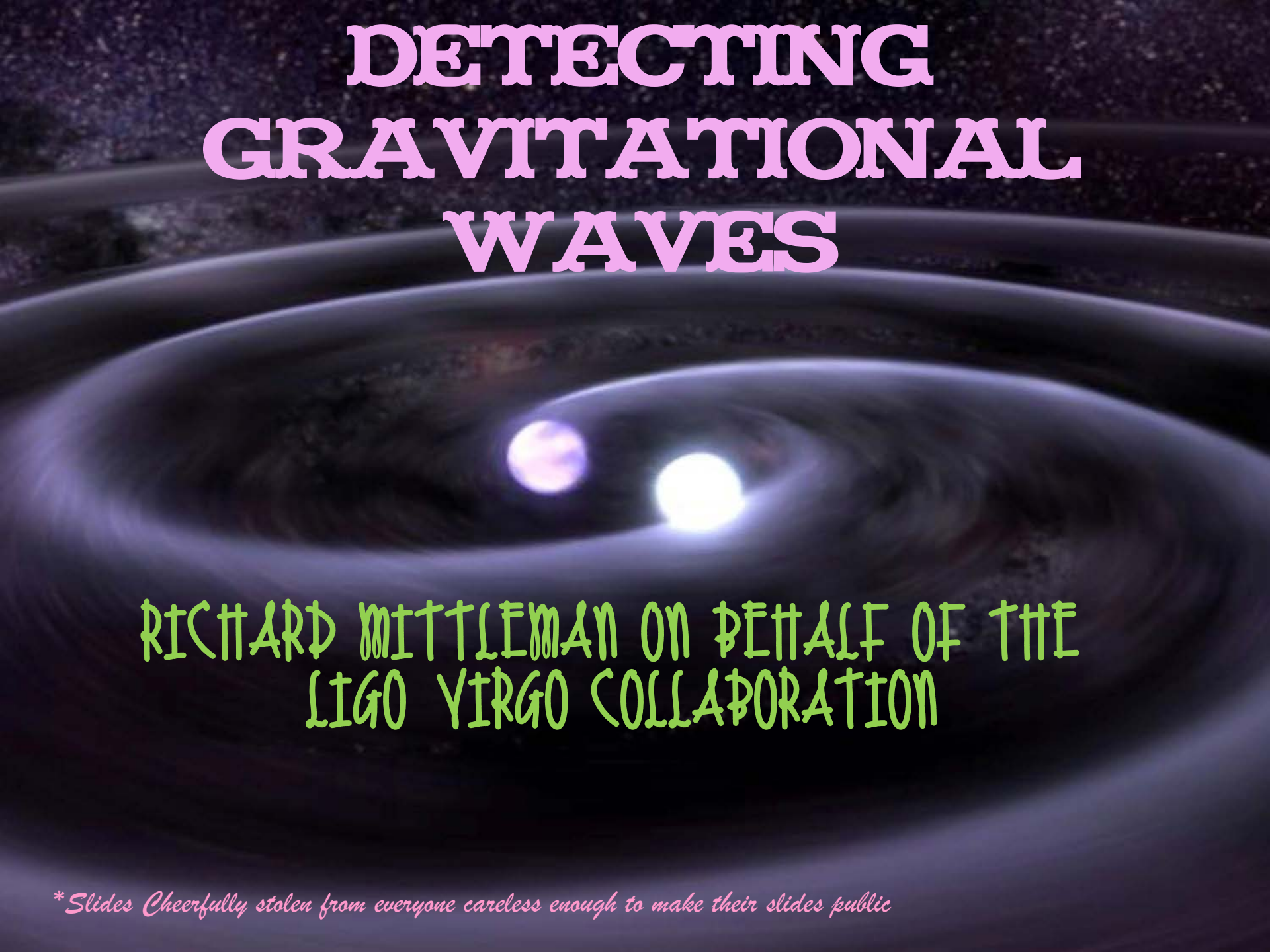
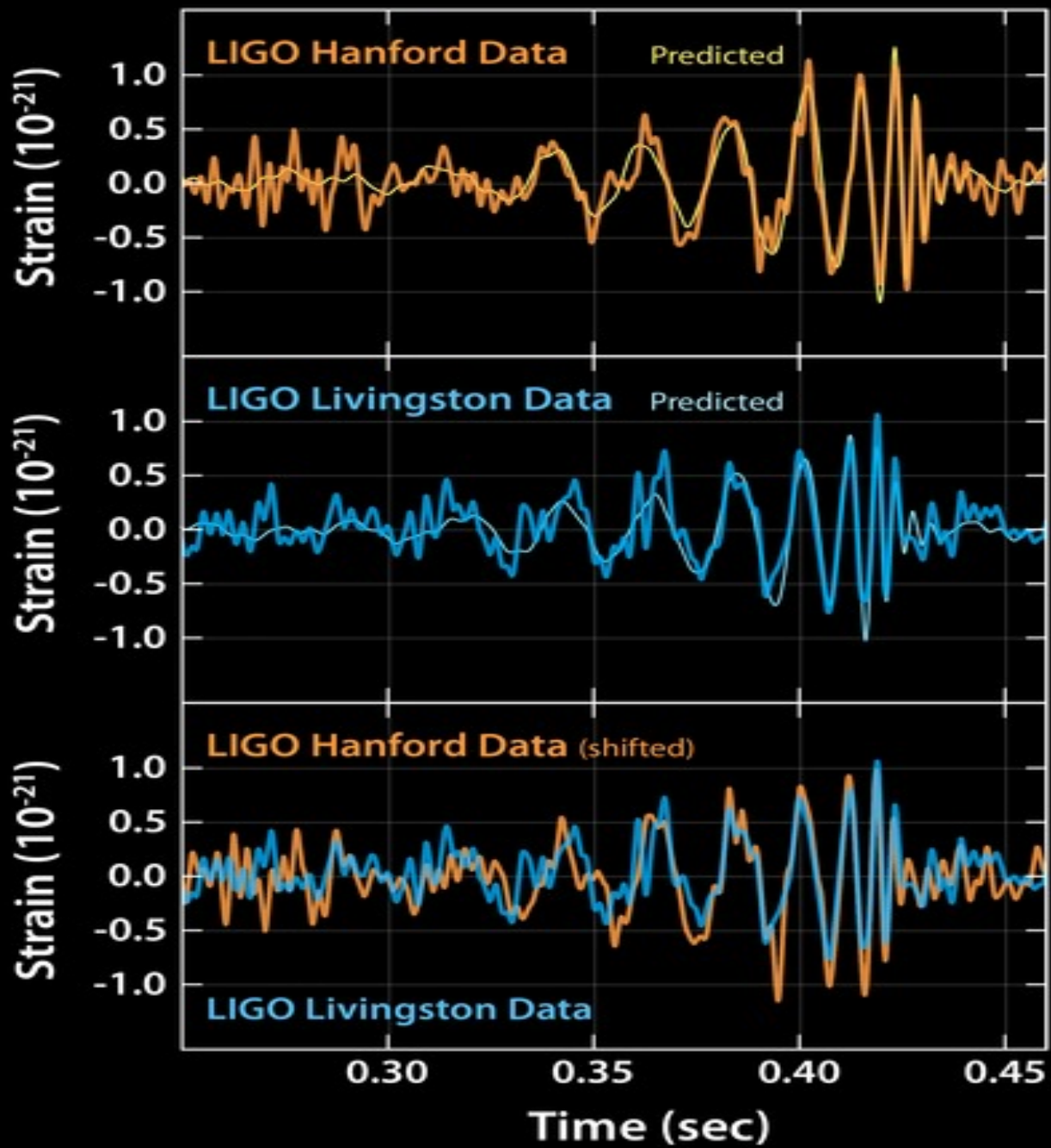


DETECTING GRAVITATIONAL WAVES

A visualization of gravitational waves as ripples in spacetime. Two bright, glowing objects, likely black holes, are shown in the center, surrounded by concentric, glowing ripples that spread outwards. The background is a dark, starry space.

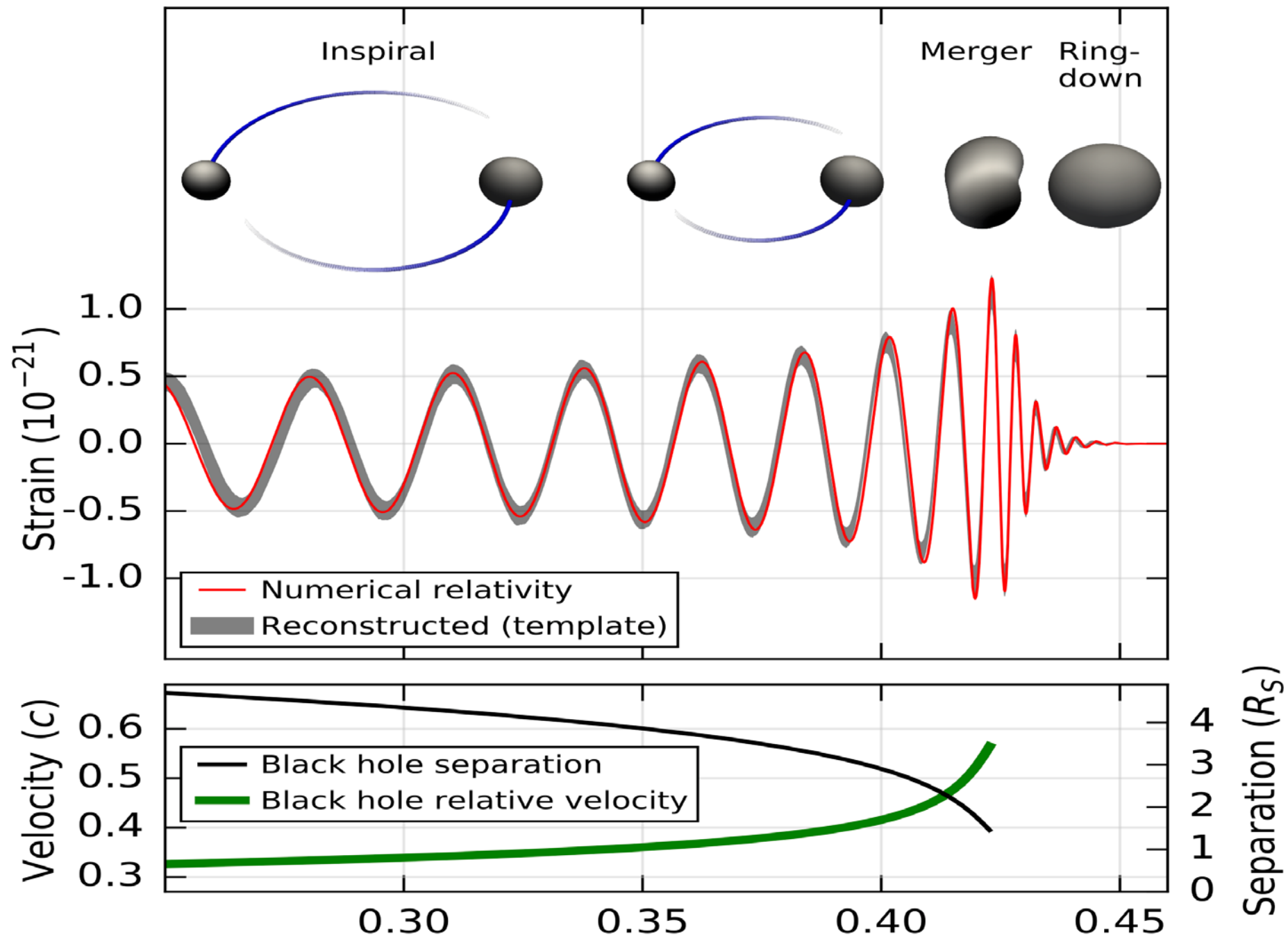
RICHARD MITTLEMAN ON BEHALF OF THE
LIGO VIRGO COLLABORATION

**Slides Cheerfully stolen from everyone careless enough to make their slides public*

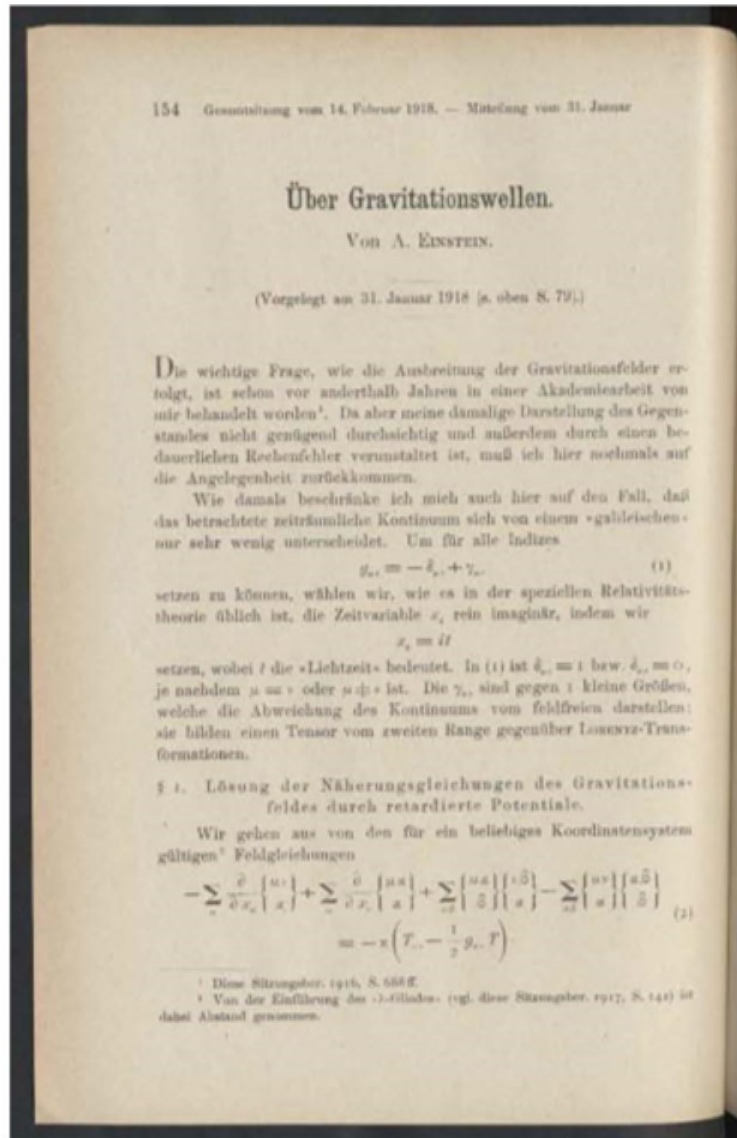


a simulation of GW150914



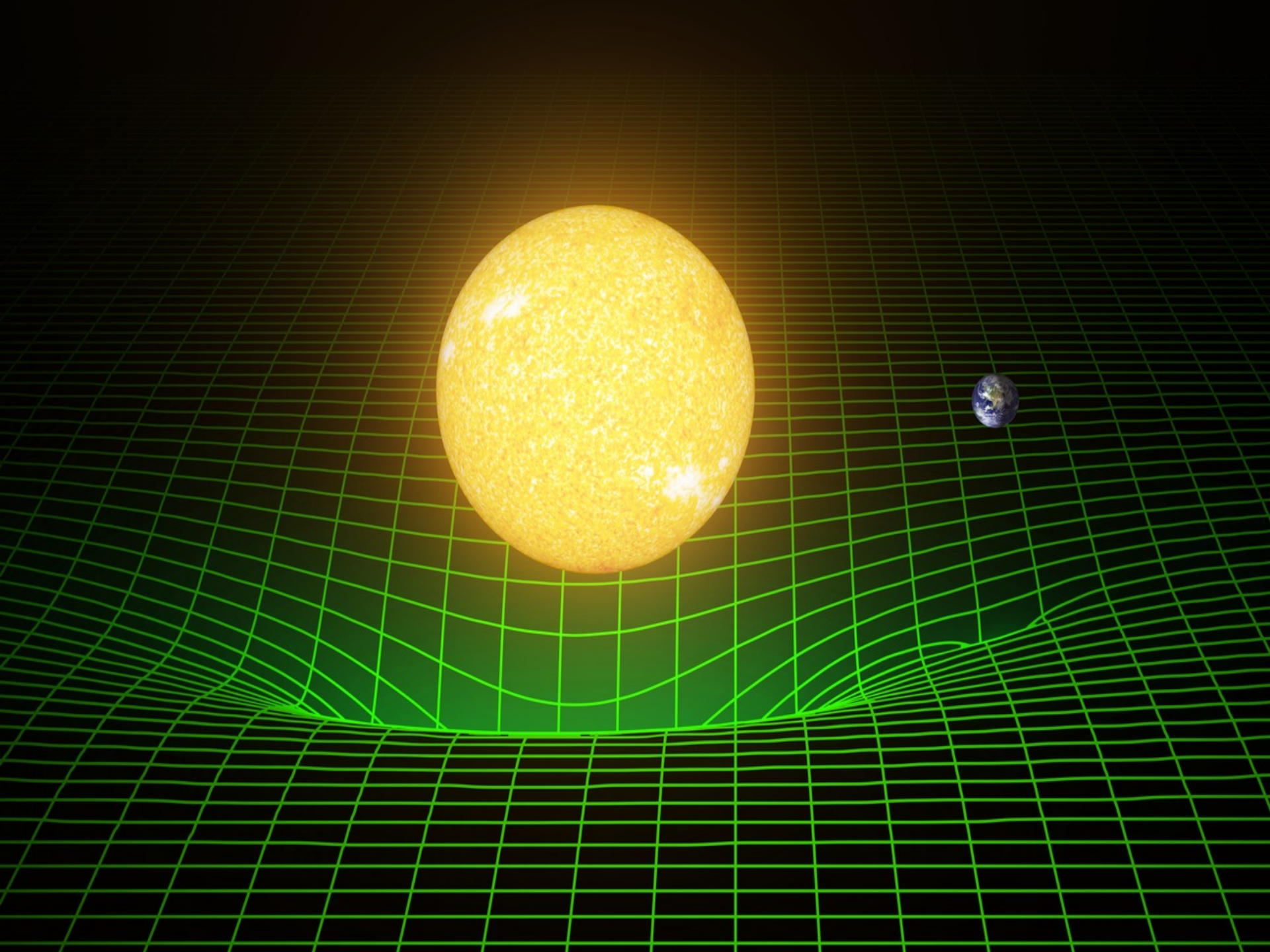


Gravitational Waves in General Relativity (Einstein 1916,1918)



