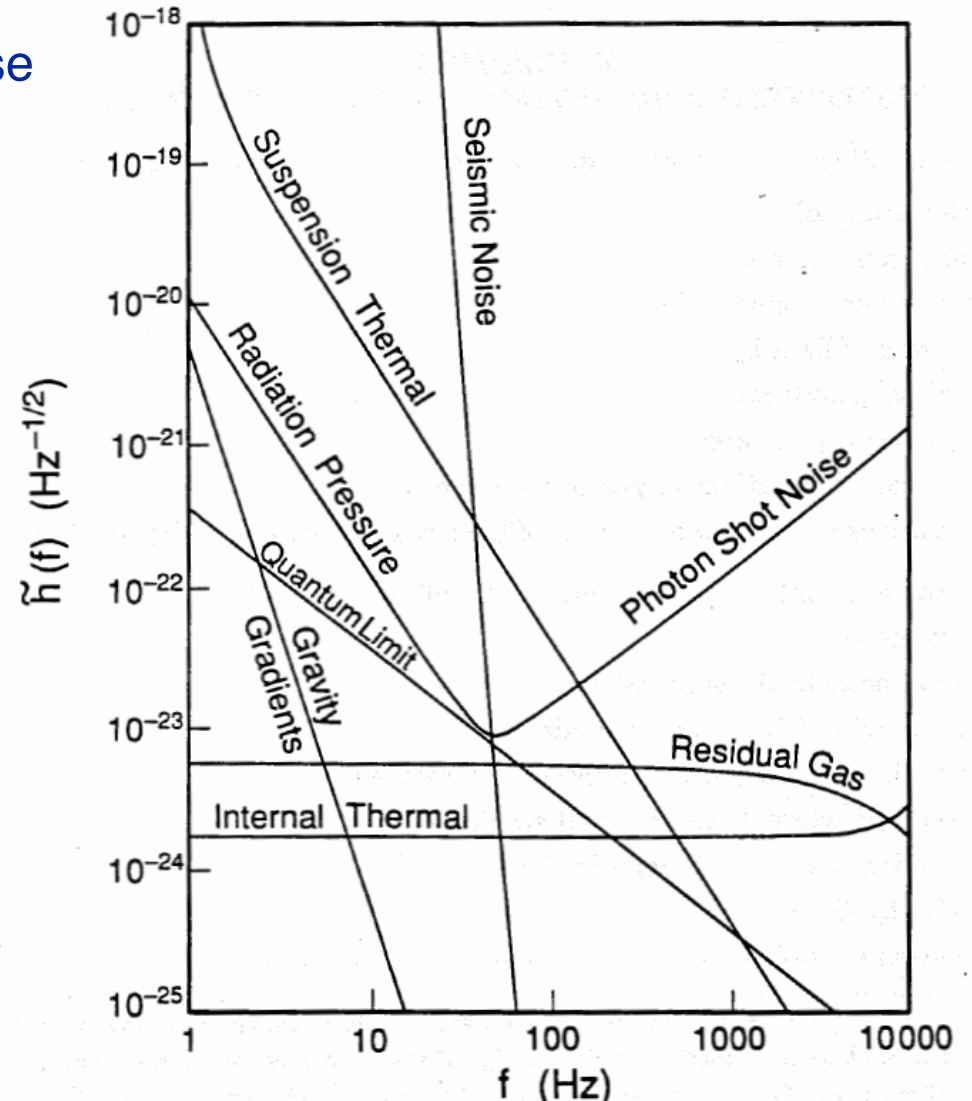
- Science and Engineering study of feasibility
- Comprehensive scope—Chapter titles
 - » Sources of Gravitational Radiation
 - » Physics and Detection
 - » Prototypes and Optical Concepts
 - » Noise sources
 - » Vacuum System
 - » Site survey
 - » Construction
 - » Proposed Design
- Important because of first engagement of real engineering



- Two Volumes
 - » Science case, detector physics, noise analysis, prototype experience
 - » Engineering design and cost basis
- Defined sensitivity goals, phased approach, scope



LIGO-G1802281-v1



Who Invented the Laser Interferometer Gravitational Wave Detector?

Because everyone asks this...

- (At least one) early gedanken experiment using interferometry to detect GWs:
 - » F.A.E. Pirani, *Acta Phys. Polon.* **15**, 389 (1956)
 - » (predates invention of laser by 4 years)
 - » Cited in Rai's RLE paper
- Often cited as first suggestion:
 - » M.E.Gertsenshtein and V.I. Pustovoit, *Zh. Eksp. Teor. Fiz.* **43**,605 (1962); *Sov. Phys JETP*,**16**, 433 (1963).
 - » Not cited in RLE paper, but was noted by Braginsky in "Gravitational radiation and the prospect of its experimental discovery," *Sov. Phys. Usp.* **8**, 513 (1966).
- Rai's RLE paper represented an independent invention ("several years" before 1972)
- RLE paper cites Philip Chapman (NASA) as having independently proposed technique

First Interferometer Prototype

- Started at Hughes Research Labs in 1966!
 - » Led by Robert Forward (former student of Joe Weber)
 - » Described in G.E. Moss, R.L. Miller and R.L. Forward, “Photon-noise-Limited Laser Transducer for Gravitational Antenna” *Applied Optics* **10**, 2495 (1971).

The idea of detecting gravitational radiation by using a laser to measure the differential motion of two isolated masses has been suggested often in the past.⁵

5. To our knowledge, the first suggestion was made by J. Weber in a telephone conversation with one of us (RLF) on 14 September 1964.

