

Tests of General Relativity with GW170817

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The recent discovery by Advanced LIGO and Advanced Virgo of a gravitational wave signal from a binary neutron star inspiral has enabled tests of general relativity (GR) with this new type of source. This source, for the first time, permits tests of strong-field dynamics of compact binaries in presence of matter. In this paper, we place constraints on the dipole radiation and possible deviations from GR in the post-Newtonian coefficients that govern the inspiral regime. Bounds on modified dispersion of gravitational waves are obtained; in combination with information from the observed electromagnetic counterpart we can also constrain effects due to large extra dimensions. Finally, the polarization content of the gravitational wave signal is studied. The results of all tests performed here show good agreement with GR.

INTRODUCTION

On August 17, 2017 at 12:41:04 UTC, the Advanced LIGO and Advanced Virgo gravitational-wave (GW) detectors made their first observation of a binary neutron star inspiral signal, called GW170817 [1]. Associated with this event, a gamma ray burst [2] was independently observed, and an optical counterpart was later discovered [3]. In terms of fundamental physics, these coincident observations led to a stringent constraint on the difference between the speed of gravity and the speed of light; allowed new bounds to be placed on local Lorentz invariance violations; and enabled a new test of the equivalence principle by constraining the Shapiro delay between gravitational and electromagnetic radiation [2]. These bounds, in turn, helped to strongly constrain the allowed parameter space of alternative theories of gravity that offered gravitational explanations for the origin of dark energy [4–10] or dark matter [11].

In this paper we present a range of tests of general relativity (GR) that have not yet been done with GW170817. Some of these are extensions of tests performed with previously discovered binary black hole coalescences [12–18], an important difference being that the neutron stars’ tidal deformabilities need to be taken into account in the waveform models. The parameter estimation settings for this analysis broadly match with those of [19, 20] which reported the properties of the source GW170817.

Three types of tests are presented. In Sec. II, we study the general-relativistic dynamics of the source, in particular constraining dipole radiation in the strong-field and radiative regime and checking for possible deviations in the post-Newtonian (PN) description of binary inspiral by studying the phase evolution of the signal. Sec. III focuses on the way gravitational waves propagate over large distances. Here we look for anomalous dispersion, which enables complementary bounds on violations of local Lorentz invariance to those of [2]; constraints on large extra spatial dimensions are obtained by comparing the distance inferred from the GW signal with the one inferred from the electromagnetic counterpart. Finally, in Sec. IV constraints are placed on alternative polarization states, where this time the position of the source on the

sky can be used, again because of the availability of an electromagnetic counterpart. We end with a summary and conclusions.

CONSTRAINTS ON DEVIATIONS FROM THE GENERAL-RELATIVISTIC DYNAMICS OF THE SOURCE

Testing GR via the dynamics of a binary system involves constructing a waveform model that allows for parameterized deformations away from the predictions of GR and then constraining the associated parameters that govern those deviations [13, 15, 16, 21–26]. For previous observations of coalescing binary black holes [13, 15], these tests relied on the frequency domain `IMRPhenomPv2` waveform model of [27–29], which describes the inspiral, merger, and ringdown of vacuum black holes, and provides an effective description of spin precession making the best use of the results from analytical and numerical relativity [30–37]. The phase evolution of this waveform is governed by a set of coefficients p_n that depend on the component masses and spins. These coefficients include post-Newtonian (PN) parameters and phenomenological constants that are calibrated against numerical relativity waveforms to describe the intermediate regime between inspiral and merger, as well as the merger-ringdown. To test GR, the waveform model is generalized to allow for relative deviations in each of the coefficients in turn, *i.e.* by replacing $p_n \rightarrow (1 + \delta\hat{p}_n)p_n$, where the $\delta\hat{p}_n$ are zero in GR. The $\delta\hat{p}_n$ are then varied along with all the parameters that are also present in the case of GR (masses, spins, and extrinsic parameters), and posterior density functions (PDFs) are obtained using `LALInference` [38]. For GR to be correct, the value $\delta\hat{p}_n = 0$ should fall within the support of each of the PDFs.