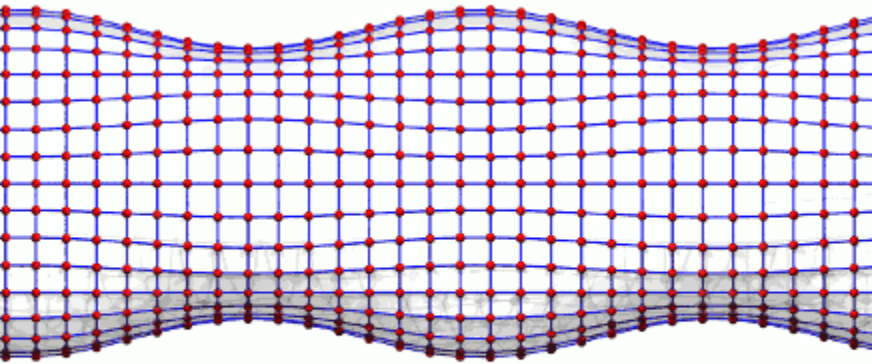
$$g_{ij} = \delta_{ij} + h_{ij}$$

h_{ij} : transverse, traceless and propagates at $v=c$

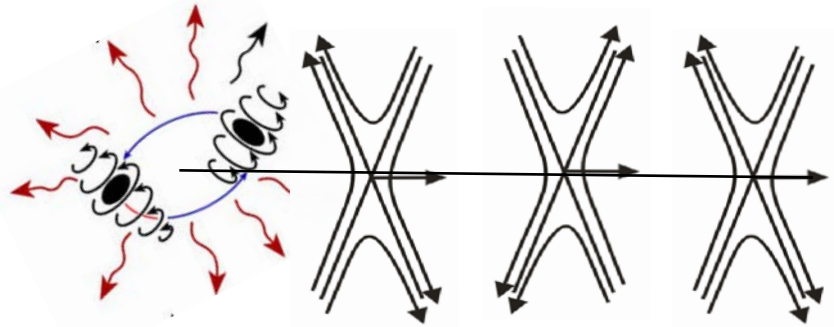


Radiation is a Quadrupolar Strain

in space-time

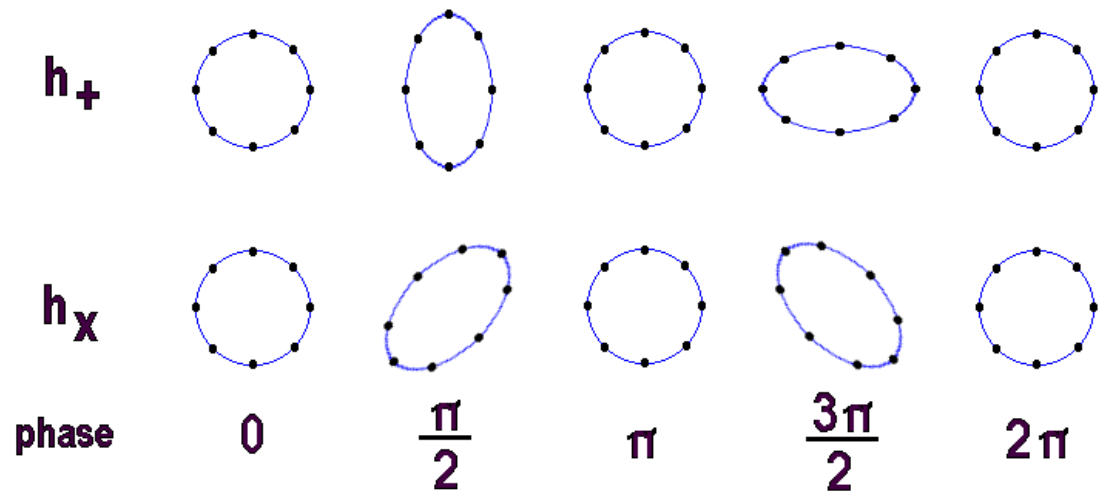


www.einstein-online.info



Space is very stiff
For astrophysical sources
you might expect $h \sim 1e-21$

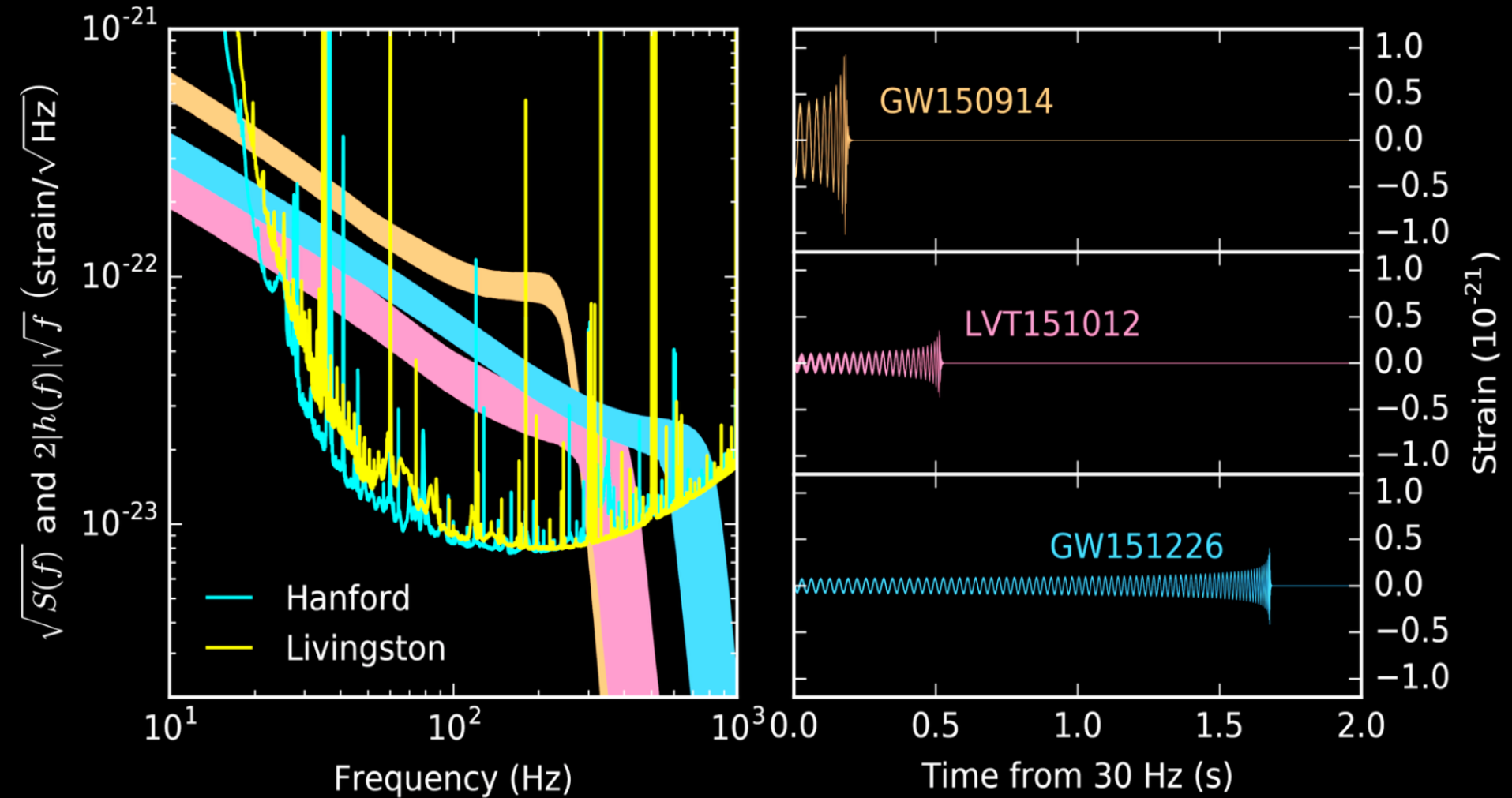
There are two
polarizations



How big is the effect?
Zooming into an Atom



Three(ish) Detections in the first science run (O1)

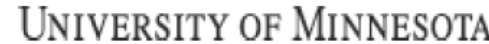
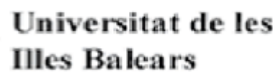
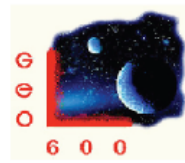


LIGO

LIGO Scientific Collaboration

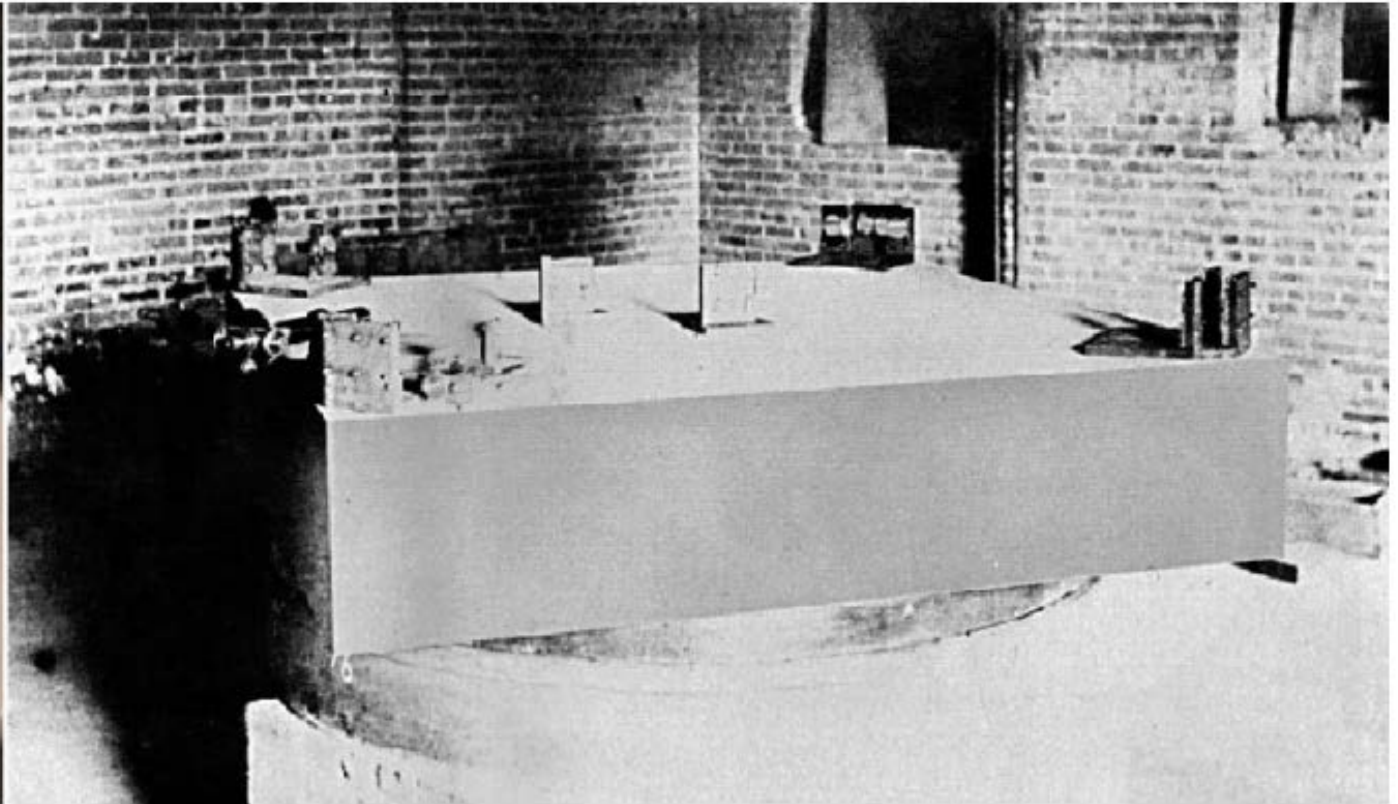


- Australian Consortium for Interferometric Gravitational Astronomy
- The Univ. of Adelaide
- Andrews University
- The Australian National Univ.
- The University of Birmingham
- California Inst. of Technology
- Cardiff University
- Carleton College
- Charles Stuart Univ.
- Columbia University
- Embry Riddle Aeronautical Univ.
- Eötvös Loránd University
- University of Florida
- German/British Collaboration for the Detection of Gravitational Waves
- University of Glasgow
- Goddard Space Flight Center
- Leibniz Universität Hannover
- Hobart & William Smith Colleges
- Inst. of Applied Physics of the Russian Academy of Sciences
- Polish Academy of Sciences
- India Inter-University Centre for Astronomy and Astrophysics
- Louisiana State University
- Louisiana Tech University
- Loyola University New Orleans
- University of Maryland
- Max Planck Institute for Gravit.



ART. XXXVI.—*On the Relative Motion of the Earth and the Luminiferous Ether*; by ALBERT A. MICHELSON and EDWARD W. MORLEY.*

American Journal of Science, Nov 1887 vol. Series 3 Vol. 34 no. 203 333-345



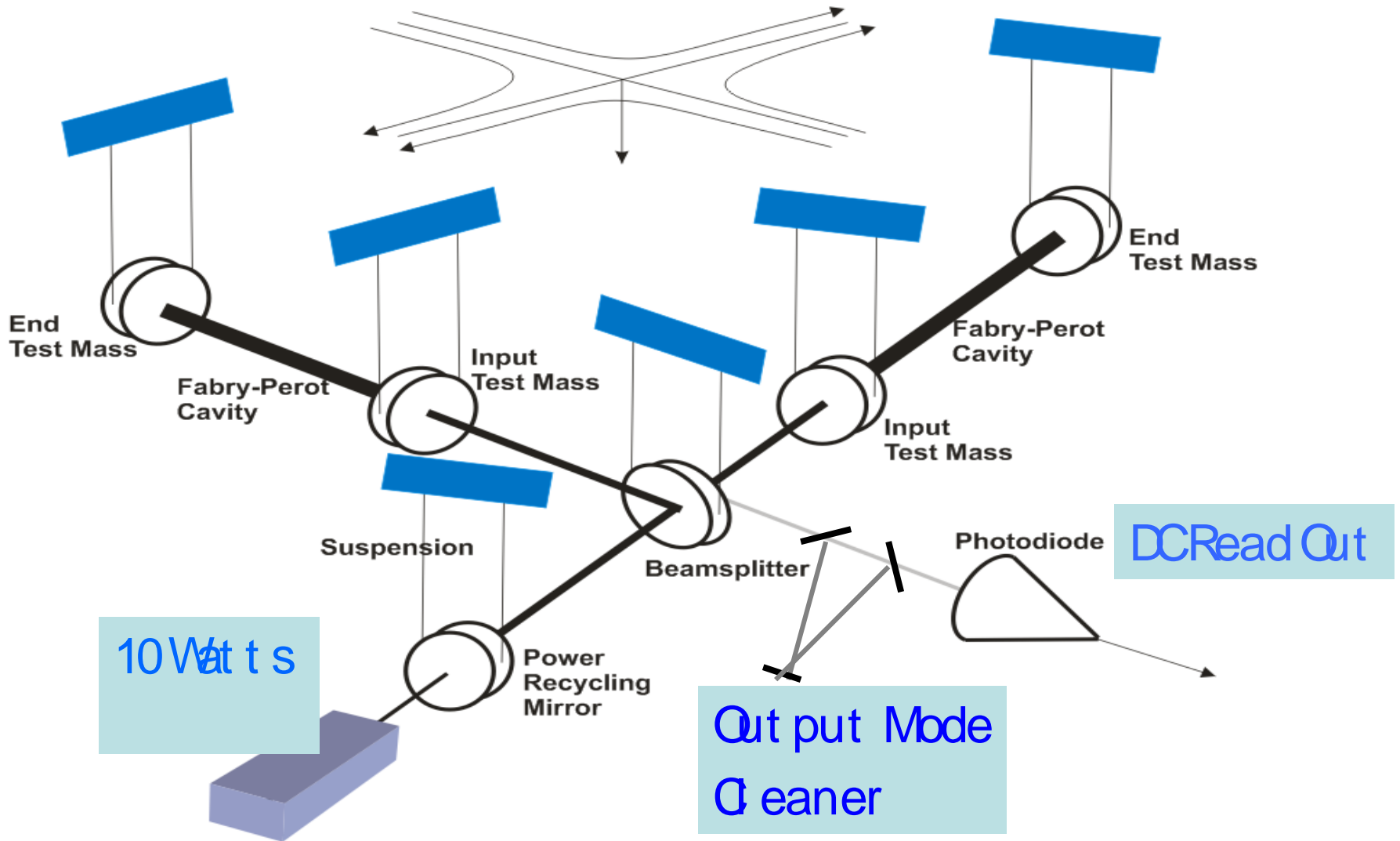
Used light interferometry to achieve sensitivity in measuring distances down to 0.01λ or $\sim 5 \times 10^{-9} \text{ m} = 0.000000005 \text{ m}$

