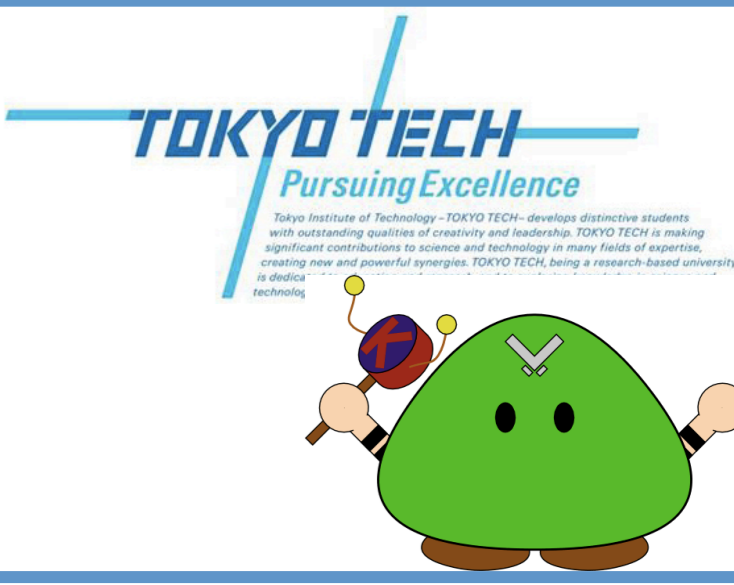


# Parametric amplification for a stiff optical