- » Also acknowledges Weiss and Chapman
- First search result published in 1978
 - » “Wideband laser-interferometer gravitational-radiation experiment,” R.L. Forward, *Phys Rev D*, **17**, 379 (1978)

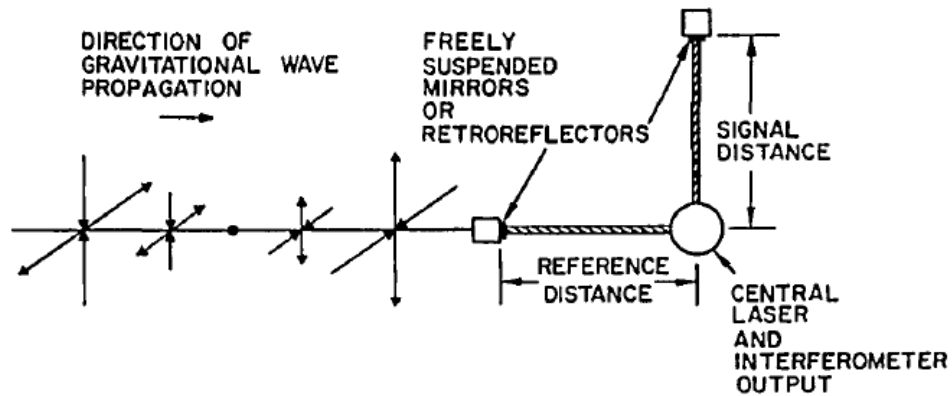


Fig. 1. Right angle interferometer antenna. The reference distance is not changed by gravitational radiation in the direction of propagation shown.

Data Analysis section of 1978 paper:
 “Calibration of the Ear”

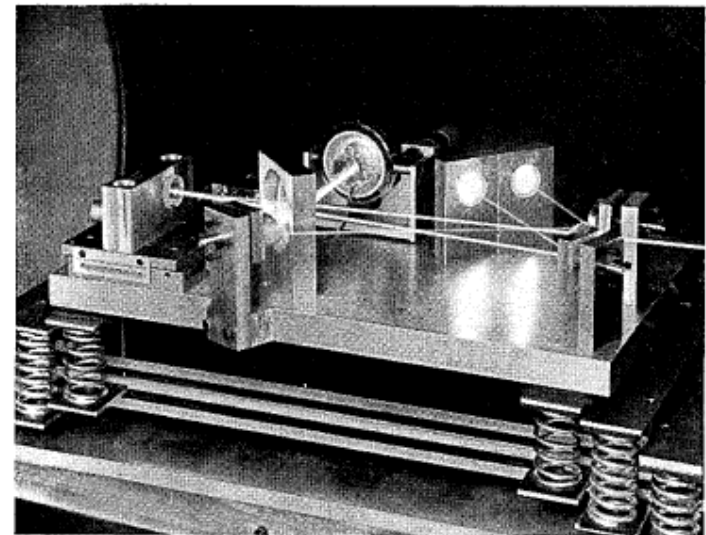


Fig. 4. Photograph of interferometer setup on 3-Hz isolation suspension.

Residual Gas Noise

- Not the most interesting noise source to typical physicist, but **important because the vacuum system was the largest cost items in (initial) LIGO**