In this work, we modify this approach in two ways. First, we use waveform models more suitable for binary neutron stars. Second, whereas the infrastructure [25] used to test GR with binary black holes observations [13, 15] was restricted to waveform models that depend directly on the coefficients p_n , we also introduce a new procedure that can include deviations to the phase

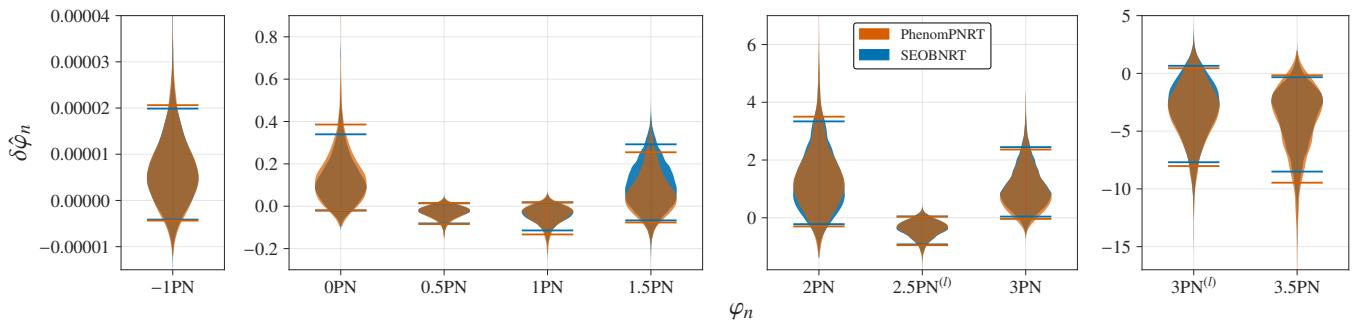


FIG. 1. Posterior density functions on deviations of PN coefficients $\delta\hat{\varphi}_n$ obtained using two different waveform models (PhenomPNRT and SEOBNRT); see the main text for details. The -1PN and 0.5PN corrections correspond to absolute deviations, whereas all others represent fractional deviations from the PN coefficient in GR. The horizontal bars indicate 90% credible regions.

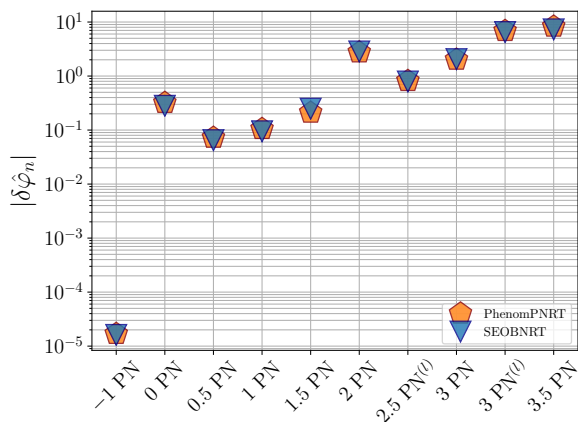


FIG. 2. 90% upper bounds on deviations $|\delta\hat{\varphi}_n|$ in the PN coefficients following from the posterior density functions shown in Fig. 1.

evolution parameterized by $\delta\hat{p}_n$ to any frequency domain waveform model [39]. We conduct independent tests of GR using inspiral-merger-ringdown models that incorporate deviations from GR using each of these two prescriptions; by comparing these analyses, we are able to estimate the magnitude of systematic modeling uncertainty in our results.

The merger and ringdown regimes of binary neutron stars differ from those of binary black holes, and tidal effects not present in binary black holes need to be included in the description of the inspiral. Significant work has been done to understand and model the dynamics of binary neutron stars analytically using the PN approximation to general relativity [40]. This includes modeling the non-spinning [30, 31] and spinning radiative/inspiral dynamics [32–37] as well as finite size effects [41–43] for binary neutron star systems. Frequency domain waveforms based on the stationary phase approximation [44] have been developed incorporating the abovementioned effects [45–47] and have been successfully employed for

the data analysis of compact binaries. A combination of these analytical results with the results from numerical relativity simulations of binary neutron star mergers (see [48] for a review) have led to the development of efficient waveform models which account for tidal effects [49–51].