spring

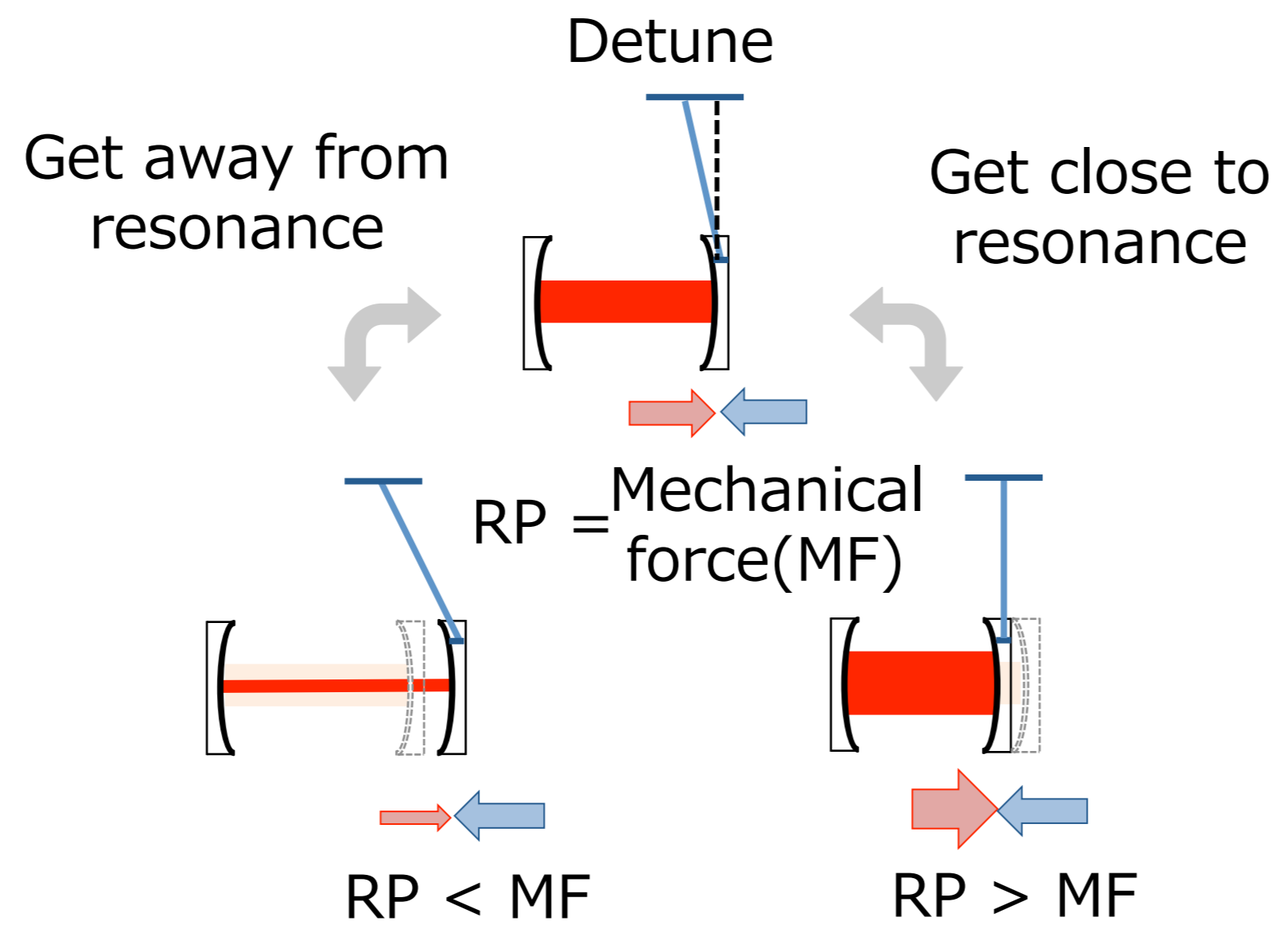
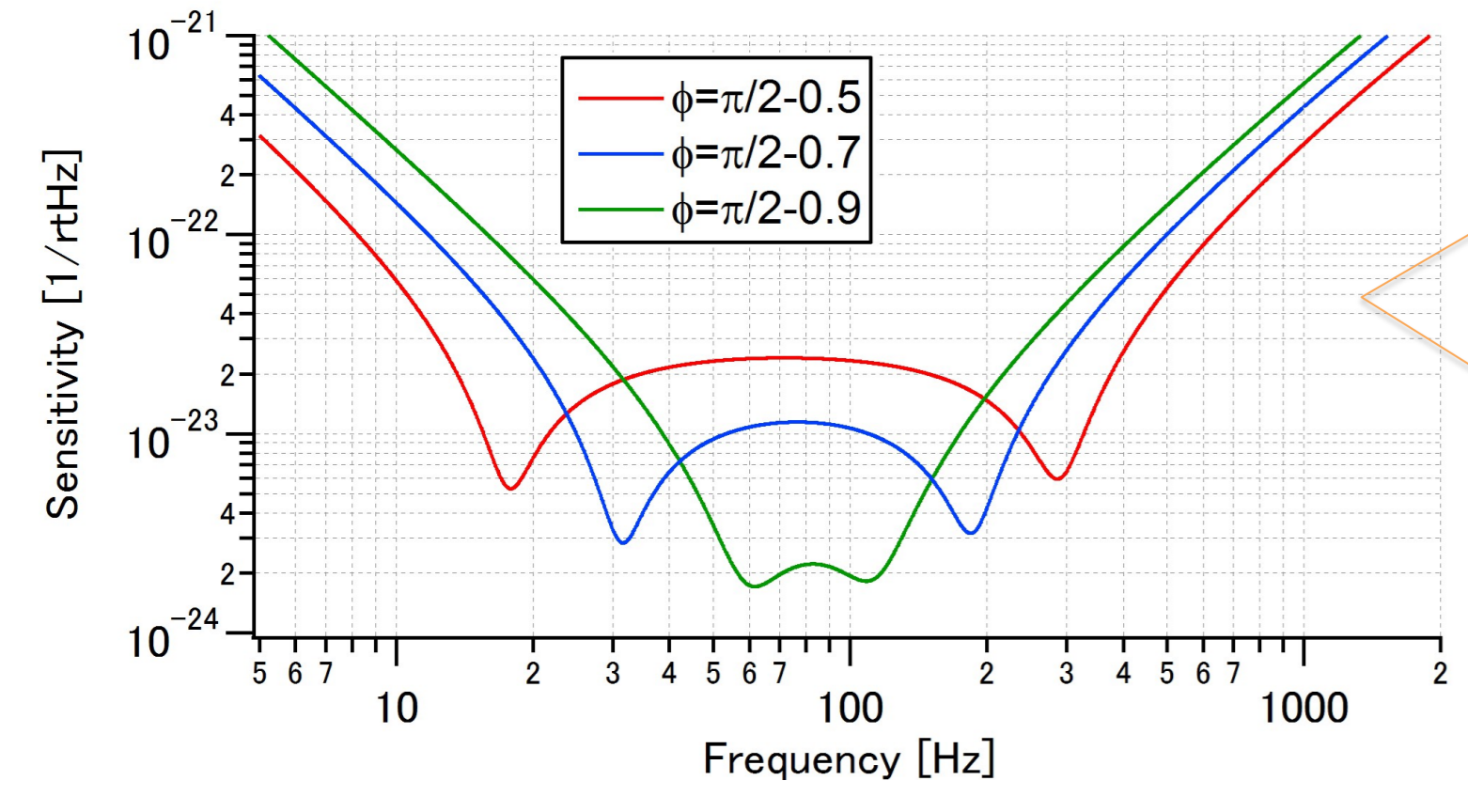


