



**lisa pathfinder**

# LISA Pathfinder: Sub-femto-g differential accelerometry for gravitational wave observation from space

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for the LISA Pathfinder Collaboration

Amaldi Meeting  
Pasadena, 11 July 2017



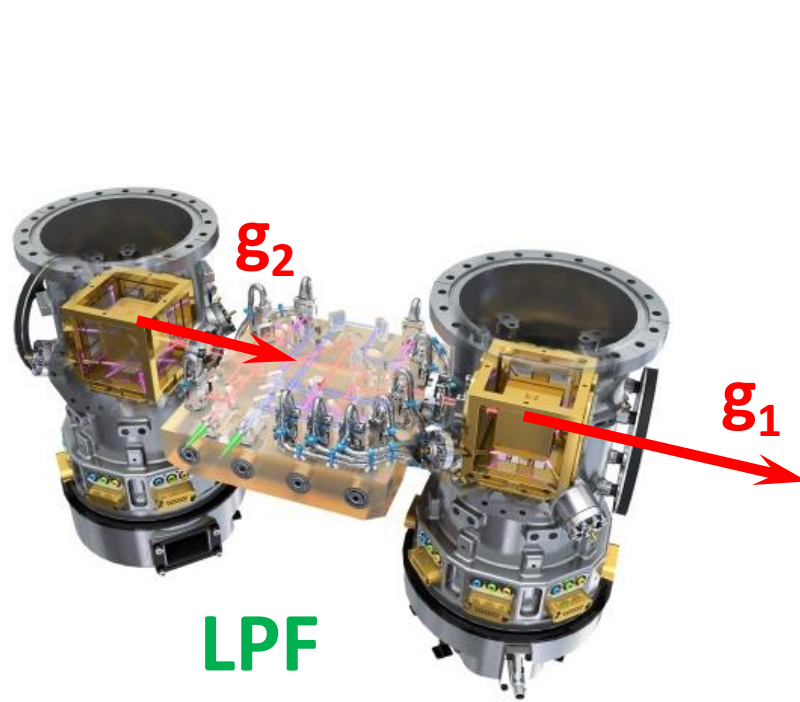
UNIVERSITÀ DEGLI STUDI  
DI TRENTO



Trento Institute for  
Fundamental Physics  
and Applications

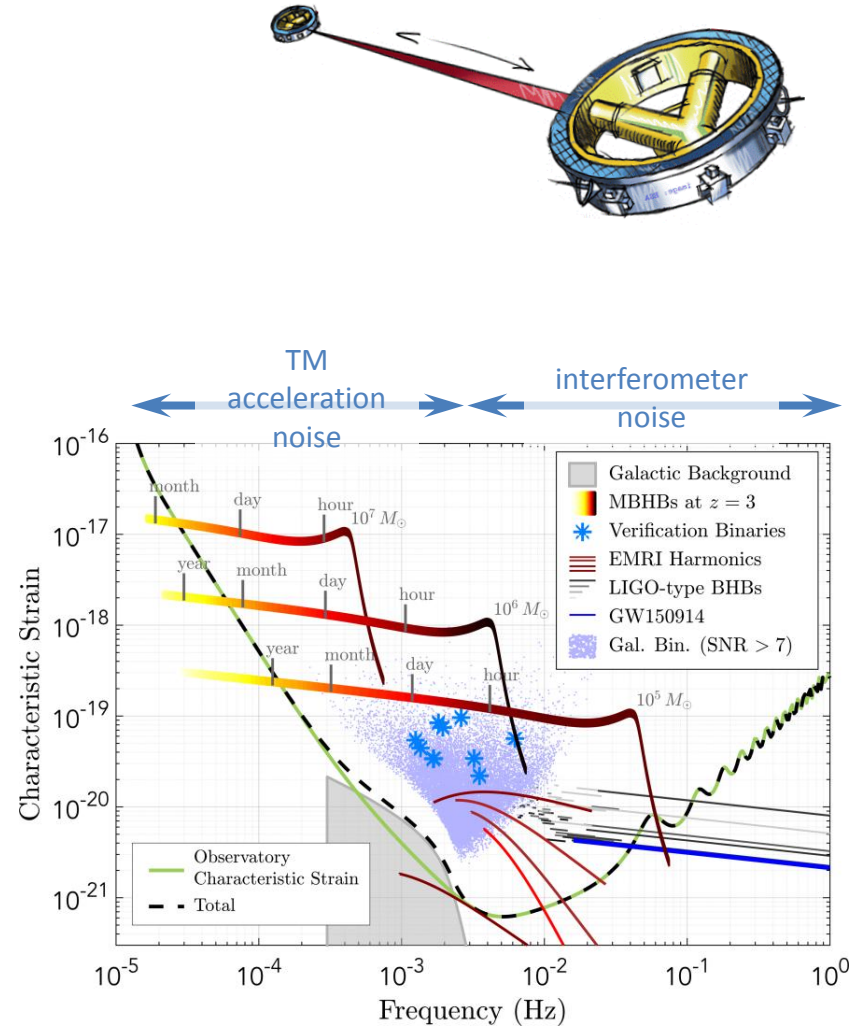
# Measuring sub-femto-g/Hz<sup>1/2</sup> differential acceleration

- LPF: gravity gradiometer 2 TM with 37.6 cm baseline in drag-free spacecraft at L1



LPF

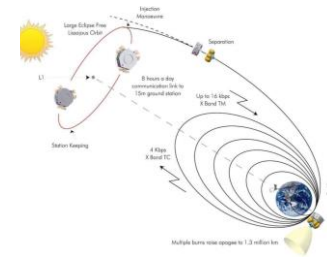
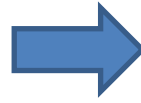
$$\Delta g \equiv g_2 - g_1$$



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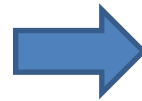
# Measuring sub-femto-g/Hz<sup>1/2</sup> differential acceleration

- LPF: gravity gradiometer 2 TM with 37.6 cm baseline in drag-free spacecraft at L1
- Similar to 1 component of GOCE geodesy mission



**Actuation force noise**  
 «accelerometer range»

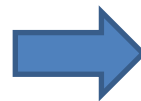
LEO  
 $\mu\text{m/s}^2$  (Terrestrial)  
 residual atmosphere



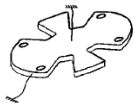
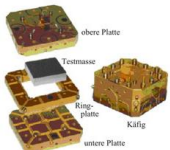
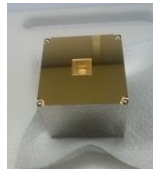
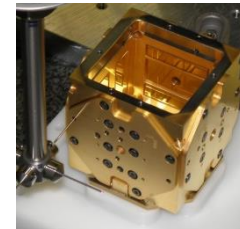
L1  
 $\text{nm/s}^2$  (spacecraft g) → **0 for eLISA !!**  
 deep space

