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Astrophysical Rates of Gravitational-Wave Compact Binary Sources in O3

Tom Dent (Albert Einstein Institute, Hannover)
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for the LIGO and Virgo Collaborations

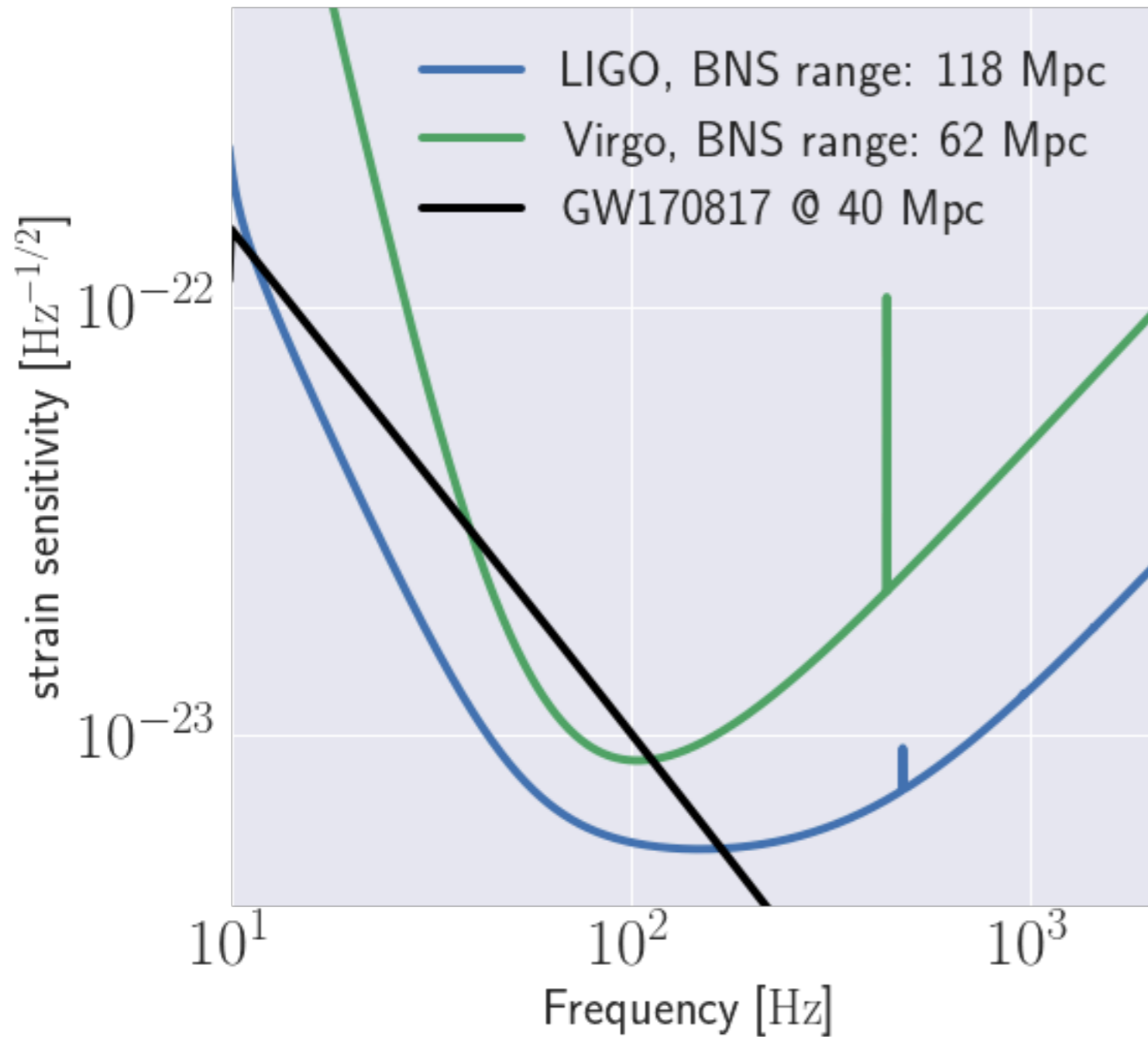
DCC: [LIGO-G1800370](#)



Strain sensitivity for LIGO and Virgo

Values are projected and representative, **but not official**

Actual strain sensitivity **may be different** in O3



BNS **ranges** quoted for a **1.4+1.4**
 M_{\odot} face-on system at **SNR 8** in a
single instrument, averaged over
binary orientations and sky location

for O3...

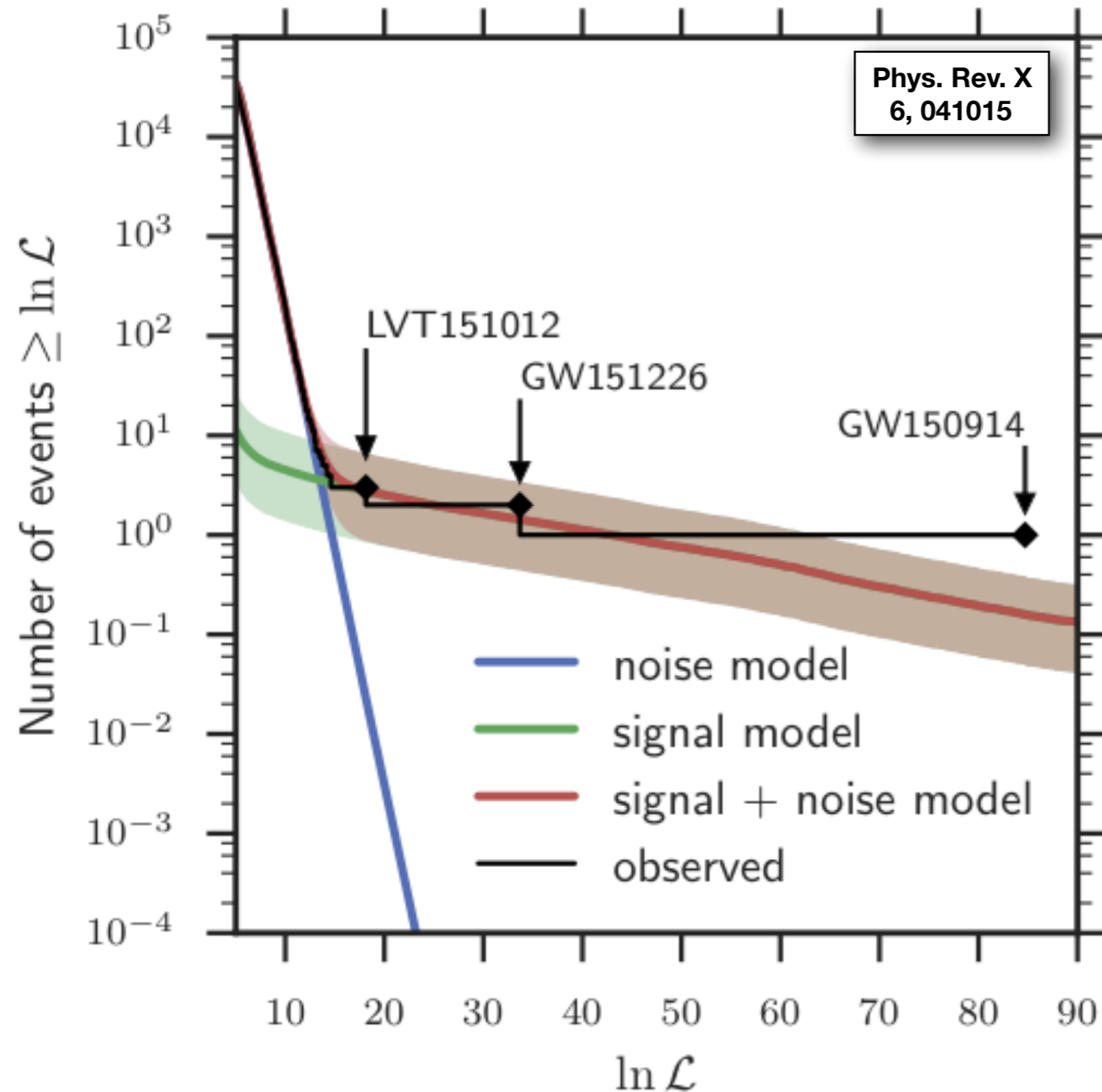
Expected LIGO BNS range: **120 Mpc**

Expected Virgo BNS range: **65 Mpc**

GW170817 is at **1/3** (LIGO) of the
sky/orientation averaged range for O3

Calculating event rates and significance

Model comparison of noise background and signal distributions of ranking statistic



Expected number of counts calibrated to surveyed space-time volume $\langle VT \rangle$

$$V = \int f(z, \mathcal{M}_c, \dots) \frac{1}{1+z} \frac{dV}{dz} dz$$

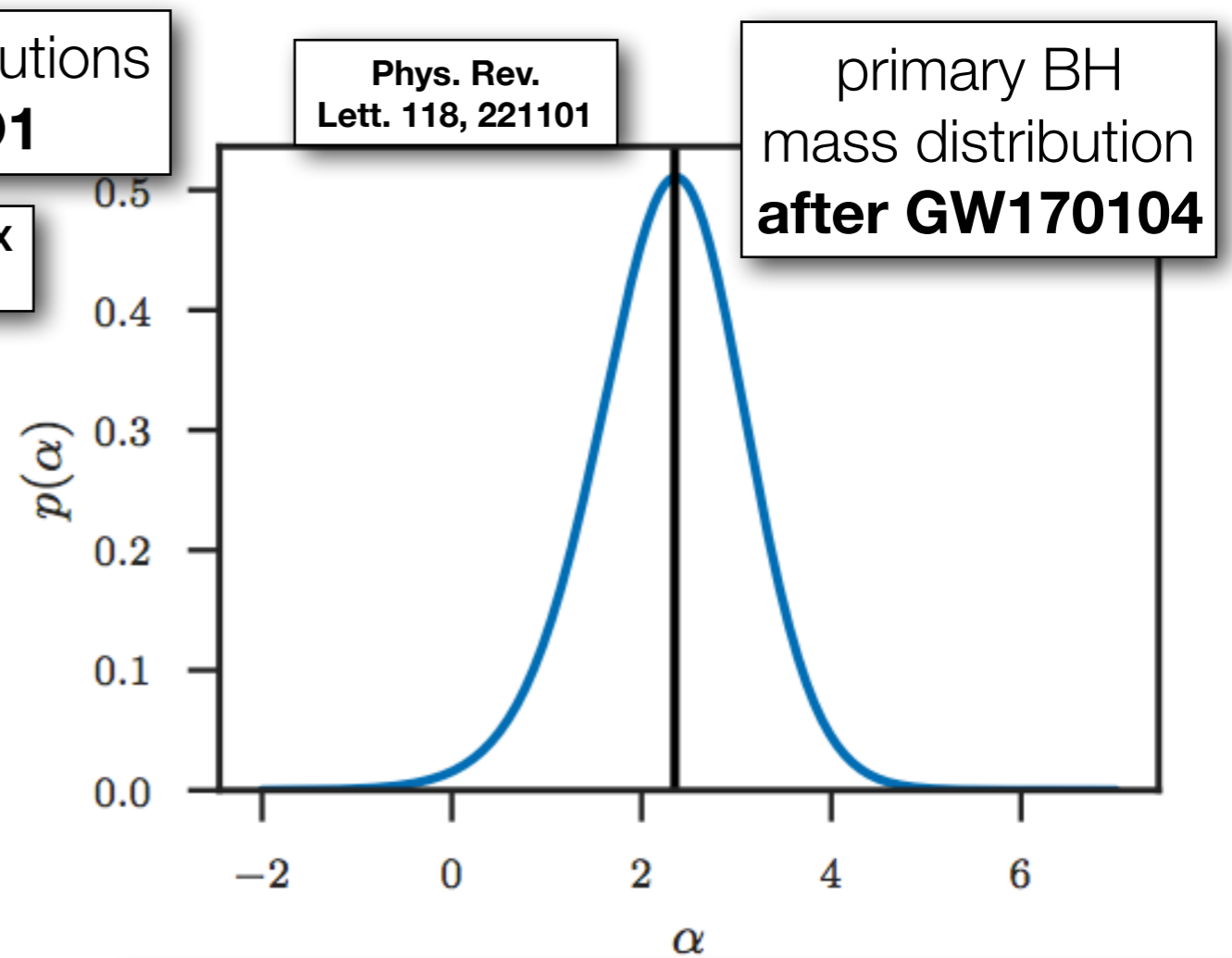
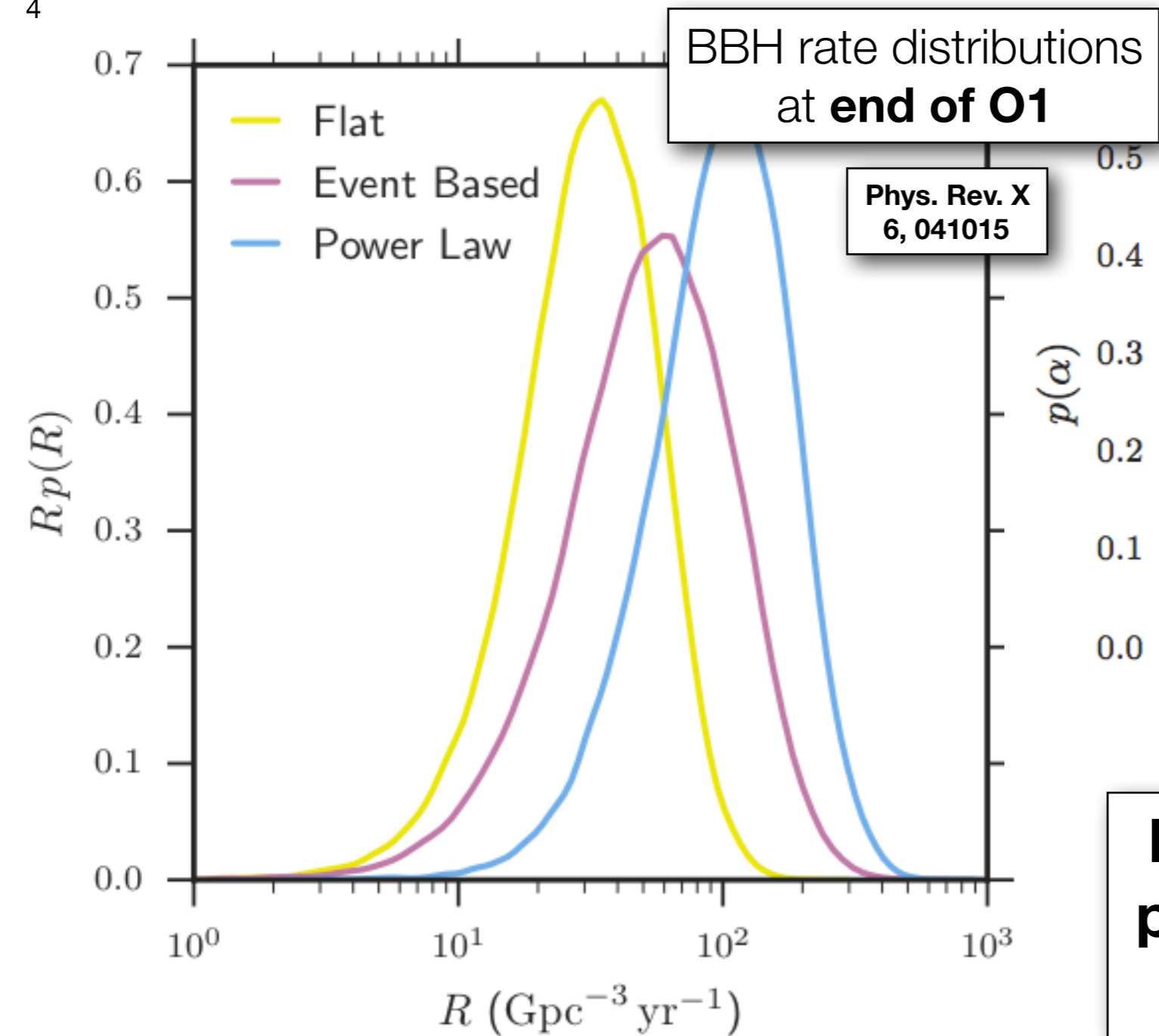
$$\rightarrow R \sim N / \langle VT \rangle$$