We employ the `NRTidal` models introduced in [51, 52] as the basis of our binary neutron star waveforms: frequency domain waveform models for binary black holes are converted into waveforms for inspiraling neutron stars that undergo tidal deformations by adding to the phase an appropriate expression $\phi_T(f)$ and windowing the amplitude such that the merger and ringdown are smoothly removed from the model; see [52] for details. The closed-form expression for $\phi_T(f)$ is built by combining PN information, the tidal effective-one-body (EOB) model of [49], and input from numerical relativity (NR). The form of $\phi_T(f)$ was originally obtained in a setting where the neutron stars were irrotational or had their spins aligned to the angular momentum. Nevertheless, a waveform model that includes both tides and *precessing* spins can be constructed by first applying $\phi_T(f)$ to an aligned-spin waveform, and then performing the twisting-up procedure that introduces spin precession [53]. We consider two waveform models that use this description of tidal effects.

The first binary neutron star model we consider is constructed by applying this procedure to `IMRPhenomPv2` waveforms. Following the nomenclature of [19], we refer to the resulting waveform model as `PhenomPNRT`. Parameterized deformations $\delta\hat{p}_n$ are then introduced as shifts in parameters describing the phase in precisely the same way as was done for binary black holes. This will allow us to naturally combine PDFs for the $\delta\hat{p}_n$ from measurements on binary black holes and binary neutron stars, arriving at increasingly sharper results in the future. Because of the unknown merger-ringdown behavior in the case of binary neutron stars, which in any case gets removed from the waveform model, in practice only deviations $\delta\hat{\varphi}_n$ in the PN parameters φ_n can be bounded. The

set of possible testing parameters is taken to be

$$\{\delta\hat{\varphi}_{-2}, \delta\hat{\varphi}_0, \delta\hat{\varphi}_1, \delta\hat{\varphi}_2, \delta\hat{\varphi}_3, \delta\hat{\varphi}_4, \delta\hat{\varphi}_5^{(\ell)}, \delta\hat{\varphi}_6, \delta\hat{\varphi}_6^{(\ell)}, \delta\hat{\varphi}_7\}, \quad (1)$$

where the $\delta\hat{\varphi}_n$ are associated with powers of frequency $f^{(-5+n)/3}$, and $\delta\hat{\varphi}_5^{(\ell)}$ and $\delta\hat{\varphi}_6^{(\ell)}$ with functions $\log(f)$ and $\log(f) f^{1/3}$, respectively; $\delta\hat{\varphi}_5$ would be completely degenerate with some reference phase ϕ_c and hence is not included in the list. In addition to corrections to the positive PN order coefficients, deviations at -1 PN are included because they can constrain the presence of dipole radiation during the inspiral (discussed below). We do not consider deviations at -0.5 PN order because they do not arise from any known physical mechanism. $\delta\hat{\varphi}_{-2}$ and $\delta\hat{\varphi}_1$ represent absolute rather than relative deviations, as both are identically zero in GR.

We also employ the SEOBNRv4 waveform model, which is constructed from an aligned-spin EOB model for binary black holes augmented with information from NR simulations [54]. Using the methods of [55], this model is evaluated in the frequency domain, and then we add the tidal correction $\phi_T(f)$ as described above; we refer to the resulting waveform model as SEOBNRT. Unlike PhenomPNRT, the SEOBNRT model is not constructed explicitly in terms of PN coefficients φ_n . Instead, we model the effect of a relative shift $\delta\hat{\varphi}_n$ following [39] by adding to the frequency domain phase a term $\delta\hat{\varphi}_n \varphi_n f^{(-5+n)/3}$ or $\delta\hat{\varphi}_n^{(\ell)} \varphi_n^{(\ell)} f^{(-5+n)/3} \log(f)$, as applicable. These corrections are then tapered to zero at the merger frequency.