1907 Nobel Prize in Physics to A. Michelson

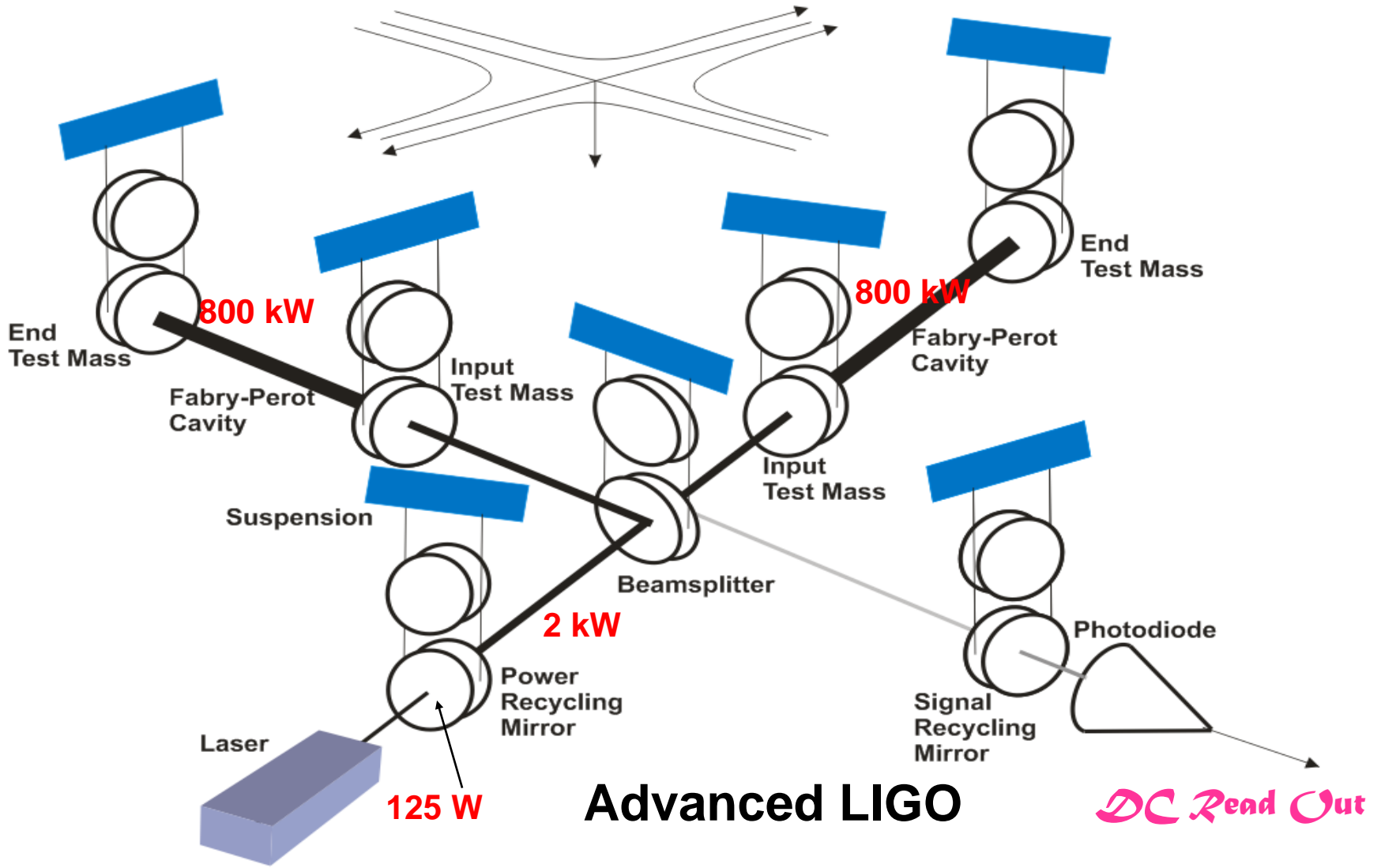
Simple Michelson Interferometer

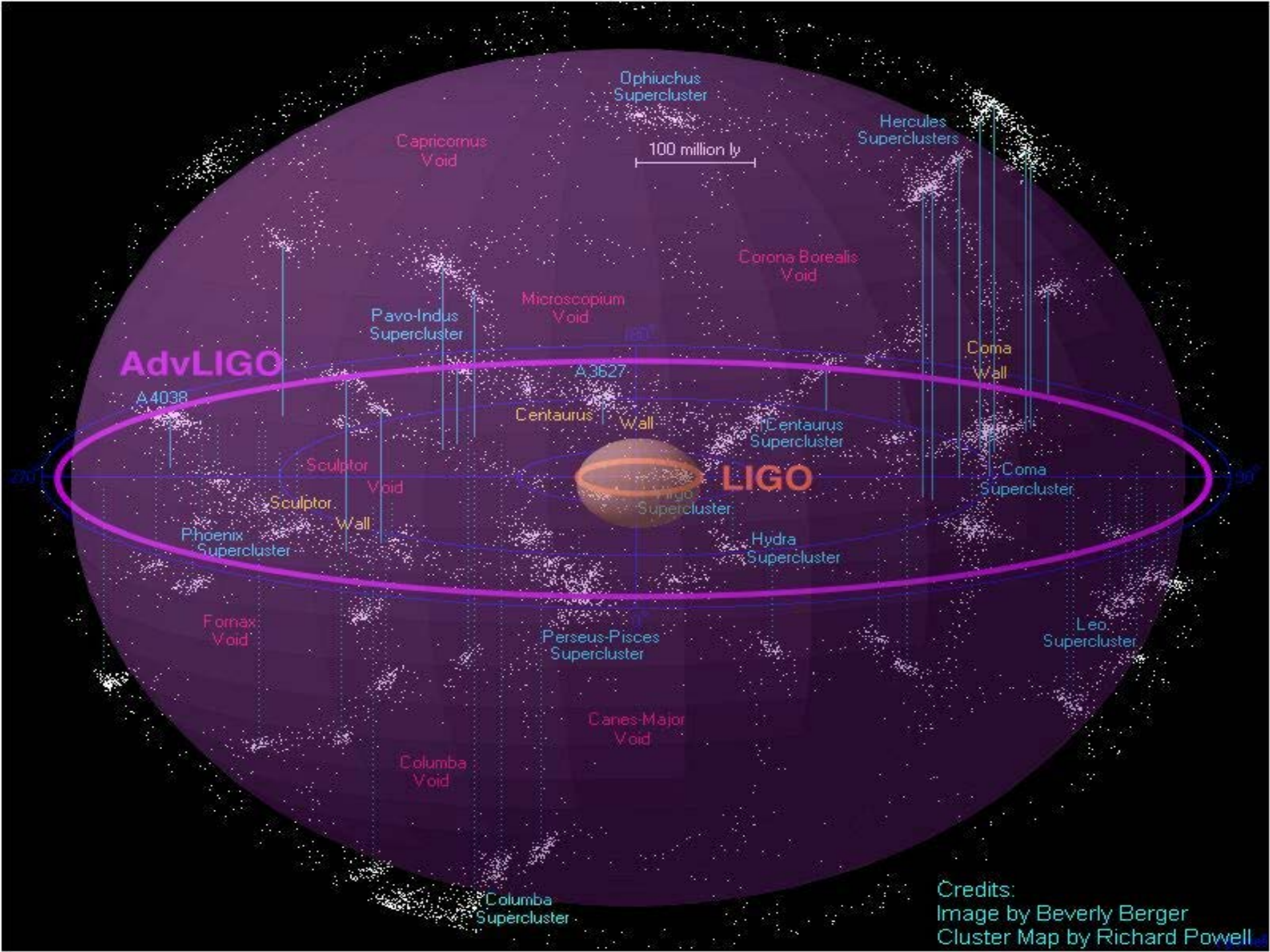


ENHANCED LIGO



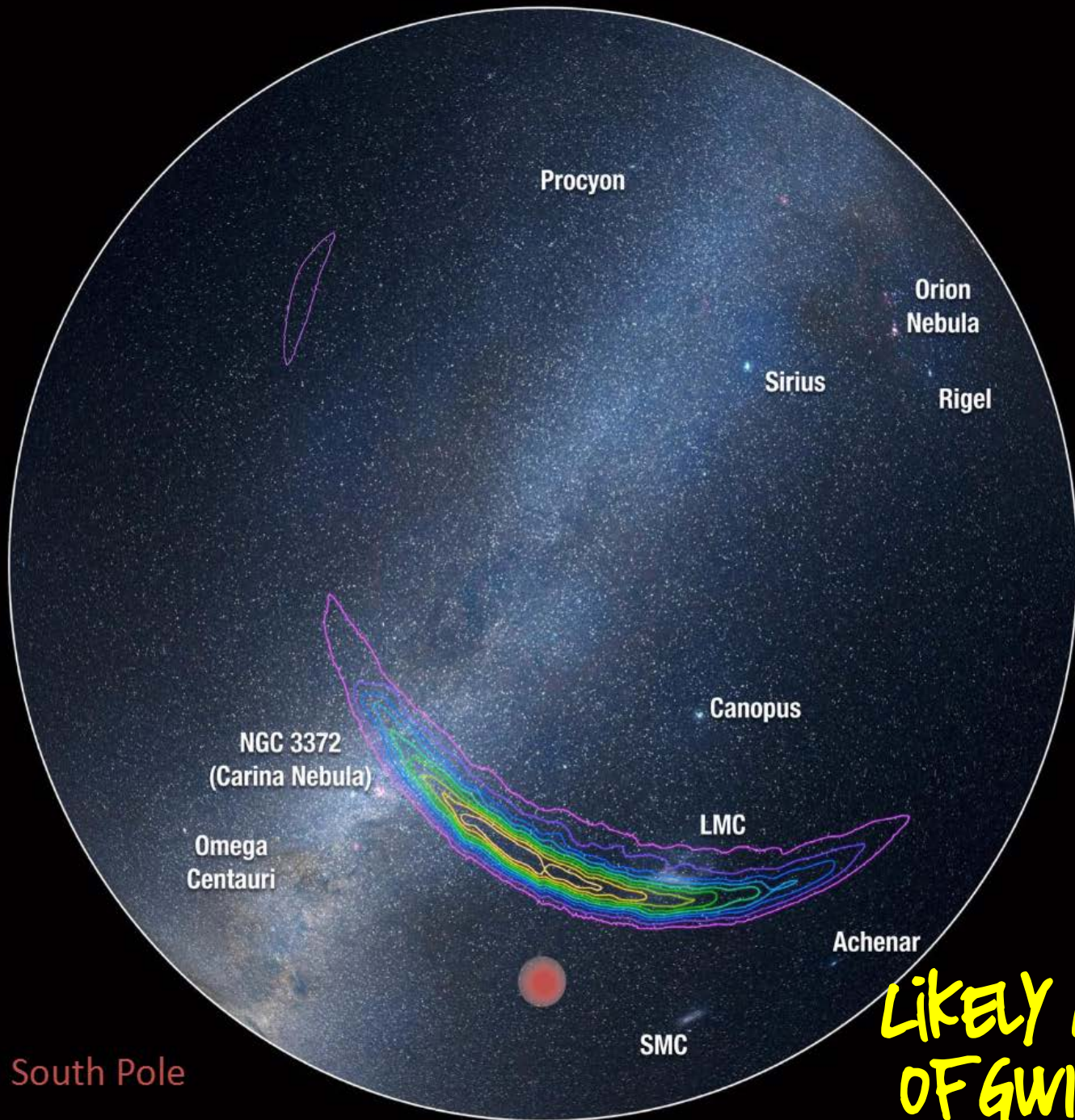
ADVANCED LIGO





Credits:
 Image by Beverly Berger
 Cluster Map by Richard Powell





LIKELY LOCATION
OF GW150914

South Pole

The **Global Network** of **Gravitational Wave Detectors**

LIGO
Hanford

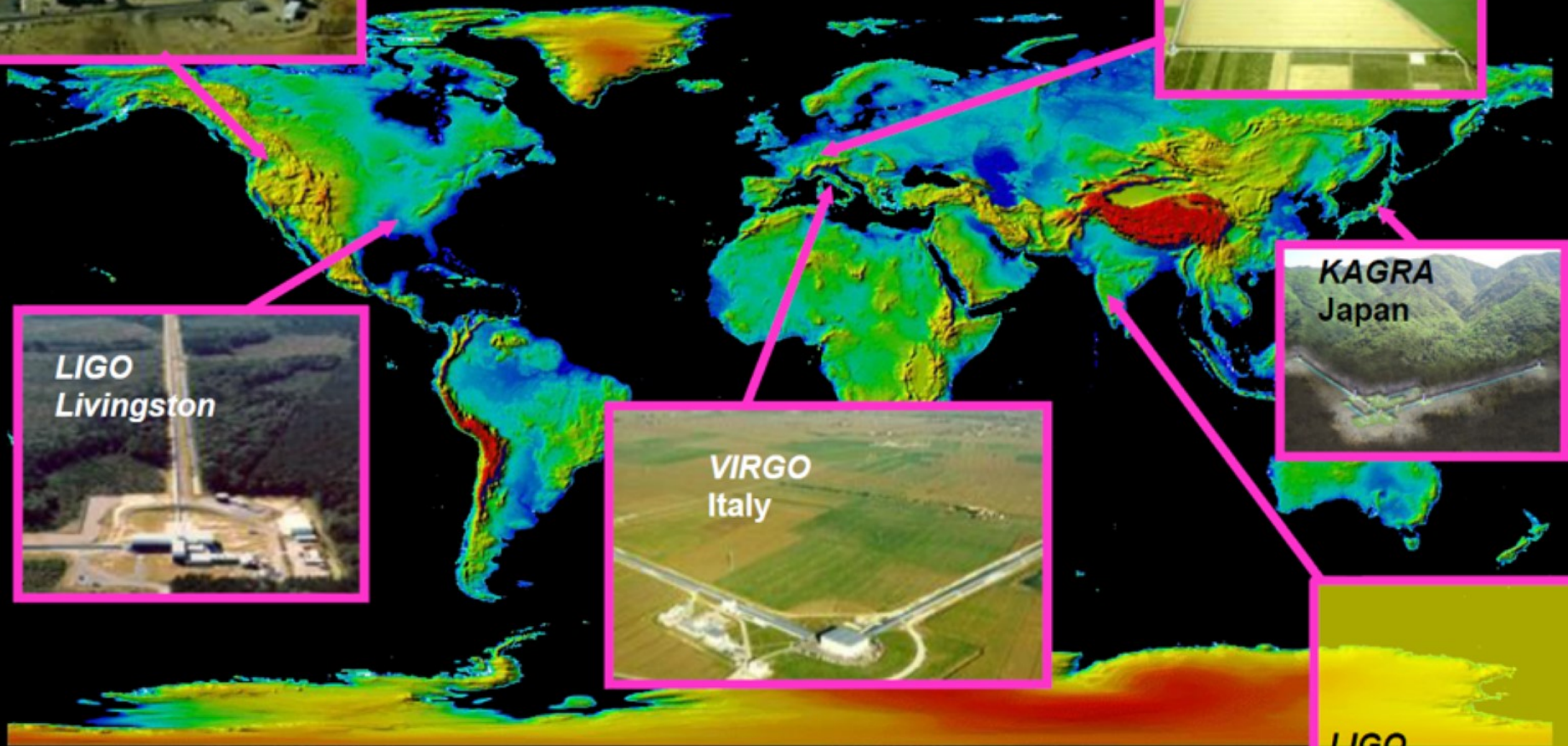
GEO600
Germany

KAGRA
Japan

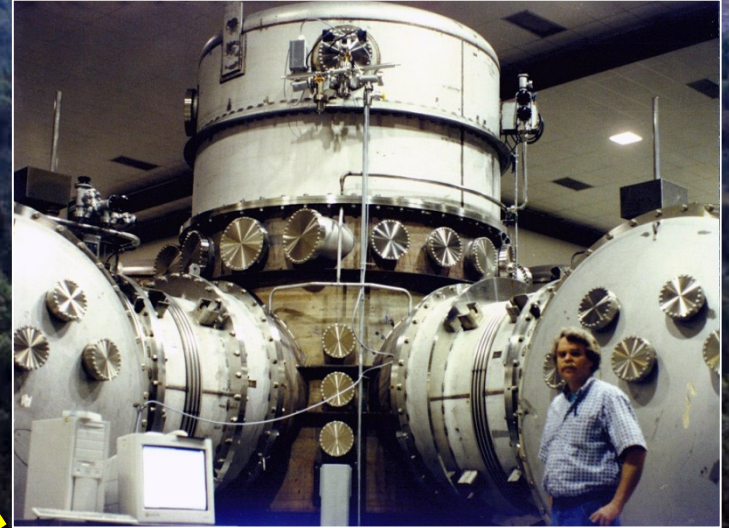
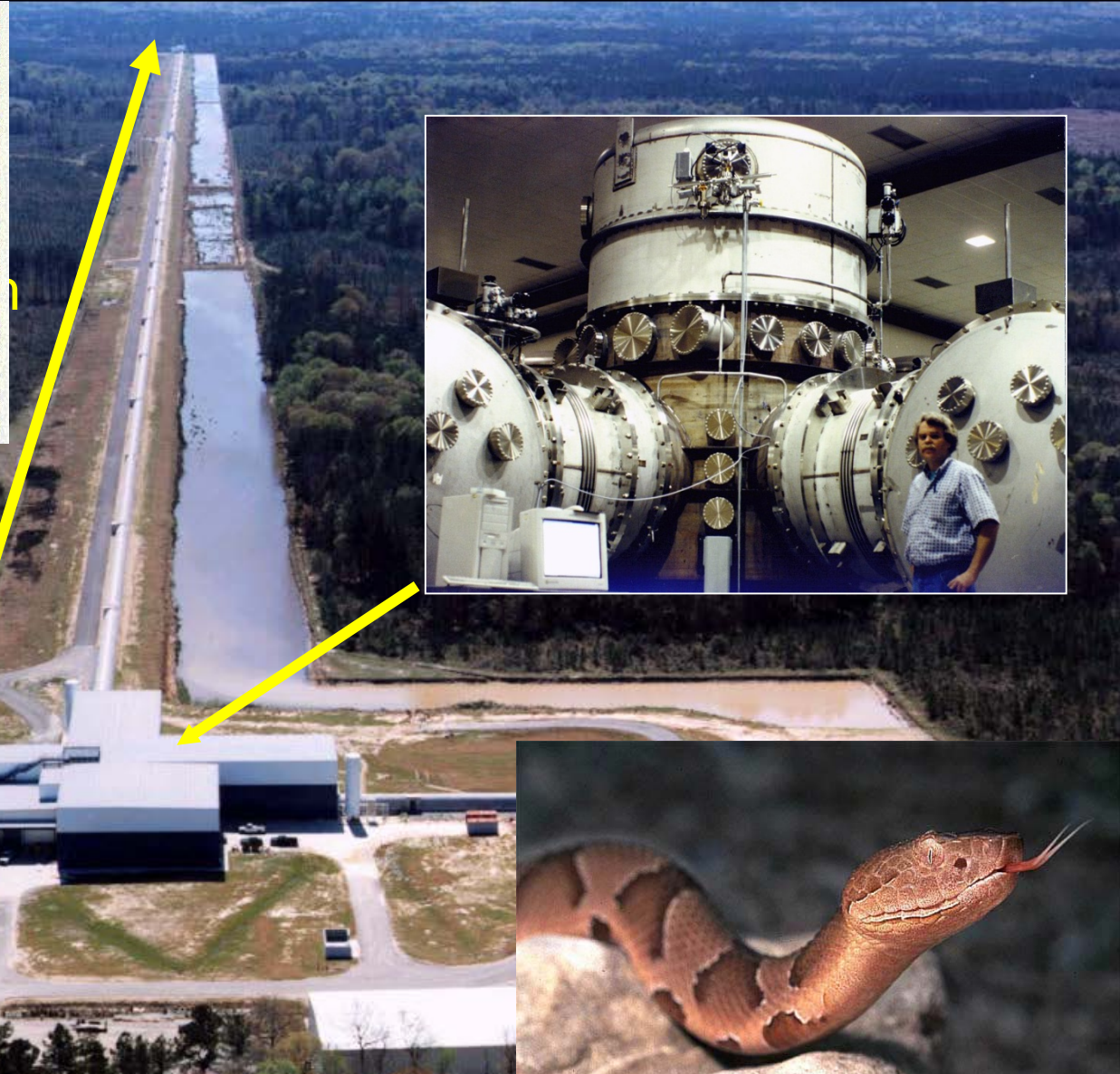
LIGO
Livingston

VIRGO
Italy

LIGO
India



LIGO Livingston



LIGO Hanford





VIRGO
CASCINA, ITALY

- Young (~300 yr) compact object
- Position is well known
- Unknown spin-down parameters



Neutron star

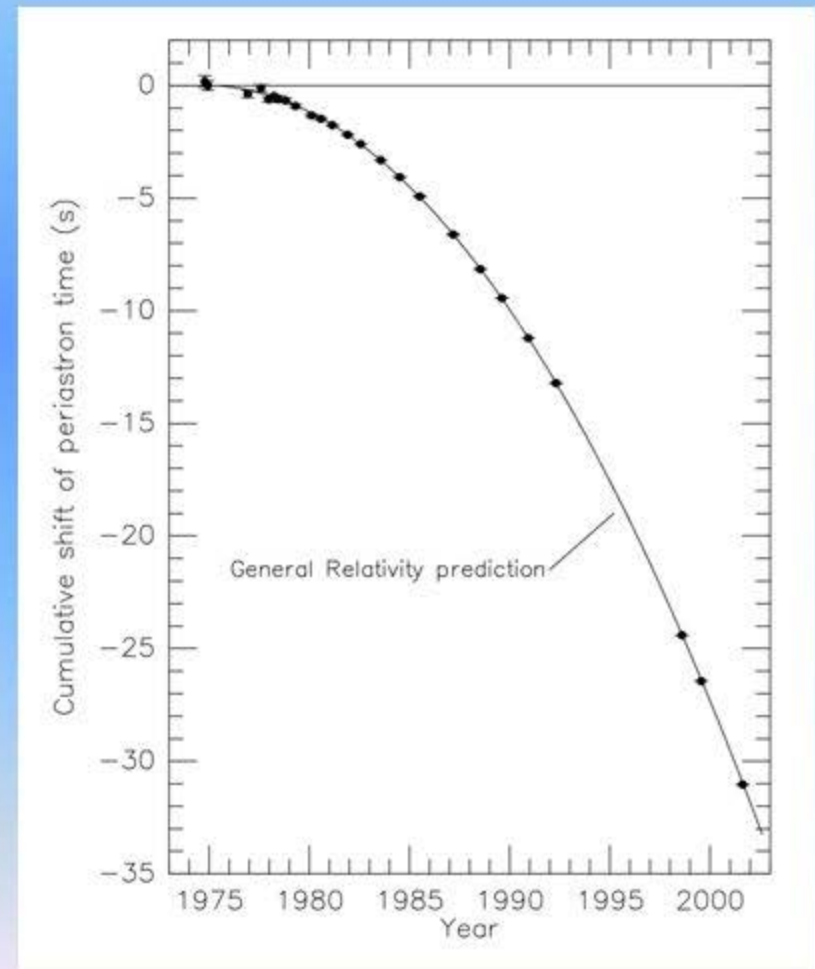
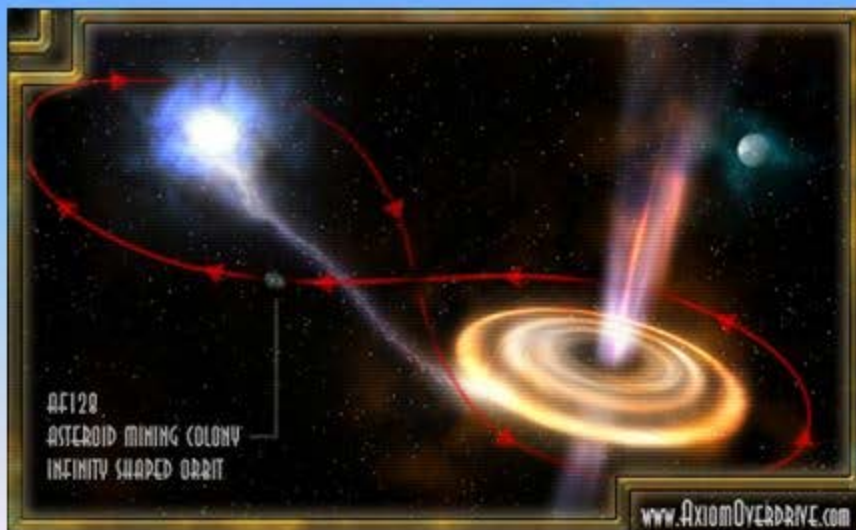
Cassiopeia A