Moving pieces

VT is dependent on instrument duty cycle and SNR threshold

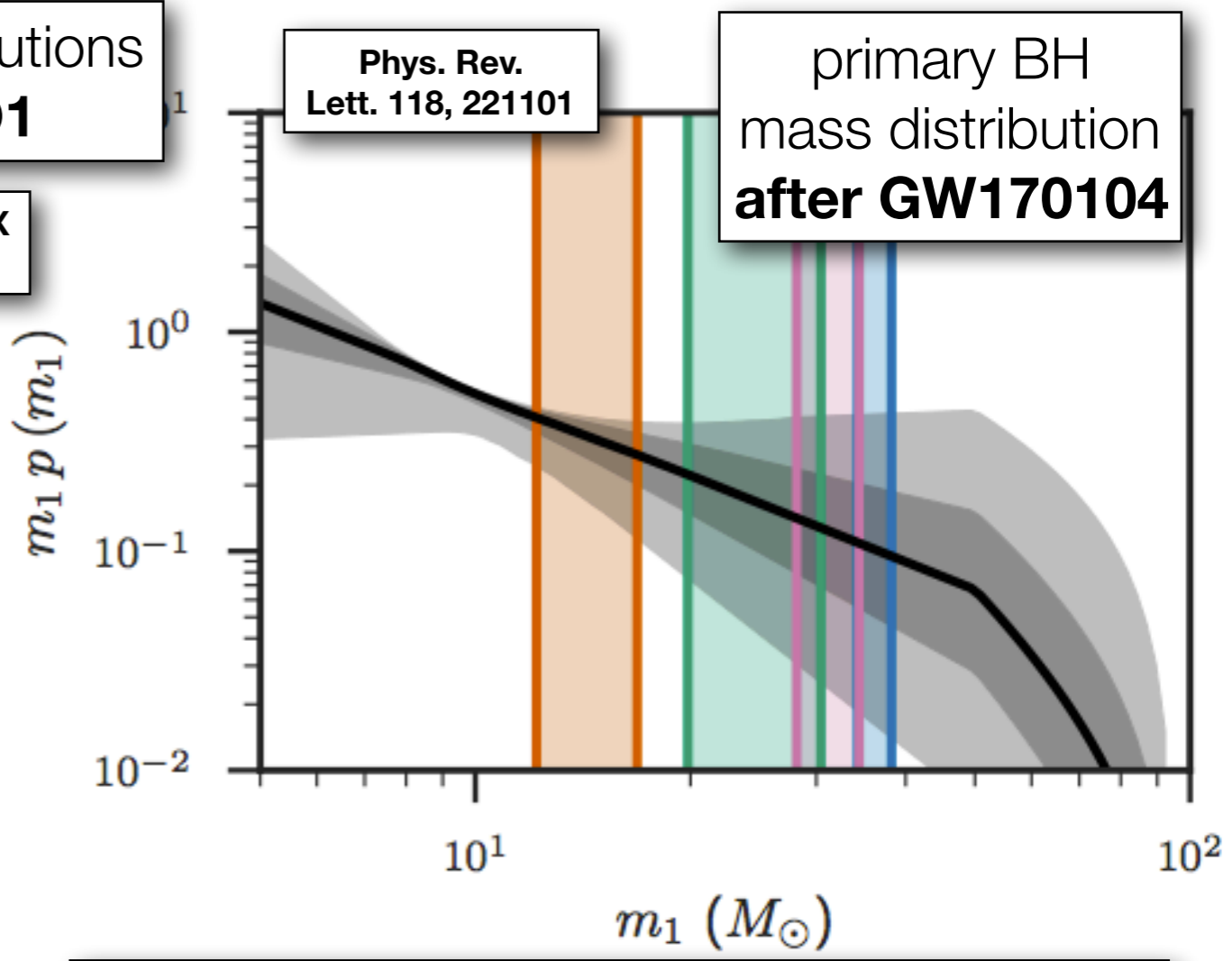
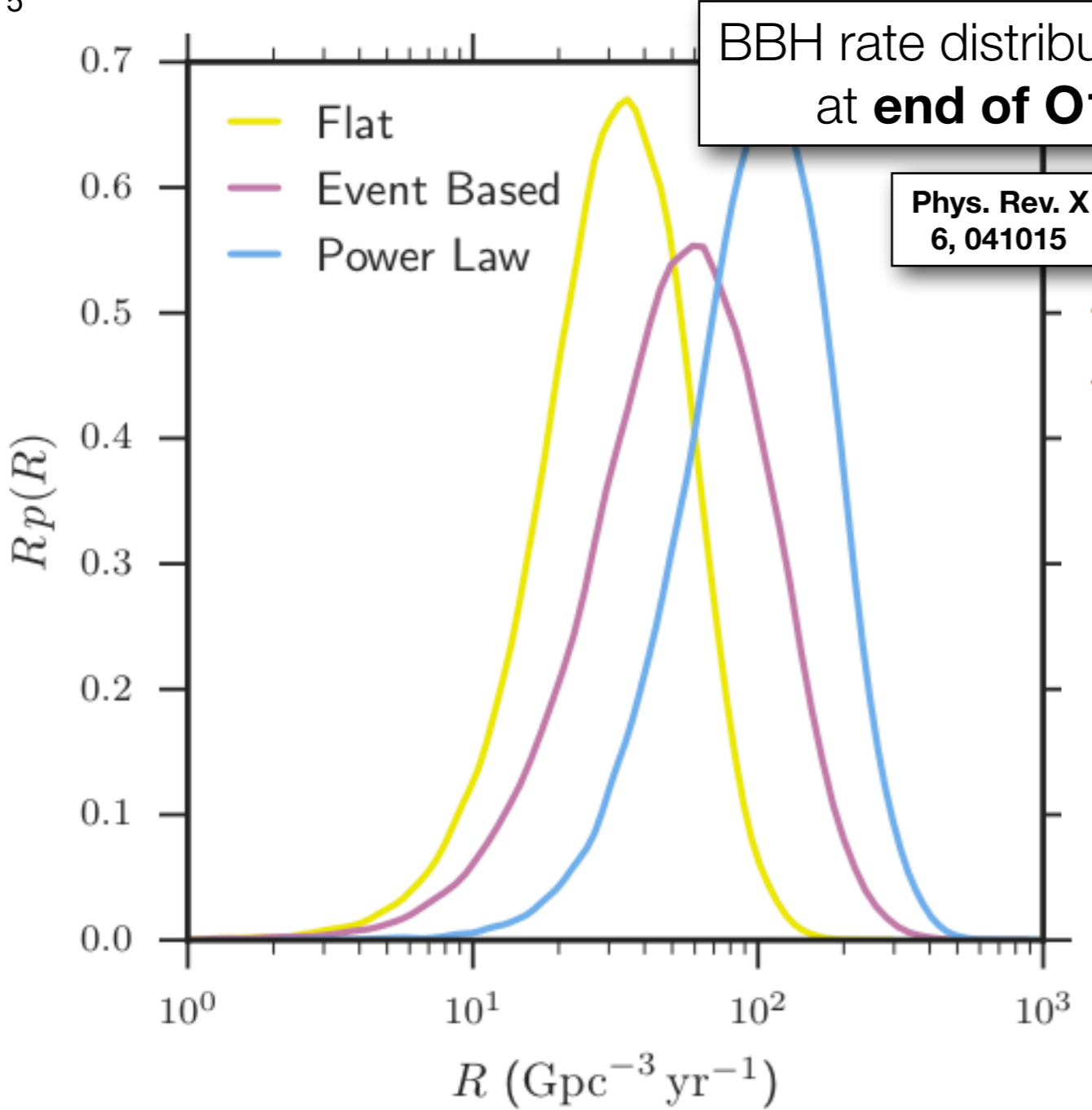
alerts could have smaller SNRs than “gold plated” events

all binary physics is not encoded in searches: *assumed SNR loss is small*



Basic Pop. Modeling: Assume $p(m_1) \propto m_1^{-\alpha}$ and fit observations to model

After GW170104 ($N_{\text{BBH}}=3.9$)
 Uniform in log mass: **12 - 65 $\text{Gpc}^{-3}\text{yr}^{-1}$**
 Power law ($\alpha=-2.35$) *only*: **40 - 213 $\text{Gpc}^{-3}\text{yr}^{-1}$**
 Unified interval: **12 - 213 $\text{Gpc}^{-3}\text{yr}^{-1}$**



Towards Pop. Distributions:
 Constraints on the primary mass distribution from current observations (assumes power law from previous slide)

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BNS/NSBH rate distributions
at **end of O1**

ApJ Letters, 832, 2

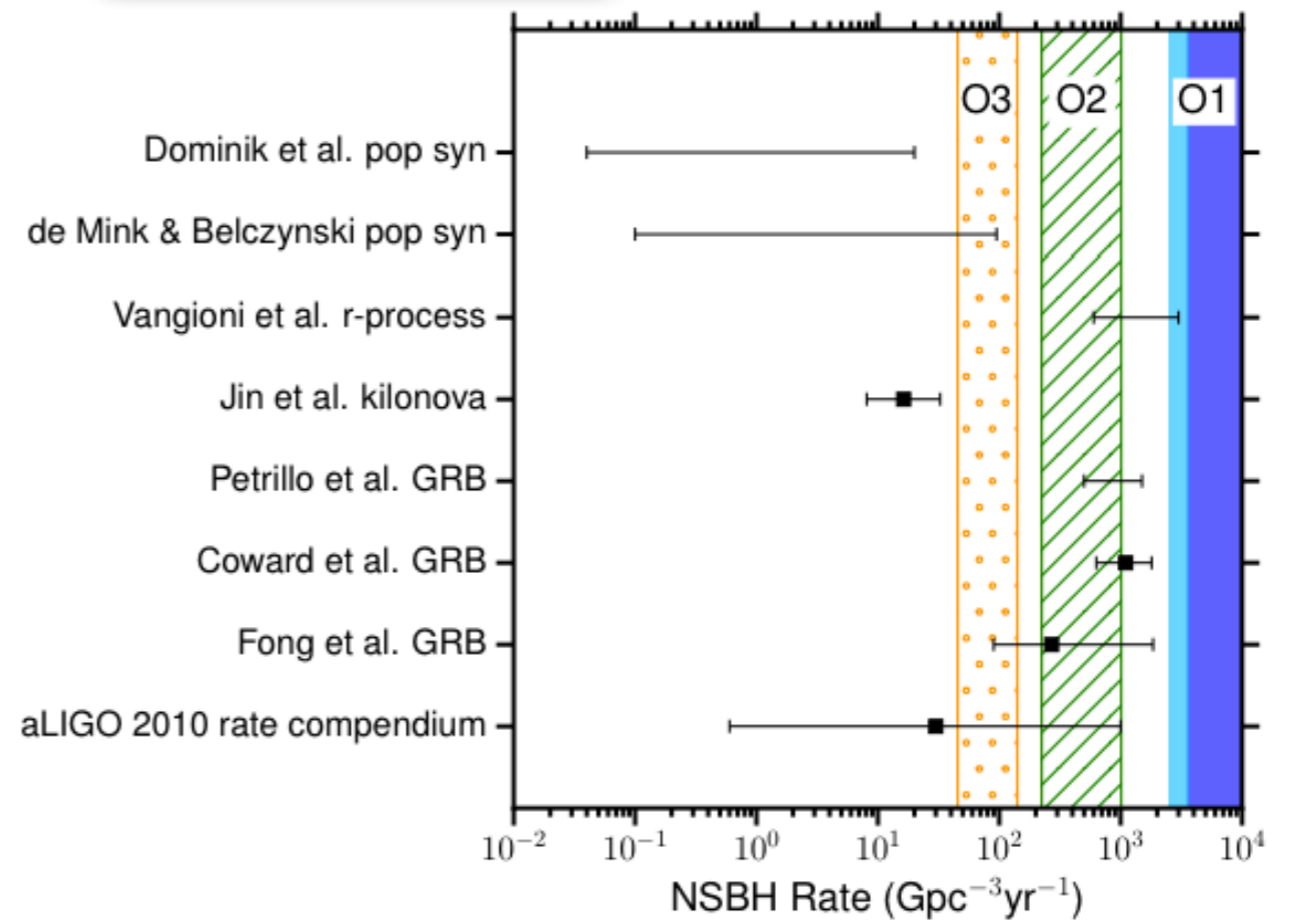
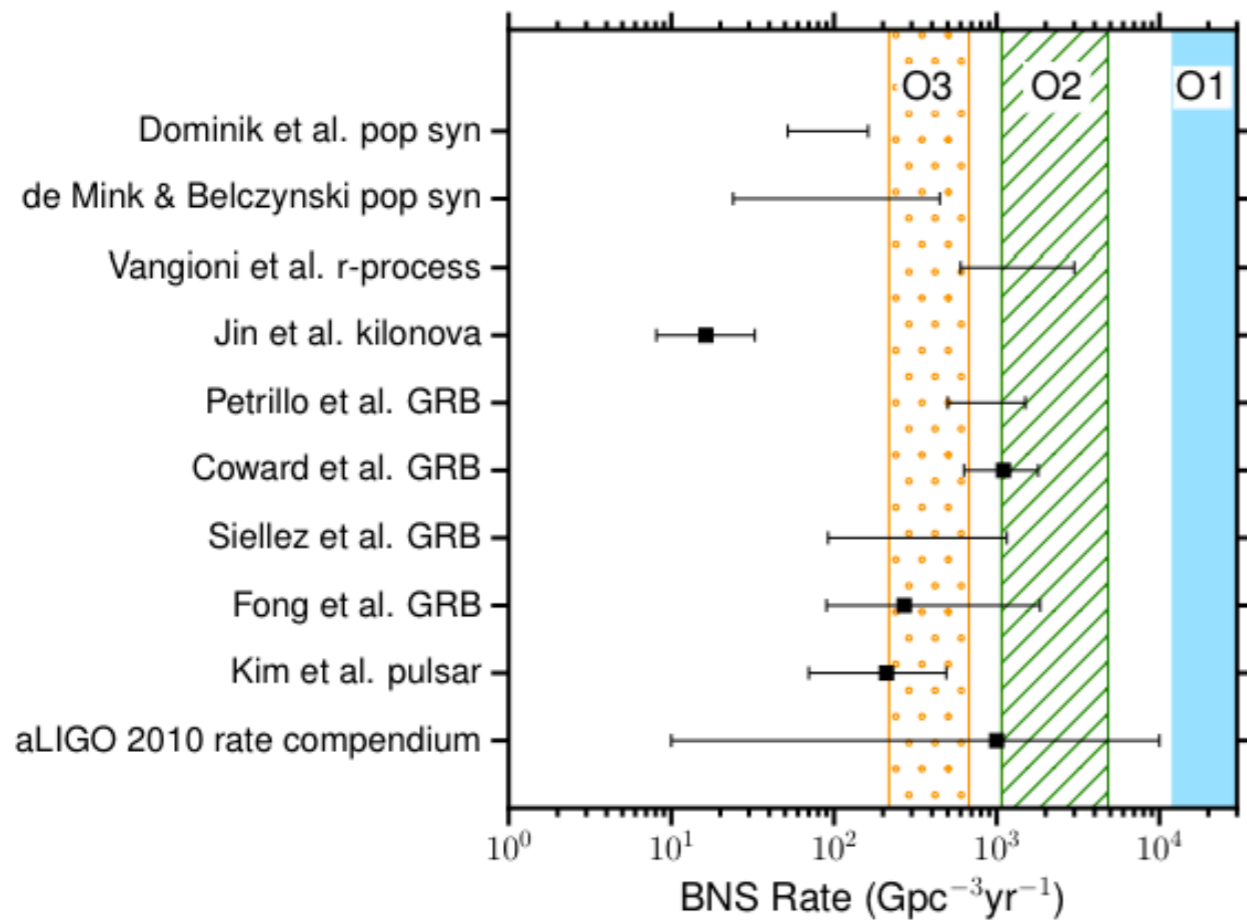