**GRS surface force noise**

300 gm TM  
 100  $\mu\text{m}$  gaps  
 discharge wire

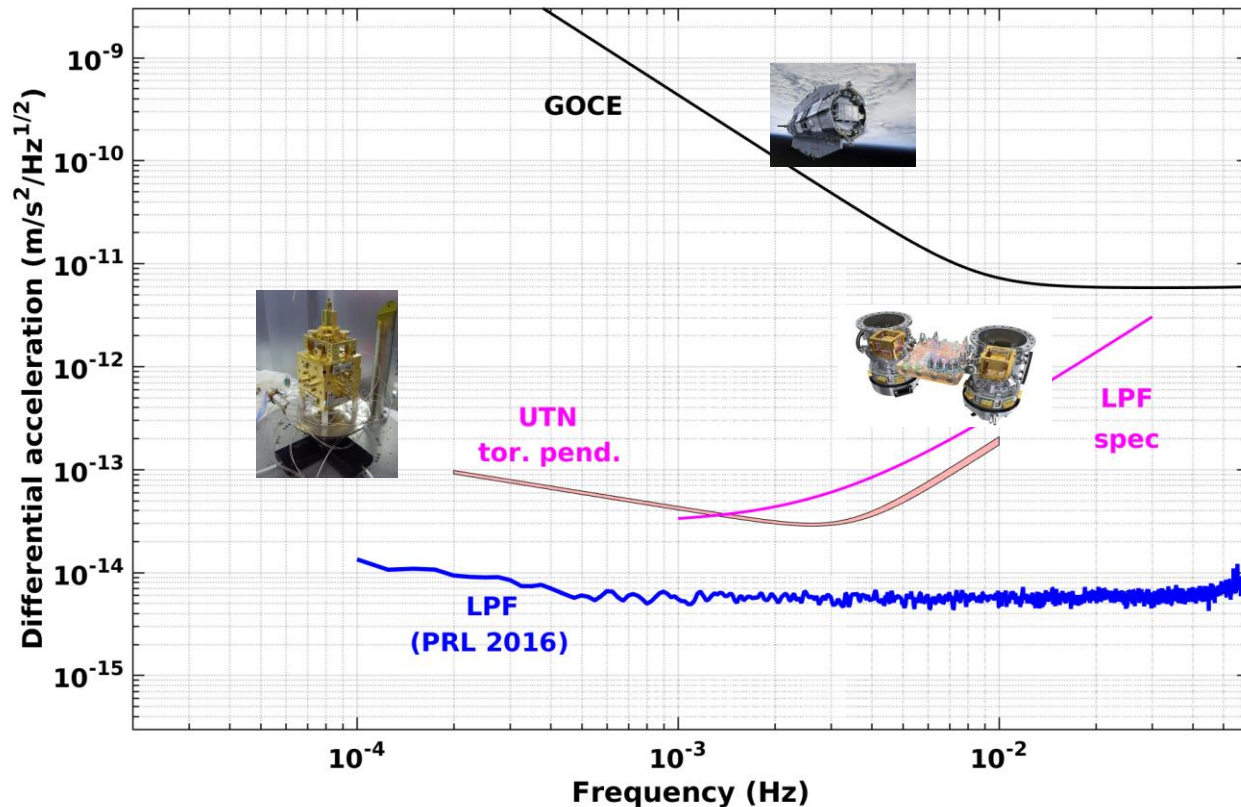


2 kg TM  
 3-4 mm gaps  
 no contacts



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# Free-falling test masses as sub-femto-g geodesic references: pre-LPF knowledge



Pre-flight torsion pendulum tests retired some GRS force risks

- Not representative of all forces (or full free-fall + control)
- Not quite to LPF specs (far from true space performance)

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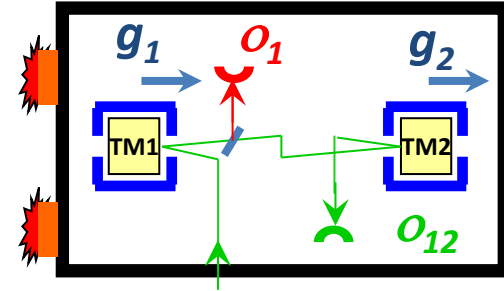
# LISA Pathfinder as a differential accelerometer

$$\Delta g \equiv g_2 - g_1$$

«gravitational observable»  
differential force per unit mass

## Control:

- Thrust SC to follow TM1
- Electrostatically force TM2 to follow TM1



## Newton's Laws:

$$\ddot{x}_1 = g_1 - \omega_{1p}^2 (x_1 - x_{SC})$$

$$\ddot{x}_2 = g_2 - \omega_{2p}^2 (x_2 - x_{SC}) + \frac{F_{ES}}{m}$$

$$\Delta g = \ddot{o}_{12} - \frac{F_{ES}}{m} + (\omega_{2p}^2 - \omega_{1p}^2) o_1 + \omega_{2p}^2 o_{12}$$

$$\Delta \hat{g}$$

Differential acceleration  
time series

## IFO Readouts :

$$o_{12} = x_2 - x_1 + n_{12}$$

$$o_1 = x_1 - x_{SC} + n_1$$

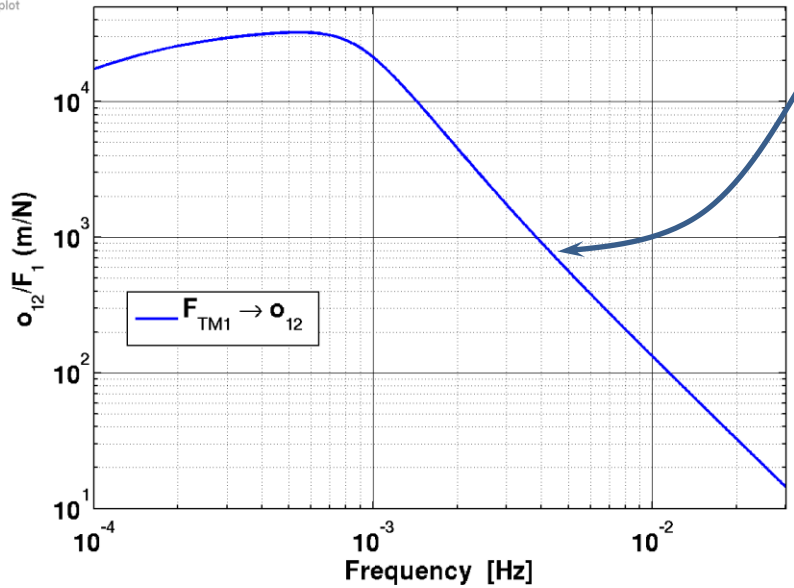
$$- \ddot{n}_{12} - (\omega_{2p}^2 - \omega_{1p}^2) n_1 - \omega_{2p}^2 n_{12}$$

$$- \Delta g_{IFO}$$

IFO Noise

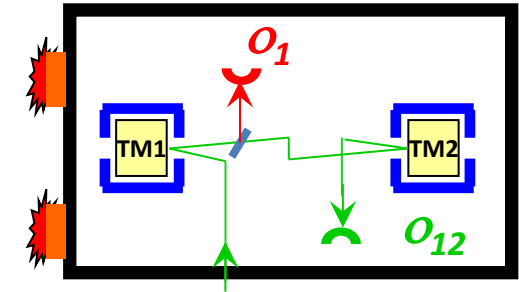
# LISA Pathfinder control, displacement and acceleration

LTPDA 2.7.1 (R2013b)  
2014-05-15 15:20:36.994 UTC  
ltpda: 8ab8cbb  
iplot



Free particle

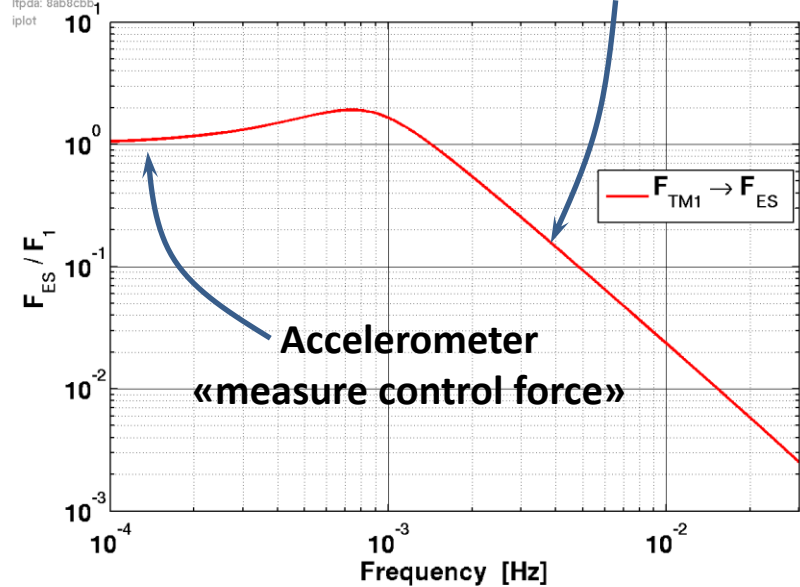
$$\Delta x \approx \frac{\Delta F}{m\omega^2}$$



Free particle

«measure acceleration»