Neutron Star Inspiral

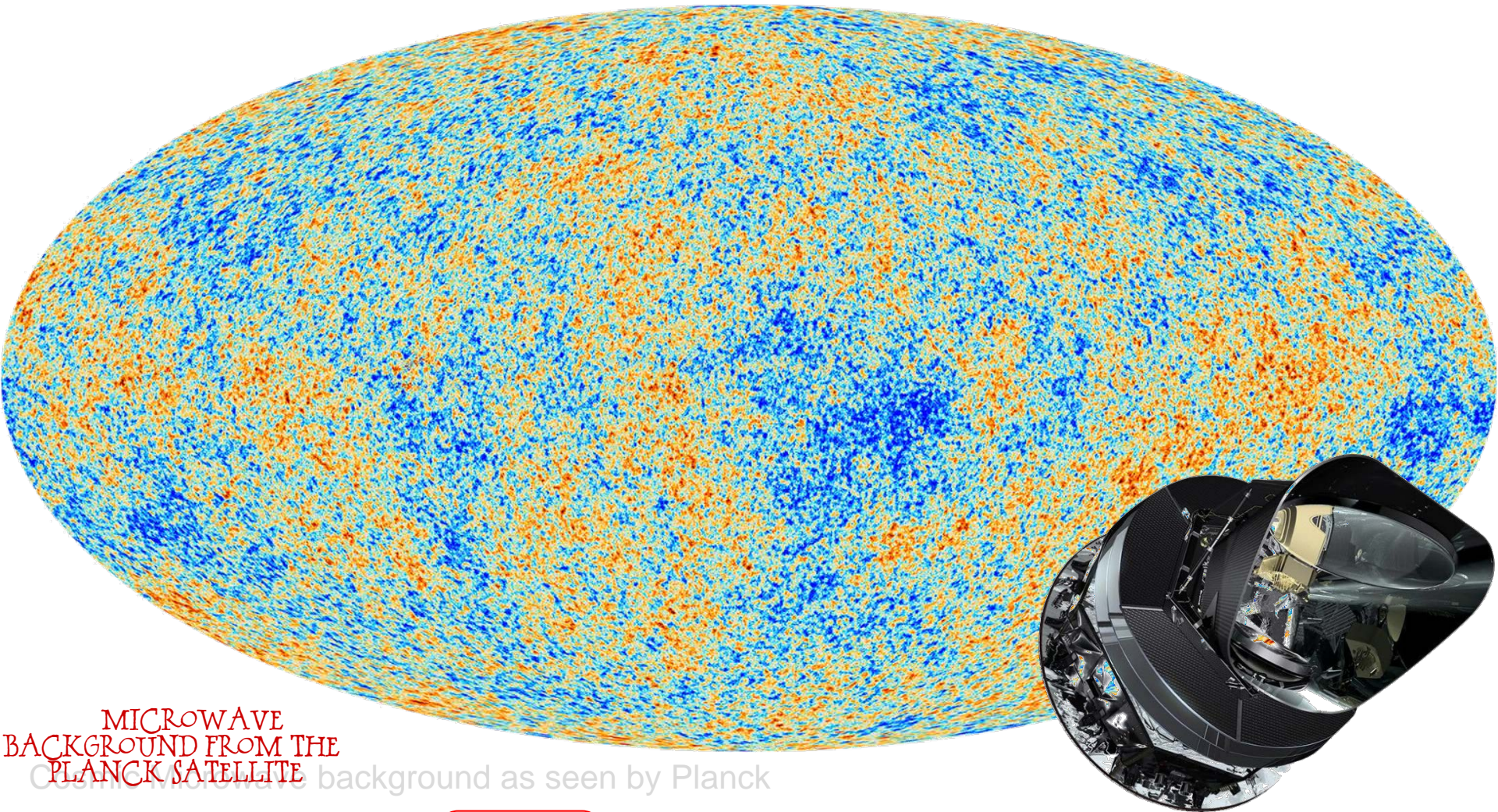


The binary pulsar

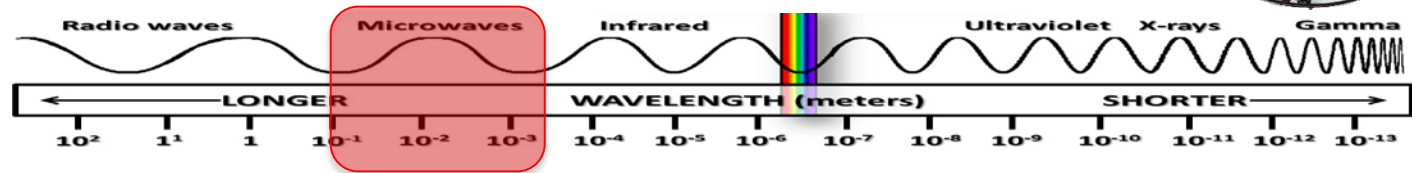
- Period speeds up 14 sec from 1975-94
- Measured to ~50 msec accuracy
- Deviation grows quadratically with time
- Merger in about 300M years
(\ll age of universe!)
- shortening of period \Leftarrow orbital energy loss
- Compact system:
negligible loss from friction, material flow
- Beautiful agreement with GR prediction
- Apparently, loss is due to GWs!
- GW emission will be strongest near the end:
– Coalescence of neutron stars!
- Nobel Prize, 1993
- By 2013, there are ~8



STOCHASTIC BACKGROUND*

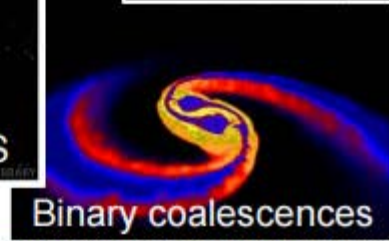
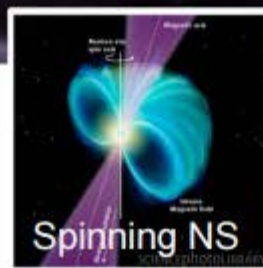
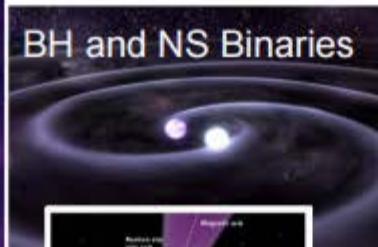
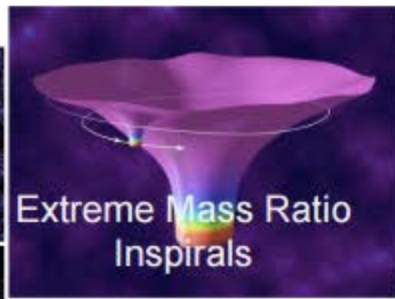
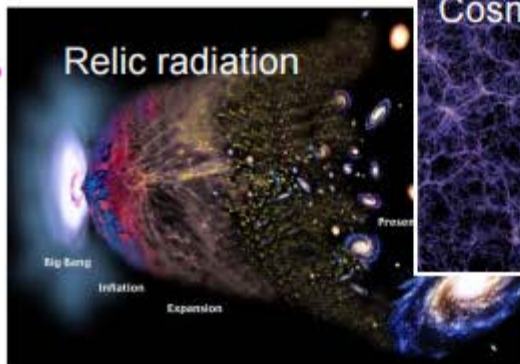


MICROWAVE
BACKGROUND FROM THE
PLANCK SATELLITE



LIGO

The GW Spectrum



10^{-16} Hz

10^{-9} Hz

10^{-4} Hz

10^0 Hz

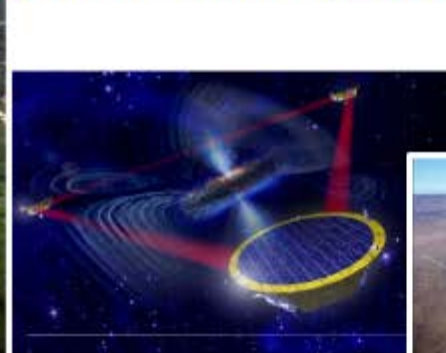
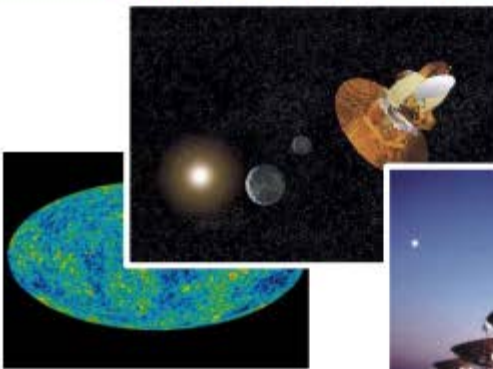
10^3 Hz

Inflation Probe

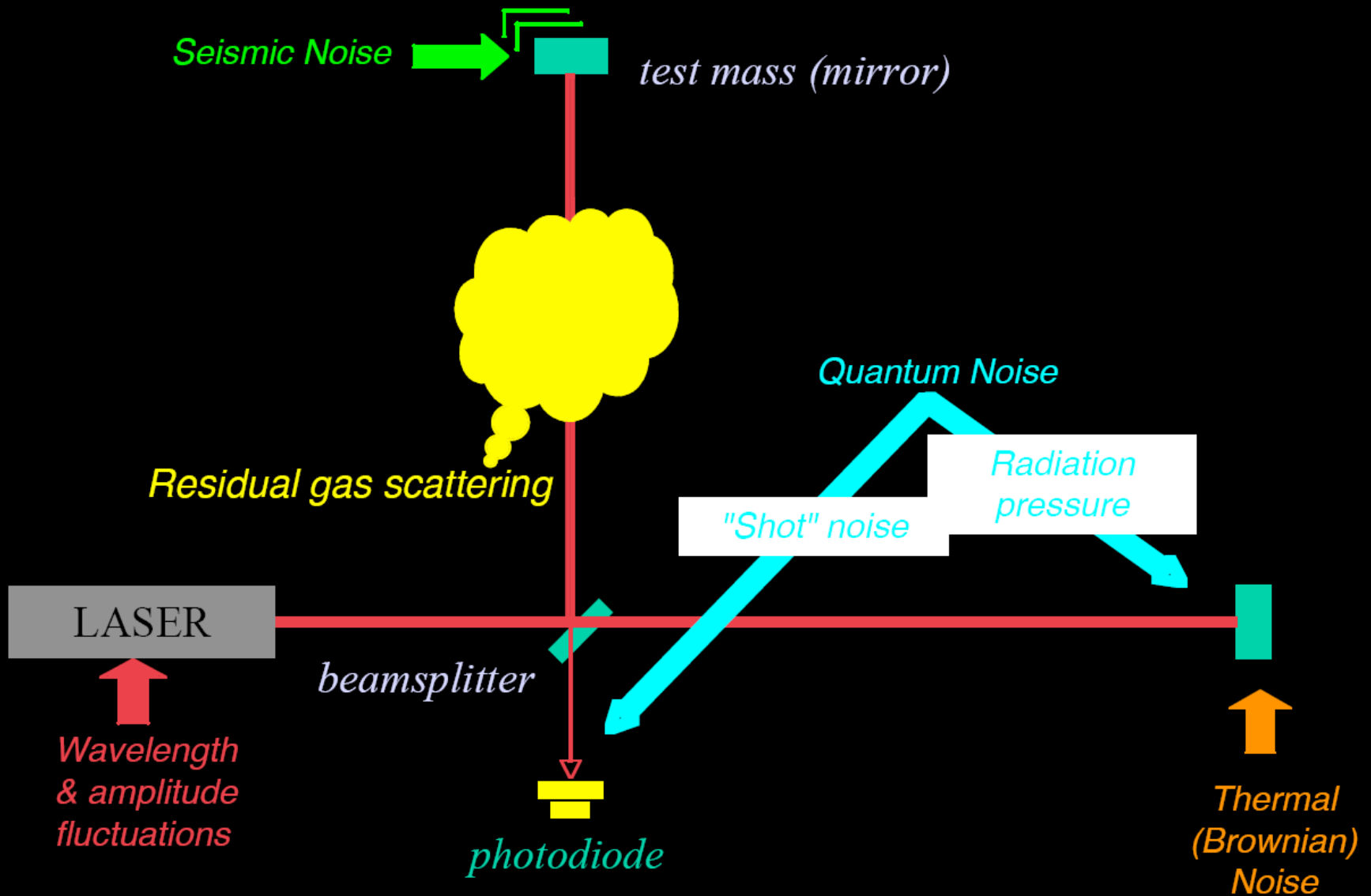
Pulsar timing

Space detectors

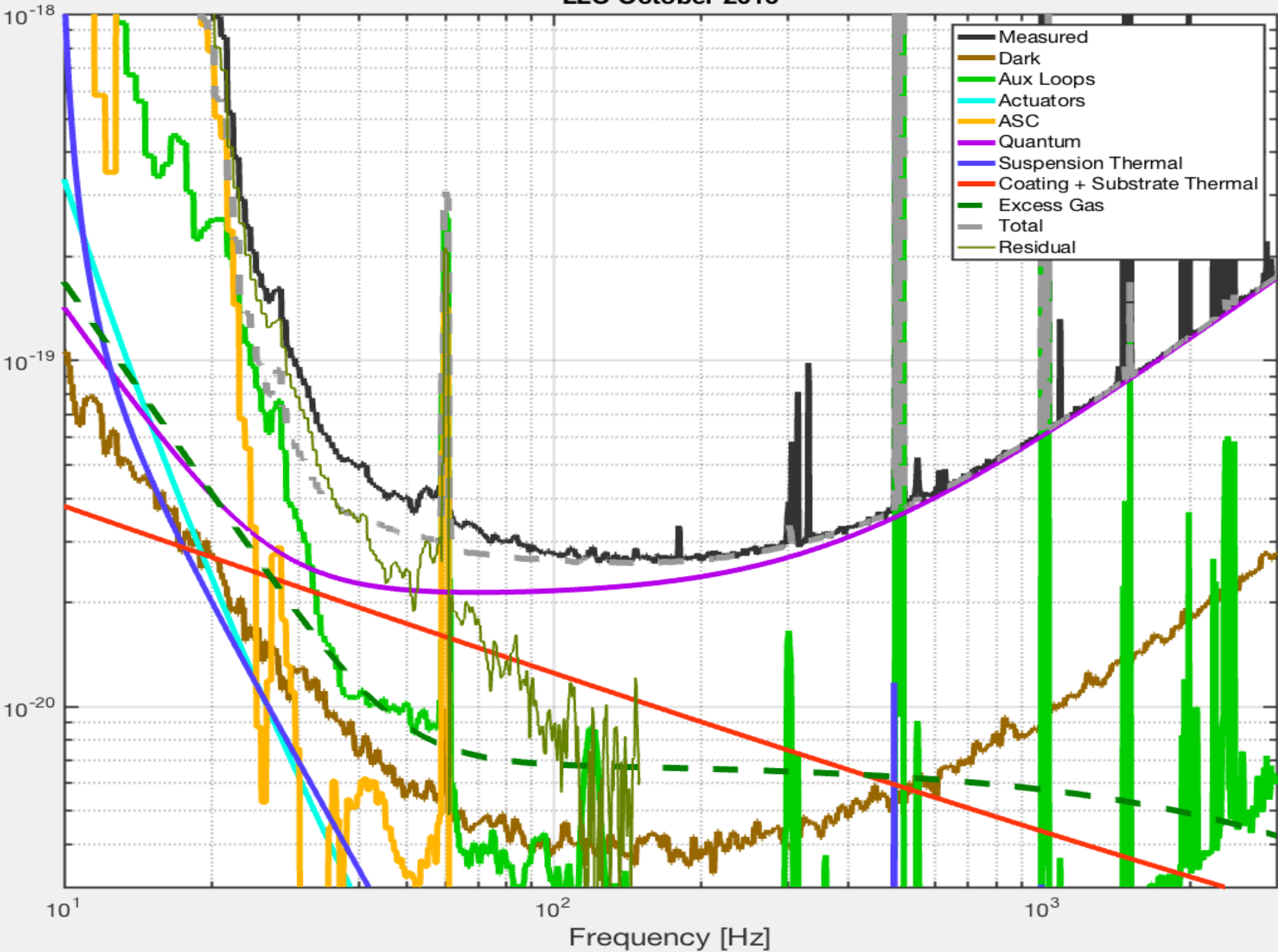
Ground interferometers

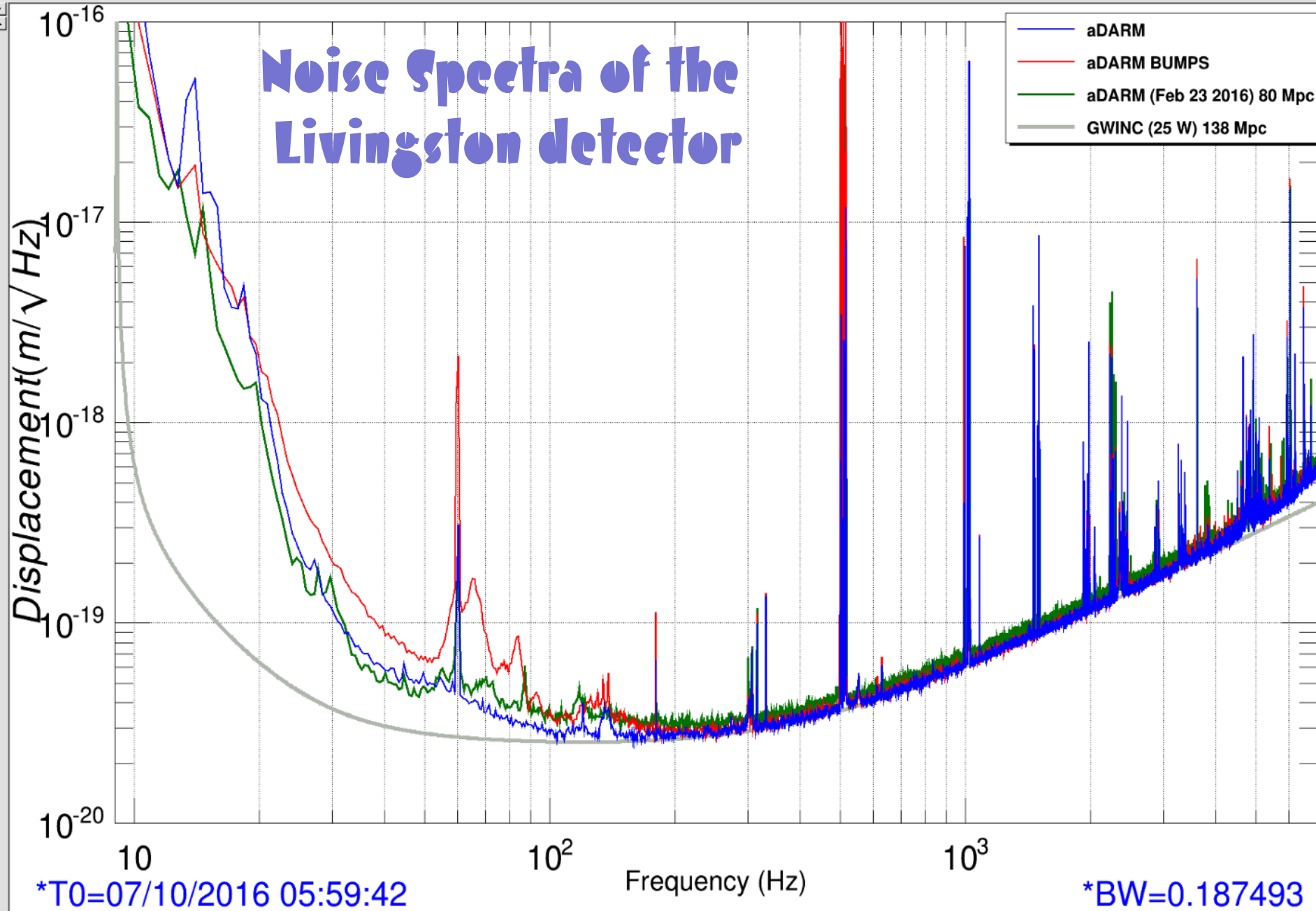


Noise Cartoon



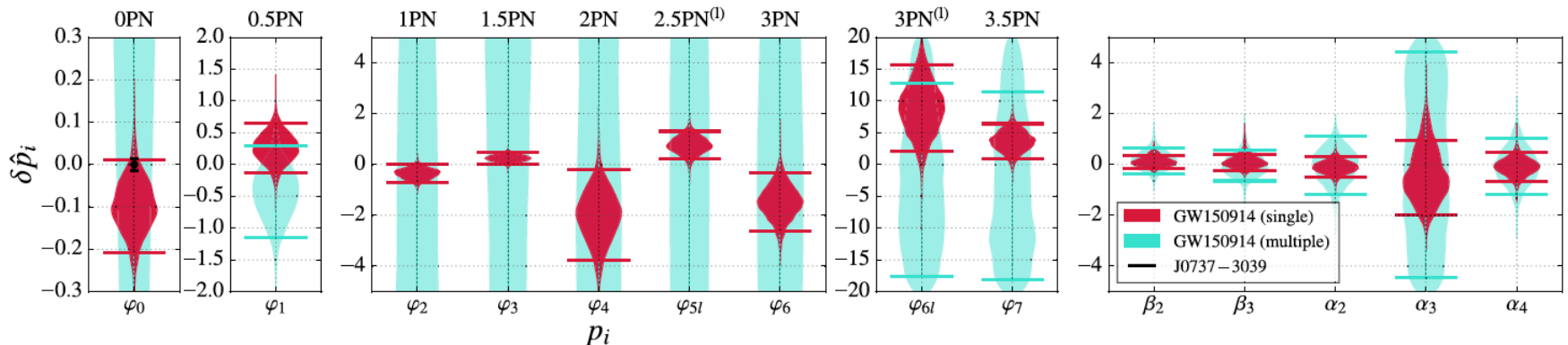
LLO October 2016





Tests of General Relativity based on GW150914

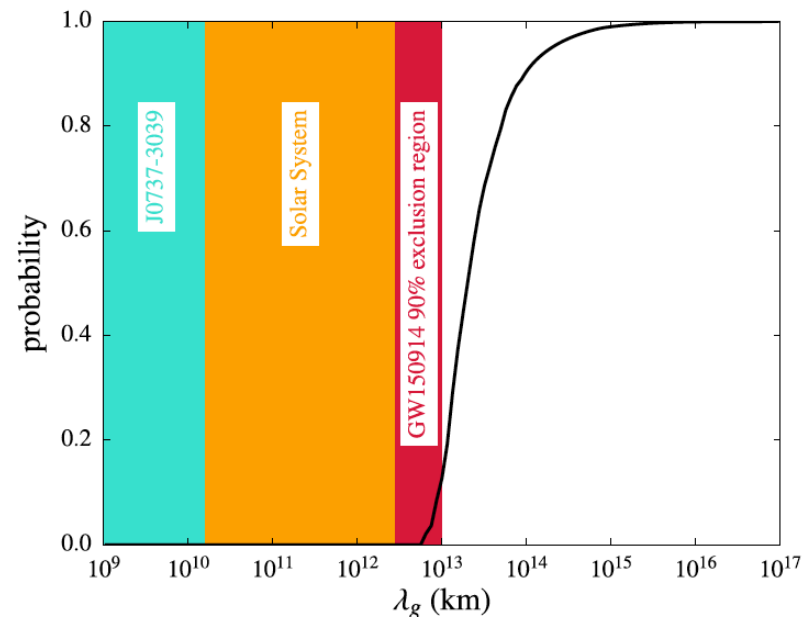
ding
2016



- Binary pulsar J0737-3039 results constrain only the 0PN term in a parameterized model of deviations from GR
- The dynamical evolution of the waveform through merger of GW150914 provides bounds on values to 3.5PN due to the dynamics of the merger
- Evolution of phase over time of the signal limits the amount of dispersion the signals suffered in propagating $\sim 1.2 \times 10^9$ years
 - Lower limit on graviton wavelength: $\lambda_g > 10^{13}$ km
 - Upper limit on graviton mass: $m_g \leq 1.2 \times 10^{-22}$ eV/c²