TABLE IV: Compact binary coalescence rates per Mpc^3 per Myr.^a

Source	R_{low}	R_{re}	R_{high}	R_{max}
NS-NS ($\text{Mpc}^{-3} \text{ Myr}^{-1}$)	0.01 [1]	1 [1]	10 [1]	50 [16]
NS-BH ($\text{Mpc}^{-3} \text{ Myr}^{-1}$)	6×10^{-4} [18]	0.03 [18]	1 [18]	
BH-BH ($\text{Mpc}^{-3} \text{ Myr}^{-1}$)	1×10^{-4} [14]	0.005 [14]	0.3 [14]	

BNS/NSBH rate distributions
at **end of O1**

ApJ Letters, 832, 2

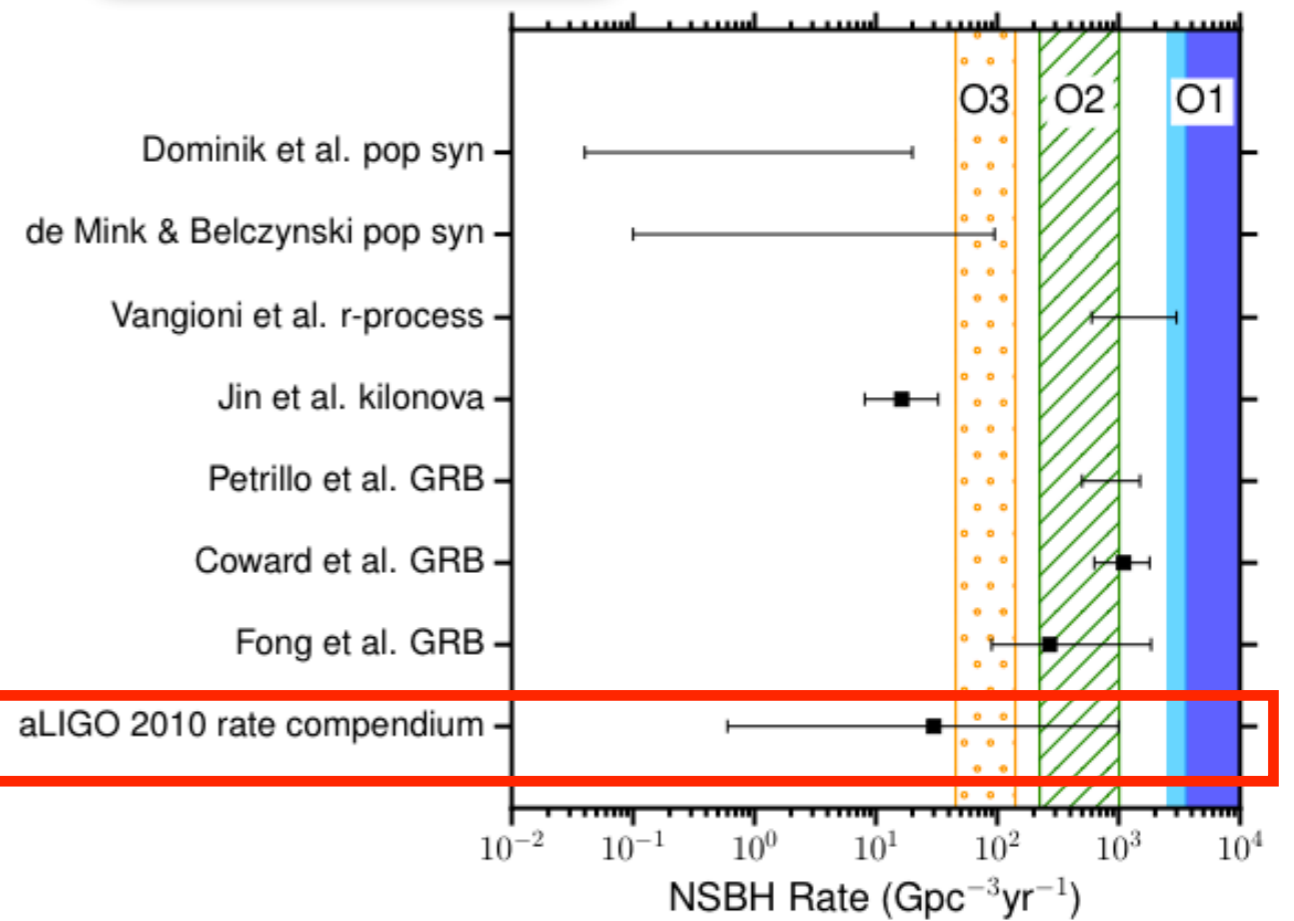
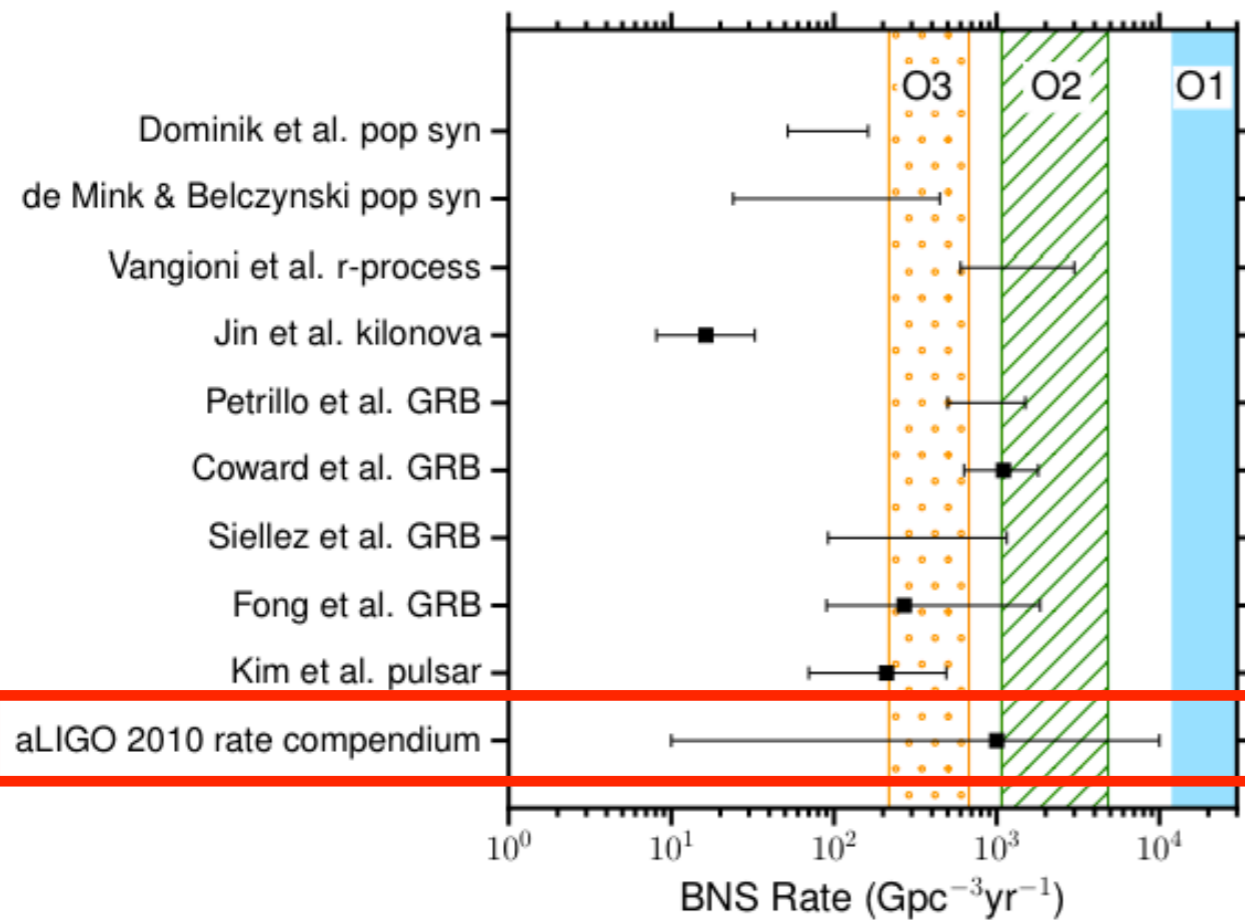


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Class. Quantum Grav. 27
(2010) 173001

Epoch			2015–2016	2016–2017	2018–2019	2020+	2024+
Planned run duration			4 months	9 months	12 months	(per year)	(per year)
Expected burst range/Mpc	LIGO		40–60	60–75	75–90	105	105
	Virgo		—	20–40	40–50	40–70	80
	KAGRA		—	—	—	—	100
Expected BNS range/Mpc	LIGO		40–80	80–120	120–170	190	190
	Virgo		—	20–65	65–85	65–115	125
	KAGRA		—	—	—	—	140
Achieved BNS range/Mpc	LIGO		60–80	60–100	—	—	—
	Virgo		—	25–30	—	—	—
	KAGRA		—	—	—	—	—
Estimated BNS detections			0.05–1	0.2–4.5	1–50	4–80	11–180
Actual BNS detections			0	1	—	—	—
90% CR	% within	5 deg ²	< 1	1–5	1–4	3–7	23–30
		20 deg ²	< 1	7–14	12–21	14–22	65–73
		median/deg ²	460–530	230–320	120–180	110–180	9–12
Searched area	% within	5 deg ²	4–6	15–21	20–26	23–29	62–67
		20 deg ²	14–17	33–41	42–50	44–52	87–90

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post-GW170817:
 $R_{\text{BNS}} \sim 3.2 \times 10^{-7} - 4 \times 10^{-6} \text{ Mpc}^{-3}\text{yr}^{-1}$