Fig. 1 depicts the PDFs on $\delta\hat{\varphi}_n$ recovered when only variations at that particular PN order are allowed. We find that the phase evolution of GW170817 is consistent with the GR prediction. The 90% credible region for each parameter contains the GR value of $\delta\hat{\varphi}_n = 0$ at all orders other than 3PN and 3.5PN.¹ The bounds on the positive-PN parameters ($n \geq 0$) obtained with GW170817 alone are comparable to those obtained by combining the binary black hole signals GW150914, GW151226, and GW170104 in [16] using the IMRPhenomPv2 waveform model. For convenience we also separately give 90% upper bounds on deviations in PN coefficients; see Fig. 2.

The PDFs shown in Fig. 1 were constructed using the same choice of prior distribution outlined in [19] with the following modifications. We use uniform priors on $\delta\hat{\varphi}_n$ that are broad enough to fully contain the plotted PDFs. Due to the degeneracy between $\delta\hat{\varphi}_0$ and the chirp mass, a broader prior distribution was chosen for the latter as compared to in [19] for runs in which $\delta\hat{\varphi}_0$ was allowed to vary. All inference was done assuming the prior $|\chi_i| \leq 0.99$, where $\chi_i = c\mathcal{S}_i/(Gm_i^2)$ is the dimensionless spin of each body. This conservative spin prior was chosen

to allow the constraints on $\delta\hat{\varphi}_n$ to be directly compared with those from binary black hole observations, which used the same prior [13, 15]. Nevertheless, throughout this paper we assume the two objects to be neutron stars, and following [19] we limit our prior on the component tidal parameters to $\Lambda_i \leq 5000$. (For a precise definition of the Λ_i , see [1] and references therein.) This choice was motivated by reasonable astrophysical assumptions regarding the expected ranges for neutron star masses and equations of state [42, 56, 57]; higher values of Λ are possible for some equations of state if the neutron star masses are small ($\simeq 0.9 M_\odot$). The extra freedom introduced by including $\delta\hat{\varphi}_n$ leads to a loss in sensitivity in the measurement of tidal parameters; in particular, the tail of the PDF for the tidal deformation of the less massive body Λ_2 touches the prior upper bound in many of the tests. The correlation between $\delta\hat{\varphi}_n$ and Λ_2 means that the upper bounds for $|\delta\hat{\varphi}_n|$ would be weaker if we did not impose our neutron star prior of $\Lambda_i \leq 5000$.

Certain differences are present between the PhenomPNRT and SEOBNRT waveform models and the way they are used. First, PhenomPNRT allows for precessing spin configurations, whereas the SEOBNRT is restricted to systems with spins aligned with the orbital angular momentum. Second, continuity conditions enforced in the construction of PhenomPNRT waveforms cause deviations from GR in the inspiral to affect the behavior of later phases of the signal, whereas the tapering of deviations in SEOBNRT ensures that the merger-ringdown of the underlying waveform is exactly reproduced. However, this discrepancy is not expected to affect measurements of $\delta\hat{\varphi}_n$ significantly, because the signal is dominated by the inspiral, and both waveform models are amplitude-tapered near merger. Third, the spin-induced quadrupole moment [58], which enters the phase at 2PN through quadrupole-monopole couplings, is computed using neutron-star universal relations [59] in PhenomPNRT and is assumed to take the black-hole value in SEOBNRT. Finally, in the PhenomPNRT model, fractional deviations are applied only to non-spinning terms in the PN expansion of the phase, *i.e.* terms dependent on the bodies' spins retain their GR values, while in SEOBNRT, fractional deviations are applied to all terms at a given post-Newtonian order. One can convert between these two parameterizations *post hoc* by requiring that the total phase correction be the same with either choice; the results shown in Figs. 1 and 2 correspond to the parameterization used by PhenomPNRT. Nevertheless, the different treatment of the spin terms may still explain the discrepancy seen at 1.5PN, where spin effects first enter. Either parameterization offers a reasonable phenomenological description of deviations from GR; the generally close correspondence at most PN orders between results from the two models indicates that the quantities measured can be interpreted in similar ways. For more details on each waveform model we use, see

¹ Using PhenomPNRT (SEOBNRT), the GR value lies at the 6.8-th (4.4-th) percentile of the PDF for the 3PN parameter and at the 95.0-th (96.7-th) percentile for the 3.5PN parameter.