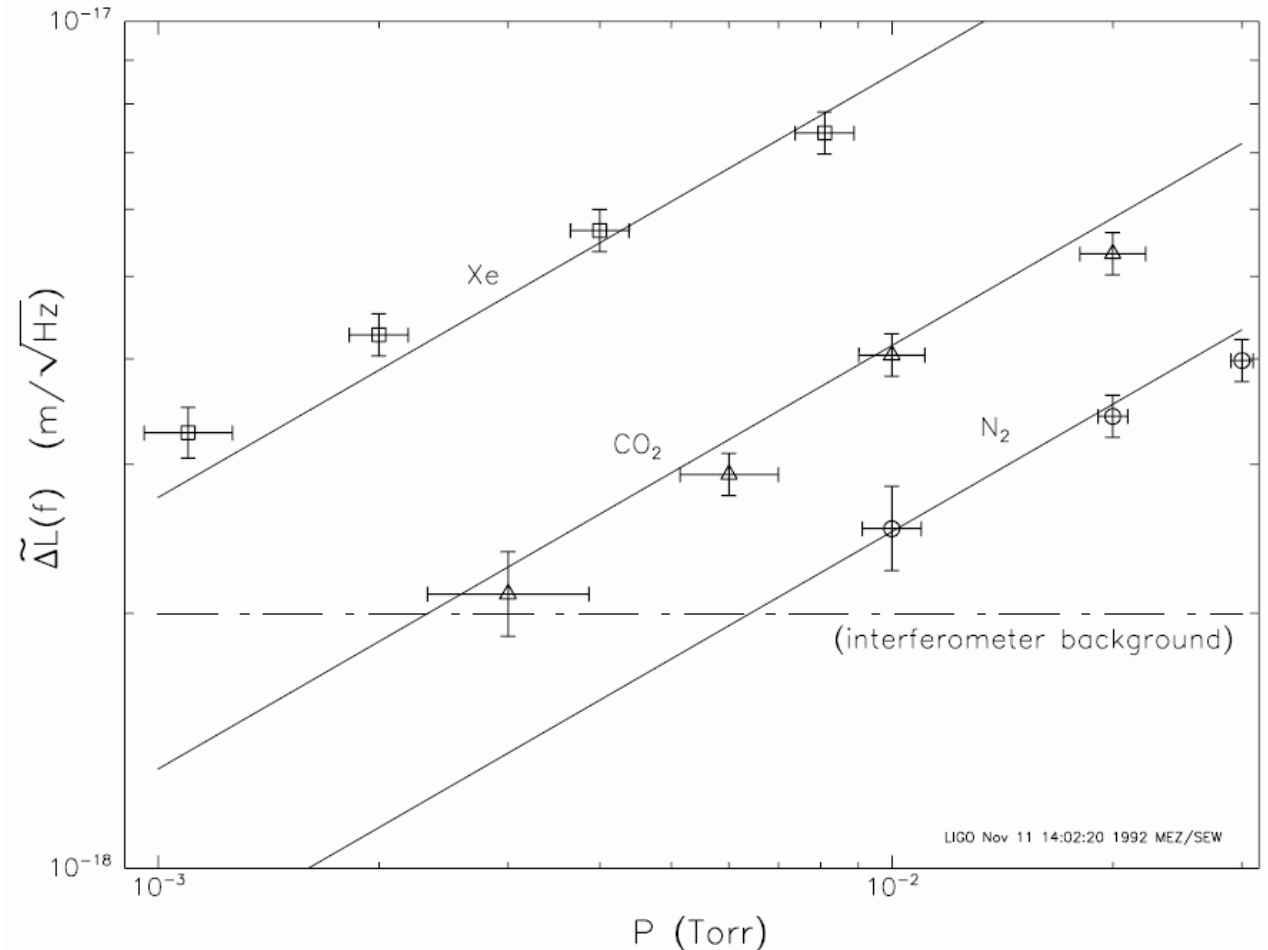


Residual Gas Noise

- Even though very small, the residual gas in the vacuum system contributes to index of refraction
- Not mentioned in Rai's RLE paper
- The Blue Book (1983)
 - » Has an essentially correct treatment of the noise due to residual gas—statistical fluctuations in the number of gas molecules in the beam causing fluctuations in refractive index
 - » Correct requirement for initial LIGO ($\sim 10^{-6}$ torr)
- Correct formulation independently published by the Munich/Garching group
 - » Referenced to Albrecht Rüdiger as unpublished derivation in paper on Munich 30 m prototype ("Noise behavior of the Garching 30-meter prototype gravitational wave detector," Shoemaker et al., *Phys Rev D* **38**, 423 (1988))

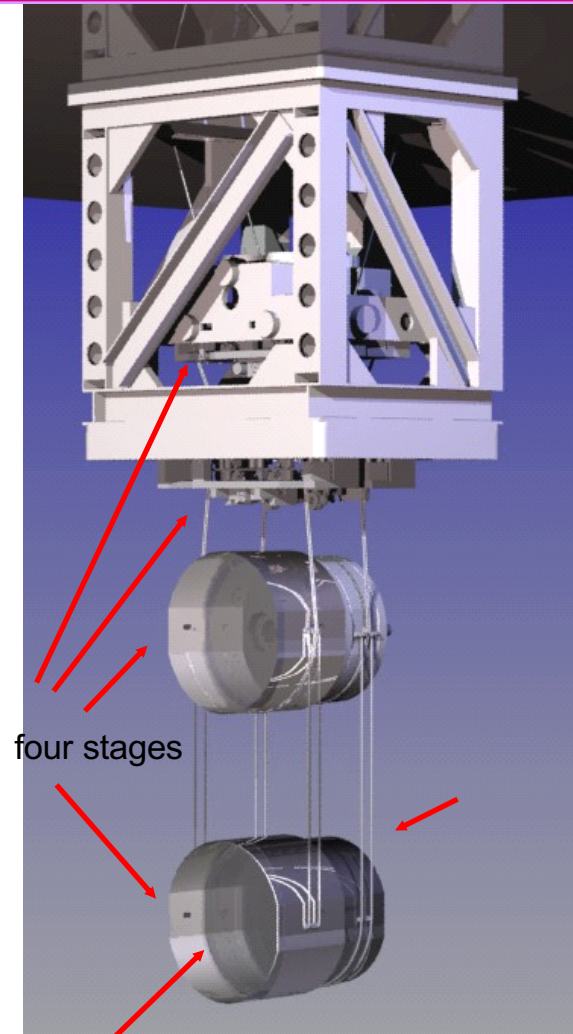
- Not entirely a straight line progression
- 1987 LIGO R&D proposal
 - » Initial LIGO requirement quoted (at least one place) as 10^{-3} torr, three orders of magnitude too high
- LIGO '89 proposal
 - » A new formulation of the problem, in terms of the forward scattering matrix for individual gas molecules
 - » Simple mathematical error ended up with incorrect formula
 - » Gave approximately correct vacuum requirement (probably why the incorrect formula was not noticed)

- Finally, definitively resolved (better than $\sqrt{2}$ level) and confirmed experimentally in 1994
 - » “Measurement of Optical Pathlength Fluctuations due to Residual Gas in the LIGO 40m Interferometer,” M. E. Zucker et al., in *Proc. Of the Seventh Marcel Grossmann Conference*, (1994)
- Just prior to beginning construction (whew!)