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ltpda: 8ab8cbb  
iplot

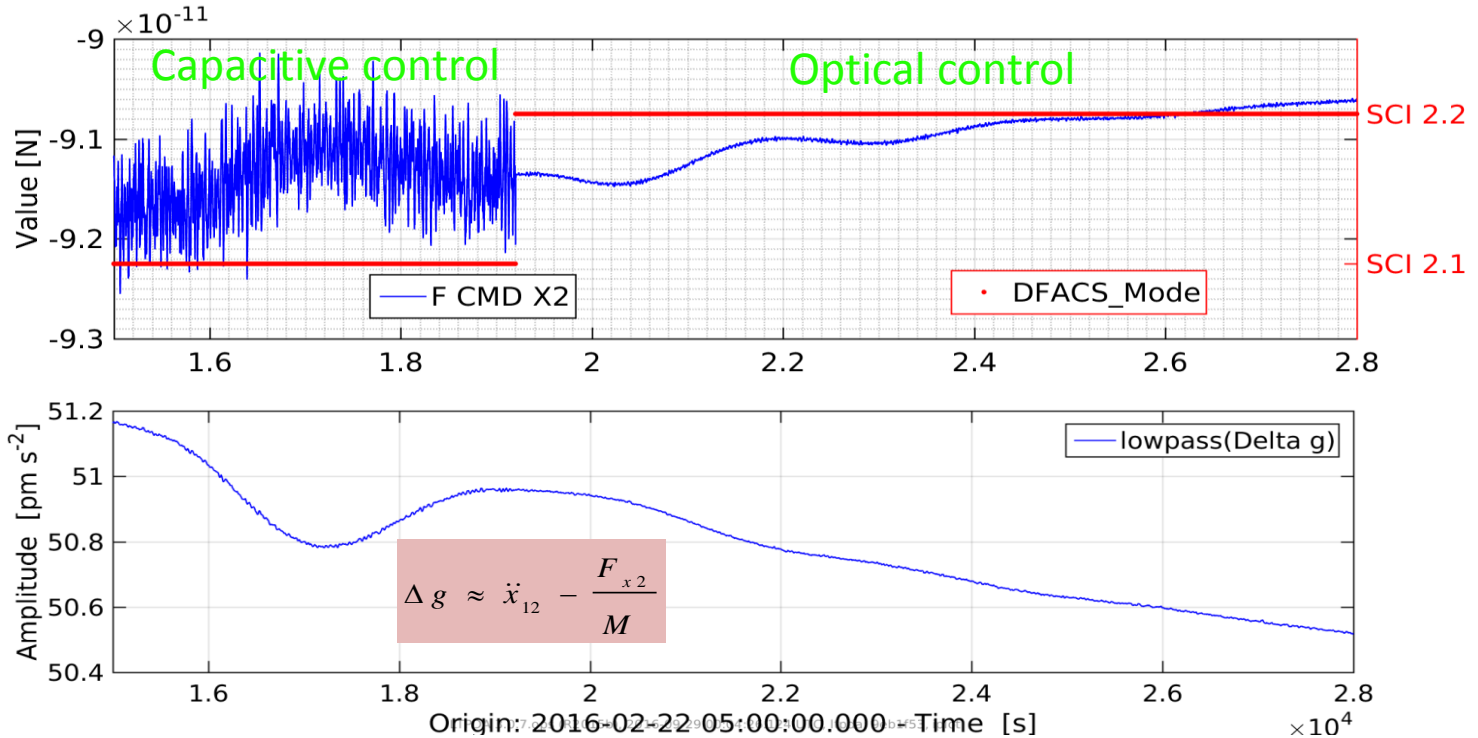


$$\Delta \hat{g} = \ddot{o}_{12} - \lambda \frac{F_{ES}}{m} + (\omega_{2p}^2 - \omega_{1p}^2) o_1 + \omega_{2p}^2 o_{12}$$

Need to calibrate actuator and SC coupling (stiffness)



# Quieting down ... Applied TM2 force across mode changes

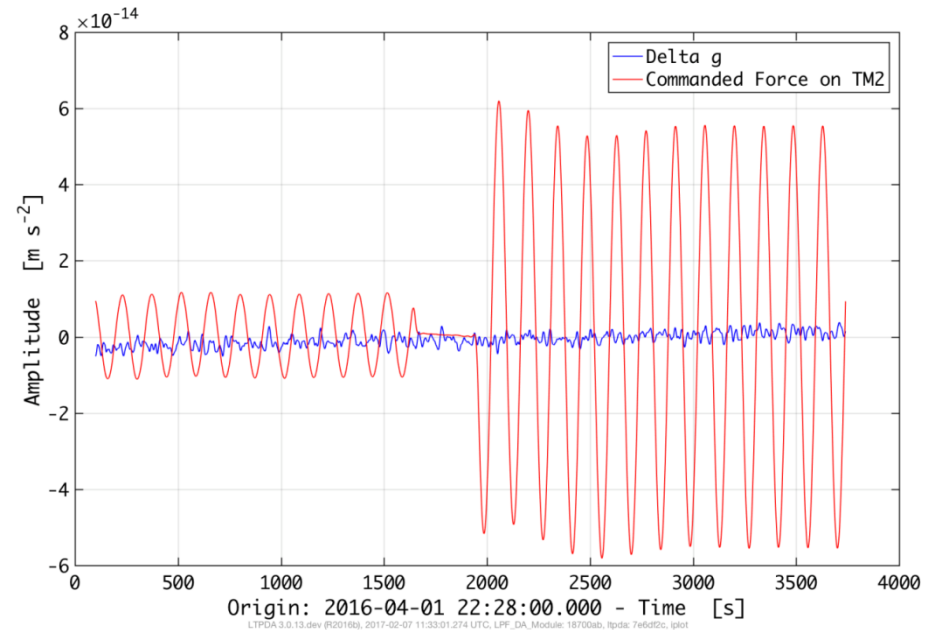


## Good news! $\Delta g < 50 \text{ pm/s}^2$ (and decreasing)

- Well below specs ( $650 \text{ pm/s}^2$ )  $\rightarrow$  less actuation  $\rightarrow$  less noise!
- Start to see our science signal ... Sub-mHz fluctuations in  $\Delta g$
- Drift ... initially  $5 \text{ pm/s}^2/\text{day}$  (residual gas TM)
- 1 year later order  $0.3 \text{ pm/s}^2/\text{day}$  (gravity from cold gas)

# $\Delta g$ calibration tone: extra known forces disappear

$$\Delta \hat{g} = \ddot{o}_{12} - \frac{F_{ES}}{m} + (\omega_{2p}^2 - \omega_{1p}^2) o_1 + \omega_{2p}^2 o_{12}$$

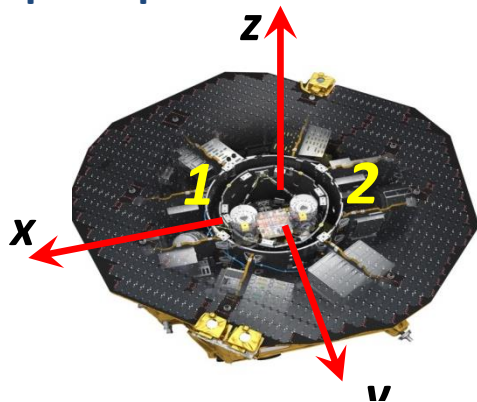


- Injection of a 20 fN or 100 fN «out-of-loop» force accurately removed in  $\Delta g$  calculation  $\rightarrow$  down to femto-Newton level
- Acceleration observable  $\rightarrow$  analysis immune to initial conditions
  - Control transients irrelevant



# Centrifugal force correction $\Delta g$

- SC rotates to point at earth/sun
- TM forced to rotate with SC
- SC low freq attitude noise from noisy star trackers
- **1st principles subtraction**

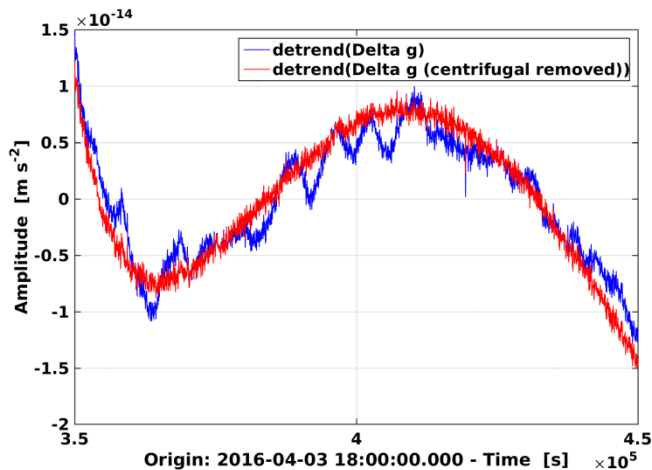


$$\Delta \hat{g}_{CENT} = -L \left( \dot{\phi}_{SC}^2 + \dot{\eta}_{SC}^2 \right)$$

$$\left( \dot{\phi}_{"DC"} + \dot{\phi}(t) \right)^2$$

Quasi-DC from star tracker angular rates

In-band (0.1-1 mHz) using 2 TM as gyroscope (applied torques)