Table I of [19].

The long inspiral observed in GW170817 (relative to previous binary black hole signals) allows us to place the first stringent constraints on $\delta\hat{\varphi}_{-2}$. Binaries comprised of compact objects with additional charges that characterize couplings with fields other than the metric will generically support a time-varying dipole moment. Such systems will emit dipole radiation in addition to the energy flux predicted in GR (given at leading order by the quadrupole formula). Provided that this additional flux is a small correction to the total flux, the dipole radiation mainly induces a negative -1PN order correction in the phase evolution. Writing the total energy flux as $\mathcal{F}_{\text{GW}} = \mathcal{F}_{\text{GR}}(1 + Bc^2/v^2)$, the leading-order modification to the phase due to theory-agnostic effects of dipole radiation is given by $\delta\hat{\varphi}_{-2} = -4B/7$ [60, 61]. Combining the PDFs shown in Fig. 1 obtained with the **PhenomPNRT** and **SEOBNRT** waveforms and restricting to the physical parameter space $B \geq 0$ corresponding to positive outgoing flux, the presence of dipole radiation in GW170817 can be constrained to $B \leq 1.2 \times 10^{-5}$. For comparison, precise timing of radio pulses from binary pulsars can constrain $|B| \lesssim 6 \times 10^{-8}$ [61]; this much stronger constraint arises, in part, because of the much longer observation time over which the inspirals of binary pulsars are tracked.

Though our bound on the dipole parameter B is weaker than existing constraints, it is the first that comes directly from the nonlinear and dynamical regime of gravity achieved during compact binary coalescences. In this regard, we note that for general scalar-tensor theories there are regions of parameter space where constraints from both Solar System and binary pulsar observations are satisfied, and yet new effects appear in the frequency range of GW detectors, such as spontaneous scalarization [62] or resonant excitation [63, 64] of a massive field, or dynamical scalarization [65–67].

CONSTRAINTS FROM GRAVITATIONAL WAVE PROPAGATION

The propagation of GWs may differ in theories beyond GR, and the deviations depend on the distance that the GWs travel. The search for such deviations provides unique tests of relativity, particularly when the distance inferred through GWs can be compared with an accurate, independent distance measurement from EM observations. In GR, GWs propagate non-dispersively at the speed of light with an amplitude inversely proportional to the distance travelled. Using GW170817, we carry out two different types of analyses to study the propagation of GWs, looking for possible deviations from GR’s predictions. The first method implements a generic modification to the GWs dispersion relation, adding terms that correct for a massive graviton, and momentum depen-

dent dispersion that could be apparent in Lorentz violating models [68, 69]. The second modifies the distance relation GWs follow in GR by adding correcting factors accounting for the GW’s *gravitational leakage* into the large extra dimensions of higher-dimensional theories of gravity [70, 71].