Thermal Noise

- One of the most important and complex **fundamental** noise sources



four stages

40 kg silica
test mass

Rai's RLE paper

- Importance clearly recognized (third noise source mentioned after shot noise and laser frequency noise)
- Single mode analysis for thermal noise, assuming viscous damping (suspension modes and internal modes)
- Suspension not defined as a pendulum
 - » Described as a “long-period seismometer suspension”

The RLE Paper

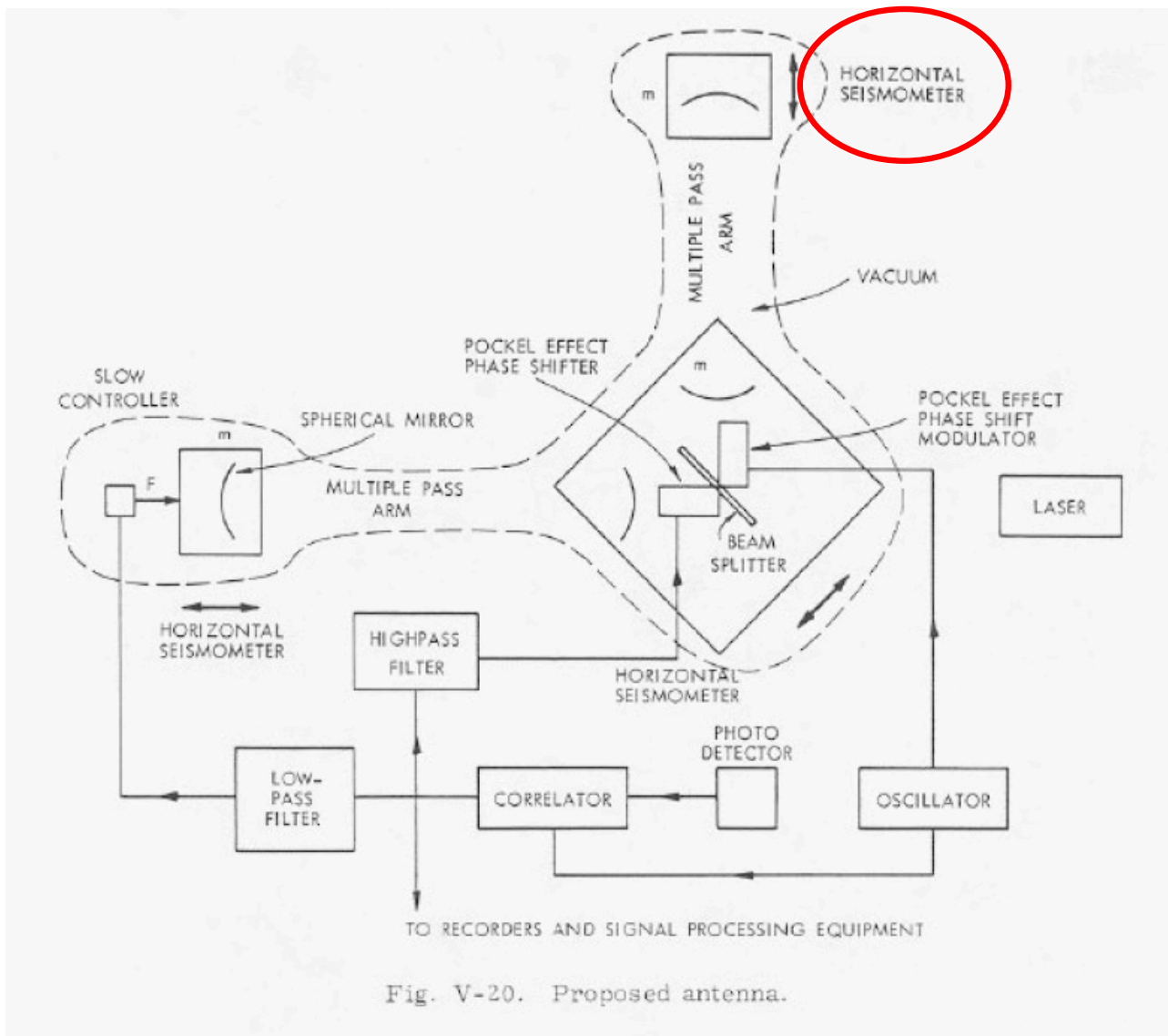


Fig. V-20. Proposed antenna.