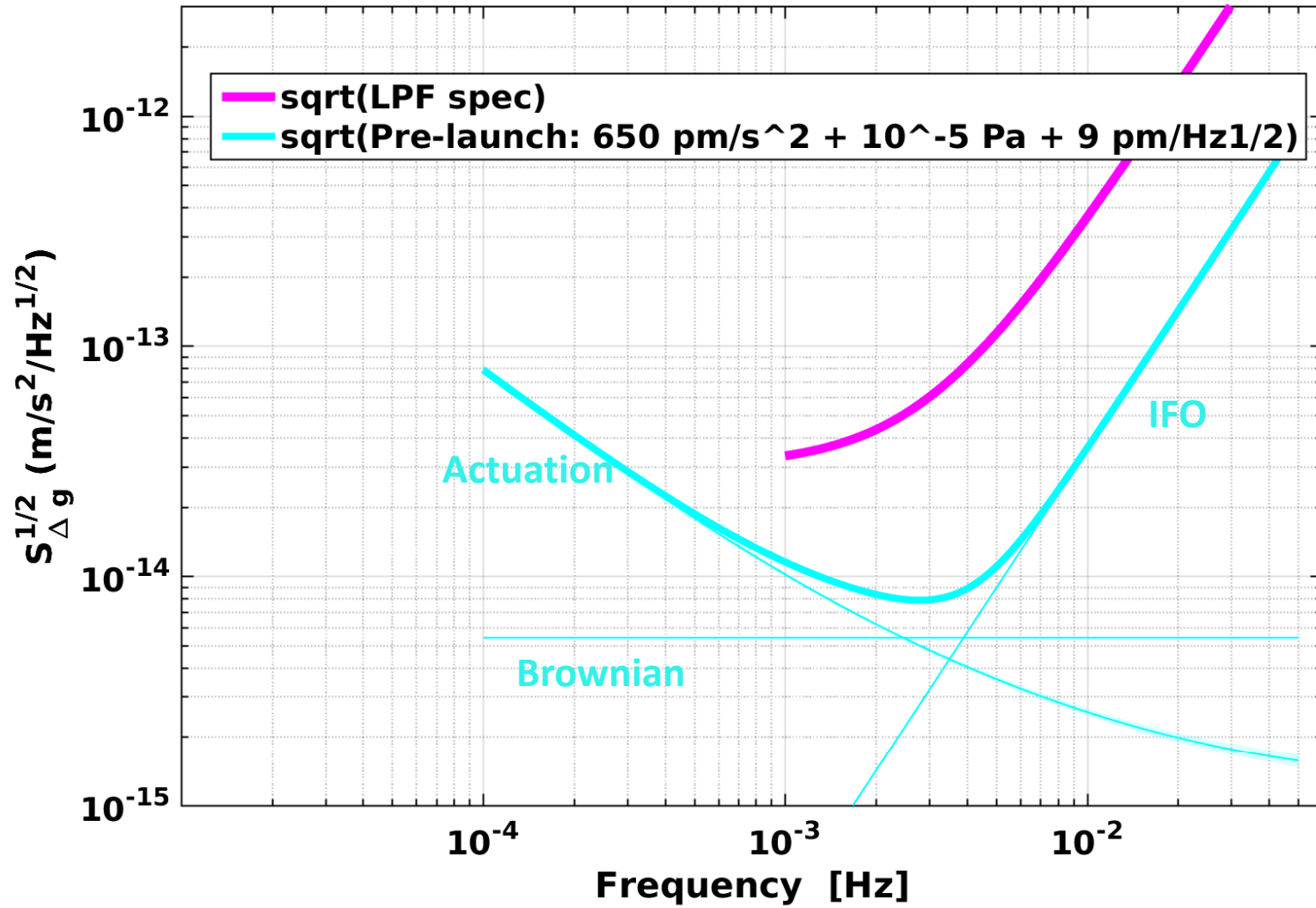


- Additional inertial correction due to angular acceleration (and TM lateral offset)

LTPDA 3.0-4.ops (R2015b), 2016-04-12 23:38:57.024 UTC, LPI\_DA\_Module: a13c385, Rtpda: 62e54e2, iplot

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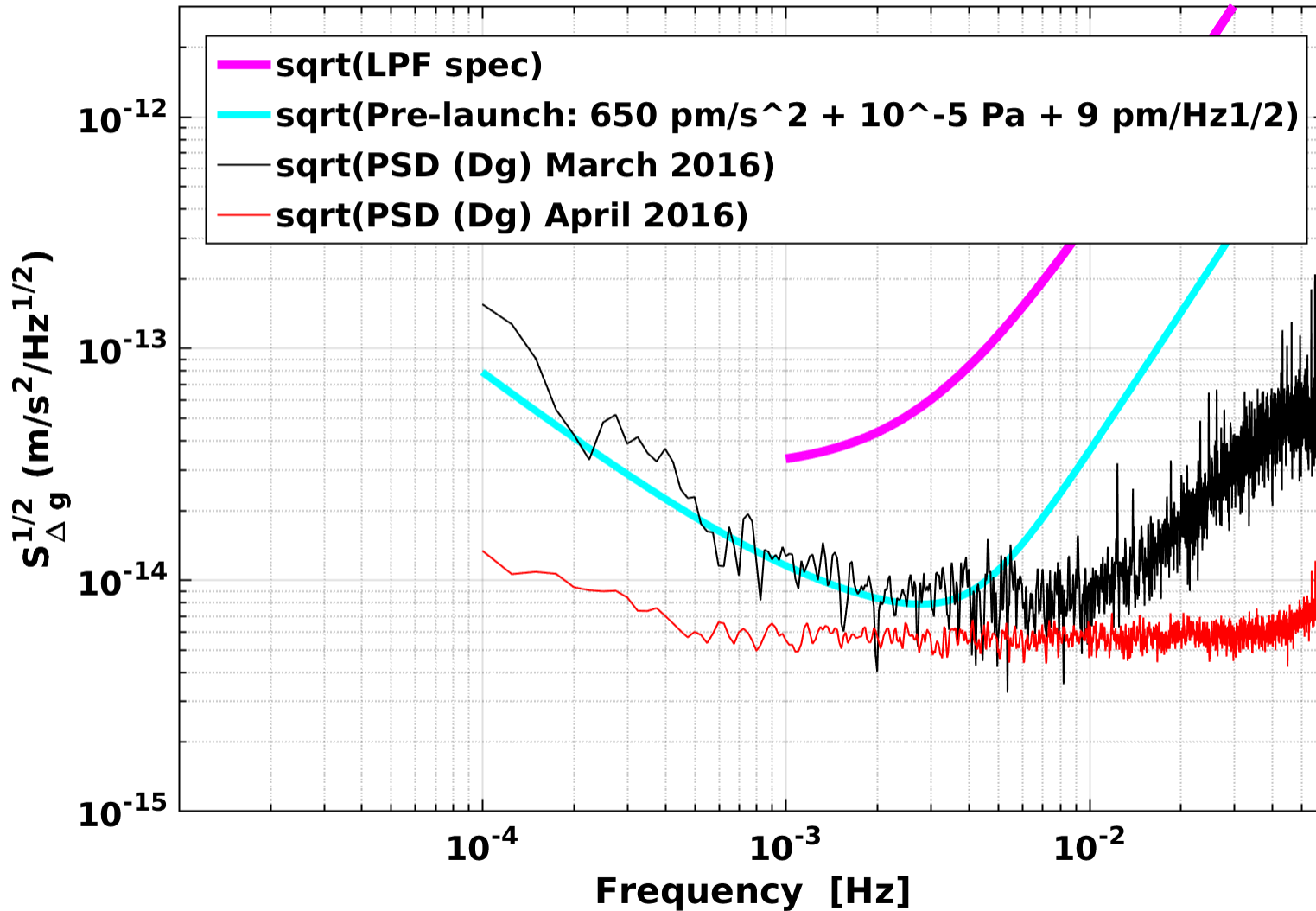
# LISA Pathfinder differential acceleration noise



LTPDA 3.0.12.ops (R2015b), 2017-07-11 00:12:22.192 UTC, ltpda: 88427c3, iplotPSD

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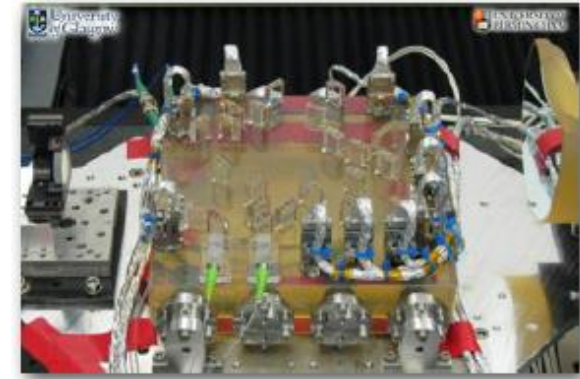
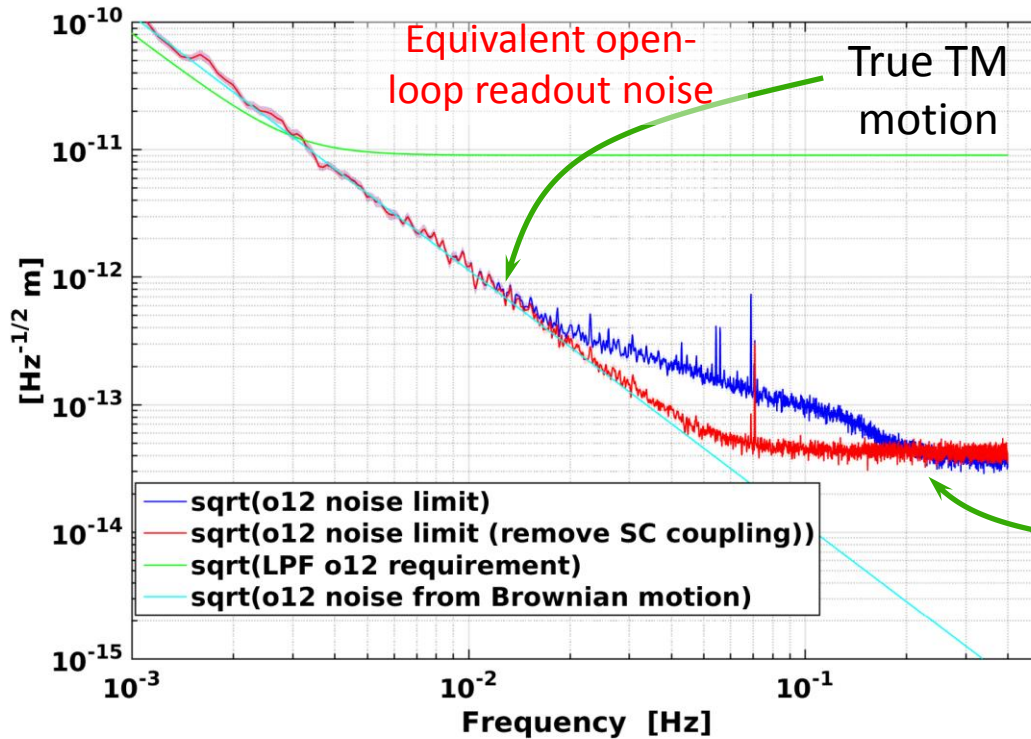
# LISA Pathfinder differential acceleration noise