PRL 116, 221101 (2016)

PHYSICAL REVIEW



Parameter estimates for the 3 events

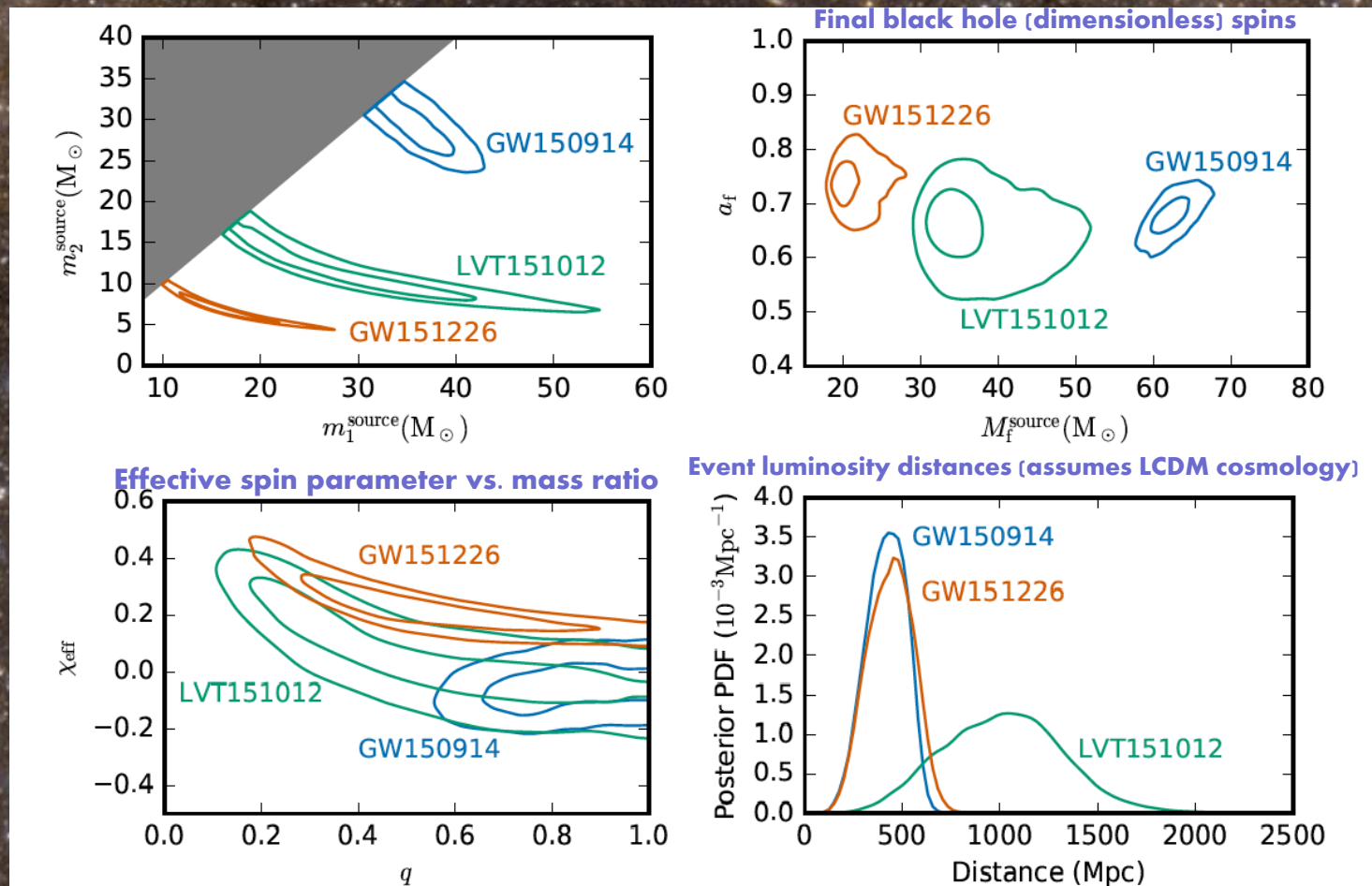
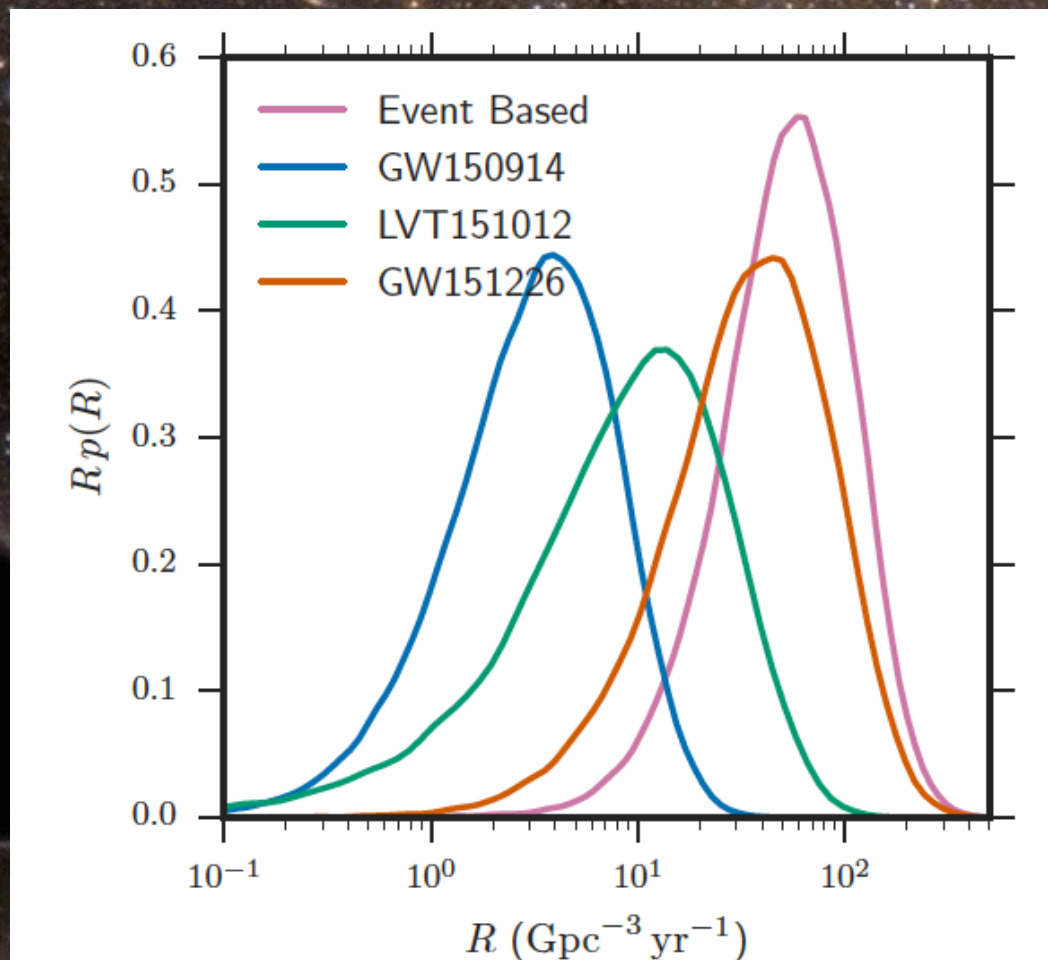


FIG. 4. Posterior probability densities of the masses, spins and distance to the three events GW150914, LVT151012 and GW151226. For the two dimensional distributions, the contours show 50% and 90% credible regions. *Top left*: component masses m_1^{source} and m_2^{source} for the three events. We use the convention that $m_1^{\text{source}} \geq m_2^{\text{source}}$, which produces the sharp cut in the two-dimensional distribution. For GW151226 and LVT151012, the contours follow lines of constant chirp mass ($\mathcal{M}^{\text{source}} = 8.9^{+0.3}_{-0.3} M_\odot$ and $\mathcal{M}^{\text{source}} = 15.1^{+1.4}_{-1.1} M_\odot$ respectively). In all three cases, both masses are consistent with being black holes. *Top right*: The mass and dimensionless spin magnitude of the final black holes. *Bottom left*: The effective spin and mass ratios of the binary components. *Bottom right*: The luminosity distance to the three events.

LIGO observations have bounded event rates for similar systems to those observed

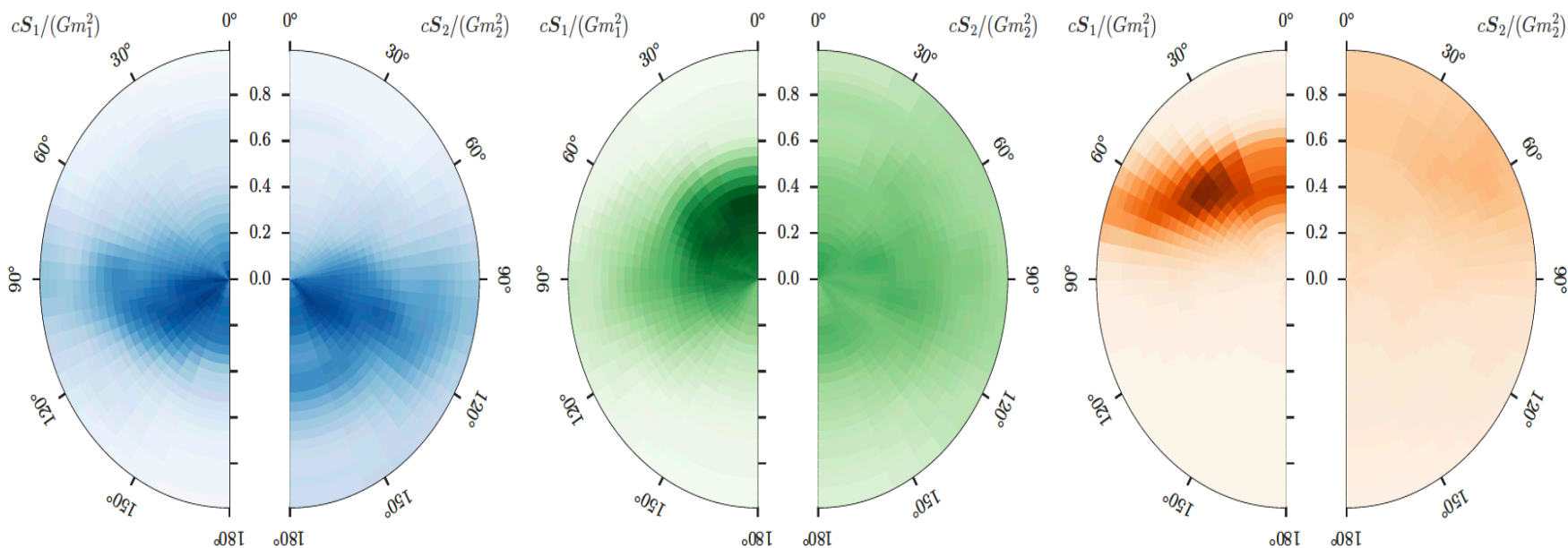
- Rates within previously estimated values prior to detection
- Rates exclude most pessimistic values



<https://arxiv.org/abs/1606.04856>

FIG. 9. The posterior density on the rate of GW150914-like BBH, LVT151012-like BBH, and GW151226-like BBH mergers. The event based rate is the sum of these. The median and 90% credible levels are given in Table II.

Observations cannot say much about spin at this time



<https://arxiv.org/abs/1606.04856>

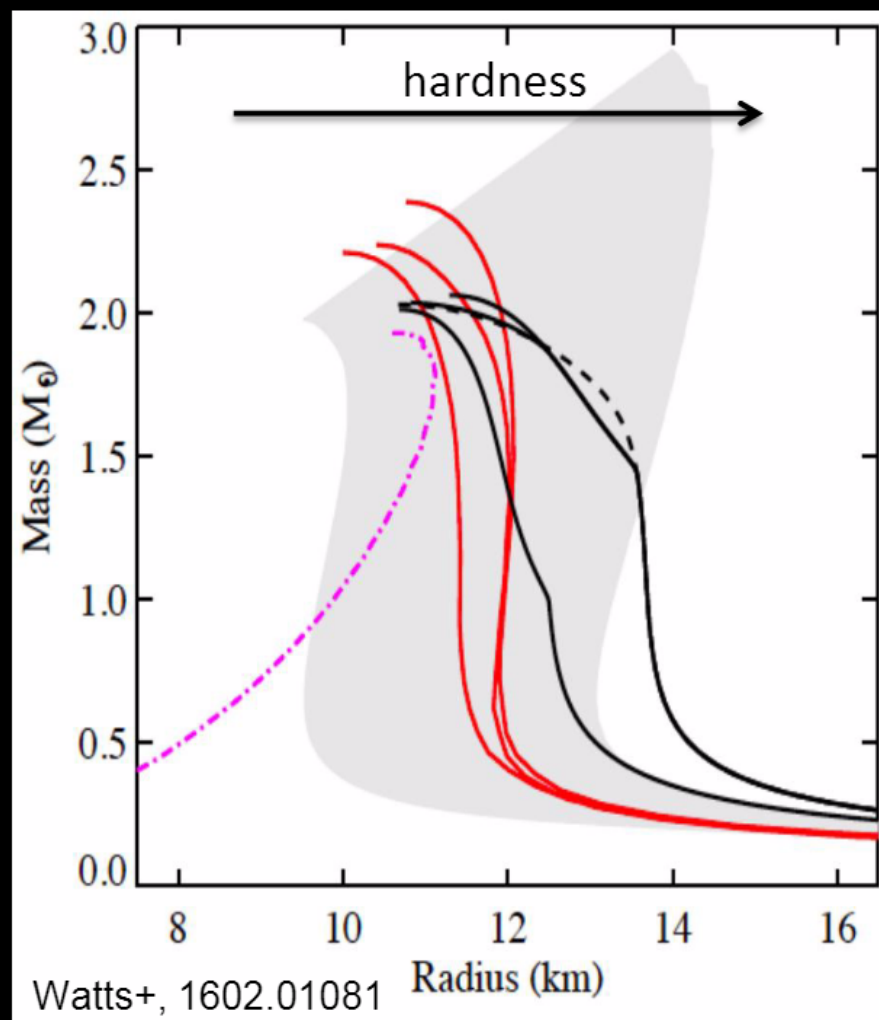
FIG. 5. Posterior probability distributions for for the dimensionless component spins $cS_1/(Gm_1^2)$ and $cS_2/(Gm_2^2)$ relative to the normal to the orbital plane L , marginalized over the azimuthal angles. The bins are constructed linearly in spin magnitude and the cosine of the tilt angles, and therefore have equal prior probability. The left plot shows the distribution for GW150914, the middle plot is for LVT151012 and the right plot is for GW151226.

TABLE IV. Parameters that characterise GW150914, GW151226 and LVT151012. For model parameters we report the median value with the range of the symmetric 90% credible interval [221]; we also quote selected 90% credible bounds. For the logarithm of the Bayes factor for a signal compared to Gaussian noise we report the mean and its 90% standard error from 4 parallel runs with a nested sampling algorithm [211], and for the deviance information criterion we report the mean and its 90% standard error from a Markov-chain Monte Carlo and a nested sampling run. The source redshift and source-frame masses assume standard cosmology [40]. Results are given for spin-aligned EOBNR and precessing IMRPhenom waveform models. The Overall results are computed by averaging the posteriors for the two models. For the Overall results we quote both the 90% credible interval or bound and an estimate for the 90% range of systematic error on this determined from the variance between waveform models. Further explanation of the parameters are given in [38].