Constraints on Modified Dispersion

In GR, gravitational waves propagate at the speed of light and are non-dispersive, leading to a dispersion relation $E^2 = p^2 c^2$. An alternative theory may generically modify this as $E^2 = p^2 c^2 + A p^\alpha c^\alpha$, where A is the coefficient of modified dispersion corresponding to the exponent denoted by α [68, 69]. When $\alpha = 0$, a modification with $A > 0$ may be interpreted as due to a non-zero graviton mass ($A = m_g^2 c^4$) [69]. It can be shown that such modified dispersion relations would lead to corrections to the GW phasing, thereby allowing us to constrain any dispersion of GWs [69]. This method, implemented in a Bayesian framework, placed bounds on A corresponding to different α using binary black hole detections [16]. We apply the above method to constrain dispersion of GWs in the case of the binary neutron star merger GW170817 [1]. We find that GW170817 places weaker bounds on dispersion of GWs than the binary black holes. For instance, the bound on the graviton mass m_g we obtain from GW170817 is $9.51 \times 10^{-22} \text{ eV}/c^2$, which is weaker compared to the bounds reported in [16]. This is not surprising as GW170817 is the closest source detected so far, and for the same SNR propagation-based tests such as this are more effective when the sources are farther away. This method complements the bounds on non-dispersive standard model extension coefficients [72] reported in [2] from GW170817.

Constraints on the Number of Spacetime Dimensions

In higher-dimensional theories of gravity the scaling between the GW strain and the luminosity distance of the source is expected to be modified, suggesting a damping of the waveform due to gravitational leakage into large extra dimensions. This deviation from the GR scaling $h_{\text{GR}} \propto d_L^{-1}$ depends on the number of dimensions $D > 4$ and would result in a systematic overestimation of the source luminosity distance inferred from GW observations [70, 71]. A comparison of distance measurements from GW and EM observations of GW170817 allows us to constrain the presence of large additional spacetime dimensions. We assume, as is the case in many extra-dimensional models, that light and matter propagate in four spacetime dimensions only, thus allowing us to infer the EM luminosity distance d_L^{EM} . In the absence of a

complete, unique GW model in higher-dimensional gravity, we use a phenomenological ansatz for the GW amplitude scaling and neglect all other effects of modified gravity in the GW phase and amplitude. This approach requires that gravity be asymptotically GR in the strong-field regime, while modifications due to leakage into extra dimensions start to appear at large distances from the source. We therefore consider gravity modifications with a screening mechanism, i.e., a phenomenological model with a characteristic length scale R_c beyond which the propagating GWs start to leak into higher dimensions. In this model, the strain scales as

$$h \propto \frac{1}{d_L^{\text{GW}}} = \frac{1}{d_L^{\text{EM}}} \left[1 + \left(\frac{d_L^{\text{EM}}}{R_c} \right)^n \right]^{-(D-4)/(2n)} \quad (2)$$

$$p(D|x_{\text{GW}}, x_{\text{EM}}) = \int p(d_L^{\text{GW}}|x_{\text{GW}})p(d_L^{\text{EM}}|x_{\text{EM}})\delta(D - D(d_L^{\text{GW}}, d_L^{\text{EM}}, R_c, n)) dd_L^{\text{GW}} dd_L^{\text{EM}}. \quad (3)$$

As in [19], we use a measurement of the surface brightness fluctuation distance to the host galaxy NGC 4993 from [73] to constrain the EM distance, assuming a Gaussian distribution for the posterior probability $p(d_L^{\text{EM}}|x_{\text{EM}})$, with the mean value and standard deviation given by 40.7 ± 2.4 Mpc [73]. Contrary to [71], our analysis relies on a direct measurement of d_L^{EM} and is independent of prior information on H_0 or any other cosmological parameter. For the measurement of the GW distance, the posterior distribution $p(d_L^{\text{GW}}|x_{\text{GW}})$ was inferred from the GW data assuming general relativity and fixing the sky position to the optical counterpart while marginalizing over all other waveform parameters [19]. Our analysis imposes a prior on the GW luminosity distance that is consistent with a four-dimensional Universe, but we have checked that other reasonable prior choices do not significantly modify the results. We invert the scaling relation in Eq. (2) to compute $D(d_L^{\text{GW}}, d_L^{\text{EM}}, R_c, n)$ in Eq. (3). Fig. 3 shows the 90% upper bounds on the number of dimensions D , for theories with a certain transition steepness n and distance scale R_c . Shading indicates the excluded regions of parameter space. Our results are consistent with the GR prediction of $D = 4$.