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**Motivation** We want to shift the optical spring resonance to higher frequency, where many interesting astronomical sources are expected and the quantum noise only limits the sensitivity.

## Optical spring

Optical spring is generated when the cavity is detuned from a resonant point. If the mirror goes away from the operating point, the mirror comes back to the prior position, where the radiation pressure and mechanical force are balanced. As the detune phase changes, the frequency gap of two dips changes. Note that the shift of the lower dip is limited by the upper dip, whereas the detune phase is chosen.



**Lower dip** the optical spring resonance.  
**Upper dip** the optical resonance of the coupled cavity with the detuned SRC and the arm cavity.

## Optical spring resonance

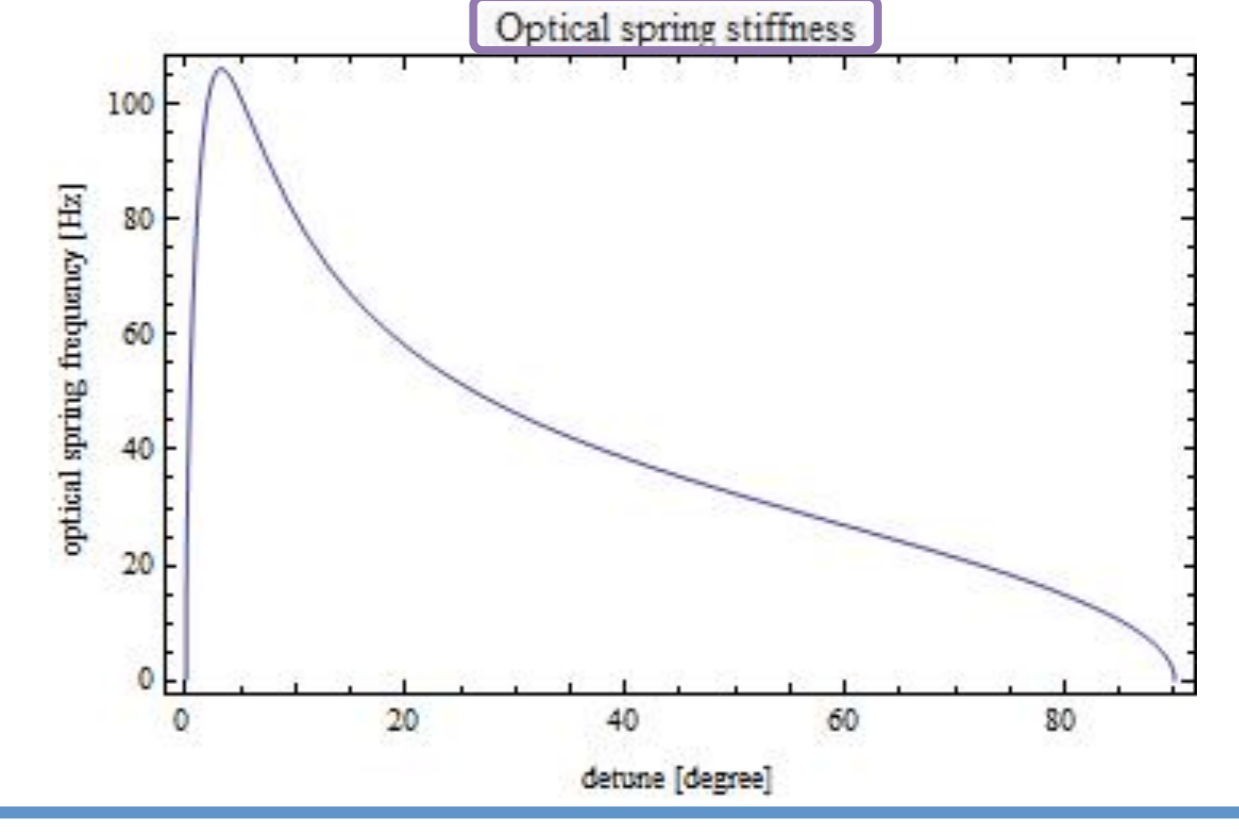
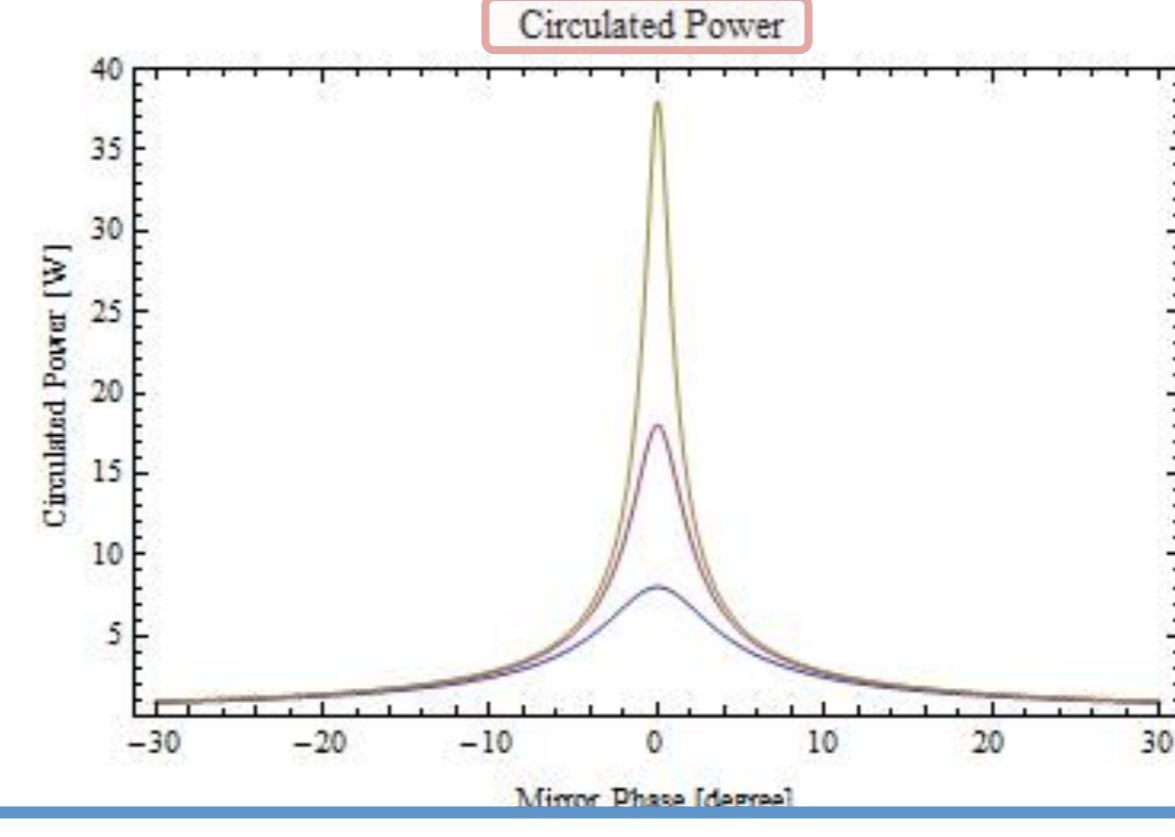
Optical spring resonance is determined by the formula below. (High cavity pole approximation)

$$f_{os} \propto \sqrt{\frac{2I_0}{m} \frac{1}{\left(r + \frac{l}{r} - 2\cos 2\phi\right)} \sin 2\phi}$$