	GW150914			GW151226			LVT151012		
	EOBNR	IMRPhenom	Overall	EOBNR	IMRPhenom	Overall	EOBNR	IMRPhenom	Overall
Detector frame									
Total mass M/M_{\odot}	71.0 $^{+4.6}_{-4.0}$	71.2 $^{+3.5}_{-3.2}$	71.1 $^{+4.1\pm 0.7}_{-3.6\pm 0.8}$	23.6 $^{+8.0}_{-1.3}$	23.8 $^{+5.1}_{-1.5}$	23.7 $^{+6.5\pm 2.2}_{-1.4\pm 0.1}$	45 $^{+17}_{-4}$	44 $^{+12}_{-3}$	44 $^{+16\pm 5}_{-3\pm 0}$
Chirp mass \mathcal{M}/M_{\odot}	30.4 $^{+2.3}_{-1.6}$	30.7 $^{+1.5}_{-1.5}$	30.6 $^{+1.9\pm 0.3}_{-1.6\pm 0.4}$	9.71 $^{+0.08}_{-0.07}$	9.72 $^{+0.06}_{-0.06}$	9.72 $^{+0.07\pm 0.01}_{-0.06\pm 0.01}$	18.1 $^{+1.3}_{-0.9}$	18.1 $^{+0.8}_{-0.8}$	18.1 $^{+1.0\pm 0.5}_{-0.8\pm 0.1}$
Primary mass m_1/M_{\odot}	40.2 $^{+5.2}_{-4.8}$	38.5 $^{+5.4}_{-3.3}$	39.4 $^{+5.4\pm 1.3}_{-4.1\pm 0.2}$	15.3 $^{+10.8}_{-3.8}$	15.8 $^{+7.2}_{-4.0}$	15.6 $^{+9.0\pm 2.6}_{-4.0\pm 0.2}$	29 $^{+23}_{-8}$	27 $^{+19}_{-6}$	28 $^{+21\pm 5}_{-7\pm 0}$
Secondary mass m_2/M_{\odot}	30.6 $^{+5.1}_{-4.2}$	32.7 $^{+3.1}_{-4.9}$	31.7 $^{+4.0\pm 0.1}_{-4.9\pm 1.2}$	8.3 $^{+5.1}_{-2.9}$	8.1 $^{+2.0}_{-2.1}$	8.2 $^{+2.6\pm 0.2}_{-2.5\pm 0.5}$	15 $^{+5}_{-6}$	16 $^{+4}_{-6}$	16 $^{+5\pm 0}_{-6\pm 1}$
Final mass M_f/M_{\odot}	67.8 $^{+4.0}_{-3.6}$	67.9 $^{+3.2}_{-2.9}$	67.8 $^{+3.7\pm 0.6}_{-3.3\pm 0.7}$	22.5 $^{+8.2}_{-1.4}$	22.8 $^{+5.3}_{-1.6}$	22.6 $^{+6.7\pm 2.2}_{-1.5\pm 0.1}$	43 $^{+17}_{-4}$	42 $^{+13}_{-2}$	42 $^{+16\pm 5}_{-3\pm 0}$
Source frame									
Total mass $M^{\text{source}}/M_{\odot}$	65.5 $^{+4.4}_{-3.9}$	65.1 $^{+3.6}_{-3.1}$	65.3 $^{+4.1\pm 1.0}_{-3.4\pm 0.3}$	21.6 $^{+7.4}_{-1.6}$	21.9 $^{+4.7}_{-1.7}$	21.8 $^{+5.9\pm 2.0}_{-1.7\pm 0.1}$	38 $^{+15}_{-5}$	37 $^{+11}_{-4}$	37 $^{+13\pm 4}_{-4\pm 0}$
Chirp mass $\mathcal{M}^{\text{source}}/M_{\odot}$	28.1 $^{+2.1}_{-1.6}$	28.1 $^{+1.6}_{-1.4}$	28.1 $^{+1.8\pm 0.4}_{-1.5\pm 0.2}$	8.87 $^{+0.35}_{-0.28}$	8.90 $^{+0.31}_{-0.27}$	8.88 $^{+0.33\pm 0.01}_{-0.28\pm 0.04}$	15.2 $^{+1.5}_{-1.1}$	15.0 $^{+1.3}_{-1.0}$	15.1 $^{+1.4\pm 0.3}_{-1.1\pm 0.0}$
Primary mass $m_1^{\text{source}}/M_{\odot}$	37.0 $^{+4.9}_{-4.4}$	35.3 $^{+5.1}_{-3.1}$	36.2 $^{+5.2\pm 1.4}_{-3.8\pm 0.4}$	14.0 $^{+10.0}_{-3.5}$	14.5 $^{+6.6}_{-3.7}$	14.2 $^{+8.3\pm 2.4}_{-3.7\pm 0.2}$	24 $^{+19}_{-7}$	23 $^{+16}_{-5}$	23 $^{+18\pm 5}_{-6\pm 0}$
Secondary mass $m_2^{\text{source}}/M_{\odot}$	28.3 $^{+4.6}_{-3.9}$	29.9 $^{+3.0}_{-4.5}$	29.1 $^{+3.7\pm 0.0}_{-4.4\pm 0.9}$	7.5 $^{+2.3}_{-2.6}$	7.4 $^{+2.3}_{-2.0}$	7.5 $^{+2.3\pm 0.2}_{-2.3\pm 0.4}$	13 $^{+4}_{-5}$	14 $^{+4}_{-5}$	13 $^{+4\pm 0}_{-5\pm 0}$
Final mass $M_f^{\text{source}}/M_{\odot}$	62.5 $^{+3.9}_{-3.5}$	62.1 $^{+3.3}_{-2.8}$	62.3 $^{+3.7\pm 0.9}_{-2.1\pm 0.3}$	20.6 $^{+7.6}_{-1.6}$	20.9 $^{+4.8}_{-1.8}$	20.8 $^{+6.1\pm 2.0}_{-1.7\pm 0.1}$	36 $^{+15}_{-4}$	35 $^{+11}_{-3}$	35 $^{+14\pm 4}_{-1\pm 0}$
Energy radiated $E_{\text{rad}}/(M_{\odot}c^2)$	2.98 $^{+0.55}_{-0.40}$	3.02 $^{+0.36}_{-0.36}$	3.00 $^{+0.47\pm 0.13}_{-0.39\pm 0.07}$	1.02 $^{+0.09}_{-0.24}$	0.99 $^{+0.11}_{-0.17}$	1.00 $^{+0.10\pm 0.01}_{-0.20\pm 0.03}$	1.48 $^{+0.39}_{-0.41}$	1.51 $^{+0.29}_{-0.44}$	1.50 $^{+0.33\pm 0.05}_{-0.43\pm 0.01}$
Mass ratio q	0.77 $^{+0.20}_{-0.18}$	0.85 $^{+0.13}_{-0.21}$	0.81 $^{+0.17\pm 0.02}_{-0.20\pm 0.04}$	0.54 $^{+0.40}_{-0.33}$	0.51 $^{+0.39}_{-0.25}$	0.52 $^{+0.40\pm 0.05}_{-0.29\pm 0.04}$	0.53 $^{+0.42}_{-0.34}$	0.60 $^{+0.35}_{-0.37}$	0.57 $^{+0.38\pm 0.01}_{-0.37\pm 0.04}$
Effective inspiral spin χ_{eff}	-0.08 $^{+0.17}_{-0.14}$	-0.05 $^{+0.11}_{-0.12}$	-0.06 $^{+0.14\pm 0.02}_{-0.14\pm 0.04}$	0.21 $^{+0.24}_{-0.11}$	0.22 $^{+0.15}_{-0.08}$	0.21 $^{+0.20\pm 0.07}_{-0.10\pm 0.03}$	0.06 $^{+0.31}_{-0.24}$	0.01 $^{+0.26}_{-0.17}$	0.03 $^{+0.31\pm 0.08}_{-0.20\pm 0.02}$
Primary spin magnitude a_1	0.33 $^{+0.39}_{-0.29}$	0.30 $^{+0.54}_{-0.27}$	0.32 $^{+0.47\pm 0.10}_{-0.29\pm 0.01}$	0.42 $^{+0.35}_{-0.37}$	0.55 $^{+0.35}_{-0.42}$	0.49 $^{+0.37\pm 0.11}_{-0.42\pm 0.07}$	0.31 $^{+0.46}_{-0.27}$	0.31 $^{+0.50}_{-0.28}$	0.31 $^{+0.48\pm 0.03}_{-0.28\pm 0.00}$
Secondary spin magnitude a_2	0.62 $^{+0.35}_{-0.54}$	0.36 $^{+0.53}_{-0.33}$	0.48 $^{+0.47\pm 0.08}_{-0.43\pm 0.03}$	0.51 $^{+0.44}_{-0.46}$	0.52 $^{+0.42}_{-0.47}$	0.52 $^{+0.43\pm 0.01}_{-0.47\pm 0.00}$	0.49 $^{+0.45}_{-0.44}$	0.42 $^{+0.50}_{-0.38}$	0.45 $^{+0.48\pm 0.02}_{-0.41\pm 0.01}$
Final spin a_f	0.68 $^{+0.05}_{-0.07}$	0.68 $^{+0.06}_{-0.05}$	0.68 $^{+0.05\pm 0.01}_{-0.06\pm 0.02}$	0.73 $^{+0.05}_{-0.06}$	0.75 $^{+0.07}_{-0.05}$	0.74 $^{+0.06\pm 0.03}_{-0.06\pm 0.03}$	0.65 $^{+0.09}_{-0.10}$	0.66 $^{+0.08}_{-0.10}$	0.66 $^{+0.09\pm 0.00}_{-0.10\pm 0.02}$
Luminosity distance D_L/Mpc	400 $^{+160}_{-180}$	440 $^{+140}_{-170}$	420 $^{+150\pm 20}_{-180\pm 40}$	450 $^{+180}_{-210}$	440 $^{+170}_{-180}$	440 $^{+180\pm 20}_{-190\pm 10}$	1000 $^{+540}_{-490}$	1030 $^{+480}_{-480}$	1020 $^{+500\pm 20}_{-490\pm 40}$
Source redshift z	0.086 $^{+0.031}_{-0.036}$	0.094 $^{+0.027}_{-0.034}$	0.090 $^{+0.029\pm 0.003}_{-0.036\pm 0.008}$	0.096 $^{+0.035}_{-0.042}$	0.092 $^{+0.033}_{-0.037}$	0.094 $^{+0.035\pm 0.004}_{-0.039\pm 0.001}$	0.198 $^{+0.091}_{-0.092}$	0.204 $^{+0.082}_{-0.088}$	0.201 $^{+0.086\pm 0.003}_{-0.091\pm 0.008}$
Upper bound									
Primary spin magnitude a_1	0.62	0.73	0.67 \pm 0.09	0.68	0.83	0.77 \pm 0.12	0.64	0.69	0.67 \pm 0.04
Secondary spin magnitude a_2	0.93	0.80	0.90 \pm 0.12	0.90	0.89	0.90 \pm 0.01	0.89	0.85	0.87 \pm 0.04
Lower bound									
Mass ratio q	0.62	0.68	0.65 \pm 0.05	0.25	0.30	0.28 \pm 0.04	0.22	0.28	0.24 \pm 0.05
Log Bayes factor $\ln \mathcal{B}_{s/n}$	287.7 \pm 0.1	289.8 \pm 0.3	—	59.5 \pm 0.1	60.2 \pm 0.2	—	22.8 \pm 0.2	23.0 \pm 0.1	—
Information criterion DIC	32977.2 \pm 0.3	32973.1 \pm 0.1	—	34296.4 \pm 0.2	34295.1 \pm 0.1	—	94695.8 \pm 0.0	94692.9 \pm 0.0	—

Neutron Star Equation of State

- Neutron stars host the highest densities in the (visible) universe
- Measuring their equation of state requires joint measurement of radius and mass
- Possible with EM, but challenging
 - Mass estimates not always reliable
 - Radius estimates non often available and not always reliable
 - NICER to launch 2016, 5% precision



Neutron Star Equation of State

- In a CBC, each NS will feel the tidal field of the companion, which induces a quadrupole moment

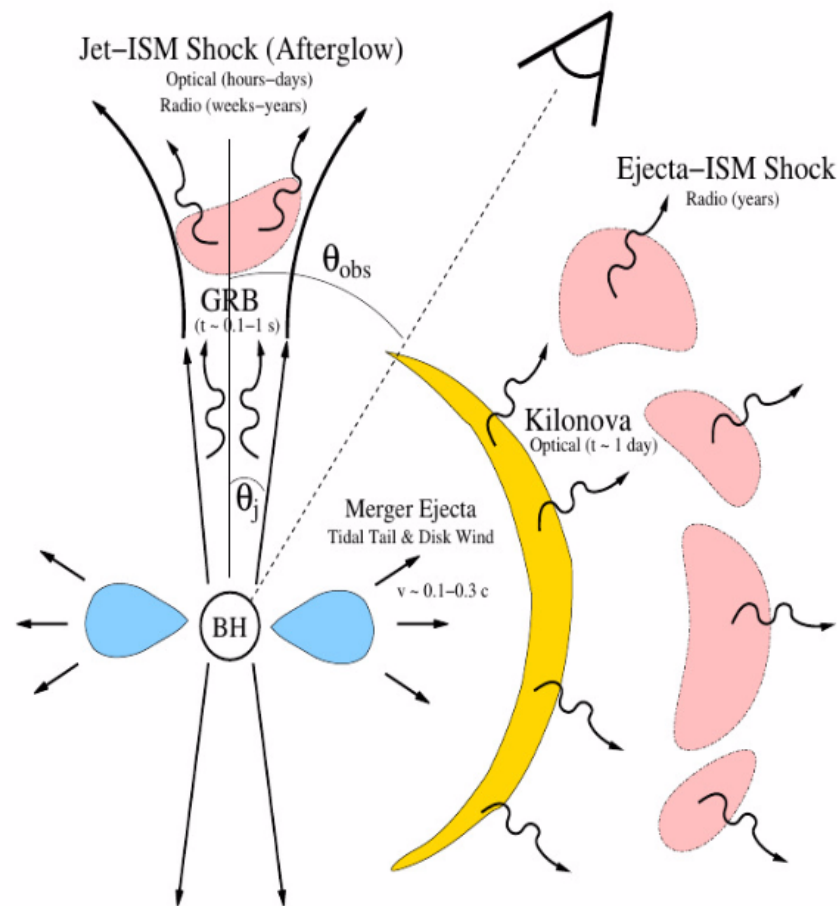
$$Q_{ij} = - \lambda(EOS, m) T_{ij}$$

- Known leading and next-to-leading effects on GW phasing
- Early studies considered single events, with contradictory findings (Read+ PRD 79 124033; Hinderer+ PRD 81 123016, many others)
- Markakis+ JPCS 189 012024 considered multiple events but used Fisher matrix, unreliable at low signal-to-noise ratios (Vallisneri PRD 77 042001, Vitale+ PRD 84 104020)
- First fully Bayesian approach in 2013 (Del Pozzo+ PRL 11 071110)
- Also see Wade+, and many more.

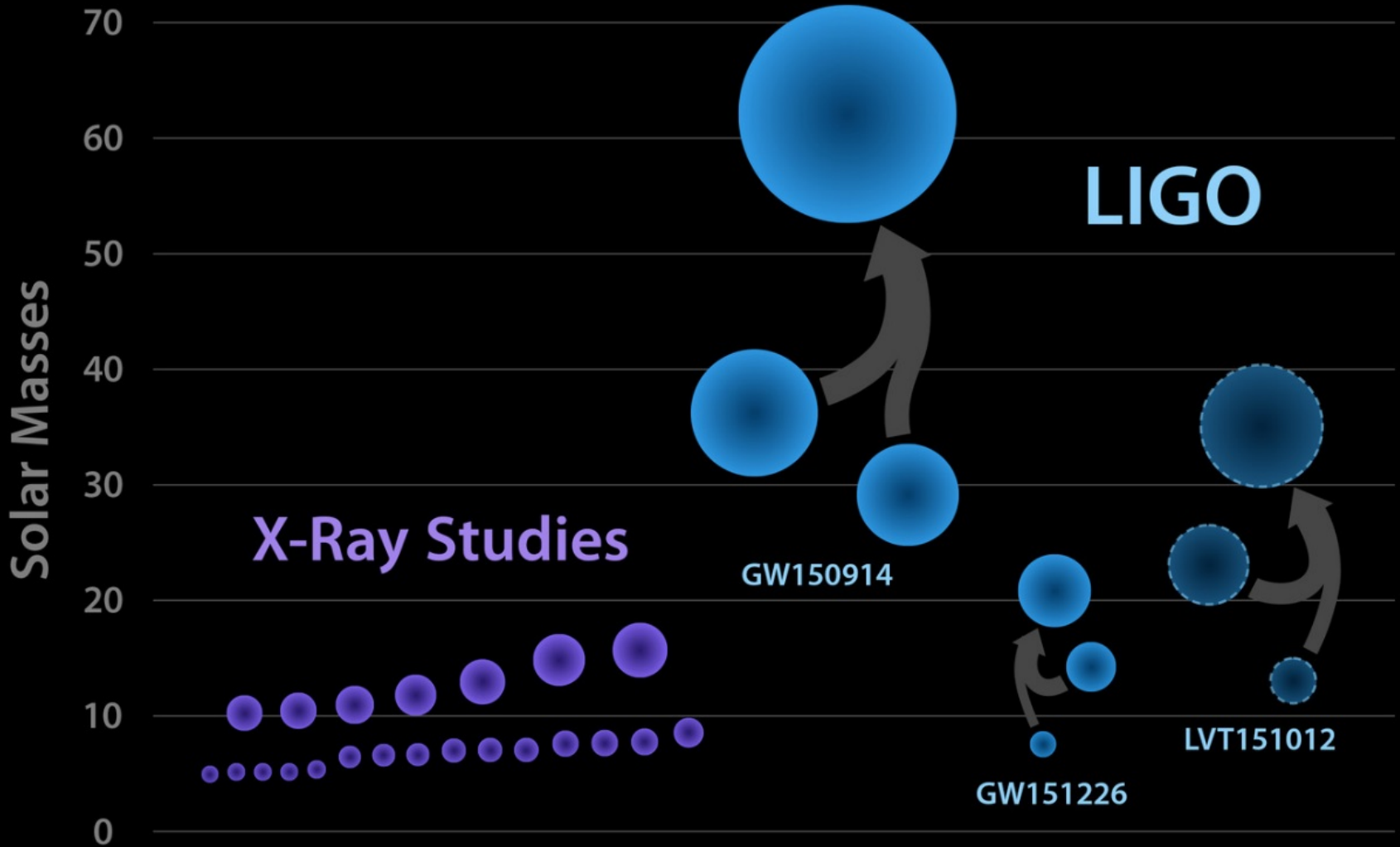
GW – Electromagnetic connection

- CBC containing neutron stars are expected to be bright in the EM band
 - Progenitors of short GRBs?
 - Rich variety of frequencies and timescales
- Core collapse supernovae are believed to power long GRBs
- And are BBH luminous??

Metzger, Berger



Black Holes of Known Mass



CBC and their formation channels

- Measuring masses and spins can help determine channel and environment in which BH and CBC are formed
- Two main formation channels
 - Common envelope evolution
 - Galactic fields
 - Final masses not too different
 - Aligned spins
 - Dynamical capture
 - Globular clusters
 - Any mass ratio (?)
 - Misaligned spins

Cosmography with GWs

- Gravitational waves provide direct measurement of *luminosity distance*
- **If** the *redshift* of the source can be estimated in some other way one can measure cosmological parameters.

$$D_L(z) = \begin{cases} \frac{(1+z)}{\sqrt{\Omega_k}} \sinh\left[\sqrt{\Omega_k} \int_0^z \frac{dz'}{H(z')}\right] & \text{for } \Omega_k > 0 \\ (1+z) \int_0^z \frac{dz'}{H(z')} & \text{for } \Omega_k = 0 \\ \frac{(1+z)}{\sqrt{|\Omega_k|}} \sin\left[\sqrt{|\Omega_k|} \int_0^z \frac{dz'}{H(z')}\right] & \text{for } \Omega_k < 0 \end{cases}$$

$$H(z) = H_0 \sqrt{\Omega_m (1+z)^3 + \Omega_k (1+z)^2 + \Omega_\Lambda E(z, w(z))}$$