Additionally, the data allows us to infer constraints on the characteristic distance scale R_c of higher-dimensional theories with a screening mechanism, while fixing D to 5, 6 or 7. The posterior for $p(R_c|x_{\text{GW}}, x_{\text{EM}})$ is obtained from the joint posterior probability of R_c, d_L^{GW} and d_L^{EM} , fixing D instead of R_c in Eq. (3) and computing $R_c(d_L^{\text{GW}}, d_L^{\text{EM}}, D, n)$ by inverting the scaling relation

where D denotes the number of spacetime dimensions, and where R_c and n are the distance scale of the screening and the transition steepness, respectively. Eq. (2) reduces to the standard GR scaling at distances much shorter than R_c , and the model is consistent with tests of GR performed in the Solar System or with binary pulsars. Unlike the scaling relation considered in [70, 71], notice that Eq. (2) reduces to the GR limit for $D = 4$ spacetime dimensions. An independent measurement of the source luminosity distance from EM observations of GW170817 allows us to infer the number of spacetime dimensions from a comparison of the GW and EM distance estimates, for given values of model parameters R_c and n . Constraints on the number of spacetime dimensions are derived in a framework of Bayesian analysis, from the joint posterior probability for D, d_L^{GW} and d_L^{EM} , given the two statistically independent measurements of EM data x_{EM} and GW data x_{GW} . The posterior for D is then given by:

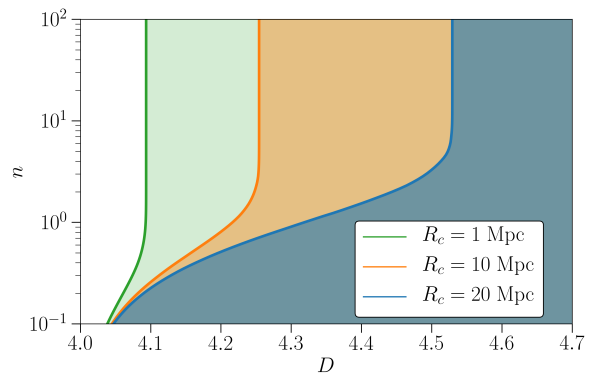


FIG. 3. 90% upper bounds on the number of spacetime dimensions D , assuming fixed transition steepness n and distance scale R_c . Shading indicates the regions of parameter space excluded by the data.

in Eq. (2). Since we consider higher-dimensional models that allow only for a relative damping of the GW signal, we select posterior samples with $d_L^{\text{GW}} > d_L^{\text{EM}}$, leading to an additional step function $\theta(d_L^{\text{GW}} - d_L^{\text{EM}})$ in $p(R_c|x_{\text{GW}}, x_{\text{EM}})$. In Fig. 4, we show 10% lower bounds on the screening radius R_c , for theories with a certain fixed transition steepness n and number of dimensions $D > 4$. Shading indicates the excluded regions of parameter space. For higher-dimensional theories of gravity with a characteristic length scale R_c of the order of the Hubble radius $R_H \sim 4$ Gpc, such as the well known Dvali-Gabadadze-Porrati (DGP) models of dark energy

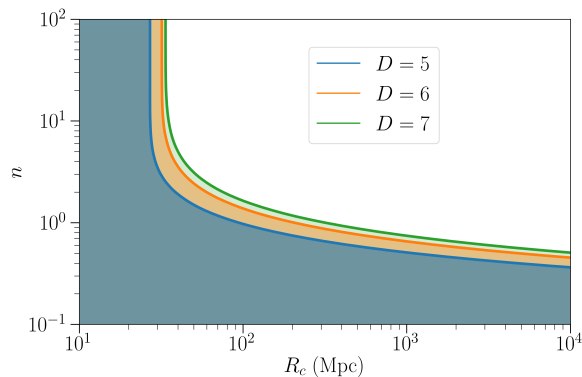


FIG. 4. 10% lower limits on the distance scale R_c (in Mpc), assuming fixed transition steepness n and number of spacetime dimensions D . Shading indicates the regions of parameter space excluded by the data.