Rai's RLE paper

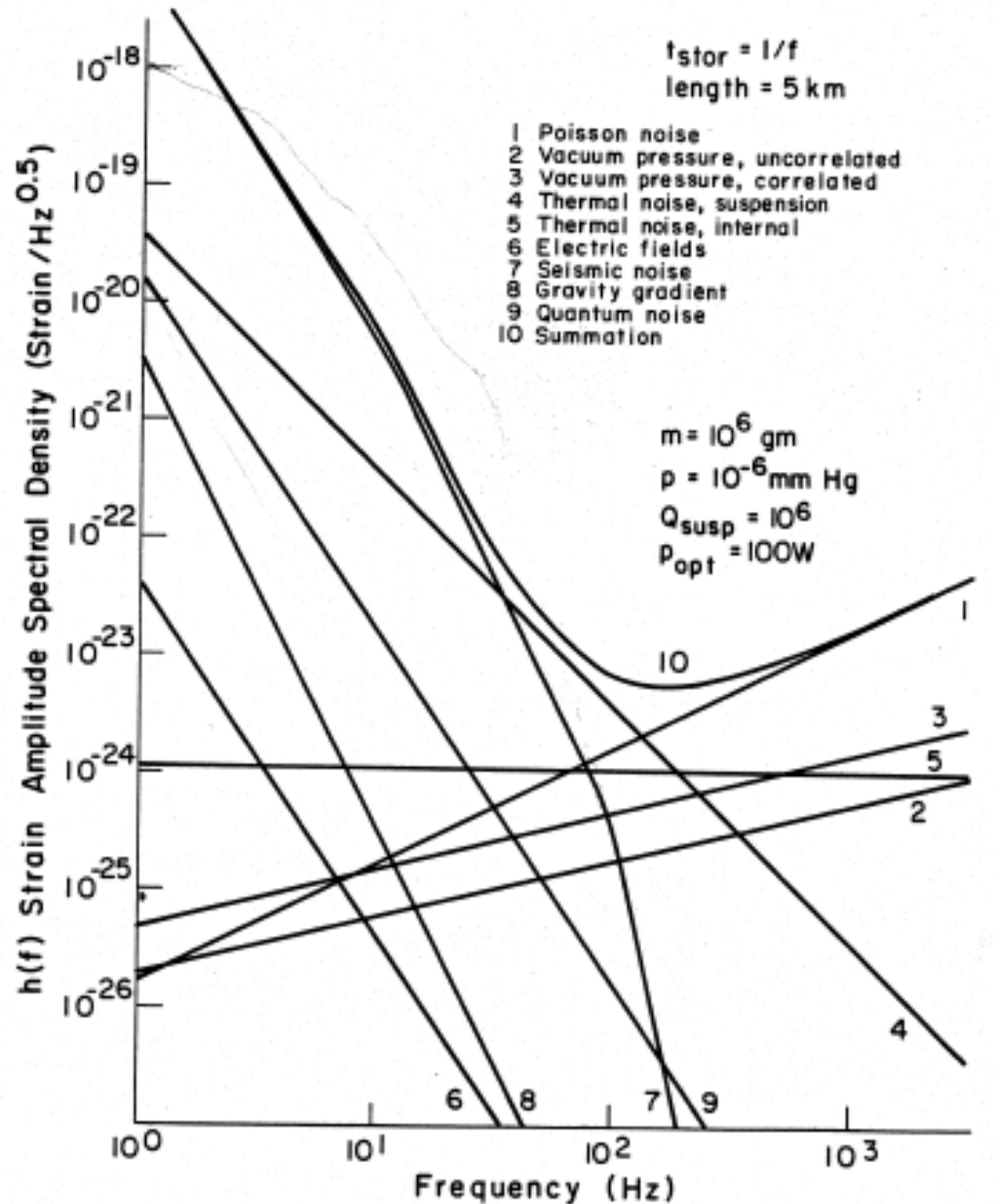
- Importance clearly recognized (third noise source mentioned after shot noise and laser frequency noise)
- Single mode analysis for thermal noise, assuming viscous damping (suspension modes and internal modes)
- Suspension not defined as a pendulum
 - » Described as a “long-period seismometer suspension”
 - » “The suspensions are critical components in the antenna, and there is no obvious optimal design”
 - » Suspension mode given as $Q \sim 10^4$
(actual requirement for Advanced LIGO $\sim 10^9$)
- Multimode nature recognized
 - » “The general problem with suspensions in the real world is that they have not one degree of freedom but many,…”

The “Blue Book”

- Still single mode analysis of thermal noise for estimating noise
- Beginning to recognize the complexity:
 - » “...a frequency independent stochastic force is at this time still only a conjecture.”
 - » “There are situations where a blithe application of the model will give the wrong results.” (coupled oscillators and servo damping)
- Largely unreferenced, so source of incorrect aspects hard to pin down
 - » Fused silica Q_{mat} given as $\sim 10^4$. (actual $Q_{\text{mat}} \sim 10^7$)

Blue Book

- Noise Budget
 - » Thermal noise from the suspensions (4) estimated to dominate in mid-frequency band



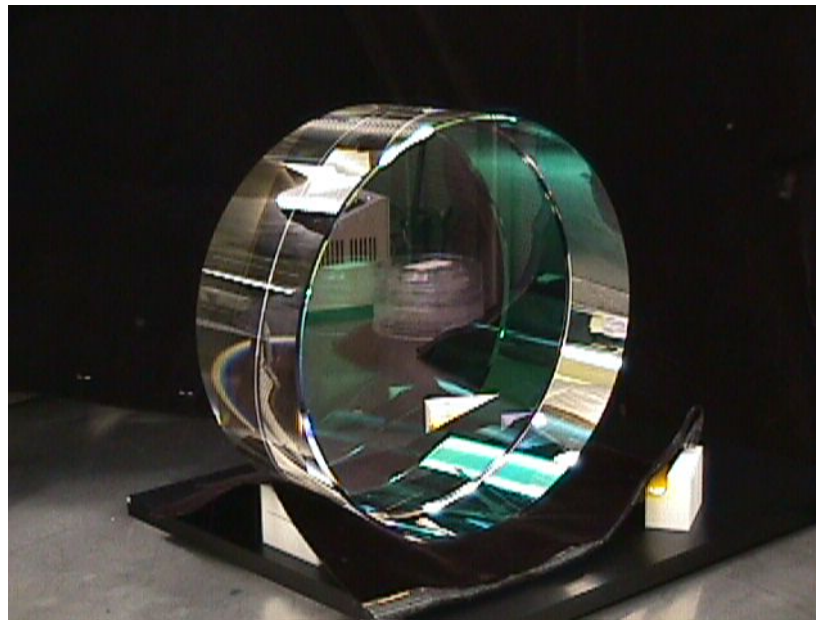
The '89 proposal

- First (?) mention of the Fluctuation-Dissipation Theorem (powerful theoretical tool)
 - » Not really used, however
- Noise estimates still based on viscous damping, but
 - » “...the damping can be frequency dependent so that a simple measurement of the Q of a resonance is not sufficient to predict the thermal noise off resonance.”
- Recognized importance of overlap between internal mechanical modes and optical modes
 - » “Estimates of the equivalent gravitational wave strain ... depend upon the overlap integral of the optical mode shape with the mechanical mode of the mass.”