Gravitational Waves propagate through space



SIMULATION OF THE BINARY BLACK-HOLE COALESCENCE GW150914



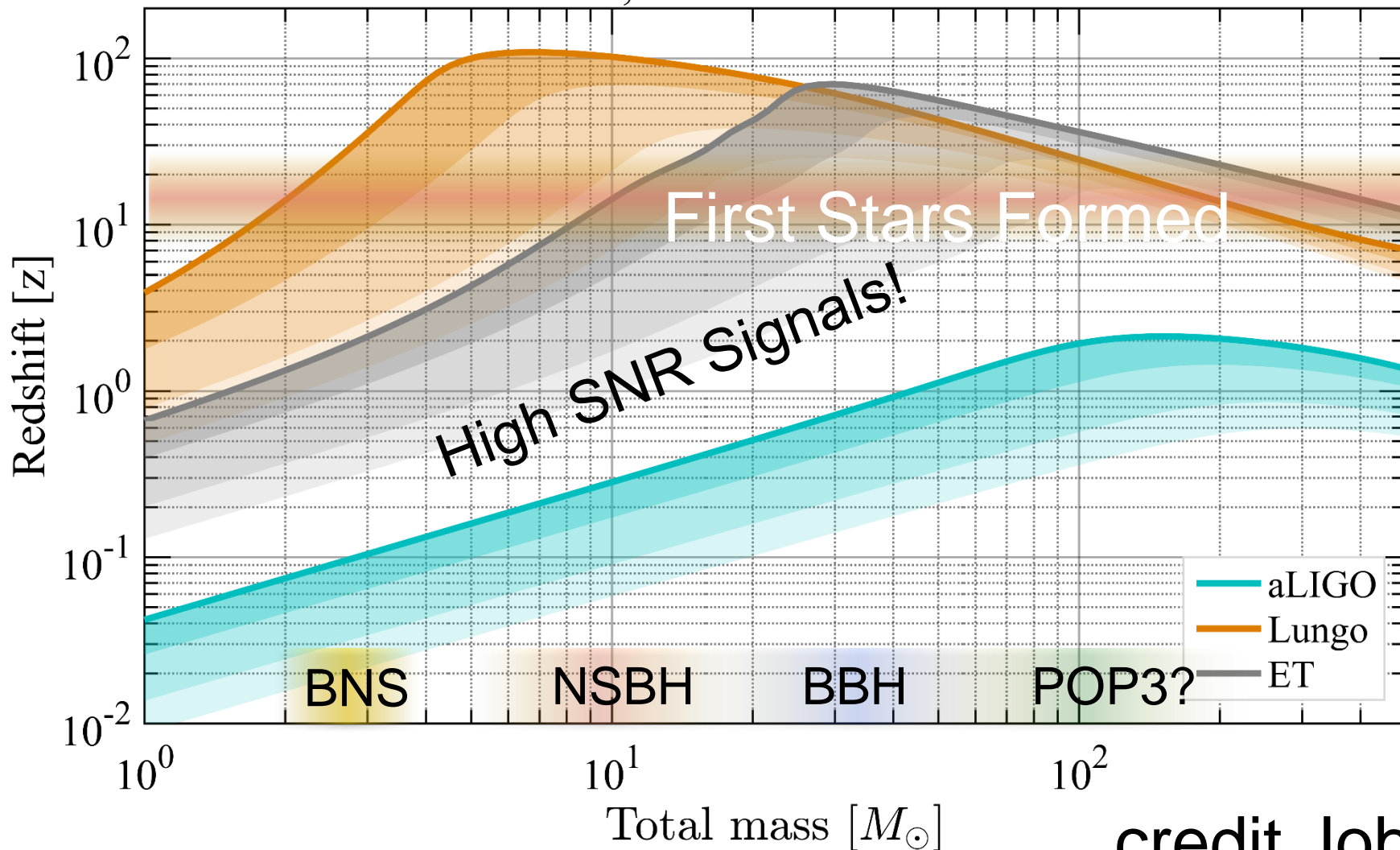
SIMULATION OF THE BINARY BLACK-HOLE COALESCENCE GW151226





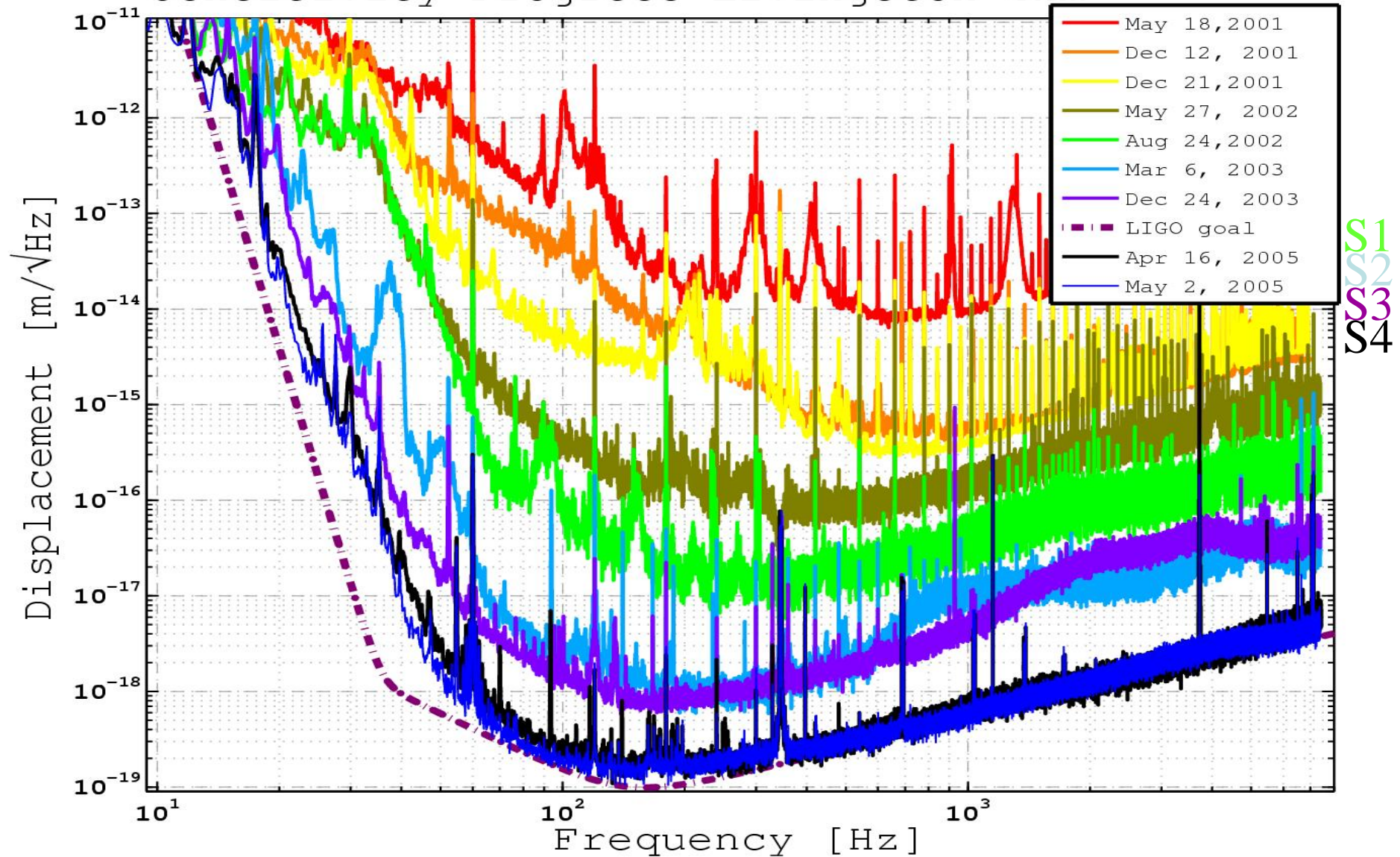
Black Holes Everywhere

Horizon and 10, 50 and 75 % confidence levels

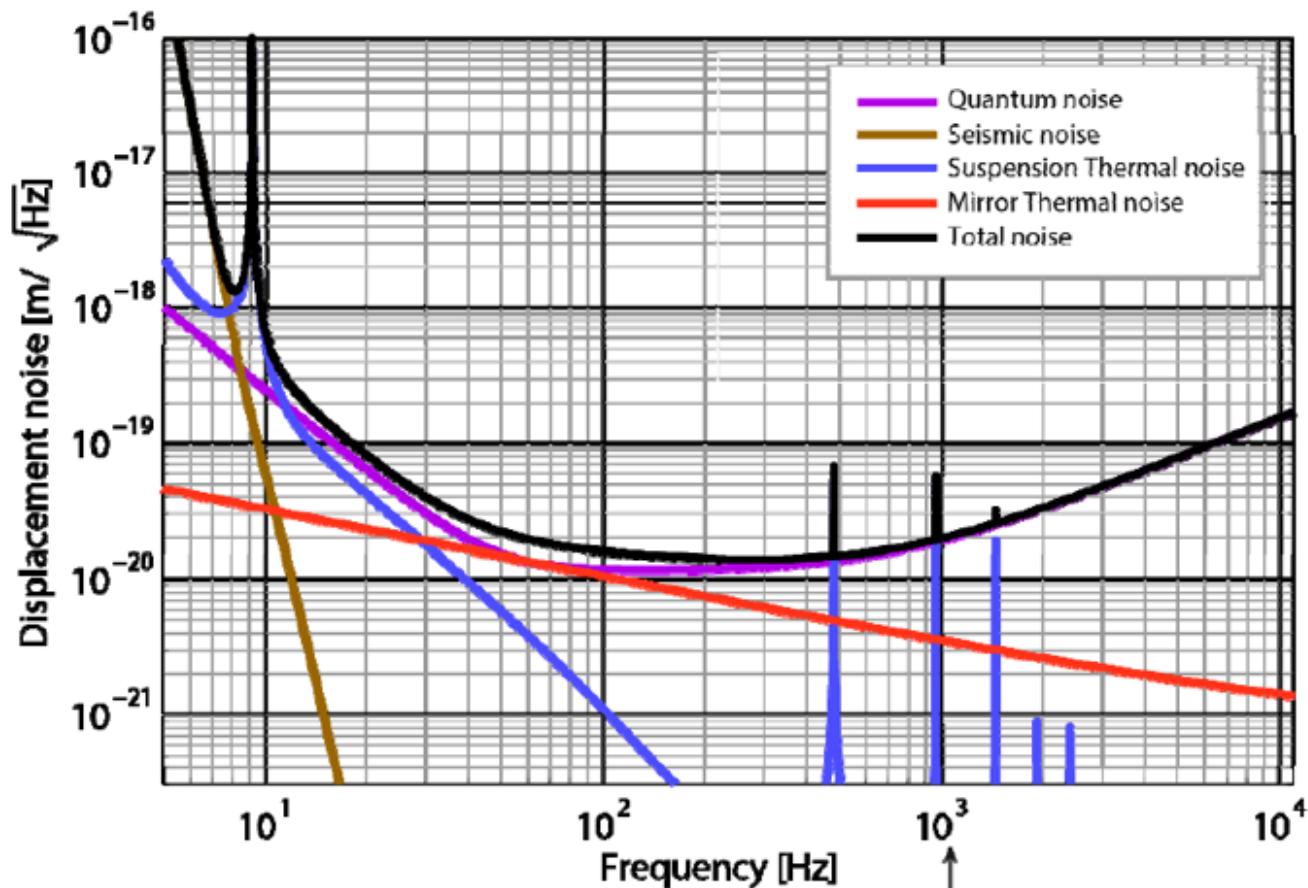
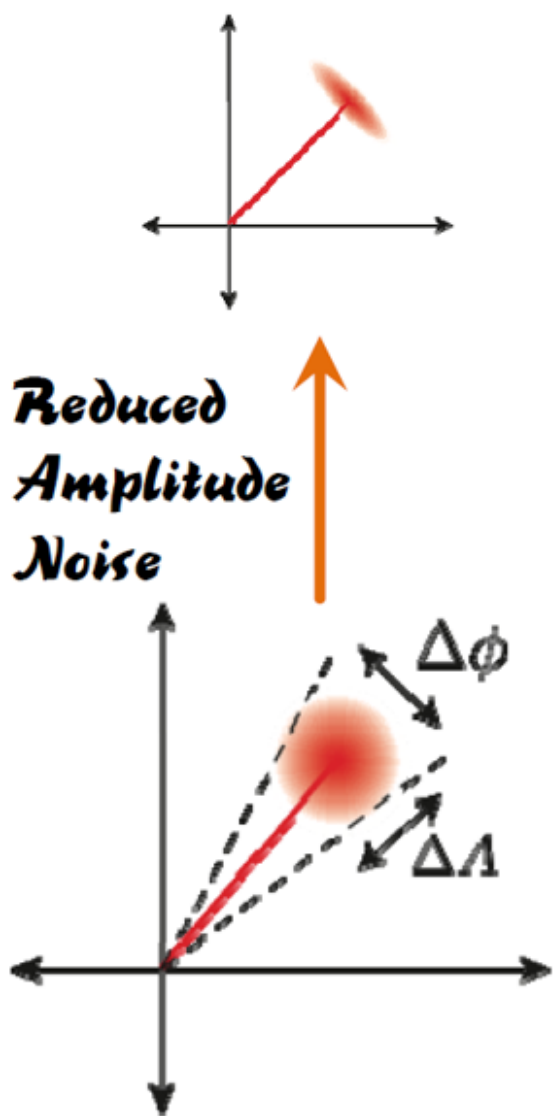


Early Noise Progression Livingston 4km

Sensitivity Progress Livingston 4km

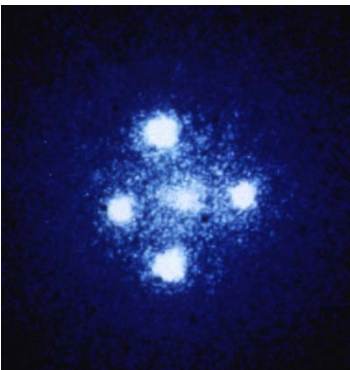
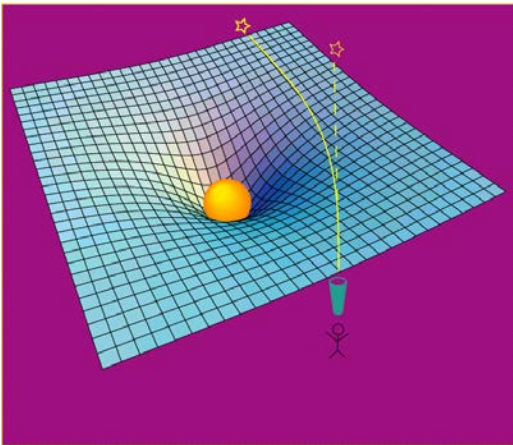


How to Beat the Quantum Limit



Observed Effects of Gravity's Distortion of Space

Gravitational Lensing – light bends around massive object



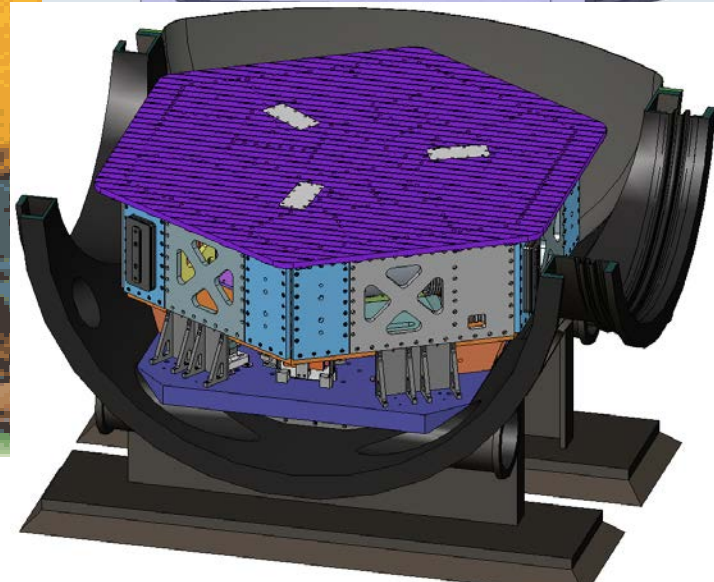
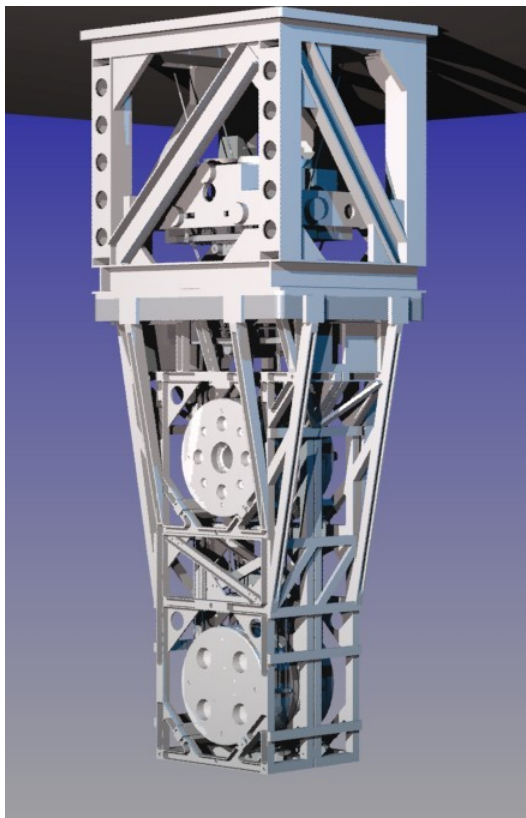
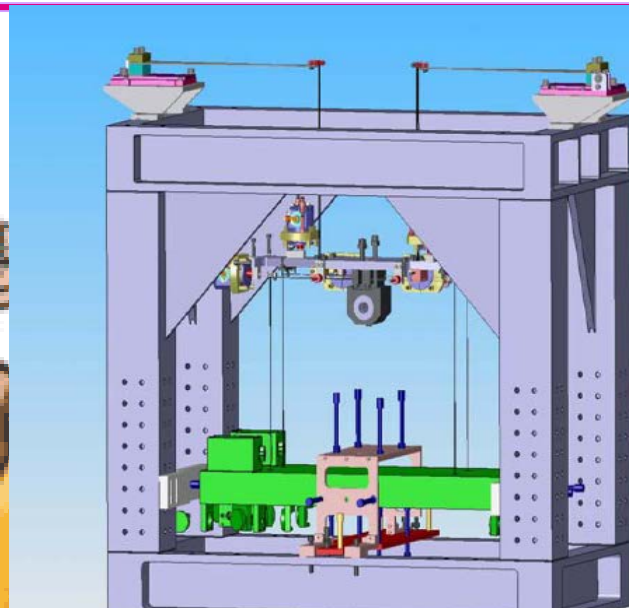
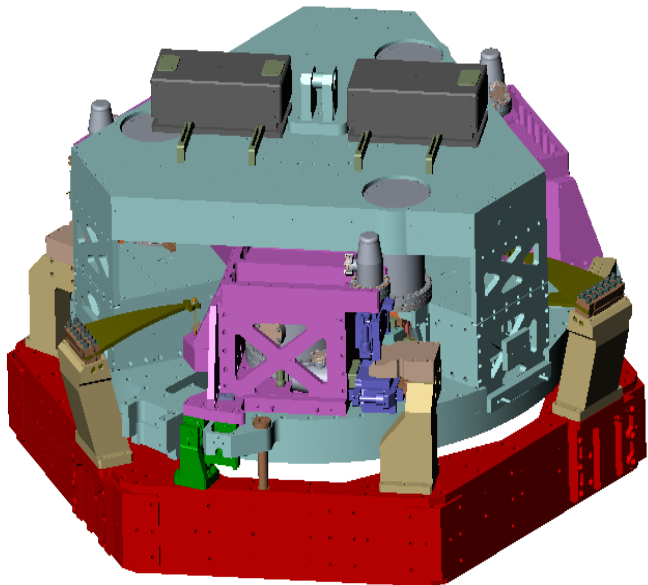
 J073728.45+321618.5	 J095629.77+510006.6	 J120540.43+491029.3	 J125028.25+052349.0
 J140228.21+632133.5	 J162746.44-005357.5	 J163028.15+452036.2	 J232120.93-093910.2

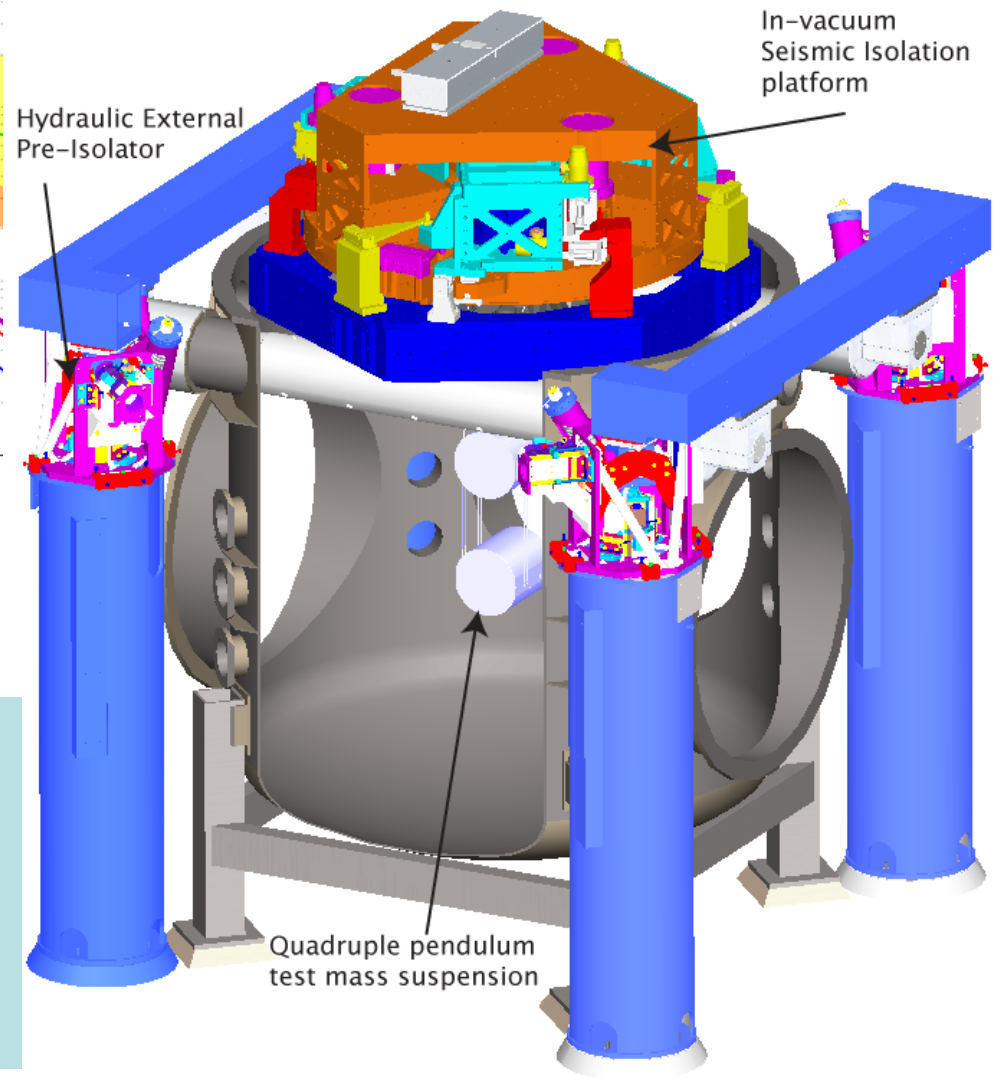
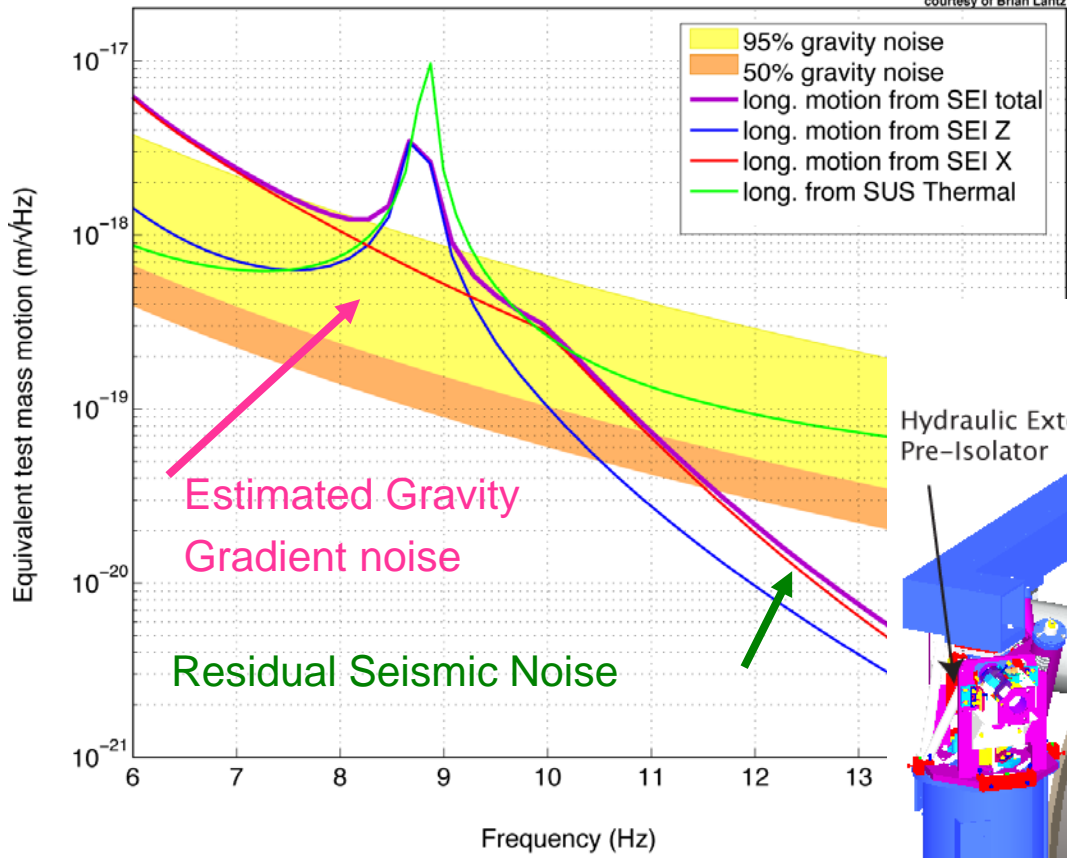
Einstein Ring Gravitational Lenses
Hubble Space Telescope • Advanced Camera for Surveys

NASA, ESA, A. Bolton (Harvard-Smithsonian CfA), and the SLACS Team STScI-PRC05-32

“Einstein’s Cross” – quasar’s light bends around a galaxy.