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# LISA Pathfinder instrument performance: interferometer



optical  
noise  
floor

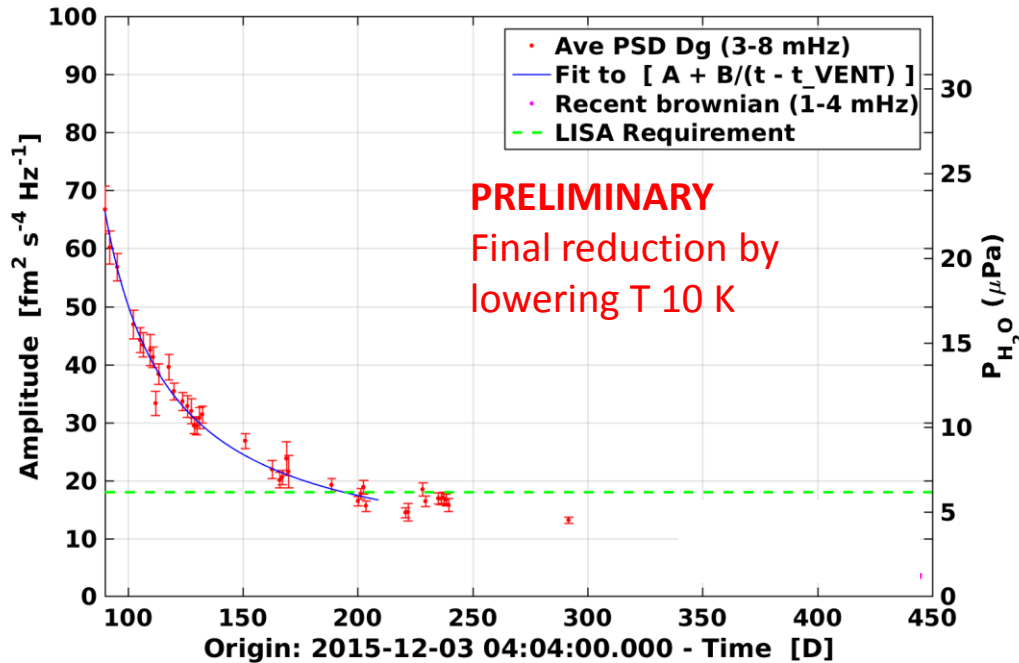
LTPDA 3.0.7.ops (R2015b), 2016-08-28 14:03:57.367 UTC, LPF\_DA\_Module: 533a2eb, ltpda: 9eb1f53, iplotPSD

## 35 fm/Hz<sup>1/2</sup> noise floor

- Dominated by (mostly understood) phase meter noise
- Visible coupling to SC motion → removal by alignment / software
- Allows measurement of true TM motion (brownian) below 50 mHz
- **Demonstration of an (overachieving) local IFO in space**

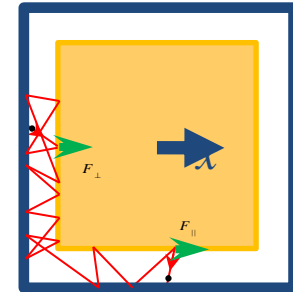
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# Brownian motion from residual gas impacts



LTPDA 3.0.12.ops (R2015b), 2017-03-08 00:12:46.567 UTC, ltpda: 88427c3, iplot

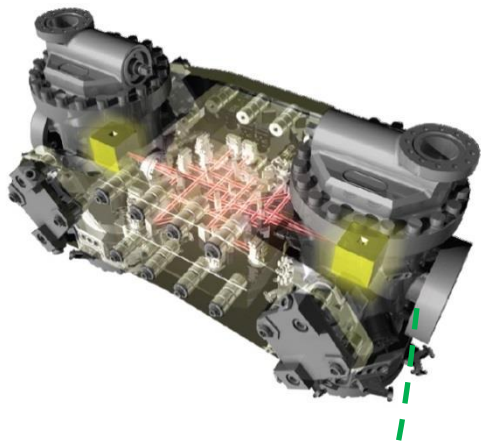
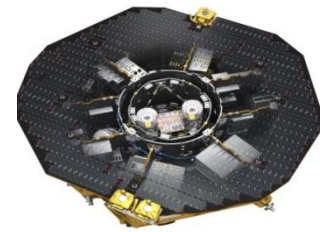
Brownian motion from gas impacts limit in 1 – 10 mHz band



Increased inside (tight) GRS due to correlated collisions

- Rough  $t^{-1}$  dependence of white noise level over time –
  - young vacuum system: launch Dec 2015, vented to space Feb 2016
  - outgassing diminishing over time
- Dependence on temperature (T)
  - roughly factor 2 (power) with 10 K
  - $\exp -\Theta/T$  dependence of adsorption

# LPF Noise: actuation gain fluctuations



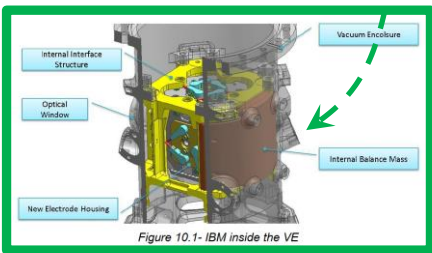
## «accelerometer dynamic range» problem

Noise in “DC” force applied to compensate local  $\Delta g$

→ in LISA (no x-axis applied force)

$$F \propto V_{ACT}^2 \quad \rightarrow \quad S_F^{1/2} \approx 2 F S_{\delta V/V}^{1/2}$$

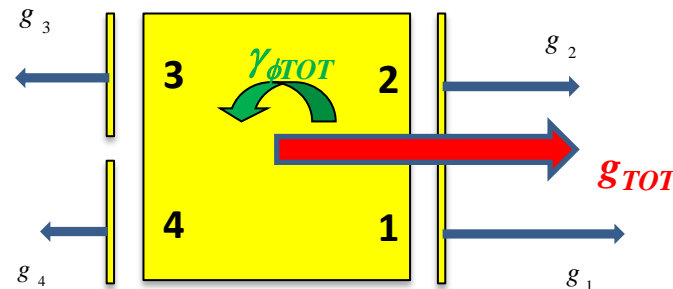
- Force noise scales with applied forces, summed over all electrodes
- Same electrodes apply  $\phi$  torque and x forces



- Voltage stability 3-8 ppm/Hz<sup>1/2</sup> at 1 mHz

## Gravitational balance:

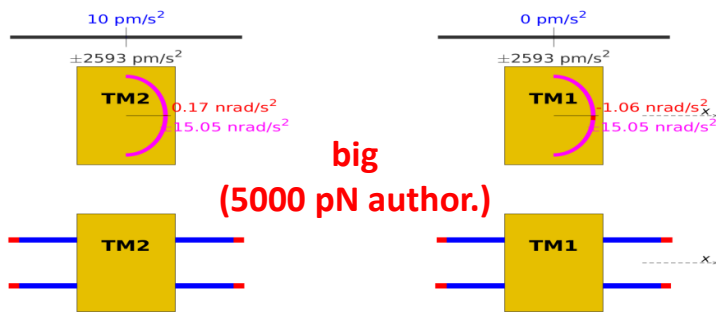
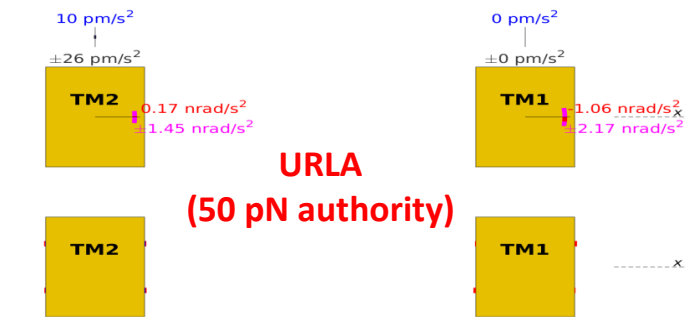
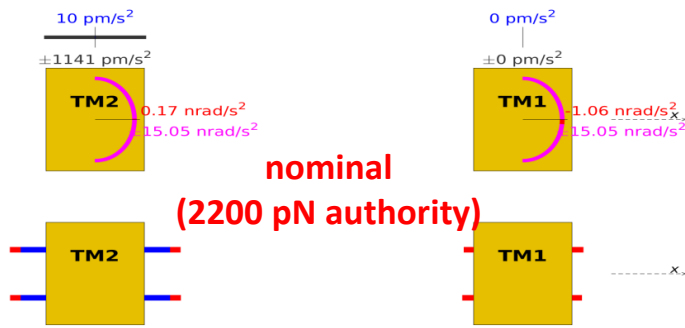
- LPF designed for  $\Delta g$  650 pm/s<sup>2</sup>
- LPF in-flight  $\Delta g < 50$  pm/s<sup>2</sup>