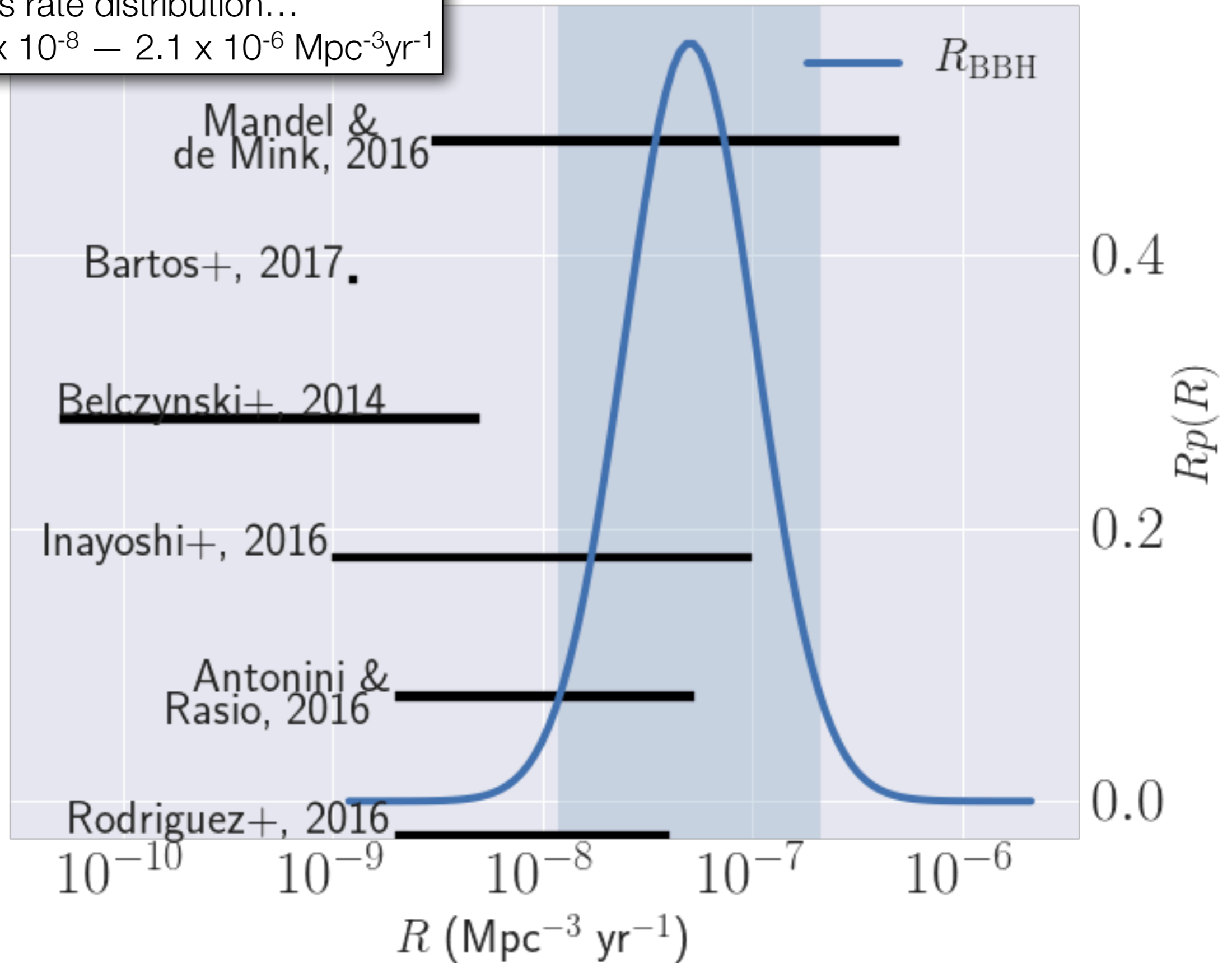
Phys. Rev.
Lett. 119, 16110

Binary Black Hole Rates
(post-GW170104)

Phys. Rev.
Lett. 118, 221101

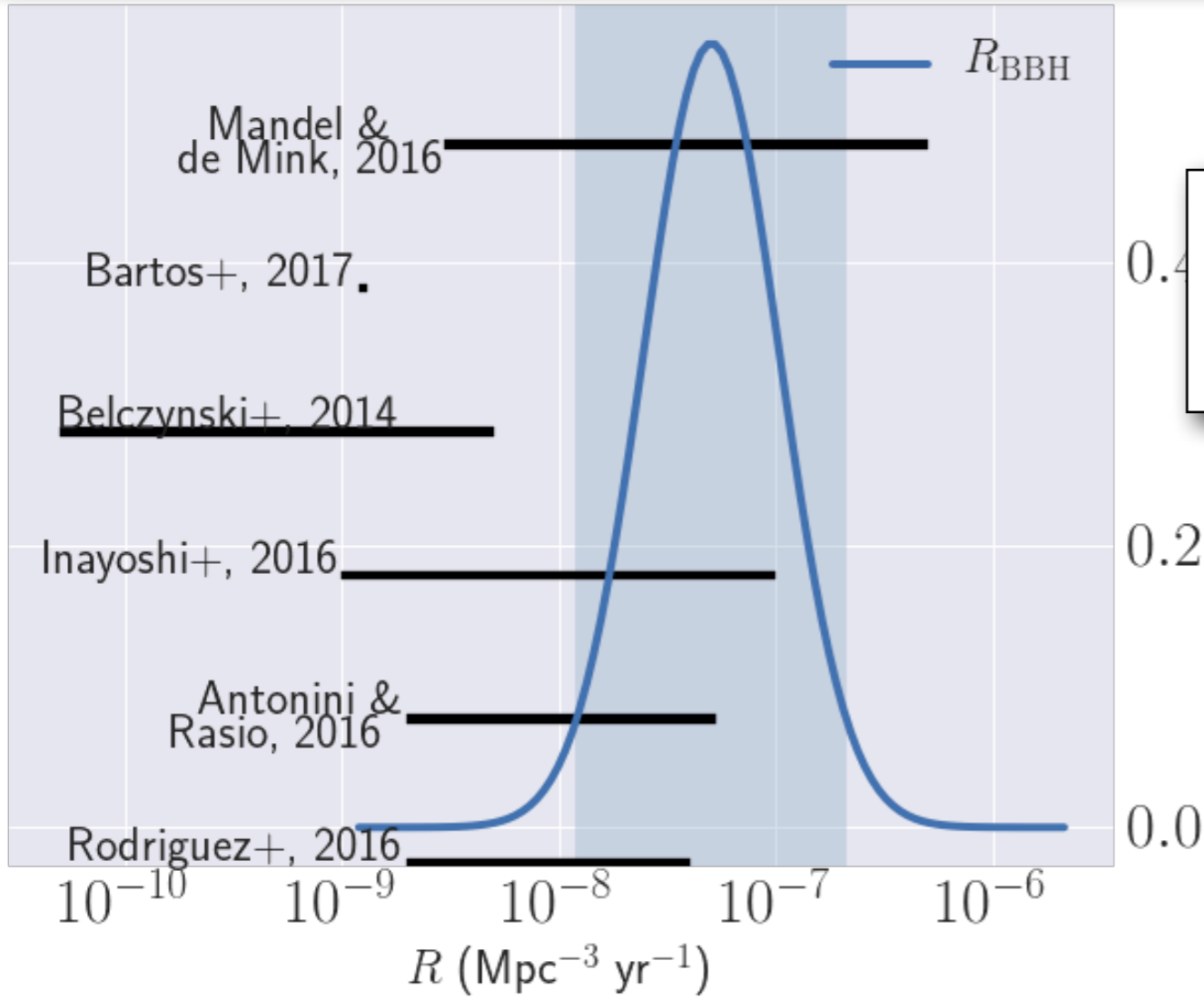
This rate distribution...

$$R_{\text{BBH}} \sim 1.2 \times 10^{-8} - 2.1 \times 10^{-6} \text{ Mpc}^{-3}\text{yr}^{-1}$$



Binary Black Hole Rates (post-GW170104)

Assumptions:
 $\rho_{\text{net}} > 12$
 $T_{\text{obs}}: 1 \text{ yr with } 50\%$
 duty cycle

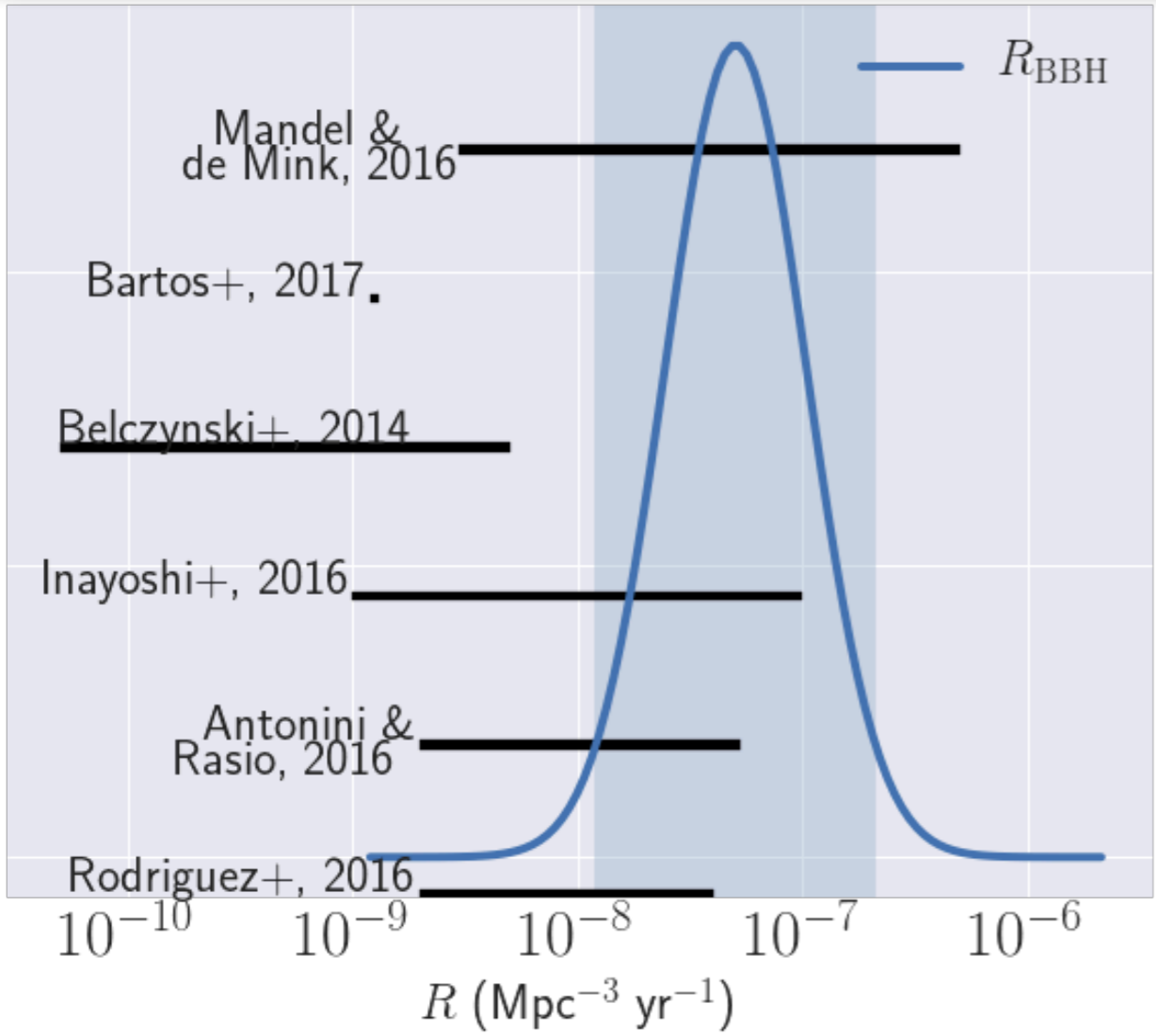


log-uniform: $p(m_1) \sim m_1^{-1}$ ($5 < m_1 < 100 M_{\odot}$)
 ...with O3 surveyed space-time volume:
 $VT_{\text{BBH}} \sim 7 \times 10^8 \text{ Mpc}^3 \text{ yr}$

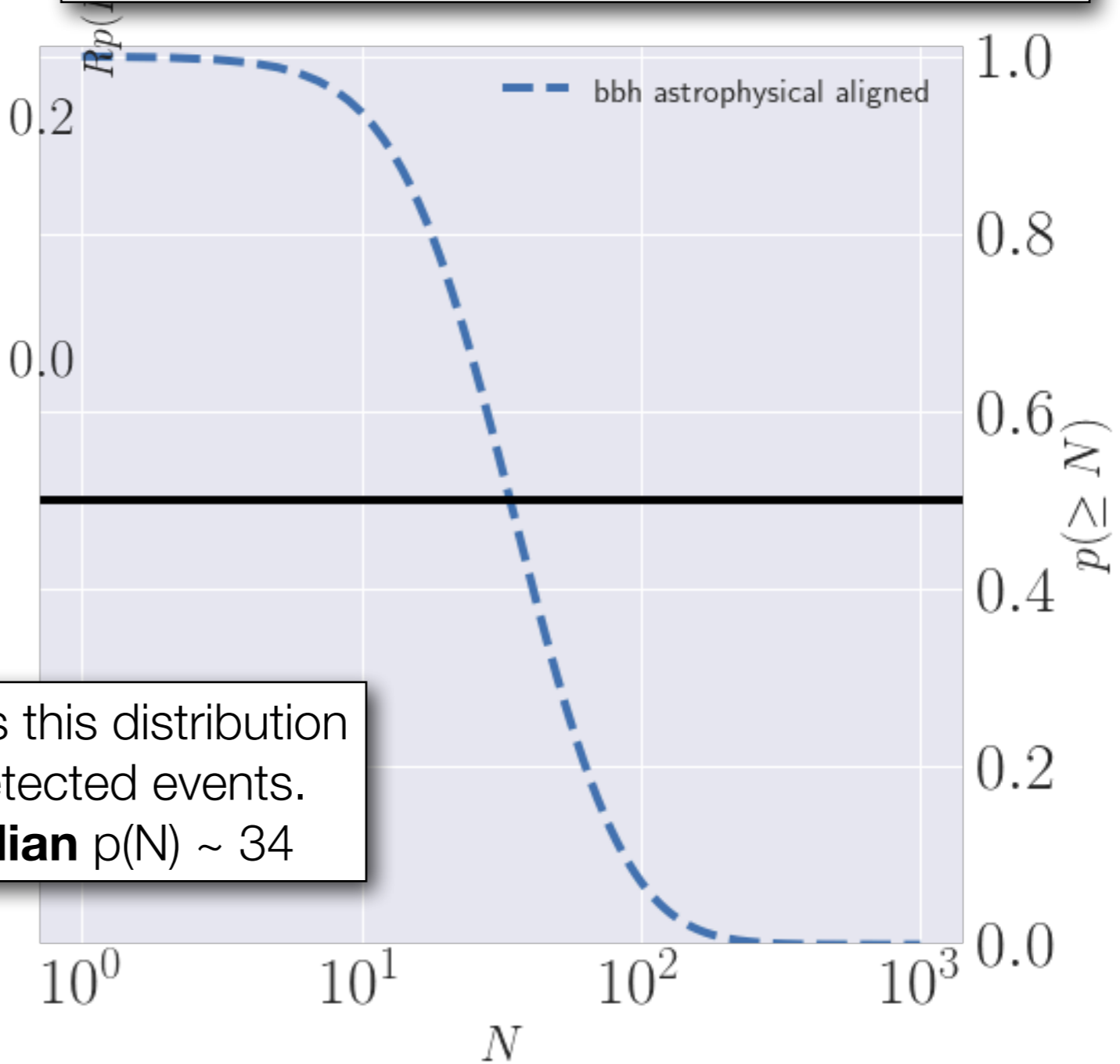
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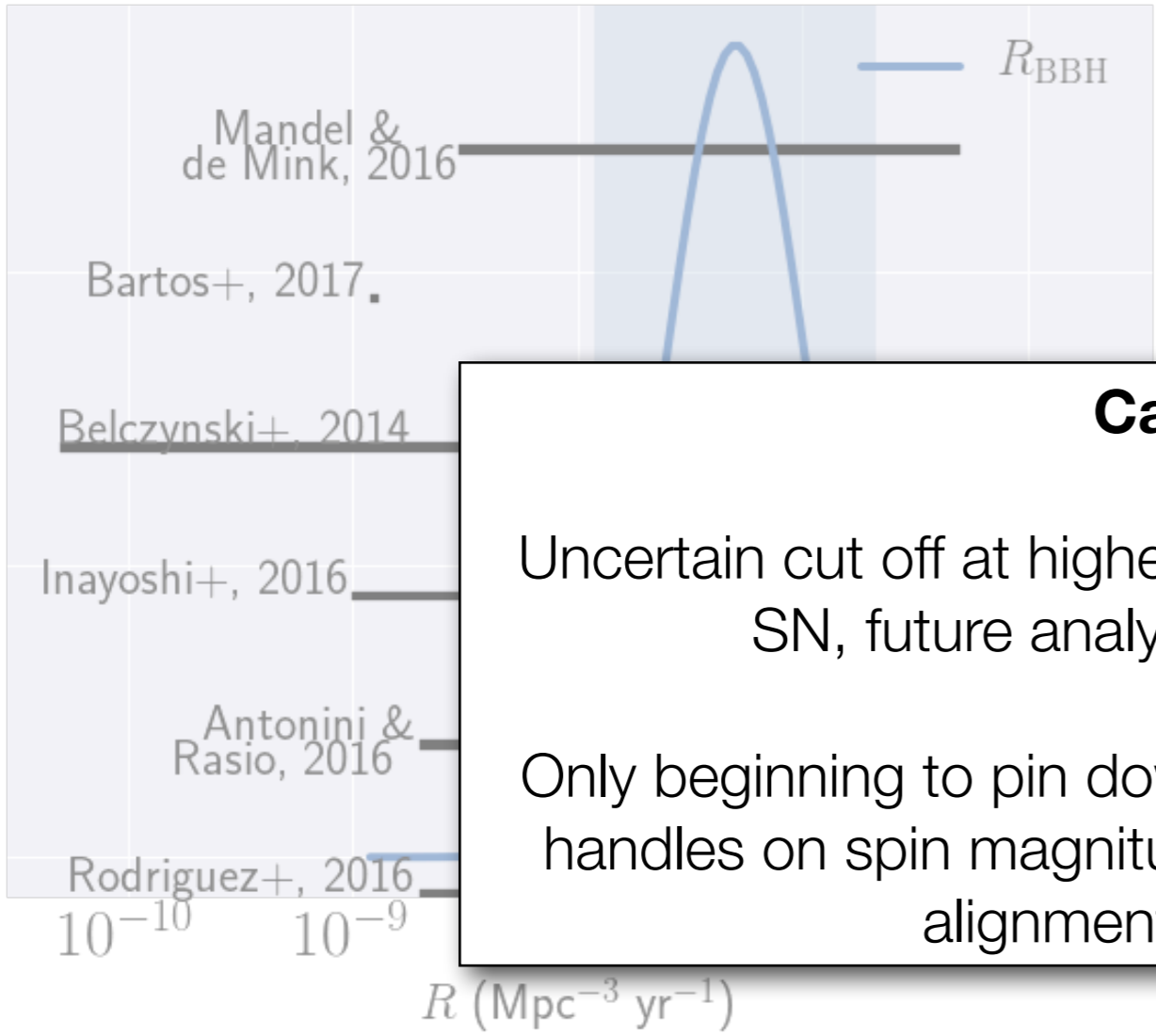