[74, 75], small transition steepnesses ($n \sim \mathcal{O}(0.1)$) are excluded by the data. Our analysis cannot conclusively rule out DGP models that provide a sufficiently steep transition ($n > 1$) between GR and the onset of gravitational leakage. Future LIGO-Virgo observations of binary neutron star mergers, especially at higher redshifts, have the potential to place stronger constraints on higher-dimensional gravity.

CONSTRAINTS ON THE POLARIZATION OF GRAVITATIONAL WAVES

Generic metric theories of gravity predict up to six polarization modes for metric perturbations: two tensor (helicity ± 2), two vector (helicity ± 1), and two scalar (helicity 0) modes [76, 77]. GWs in GR, however, have only the two tensor modes regardless of the source properties; any detection of a non-tensor mode would be unambiguous indication of physics beyond GR. The GW strain measured by a detector can be written in general as $h(t) = F^A h_A$, where h_A are the 6 independent polarization modes and F^A represent the detector responses to the different modes $A = (+, \times, x, y, b, l)$. The antenna response functions depend only on the detector orientation and GW helicity, i.e. they are independent of the intrinsic properties of the source. We can therefore place bounds on the polarization content of GW170817 by studying which combination of response functions is consistent with the signal observed [78–82].

The first test on the polarization of GWs was performed for GW150914 [13]. The number of GR polarization modes expected was equal to the number of detectors in the network that observed GW150914, rendering this test inconclusive. The addition of Virgo to the network of GW detectors allowed for the first informative test of polarization for GW170814 [17]. This analysis established that the GW data was better described by pure tensor

modes than pure vector or pure scalar modes with Bayes factors in favor of tensor modes of more than 200 and 1000 respectively.

We here carry out a test similar to [17] by performing a coherent Bayesian analysis of the signal properties with the three interferometer outputs, using either the tensor or the vector or the scalar response functions. (Note that although the SNR in Virgo was significantly lower than in the two LIGO detectors, the Virgo data stream still carries information about the signal.) We assume that the phase evolution of the GW can be described by GR templates, but the polarization content can vary [83]. The phase evolution is modeled with the GR waveform model `IMRPhenomPv2` and the analysis is carried out with `LALInference` [38]. Tidal effects are not included in this waveform model, but this is not expected to affect the results presented below, since the polarization test is sensitive to the antenna pattern functions of the detectors and not the phase evolution of the signal, as argued above. The analysis described above tests for the presence of pure tensor, vector, or scalar modes. We leave the analysis of mixed-mode content to future work.

If the sky location of GW170817 is constrained to NGC 4993, we find overwhelming evidence in favor of pure tensor polarization modes in comparison to pure vector and pure scalar modes with a (base ten) logarithm of the Bayes factor of $+20.81 \pm 0.08$ and $+23.09 \pm 0.08$ respectively. This result is many orders of magnitude stronger than the GW170814 case both due to the sky position of GW170817 relative to the detectors and the fact that the sky position is determined precisely by electromagnetic observations. Indeed if the sky location is unconstrained we find evidence against scalar modes with $+5.84 \pm 0.09$, while the test is inconclusive for vector modes with $+0.72 \pm 0.09$.

CONCLUSIONS

Using the binary neutron star coalescence signal GW170817, and in some cases also its associated electromagnetic counterpart, we have subjected general relativity to a range of tests related to the dynamics of the source (putting bounds on deviations of PN coefficients), the propagation of gravitational waves (constraining local Lorentz invariance violations, as well as large extra dimensions), and the polarization content of gravitational waves. In all cases we find agreement with the predictions of GR.

The upcoming observing runs of the LIGO and Virgo detectors are expected to result in more detections of binary neutron star coalescences [84]. Along with electromagnetic observations, combining information from gravitational wave events (including binary black hole mergers) will lead to increasingly more stringent constraints on deviations from general relativity [25, 26], or conceiv-

ably potential evidence of the theory's shortcomings.

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† Deceased, November 2017.

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