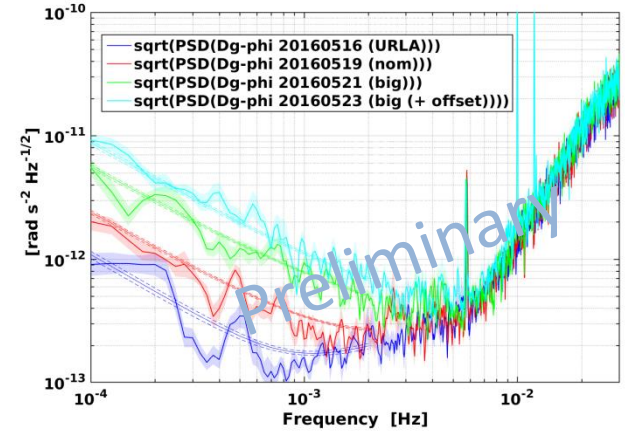
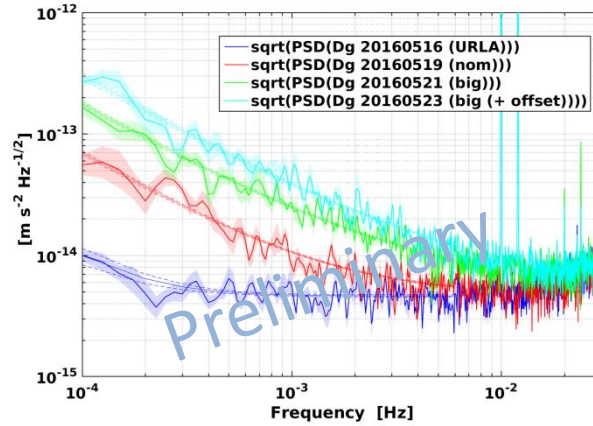
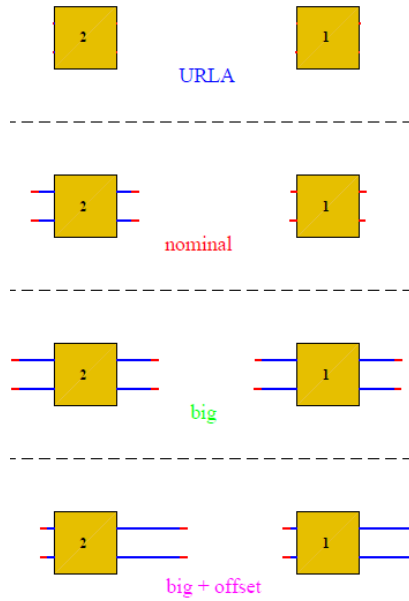


# Quantifying actuation noise

- Increase actuation forces (without letting TM hit SC) to exaggerate force noise
- Measure both force and torque noise
- Parametric model to «extract» intrinsic voltage fluctuations from combinations of electrodes
- Distinguish correlated fluctuations from uncorrelated fluctuations
- Distinguish +X actuators from -X



# Actuation noise test campaign: results



Noise in  $\Delta g$ ,  $\Delta \gamma_\phi$  increases with larger authorities and same net forces / torques

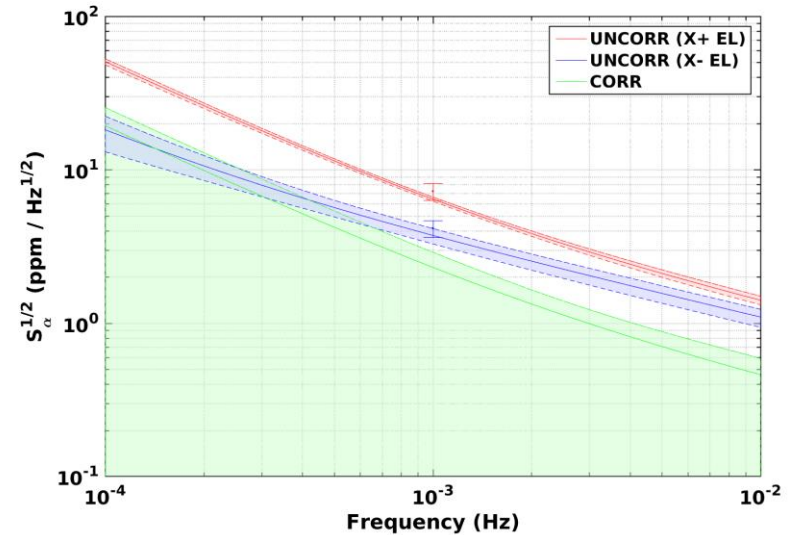
→ Uncorrelated gain fluctuations

Noise increase with large applied +X force

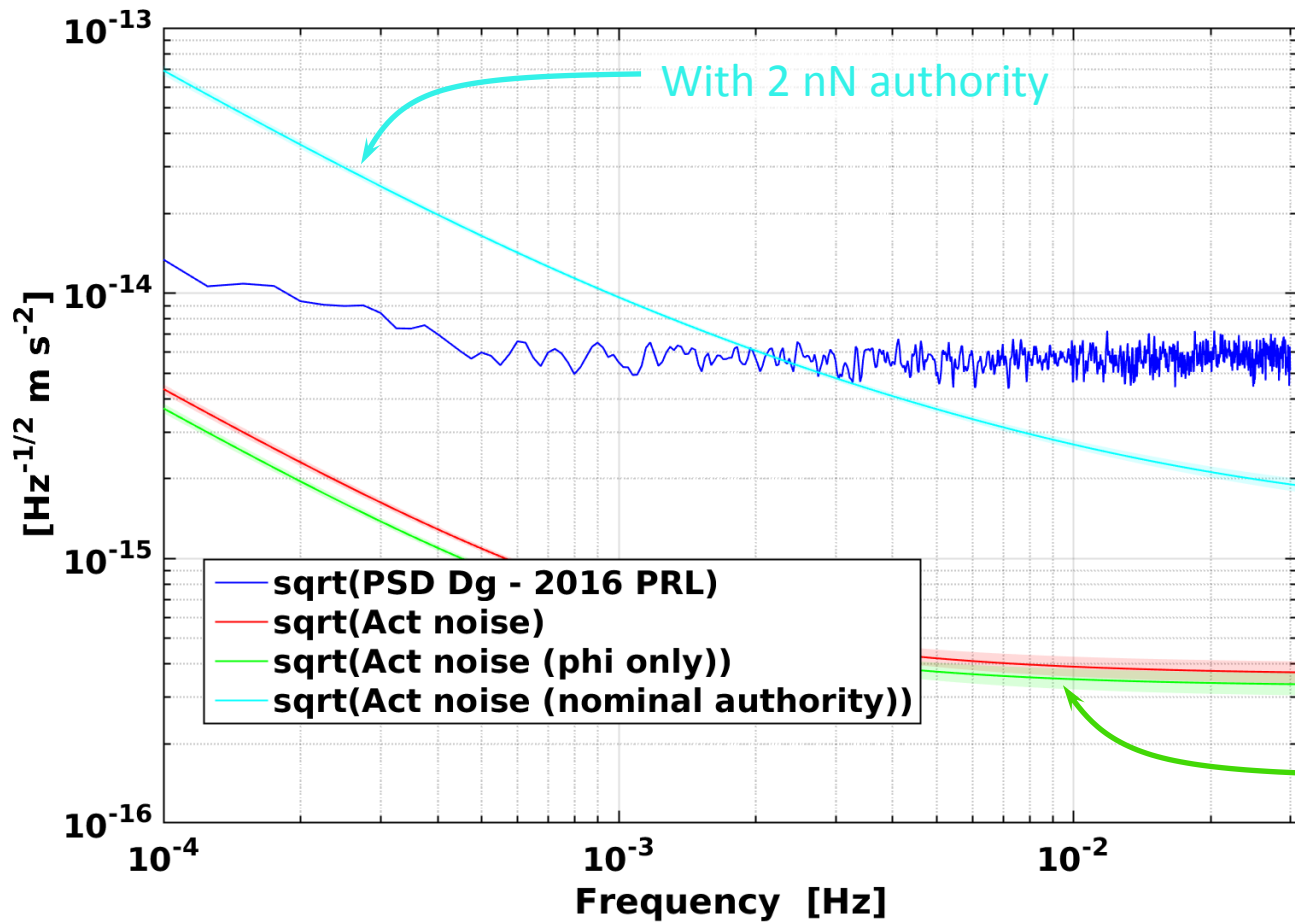
→ X+ actuators worse!