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...gives this distribution of detected events.
median $p(N) \sim 34$

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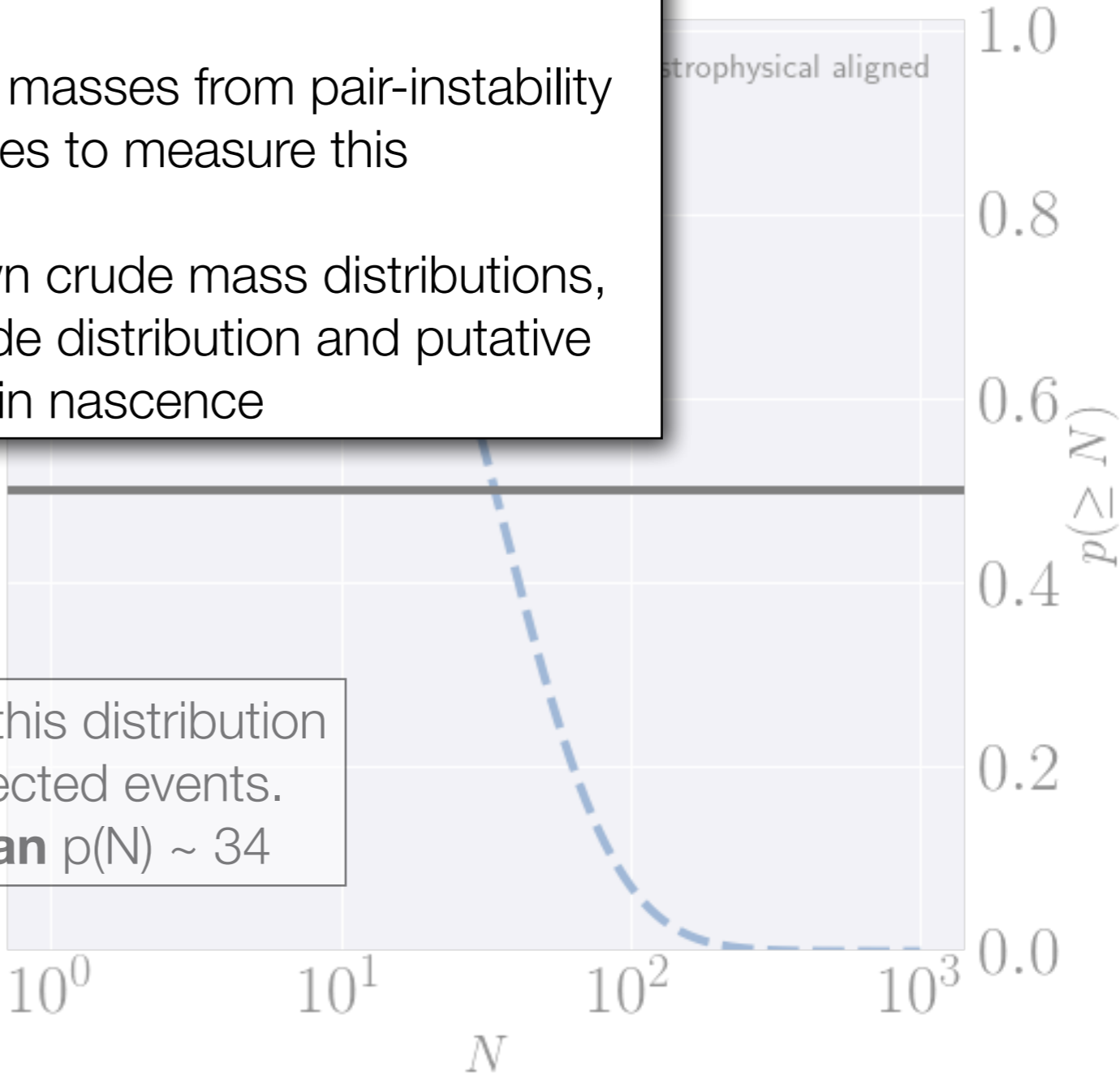


log-uniform: $p(m_1) \sim m_1^{-1}$ ($5 < m_1 < 100 M_{\odot}$)
 ...with O3 surveyed space-time volume:
 $100 \text{ Mpc}^3 \text{ yr}$

Caveats

Uncertain cut off at higher masses from pair-instability SN, future analyses to measure this

Only beginning to pin down crude mass distributions, handles on spin magnitude distribution and putative alignment in nascence



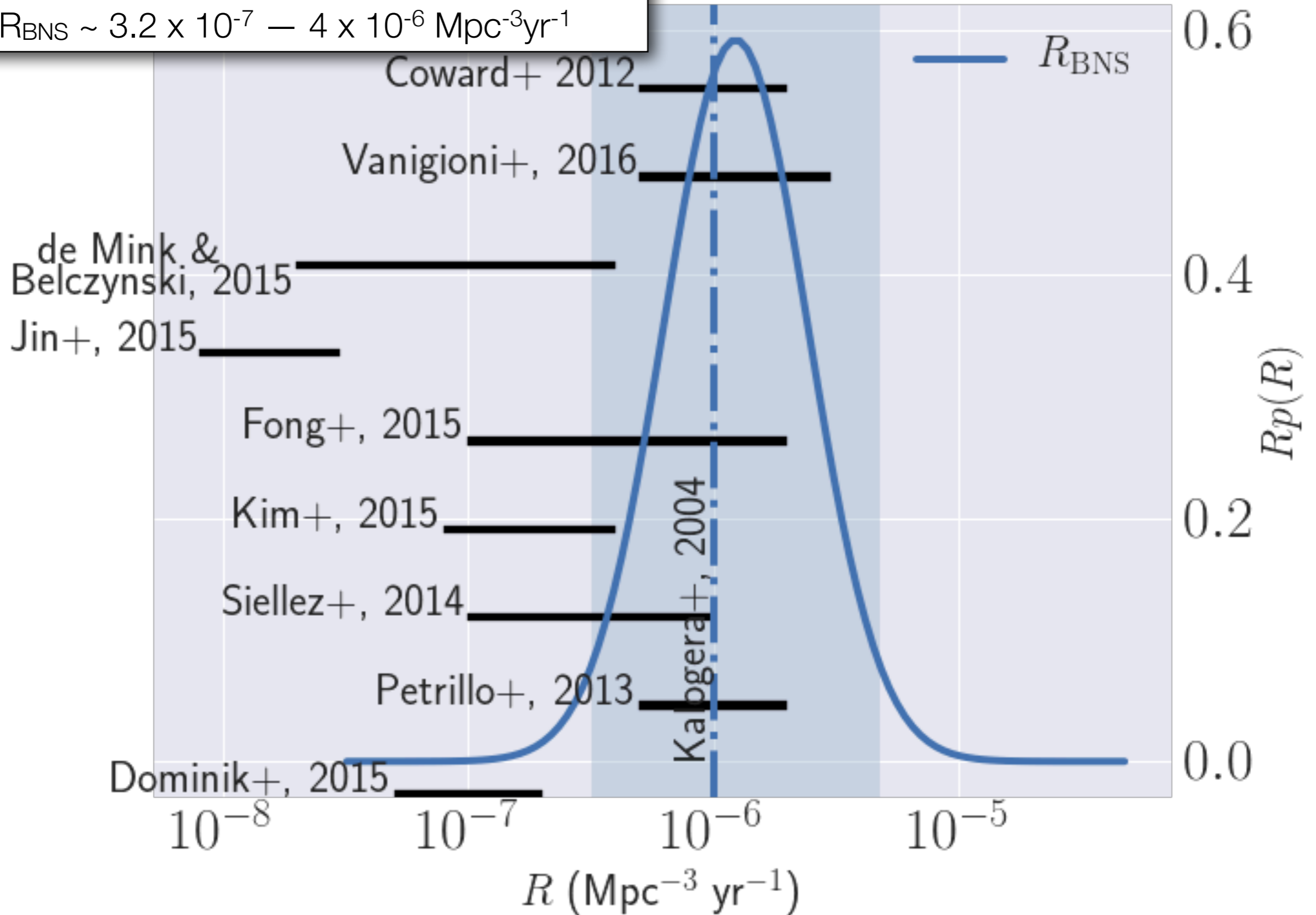
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Binary Neutron Star Rates
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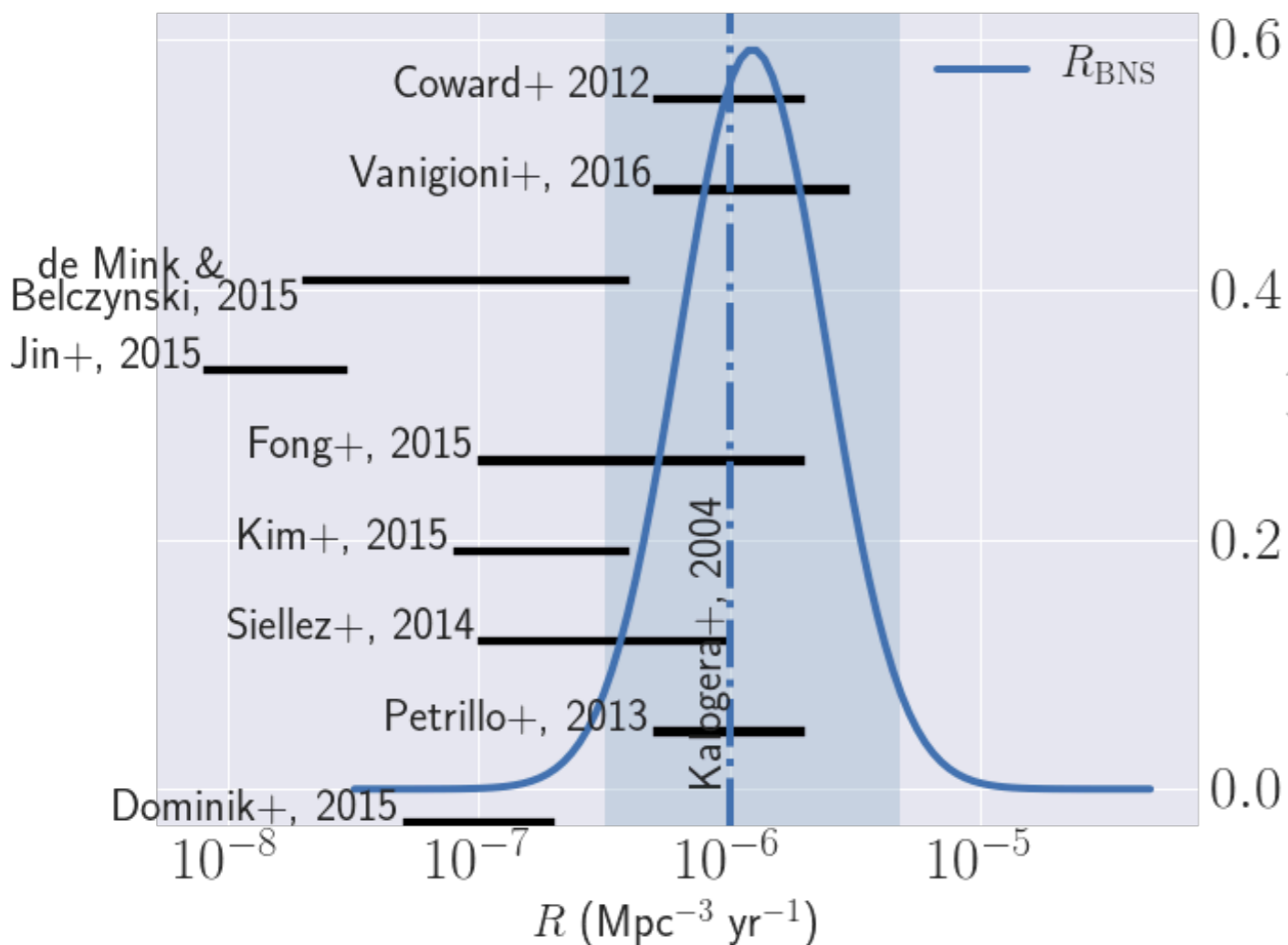
ApJ Letters, 832, 2
Phys. Rev. Lett. 119,
16110