Seismic Noise





Advance Ligo Seismic Isolation is designed so as not to be a limiting noise source

Quad Suspensions

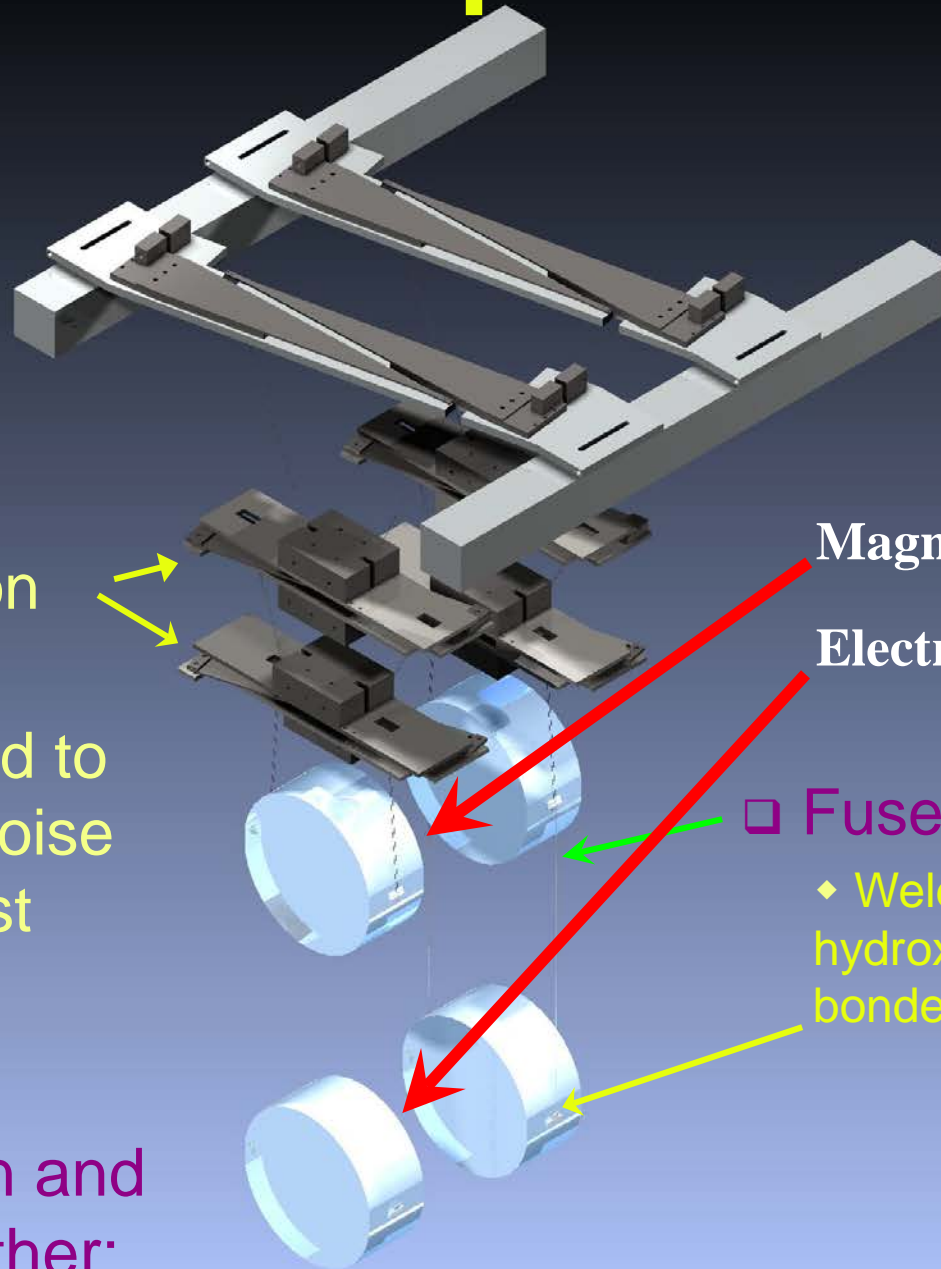
- Quadruple pendulum:

- $\sim 10^7$ attenuation @ 10 Hz

- Controls applied to upper layers; noise filtered from test masses

- Seismic isolation and suspension together:

- 10^{-10} g / Hz^{1/2} @ 10 Hz



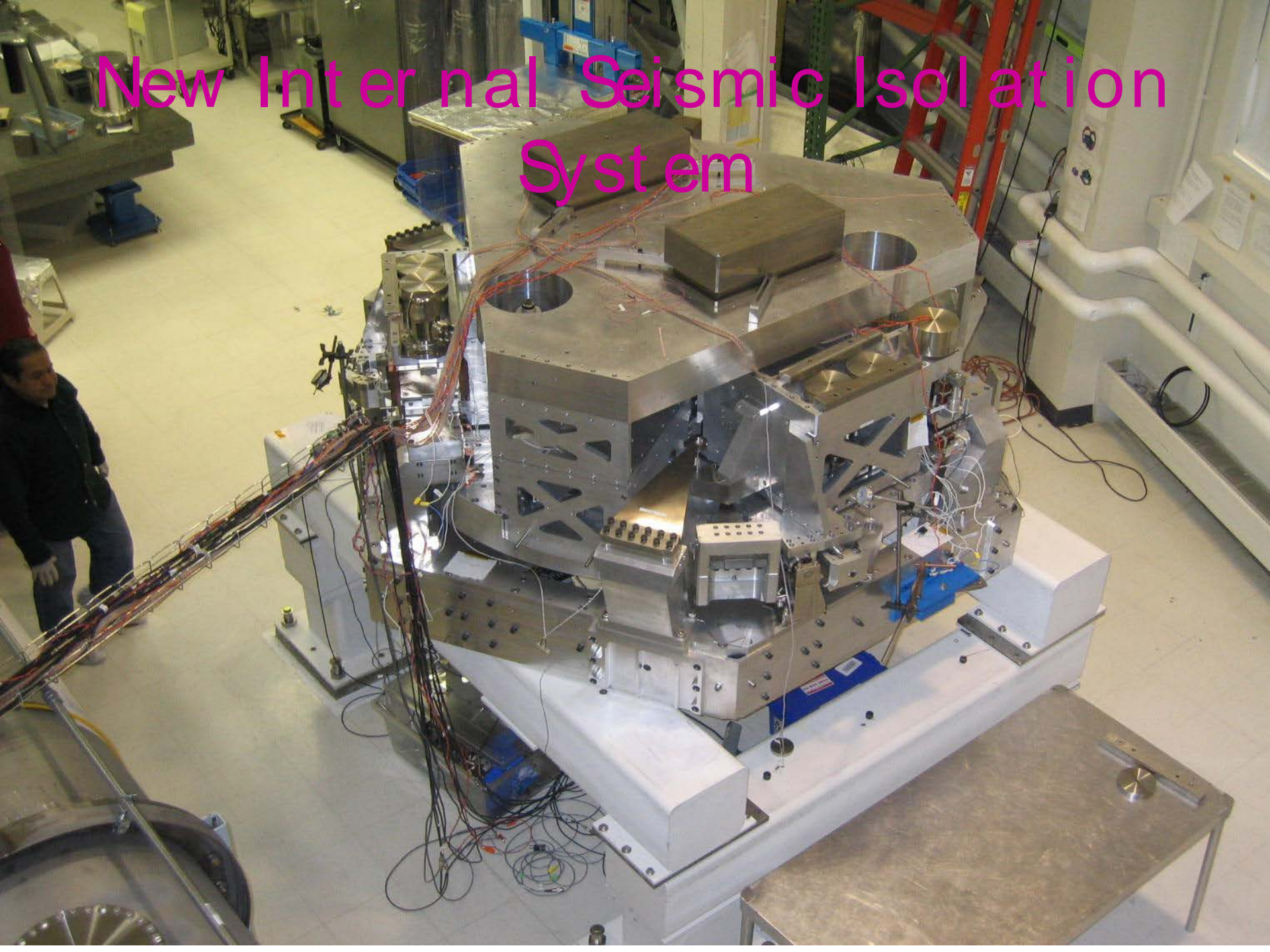
Magnets

Electrostatic

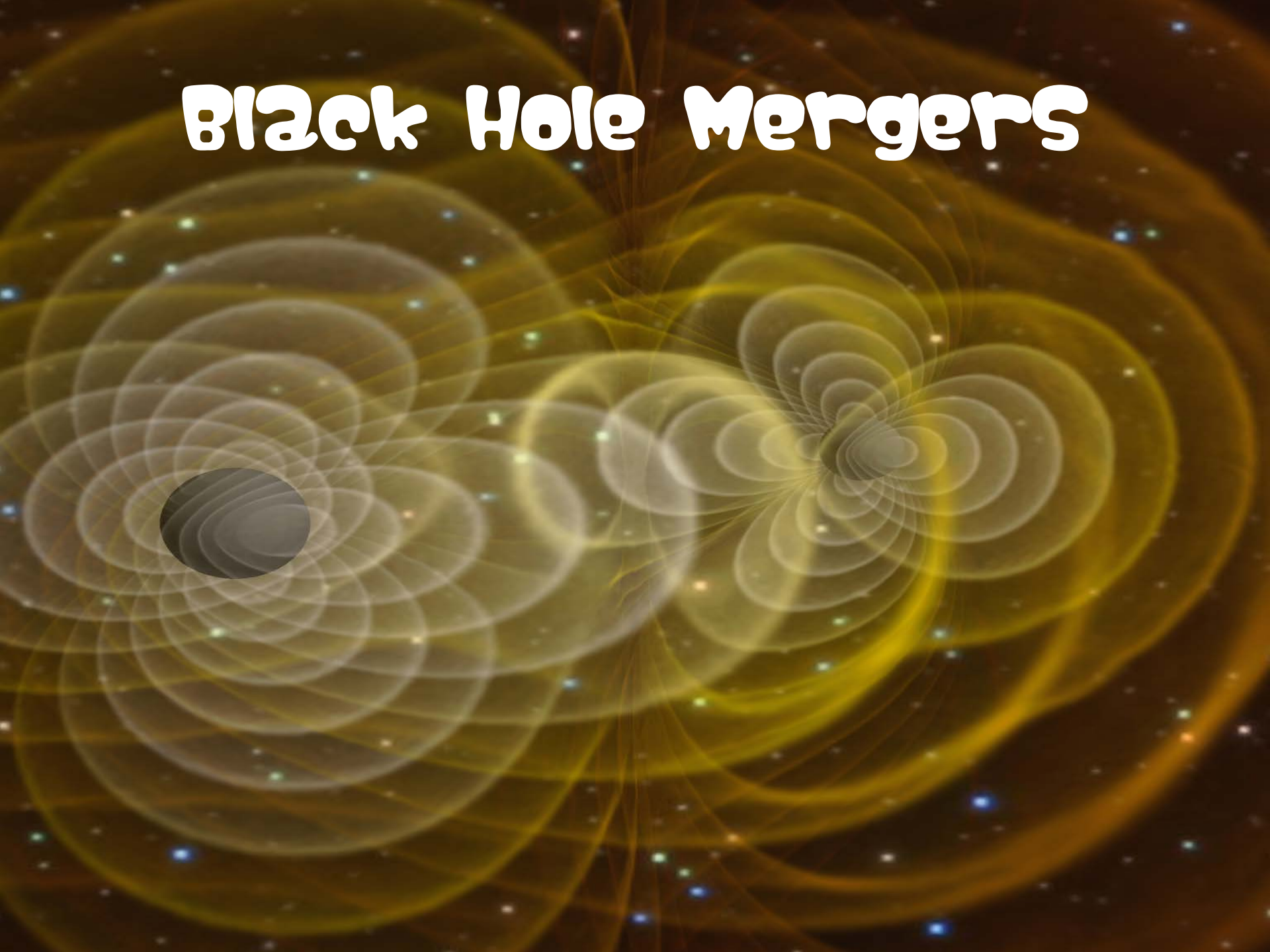
□ Fused silica fiber

- ◆ Welded to 'ears', hydroxy-catalysis bonded to optic

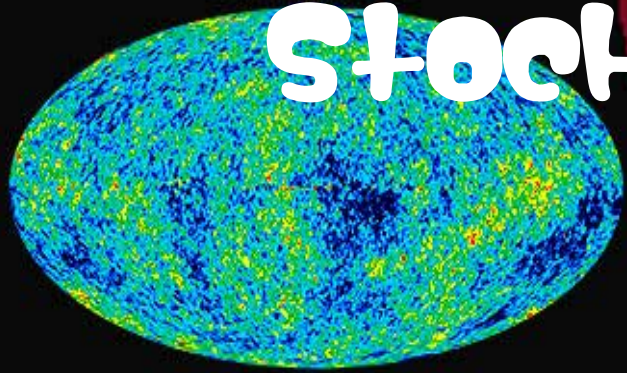
New Internal Seismic Isolation System



Black Hole Mergers



Stochastic Waves



(a)



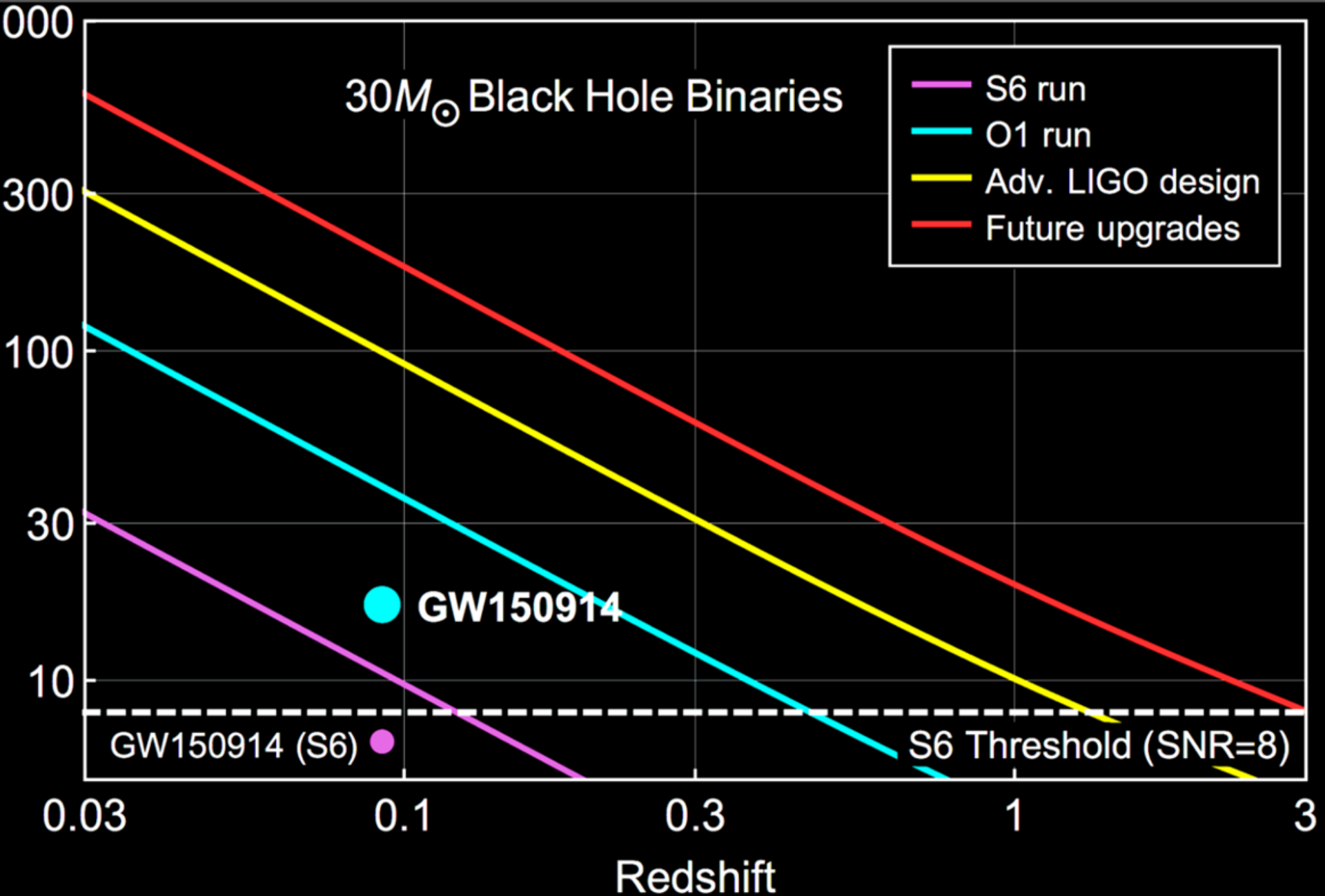
(b)

Σ

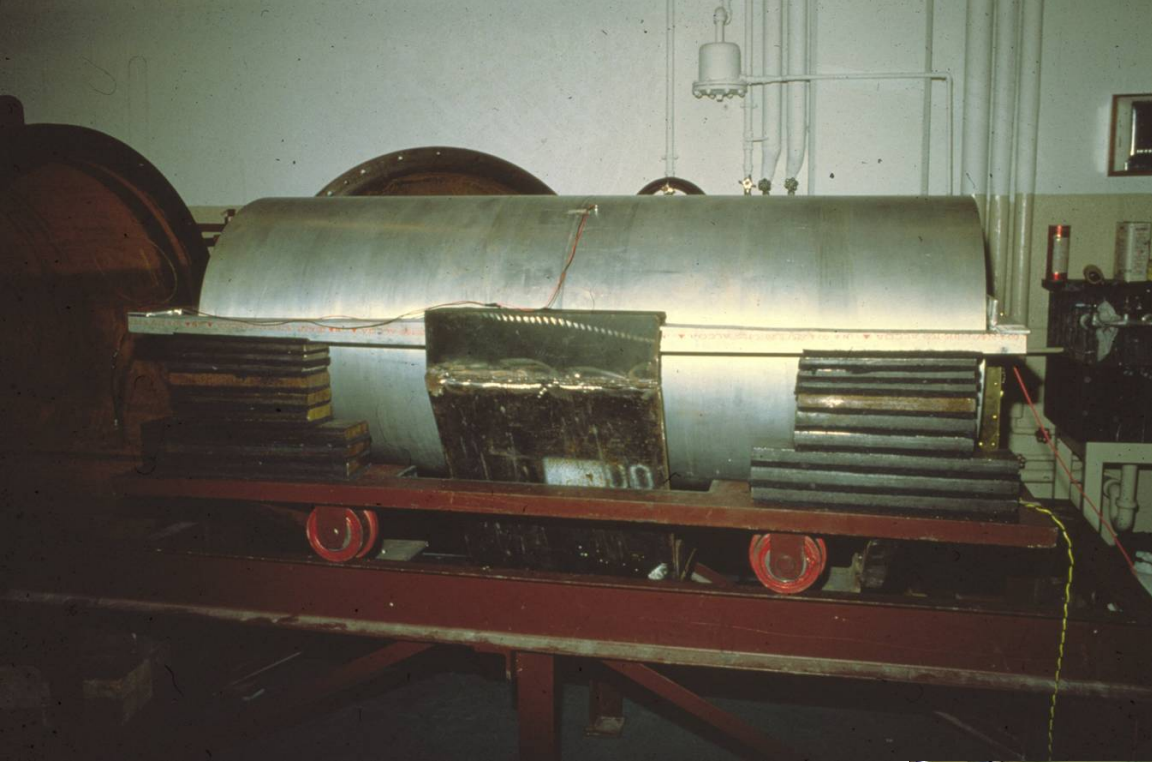
α



(c)



Bar Detectors



Vacuum tube enclosures test



Advanced Ligo