→ In agreement with ground tests!

No correlated (voltage reference) noise



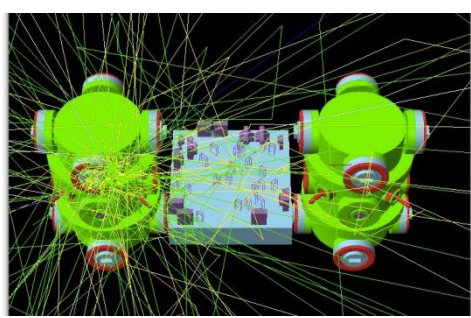
# Actuation noise projection



- Actuation noise important but not dominant
- Mostly from  $\phi$  torques
- Would have dominated with  $\Delta g_{DC}$  1 nm/s<sup>2</sup>

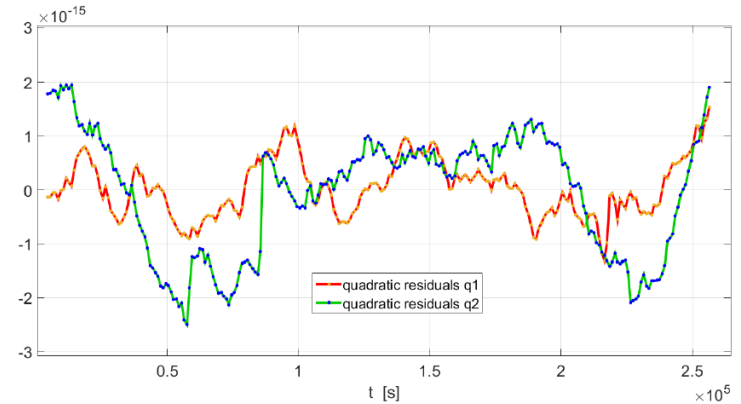
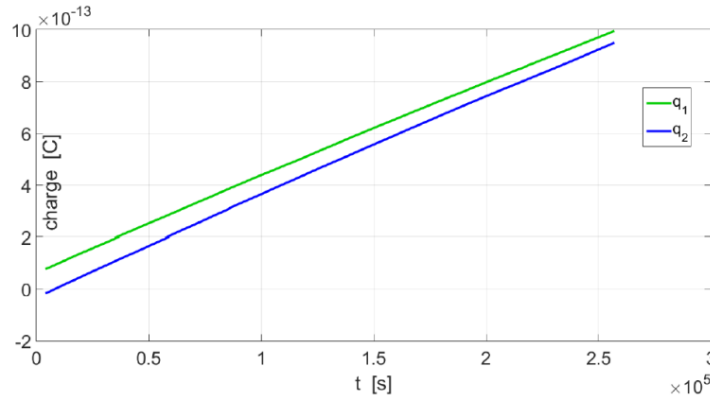
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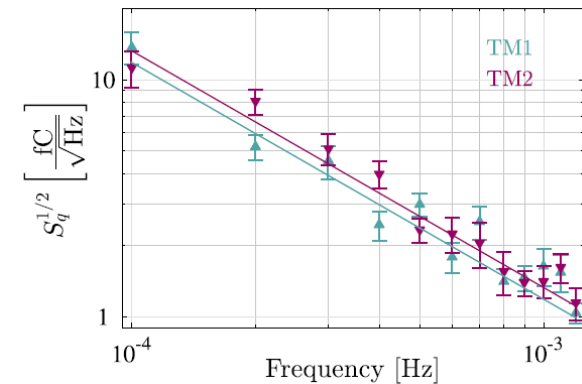


# TM charging: steady and stochastic

- Cosmic ray + solar particle events accumulate TM charge
- Mix with stray electrostatic fields to give forces (and noise)



Net charge rate: +25 e/s  
 Effective shot noise rate: 1200 e/s



PRL 118, 171101 (2017)

PHYSICAL REVIEW LETTERS

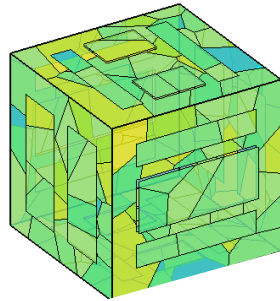
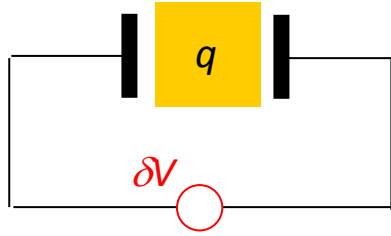
week ending  
28 APRIL 2017



**Charge-Induced Force Noise on Free-Falling Test Masses: Results from LISA Pathfinder**

*Weber – Amaldi 2017, Pasadena – 11 July 2017*

# TM charging and stray electrostatic fields



$$F = - \frac{q}{C_{TOT}} \left| \frac{\partial C_x}{\partial x} \right| \Delta_x$$

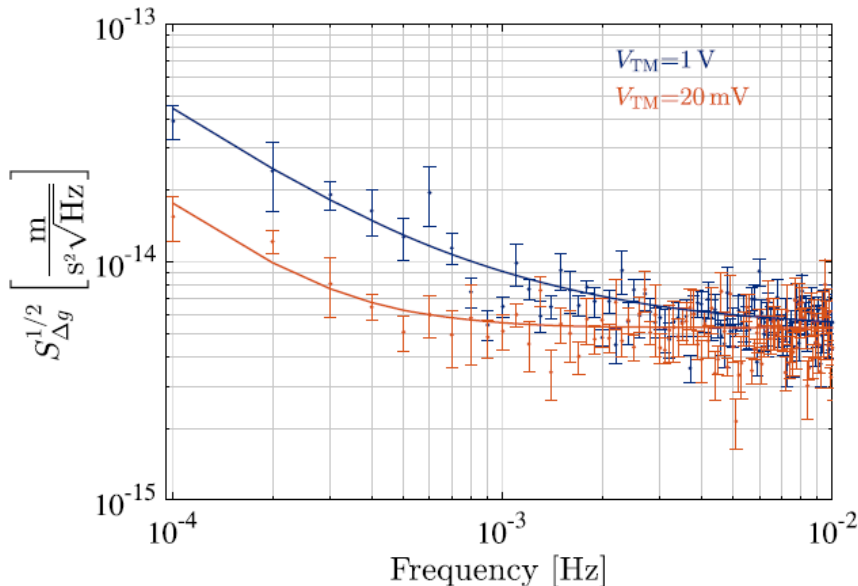
TM charge  
 Stray E-field (equiv.  $\Delta V$  on 1 electrode)