This rate distribution...
 $R_{\text{BNS}} \sim 3.2 \times 10^{-7} - 4 \times 10^{-6} \text{ Mpc}^{-3}\text{yr}^{-1}$



Binary Neutron Star Rates (post-GW170817)

Assumptions:
 $\rho_{\text{net}} > 12$
 T_{obs} : 1 yr with 50%
 duty cycle

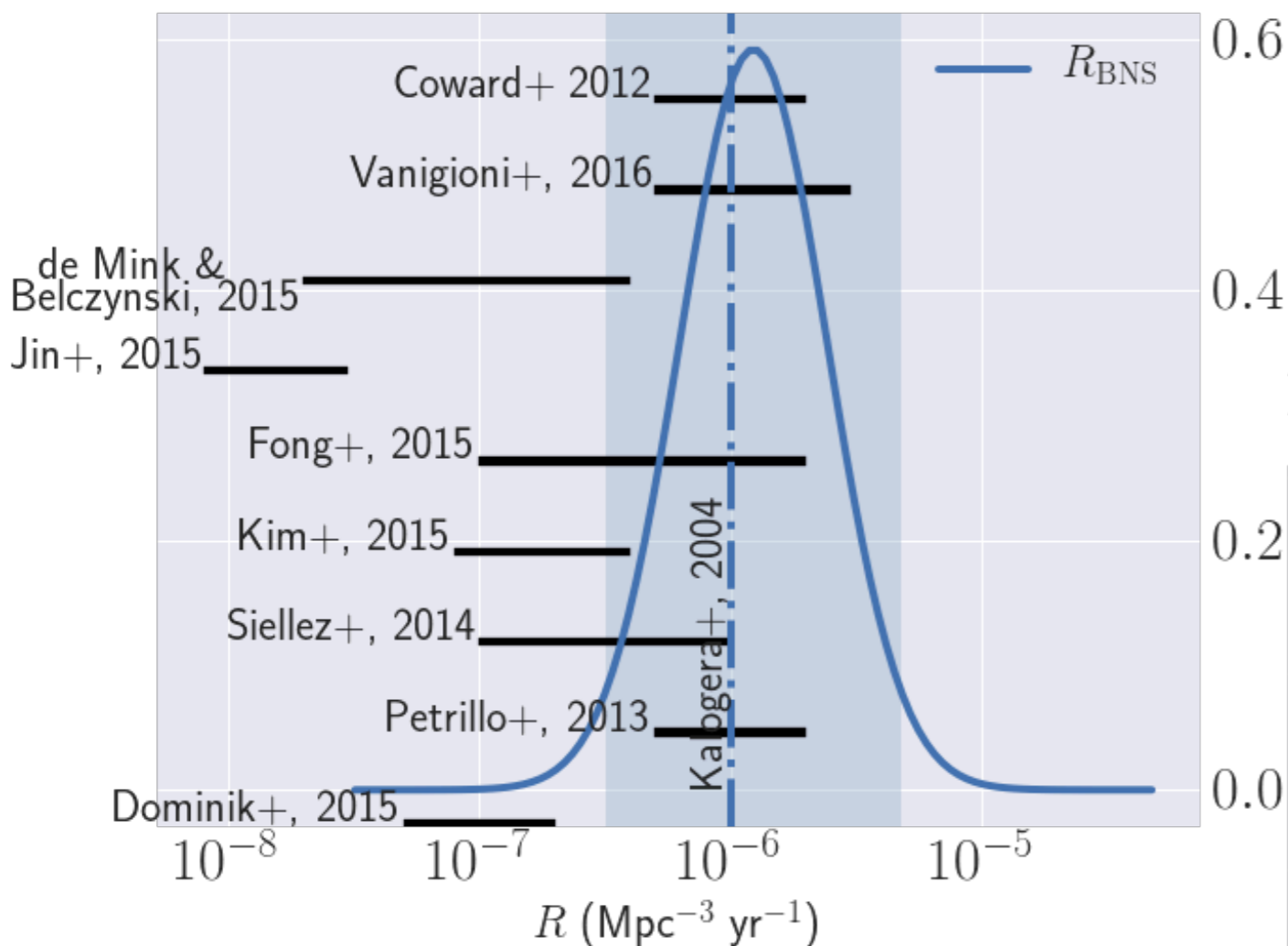


Broad (uniform): 1-3 M_{\odot}
 'Milky Way-like': $1.33 \pm 0.09 M_{\odot}$
 ...with O3 surveyed space-time volume:
 $VT_{\text{BNS}} \sim 2-4 \times 10^7 \text{ Mpc}^3 \text{yr}$

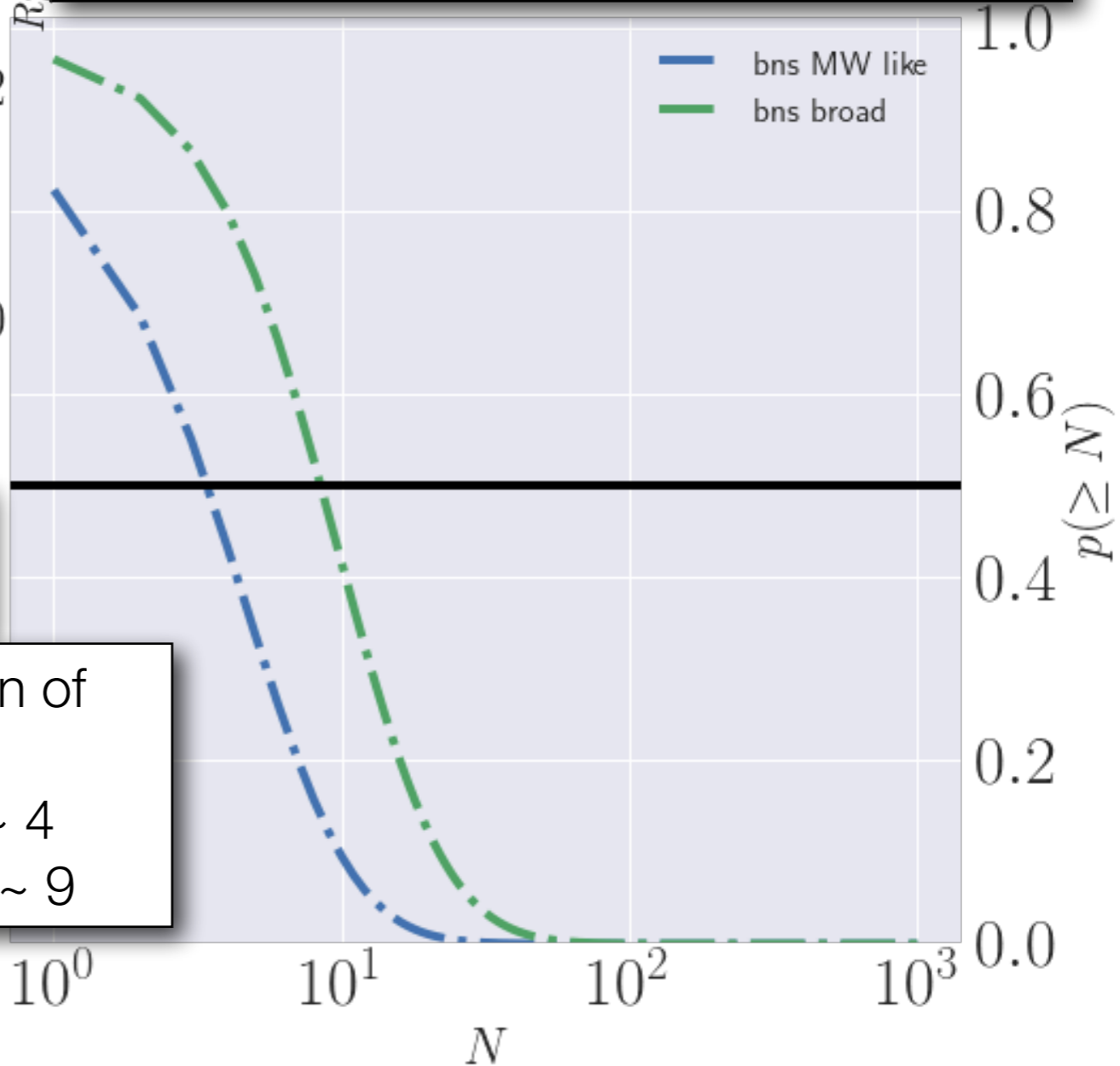
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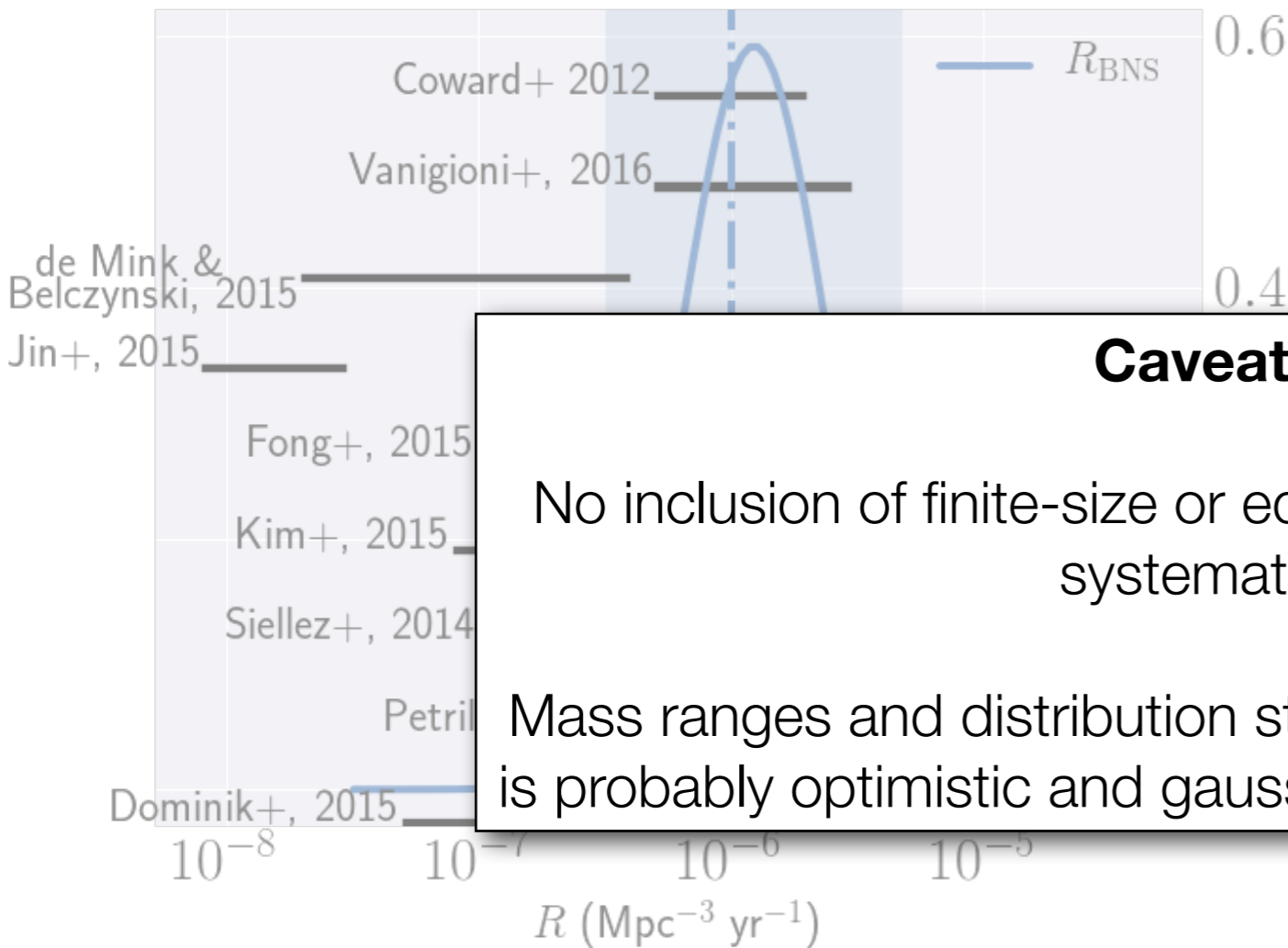


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...gives this distribution of
 detected events.
median $p(N)$ / MW ~ 4
median $p(N)$ / broad ~ 9

Binary Neutron Star Rates (post-GW170817)

Assumptions:
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 T_{obs} : 1 yr with 50%
 duty cycle