- Peter Saulson's paper
 - » "Thermal Noise in mechanical experiments," *Phys Rev D* **42**, 2437 (1990)
 - » Complete set of references!
- Began while Peter was at MIT, during writing of '89 proposal, completed during a sabbatical at JILA
- First (?) presentation in the GW literature of:
 - » Structural damping on an equal basis with viscous damping
 - » Thermoelastic damping
 - » Clear discussion of Fluctuation-Dissipation Theorem
 - » Multi-mode systems, systems with localized losses, etc.
- Set the stage for progress in several areas: Yuri Levin's work, modern appreciation of coating thermal noise, etc.

Mirror Figure Requirement

- One of the biggest challenges in initial LIGO
- Requirement for Initial LIGO detectors: **0.6 nm rms**



- Not mentioned in RLE paper
- Not mentioned in Blue Book
- 1987 LIGO R&D Proposal:
 - » “Mirror specifications (substrate material, surface polish, figure and slope errors) have been developed with industry.”
 - » No clear discussion of where those requirements came from
 - » Requirement given as 20 nm (for laser wavelength ~ 500 nm) (Correcting for wavelength difference, ~ 60 times poorer than eventual initial LIGO requirement)

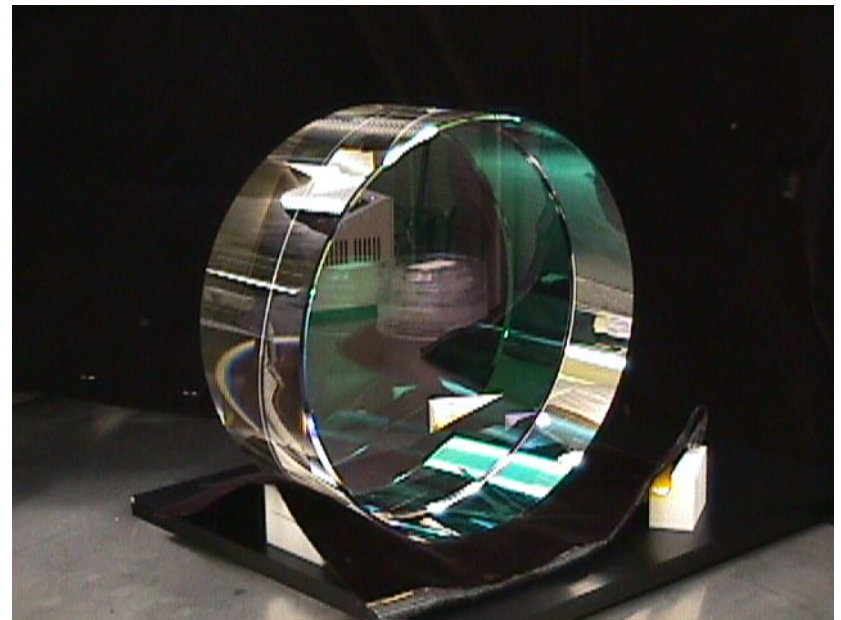
- Same requirement repeated, without elaboration in '89 proposal (still for wavelength ~ 500 nm)

TABLE IV-B-3
PARAMETERS FOR MAIN OPTICAL CAVITIES

Parameter	Value	Notes ¹
Mirror Coatings		
Cavity storage time	2 msec	
Scattering + absorption	$\lesssim 50$ ppm	
Surface microroughness	$< 3 \text{ \AA}$ rms	for < 50 ppm scattering
Coating uniformity	$\lesssim 1.5\%$	rms variation of transmission coefficient over central 8 cm
Cavity length L	4.0 km	(2.0 km)
Mirror curvature R	3.0 km	(1.5 km)
Figure error	200 \AA	rms over central 8 cm
Cavity stability parameter		
$g = 1 - \frac{L}{R}$	-0.33	(-0.33)

- Began to realize challenge as a result of effort to define specification of the substrate uniformity
 - » Mike Burka (MIT postdoc) undertook a program of measurements and modeling to study effects of mirror substrate inhomogenities on the dark port contrast (to assure adequate recycling gain)
- Slowly the requirement began to tighten
 - » Developed optical modal model for full interferometer
 - » First FFT models for interferometer a few years later (Brett Bochner, Hiro Yamamoto, others)
- By 1995, when construction of detectors began
 - » Requirement had tightened to $\lambda/400$
 - » Laser type changed from Ar+ laser to Nd:YAG (wavelength from 500 nm to 1064 nm)
 - » “Discovered” the AXAF Test Flat (LIGO sized optic polished by Perkin-Elmer for NASA x-ray satellite—approximately 1 nm rms)

- Detailed optical modelling led to final specification (another factor of ~ 4)
- Polishing
 - » Surface uniformity < 0.6 nm rms ($\lambda / 1600$)
 - » Radii of curvature matched $< 3\%$
- Coating
 - » Scatter < 50 ppm
 - » Absorption < 2 ppm
 - » Uniformity $< 10^{-3}$
- The challenge was to convince industry that not only **could** they do it, they were **already** doing it



Mirror Orientation Noise

- Was a dominant source of noise in 40m prototype interferometer circa 1990
- Significant because (one of?) the first bi-linear noise mechanisms studied



- Not mentioned in RLE paper
- Mentioned, but not discussed as a serious noise source in Blue Book
 - » “These effects are only second order in the [angles.]”

$$\Delta d = - (R+D)^2 \phi^2 \left(\frac{1}{r} + \frac{1}{2(R+D)} \right)$$

- Not discussed in detail in '89 Proposal, but requirements indicate that it is still dismissed as second order