## Charge fluctuations

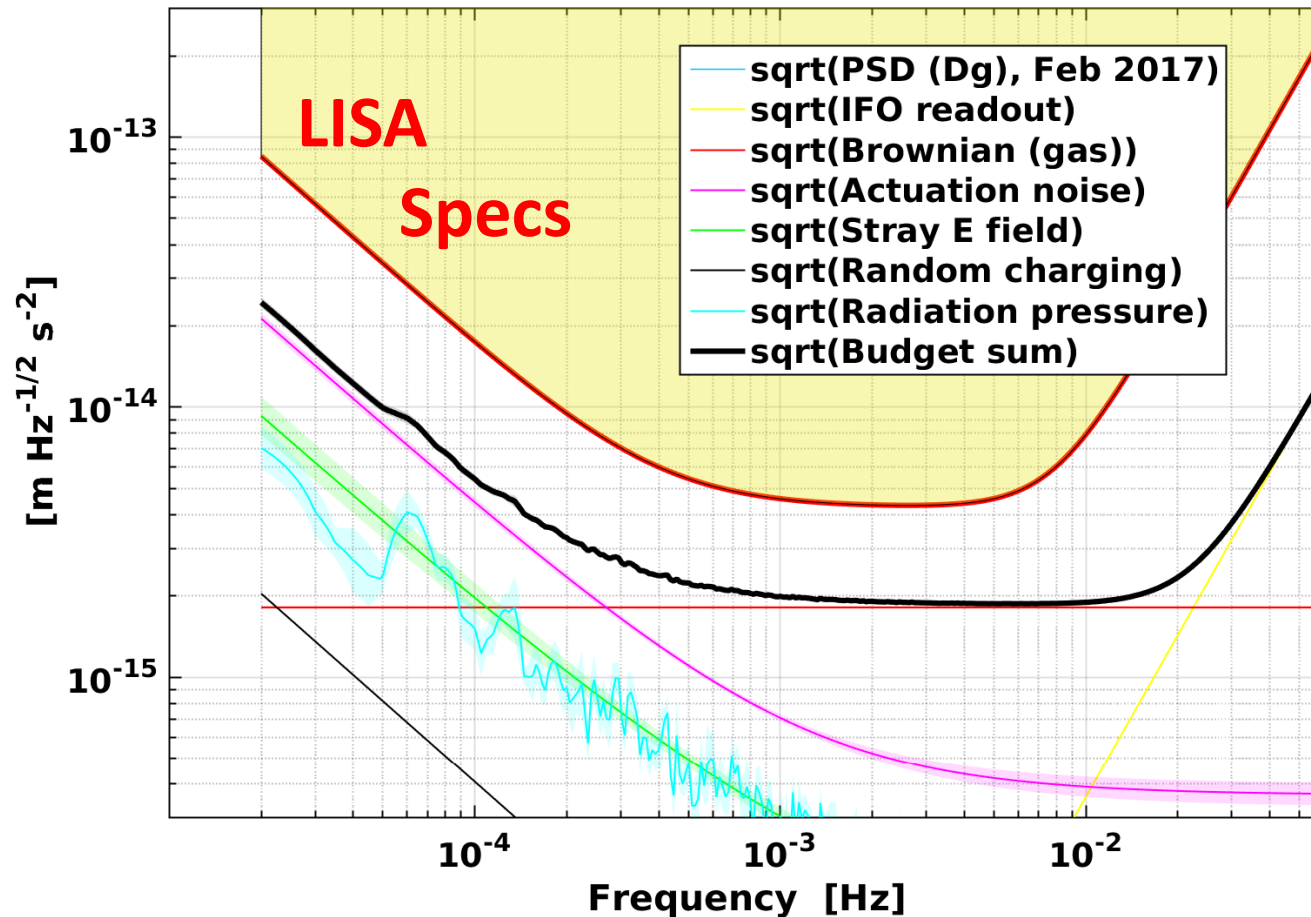
- measure 10 aA/Hz<sup>1/2</sup>
- need to limit stray DC field ( $\Delta_x < 10$  mV)

## Stray field fluctuations

- measure  $S_{\Delta X}^{1/2}$  200  $\mu$ V/Hz<sup>1/2</sup> at 100  $\mu$ Hz
- consistent with actuation voltage noise
- need to keep TM charge  $< 10^7$  e (50 mV)
- OK for 2 weeks between discharge
- continuous discharge better, eliminates interruptions
- also demonstrated on LPF!



# LISA Pathfinder $\Delta g$ noise budget (February 2017)



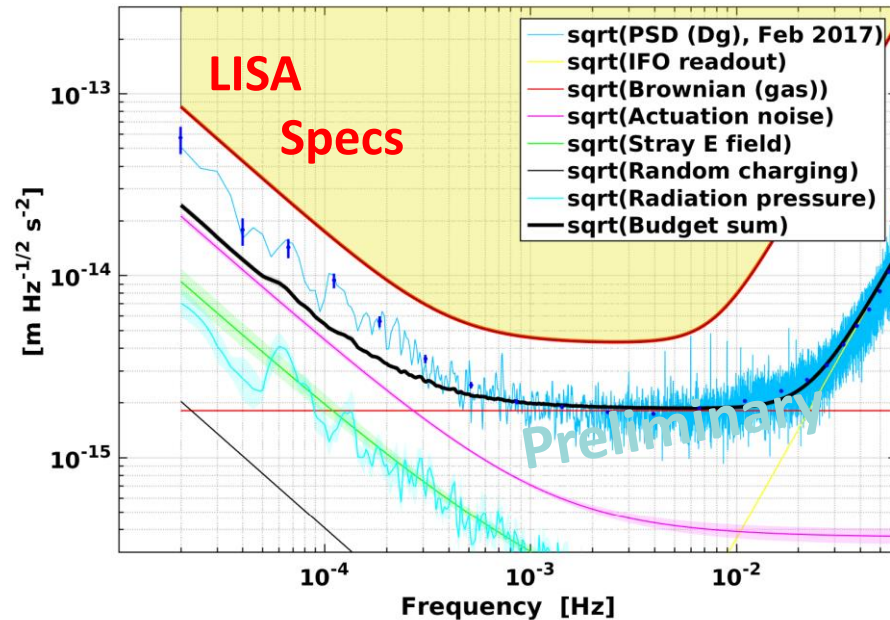
LTPDA 3.0.12.ops (R2015b), 2017-07-11 00:44:52.225 UTC, LPF\_DA\_Module: 8a04b9f, ltpda: 88427c3, iplotPSD

Work ongoing for low freq sources (thermal, inertial, magnetic ...)

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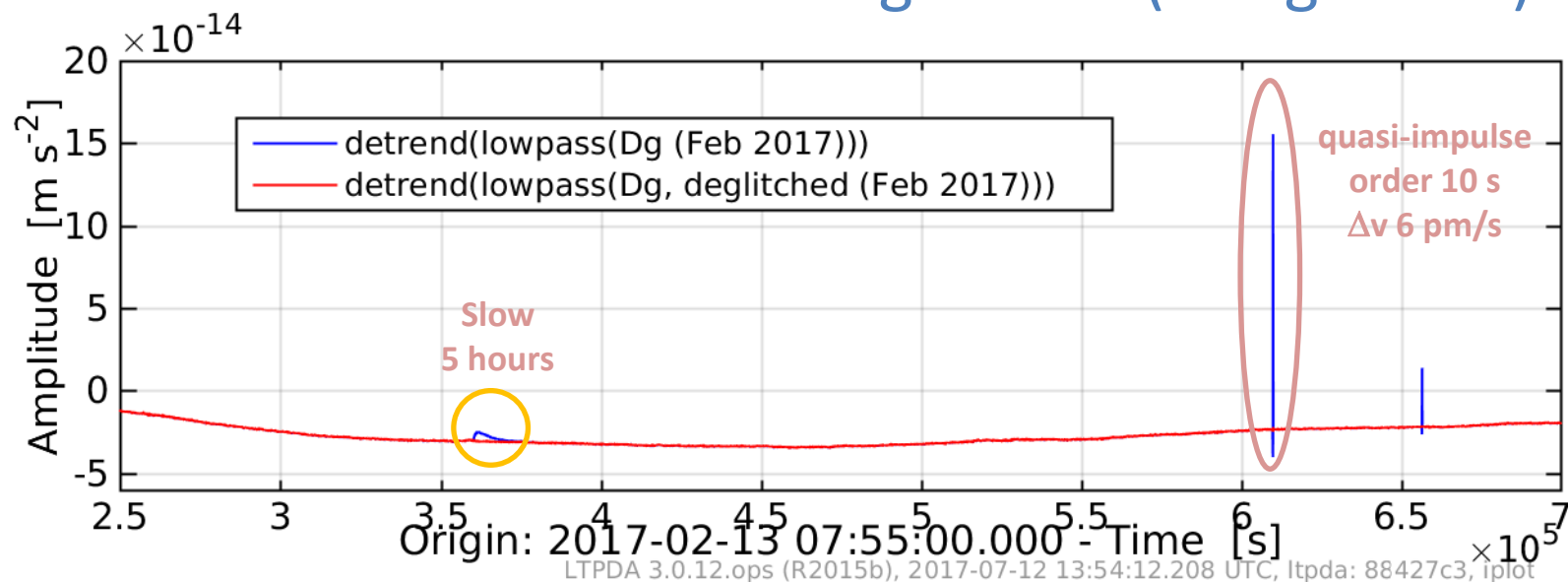
# LISA Pathfinder $\Delta g$ noise budget (February 2017)



LTPDA 3.0.12.ops (R2015b), 2017-07-11 00:44:52.225 UTC, LPF\_DA\_Module: 8a04b9f, ltpda: 88427c3, iplotPSD

- LPF acceleration noise below LISA requirement at all frequencies
- Noise budget (conservative) explains less than half noise (power) at low frequencies
  - Work ongoing for low freq sources (gravitational, thermal, inertial, magnetic ...)
  - Need to understand, test, and reproduce with LISA

# Transient non-Gaussian $\Delta g$ events (aka glitches)



- Mostly fast (10's seconds), up to of order 1/day
- (as yet) cause unidentified
- Fit with «simple» phenomenological model (4-8 params)
- Need to handle these in LISA data analysis?
  - Ideally discriminated at instrument / SC level (correlation with a disturbance)
  - Sagnac (less sensitive to GW) discrimination?
  - Population of unmodelled gravitational wave sources?

Thank you!