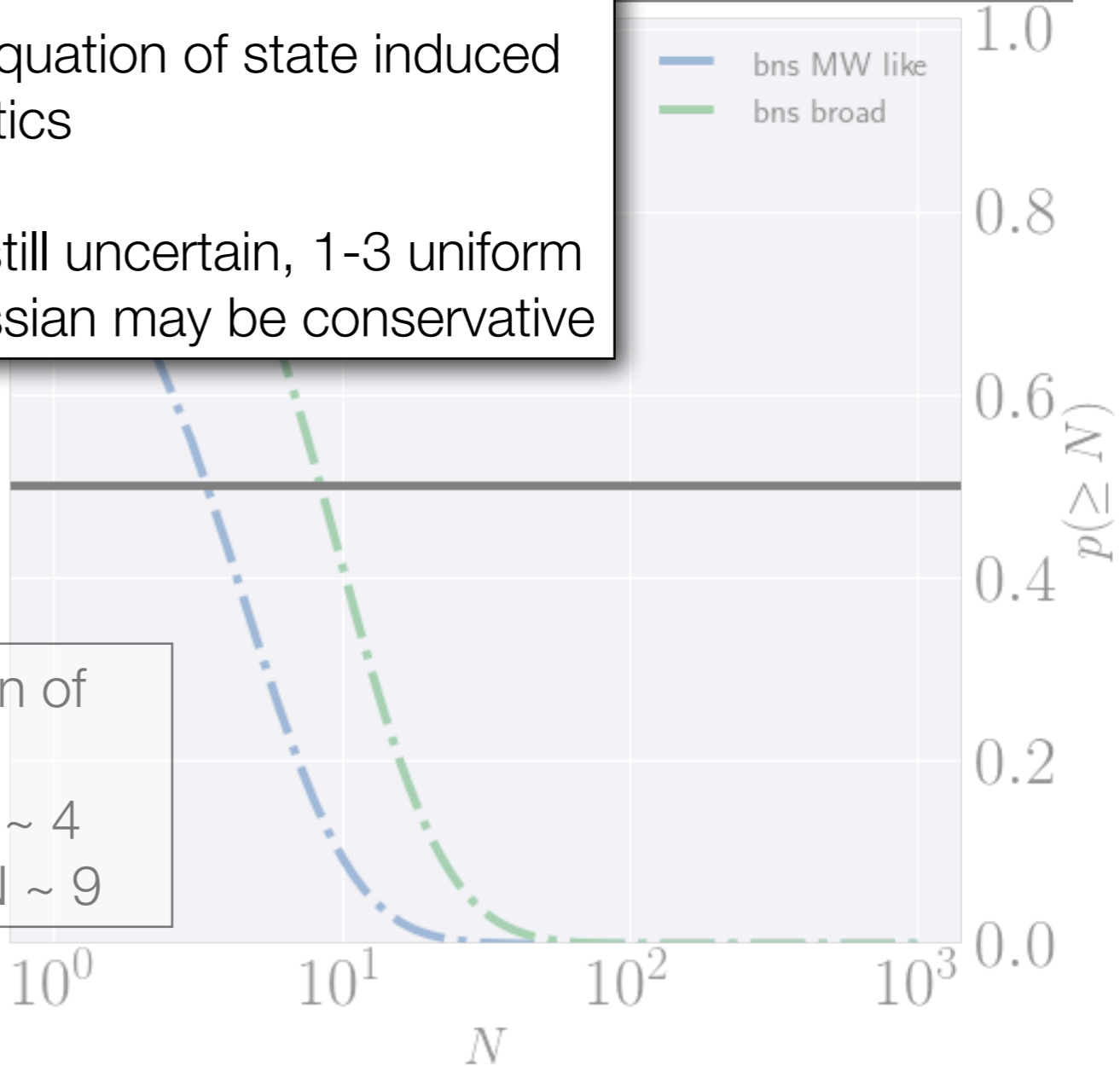


Broad (uniform): 1-3 M_{\odot}
 'Milky Way-like': $1.33 \pm 0.09 M_{\odot}$
 Space-time volume:
 $10^7 \text{ Mpc}^3 \text{ yr}$

Caveats

No inclusion of finite-size or equation of state induced systematics

Mass ranges and distribution still uncertain, 1-3 uniform is probably optimistic and gaussian may be conservative



This rate distribution...
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...gives this distribution of detected events.
median $p(N) / \text{MW } N \sim 4$
median $p(N) / \text{broad } N \sim 9$

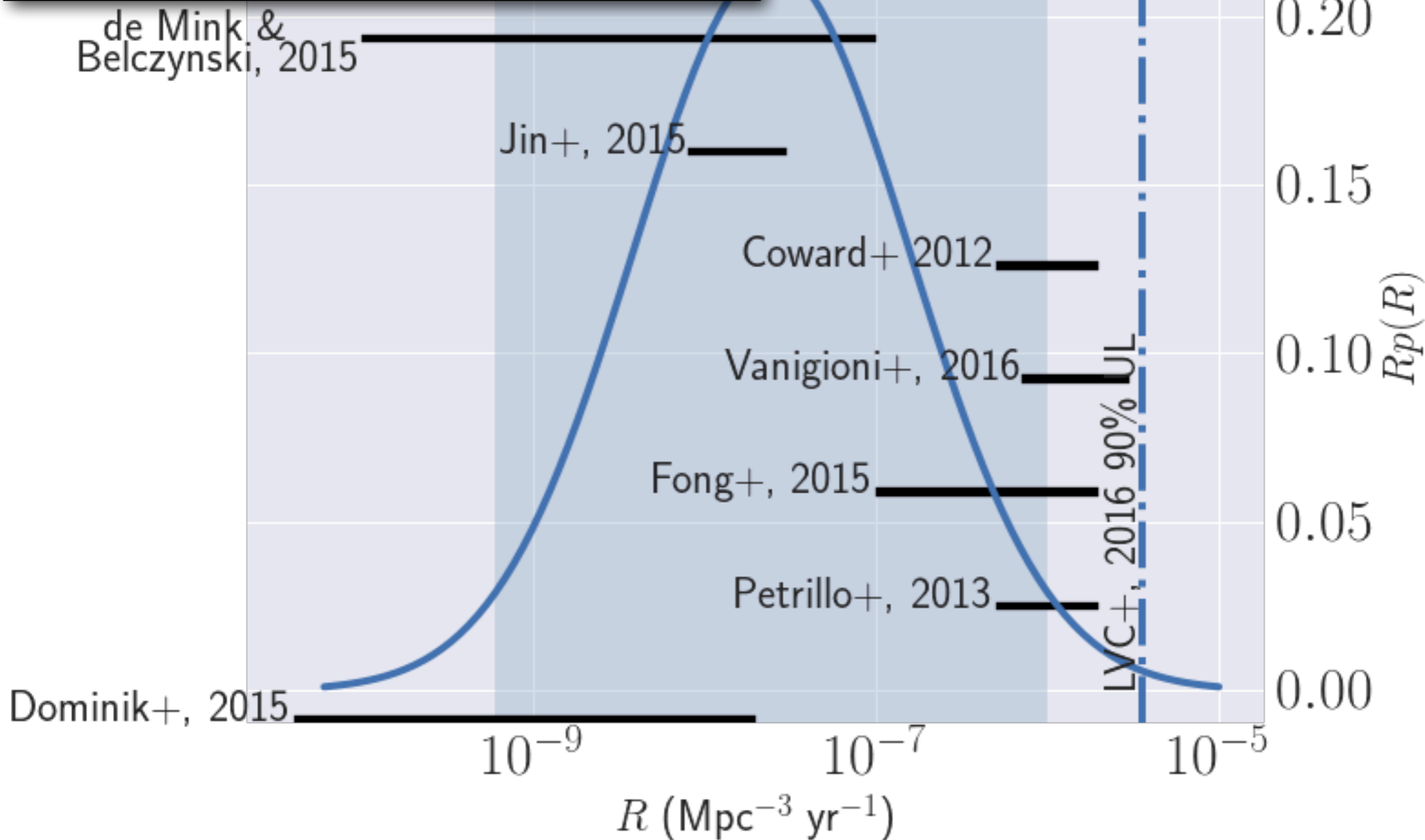
NSBH Rates (much uncertainty)

$p(R)$ limits taken from Abbott+, 2010, assumes log-normal peaked away from zero

ApJ Letters, 832, 2

This rate distribution...

$$R_{\text{NSBH}} \sim 6 \times 10^{-10} - 1 \times 10^{-6} \text{ Mpc}^{-3} \text{ yr}^{-1}$$