TABLE IV-B-6
STABILITY OF CAVITY BEAMS AND TEST MASSES

Parameter	Value	Notes
Test-mass stability		
Angular stability	$< 4 \cdot 10^{-7}$ rad	Peak motion at low frequency
Position stability	$\lesssim 0.7$ mm	Peak motion at low frequency
Beam stability		
Angular fluctuations	$< 10^{-12}$ rad/ $\sqrt{\text{Hz}}$	$f \approx 1$ kHz
Position stability	$\lesssim 0.7$ mm	Peak motion at low frequency

- 1990: 40 m prototype interferometer noise was high, not understood
 - » LIGO construction proposal under review, and it was important for the prototypes to show steady progress on sensitivity
 - » Seiji Kawamura began investigations of orientation control systems, eventually engaged Mike Zucker
 - » Injection of dither peaks (to measure noise coupling) showed huge sidebands in addition to the expected peak—sideband structure mirrored low frequency orientation noise

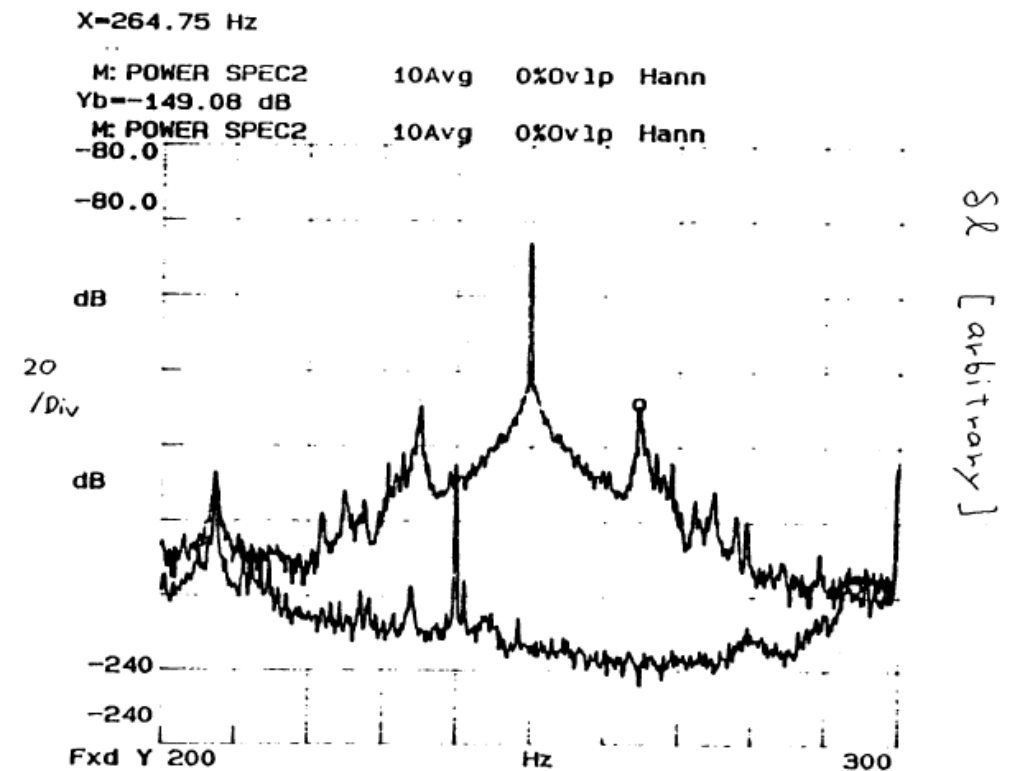


Fig. 3 Displacement spectrum.
 Upper : with angle variations at 250 Hz
 Lower : natural

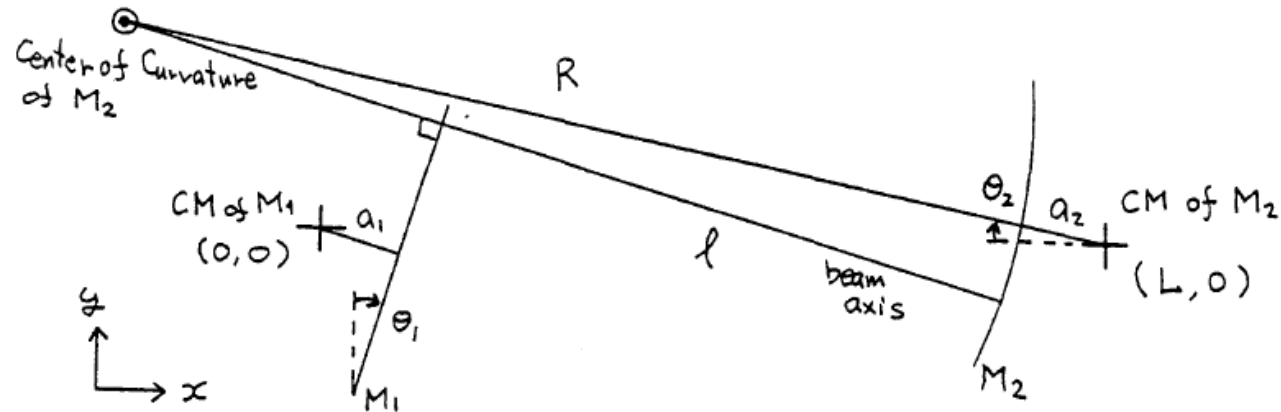


Fig. 1 Arm cavity of the 40m prototype

- Worked out the geometrical length of a misaligned cavity
- First interpretation was in terms of a static misalignment (displacement of the cavity spot from the center of rotation)