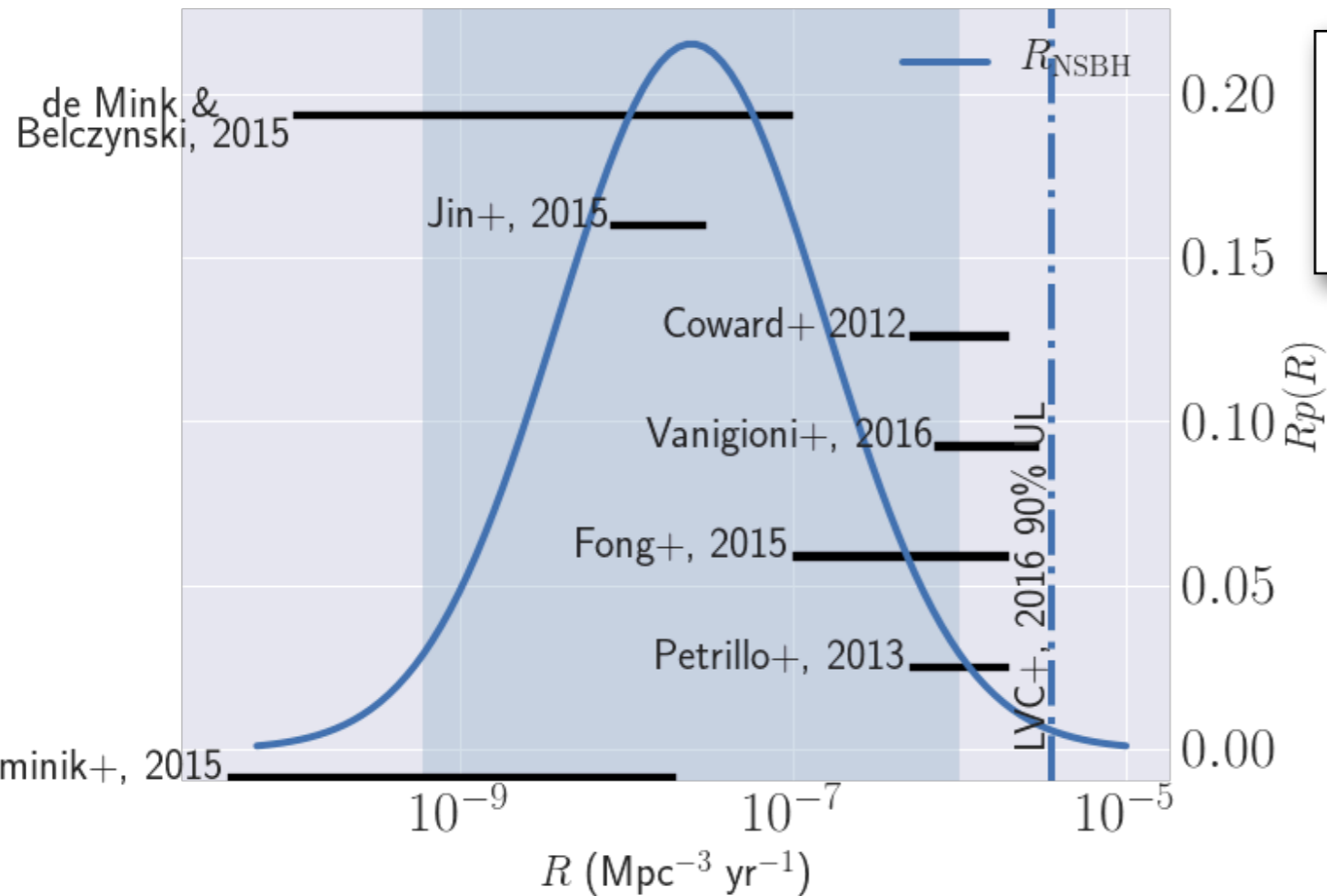


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 With O3 surveyed space-time volume
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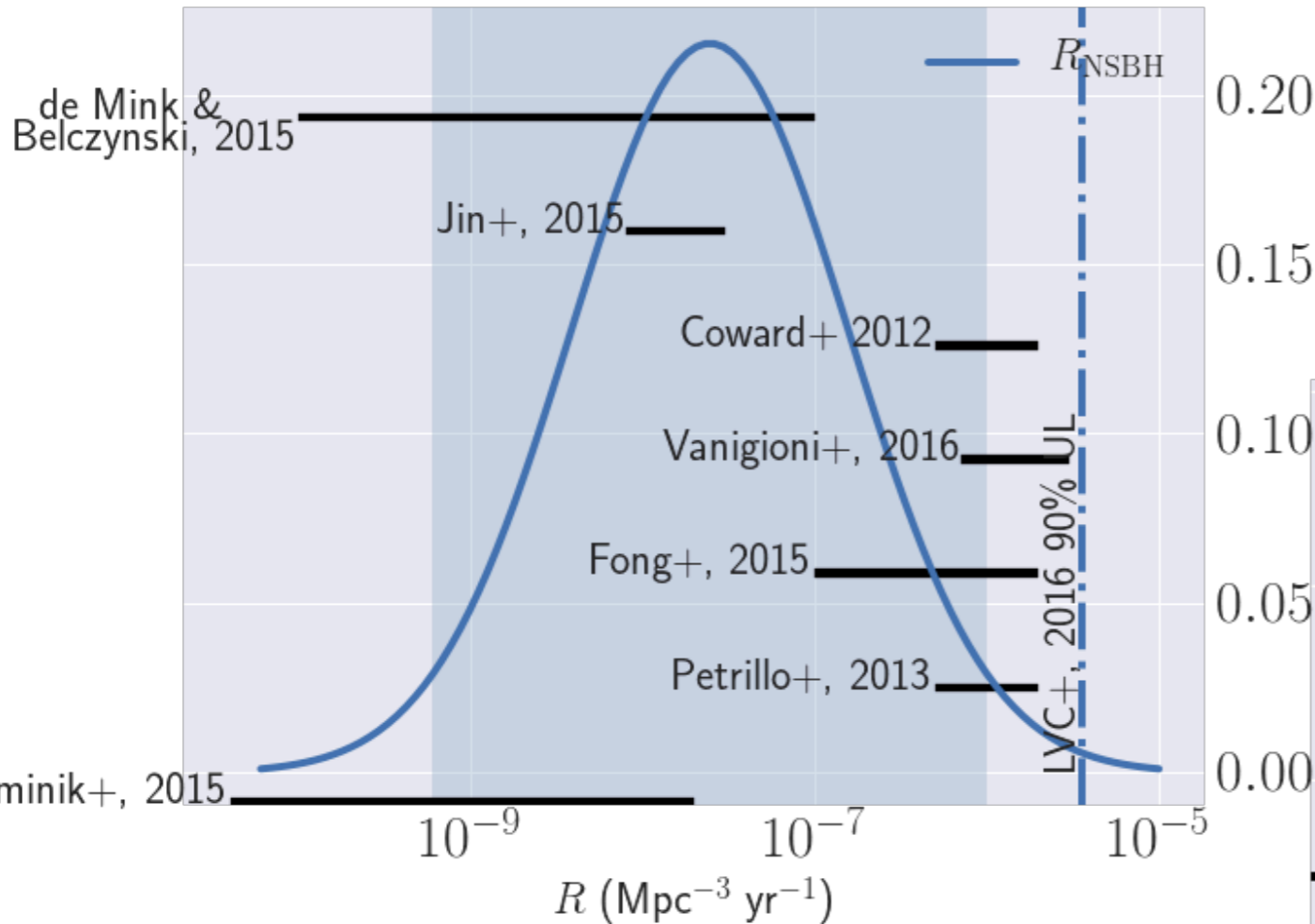
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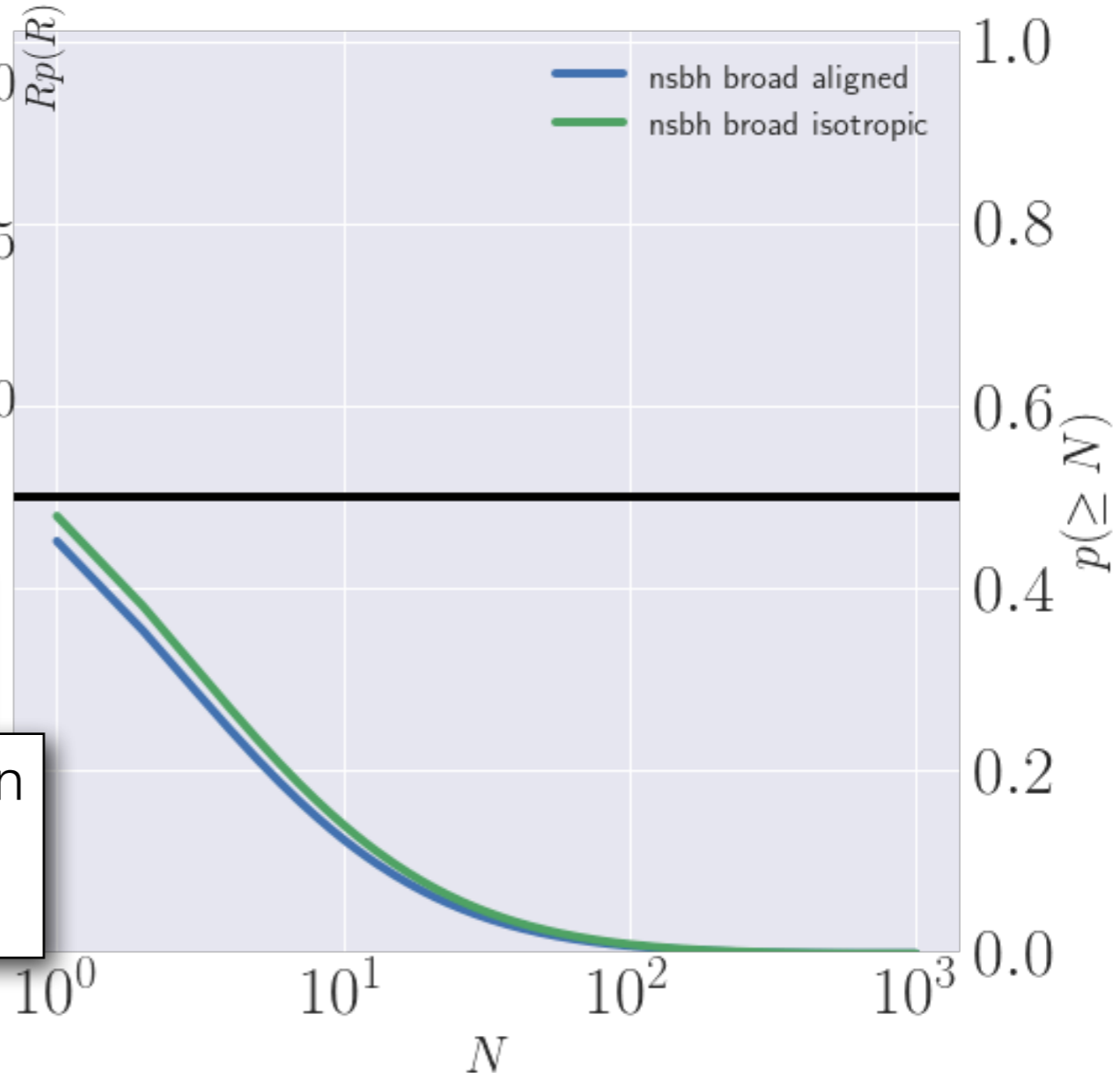
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Assumptions:

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 T_{obs} : 1 yr with 50% duty cycle

de Mink & Belczynski, 2015

Caveats

Widest potential variation in mass ratio, no reliable models for high mass ratio events

Physics encoded in waveforms (e.g. precession) which is not completely captured by online searches

Uncertain mass and spin distributions
 Uncertainty of about width (or even existence) of ccSN induced mass gap and/or upper limit on NS mass

ρ_{net}^{-1} ($5 < m_1 < 100 M_{\odot}$)
 space-time volume
 $\times 10^8 \text{ Mpc}^3 \text{ yr}$

Dominik+, 2015

R ($\text{Mpc}^{-3} \text{ yr}^{-1}$)



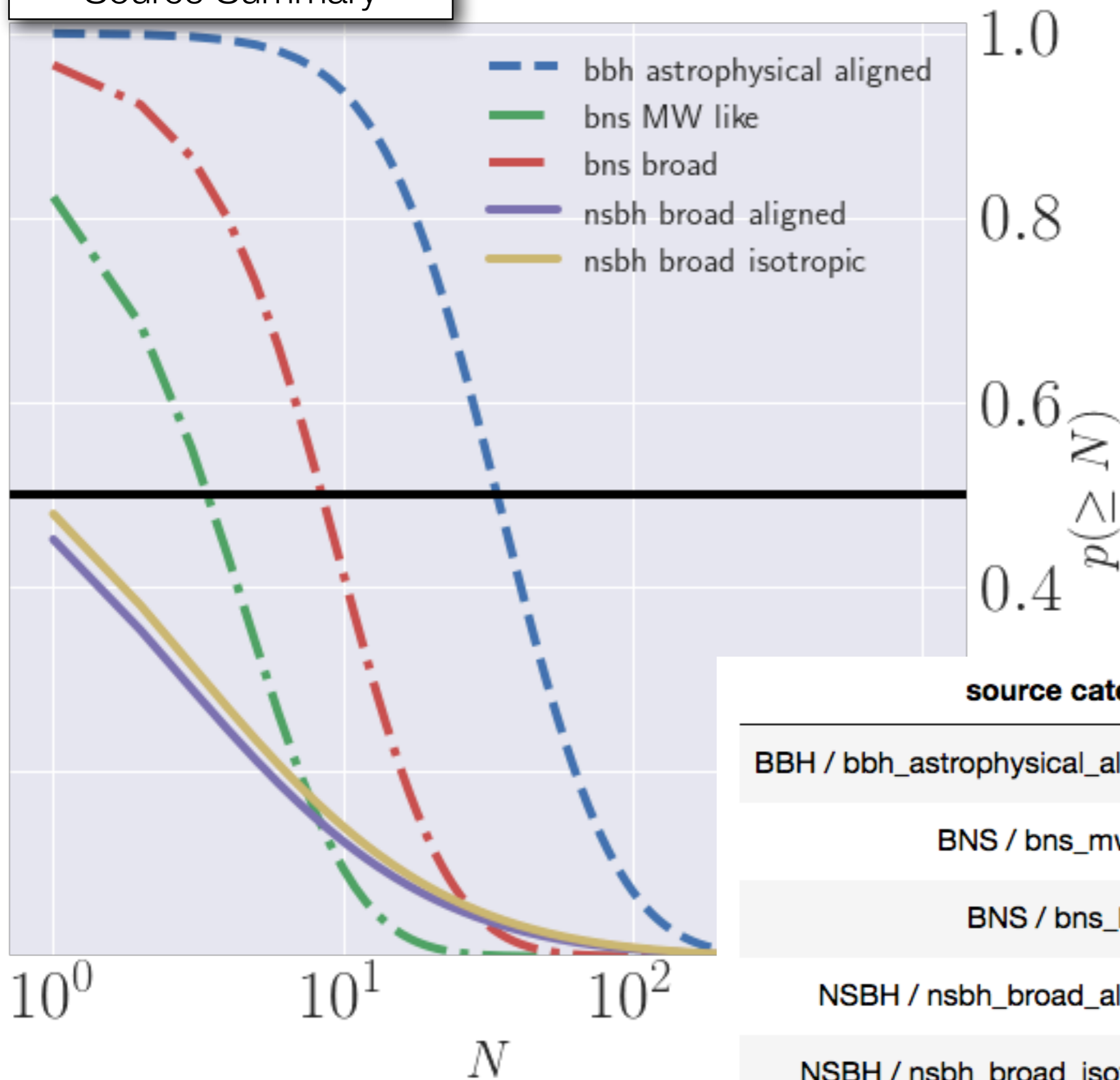
This rate distribution...

$$R_{\text{NSBH}} \sim 6 \times 10^{-10} - 1 \times 10^{-6} \text{ Mpc}^{-3} \text{ yr}^{-1}$$

...gives this distribution of detected events.

median $p(N) \sim 1$

Source Summary



source category	full year VT	N_d
BBH / bbh_astrophysical_aligned	$6.8 \times 10^8 \text{ Mpc}^3 \text{ yr}$	35_{-26}^{+78}
BNS / bns_mw_like	$3.2 \times 10^6 \text{ Mpc}^3 \text{ yr}$	4_{-4}^{+9}
BNS / bns_broad	$7.3 \times 10^6 \text{ Mpc}^3 \text{ yr}$	9_{-7}^{+19}
NSBH / nsbh_broad_aligned	$4.9 \times 10^7 \text{ Mpc}^3 \text{ yr}$	1_{-1}^{+24}
NSBH / nsbh_broad_isotropic	$5.7 \times 10^7 \text{ Mpc}^3 \text{ yr}$	1_{-1}^{+28}

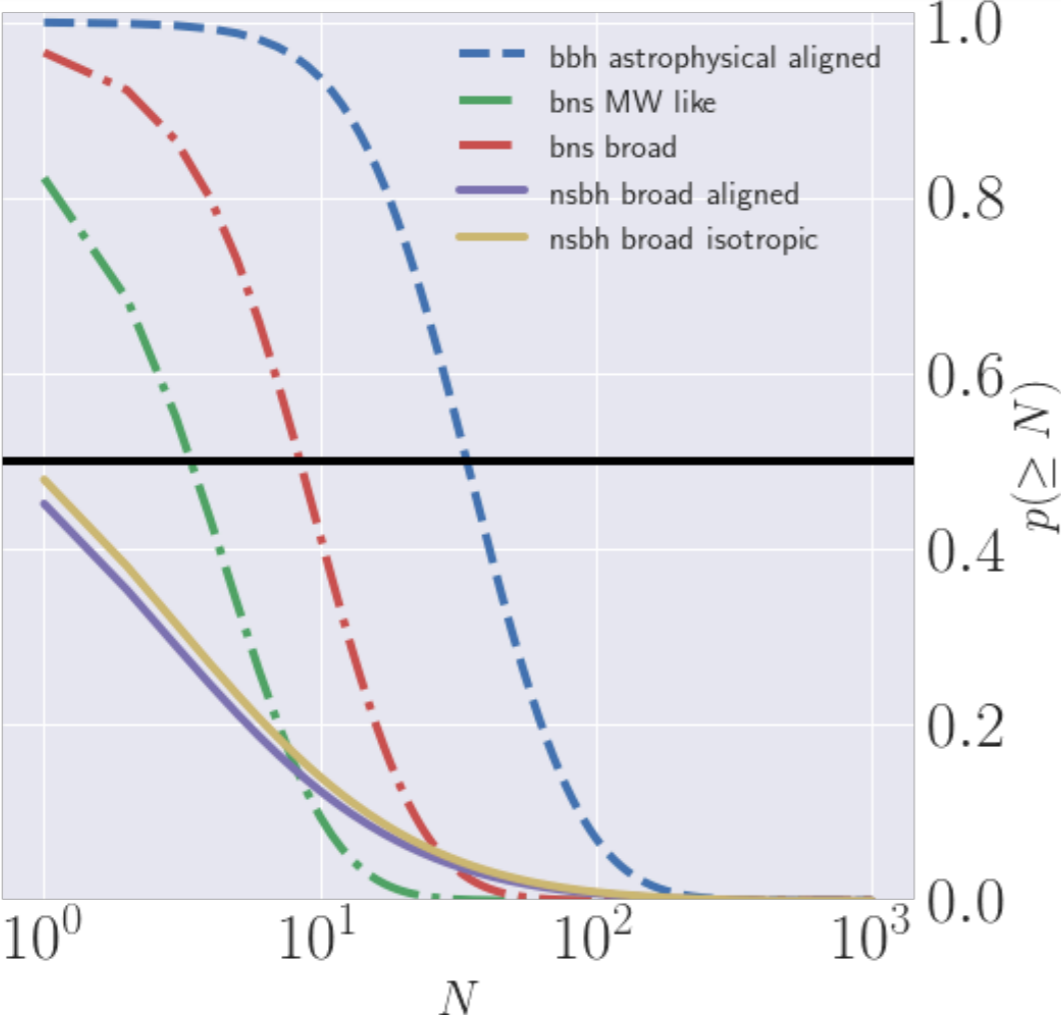
Take Aways

BBH rate will **dominate**, possibly by more than an order of magnitude, up to **~few/wk., at least ~few/mo.**

1-10 BNS, possibly up to **~1/mo.**

VT has **strong mass dependence** but **very mild dependence** on assumed spin distribution

NSBH: N=0 not ruled out in any scenario, most give **~50% N>0**



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BNS / bns_mw_like	$3.2 \times 10^6 \text{ Mpc}^3 \text{ yr}$	4^{+9}_{-4}
BNS / bns_broad	$7.3 \times 10^6 \text{ Mpc}^3 \text{ yr}$	9^{+19}_{-7}
NSBH / nsbh_broad_aligned	$4.9 \times 10^7 \text{ Mpc}^3 \text{ yr}$	1^{+24}_{-1}
NSBH / nsbh_broad_isotropic	$5.7 \times 10^7 \text{ Mpc}^3 \text{ yr}$	1^{+28}_{-1}