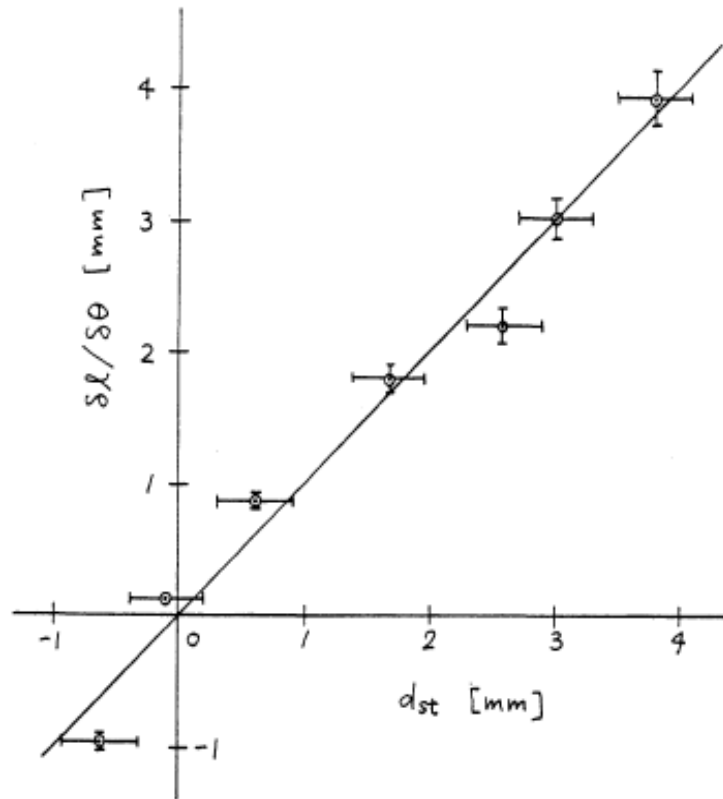
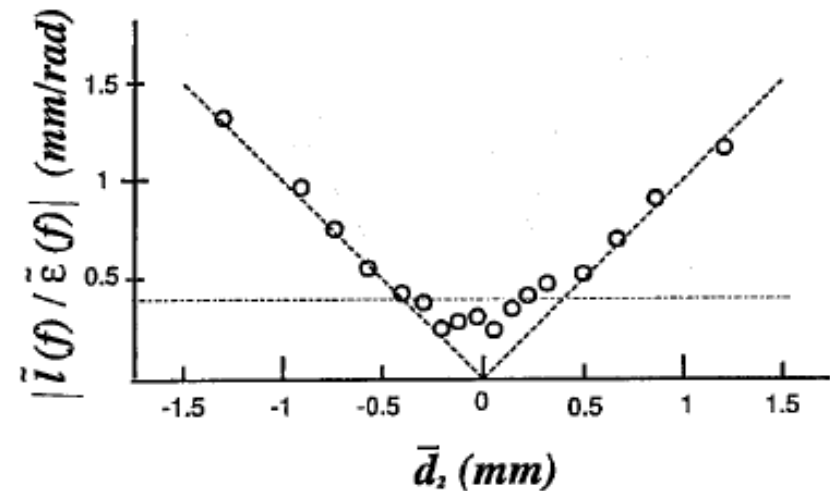
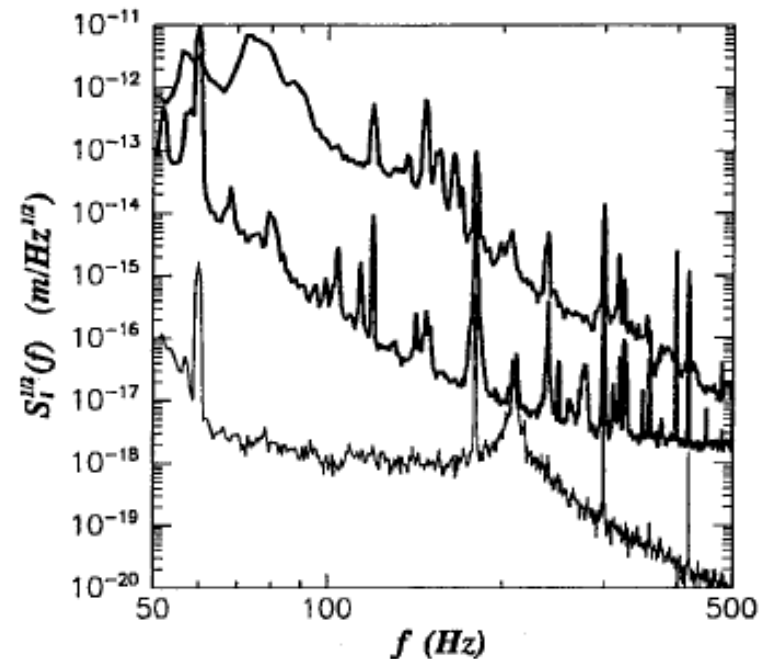


Fig. 2 Linear effect of mirror angle - displacement coupling as a function of static beam spot position. The solid line is $\delta L / \delta \theta = d_{st}$

Important recognition was that the large amplitude low frequency mixes with in-band angular noise to create displacement noise



- Improved noise in 40 m at a critical time
 - » Published as “Mirror-orientation noise in a Fabry-Perot interferometer gravitational wave detector,” S. Kawamura and M Zucker, *Applied Optics*, **33**, 3912 (1994).
 - » Obvious once it is pointed out, but under-appreciated (in my view)
- Opened many people’s eyes to the large class of bi-linear noise sources



- Some of the challenges facing LIGO were recognized early, and the path to overcoming them was steady, even if difficult (thermal noise)
- Some of the challenges were recognized early, and the path to overcoming them involved both positive and negative progress (residual gas noise)
- Some of the challenges were not recognized until rather late in the project, and had to be overcome under intense pressure (mirror figure reqt.)

Extra Slides