$I_0$ : laser power  
 $m$ : mass of the mirror  
 $r$ : reflectance of the mirror  
 $\phi$ : detune phase

**Red term** – the amplification of the cavity  
**Purple term** – the amount of the amplitude signal

**Optical spring resonance cannot exceed a certain frequency just by changing the detune phase.**



## Improvement of the detection band – Stiff optical spring

In order to realize a stiffer optical spring, two methods are known : to increase the laser power and to change the detune phase. However these conventional methods have some weak points.

<b>High power laser</b>	Induces the thermal noise on the mirror. Technically hard to keep high power stable.
<b>Change the detune phase</b>	Limited by the optical resonance frequency.

Based on these points, we suggest a **signal amplification** to realize the stiff optical spring without the high power laser.

## Shift of the optical spring resonance

$$f_{os} \propto \sqrt{\frac{2sI_0}{m} \frac{1}{\left(r + \frac{l}{r} - \left(s + \frac{l}{s}\right) \cos 2\phi\right)} \sin 2\phi}$$

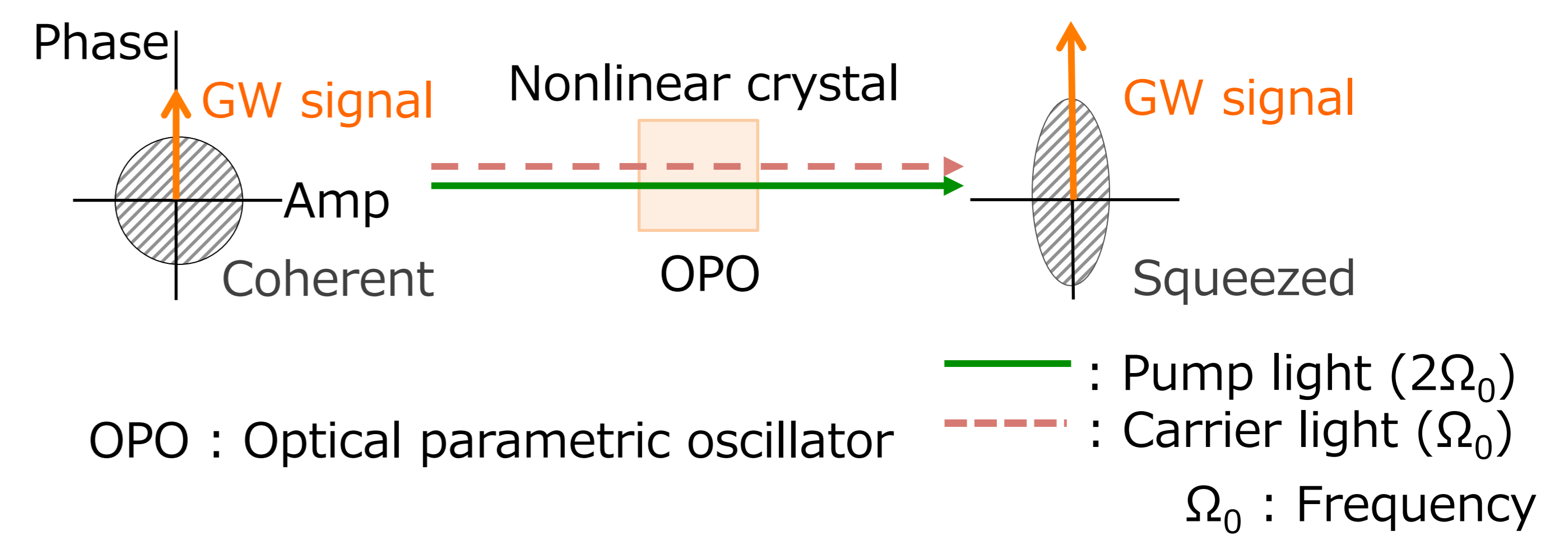
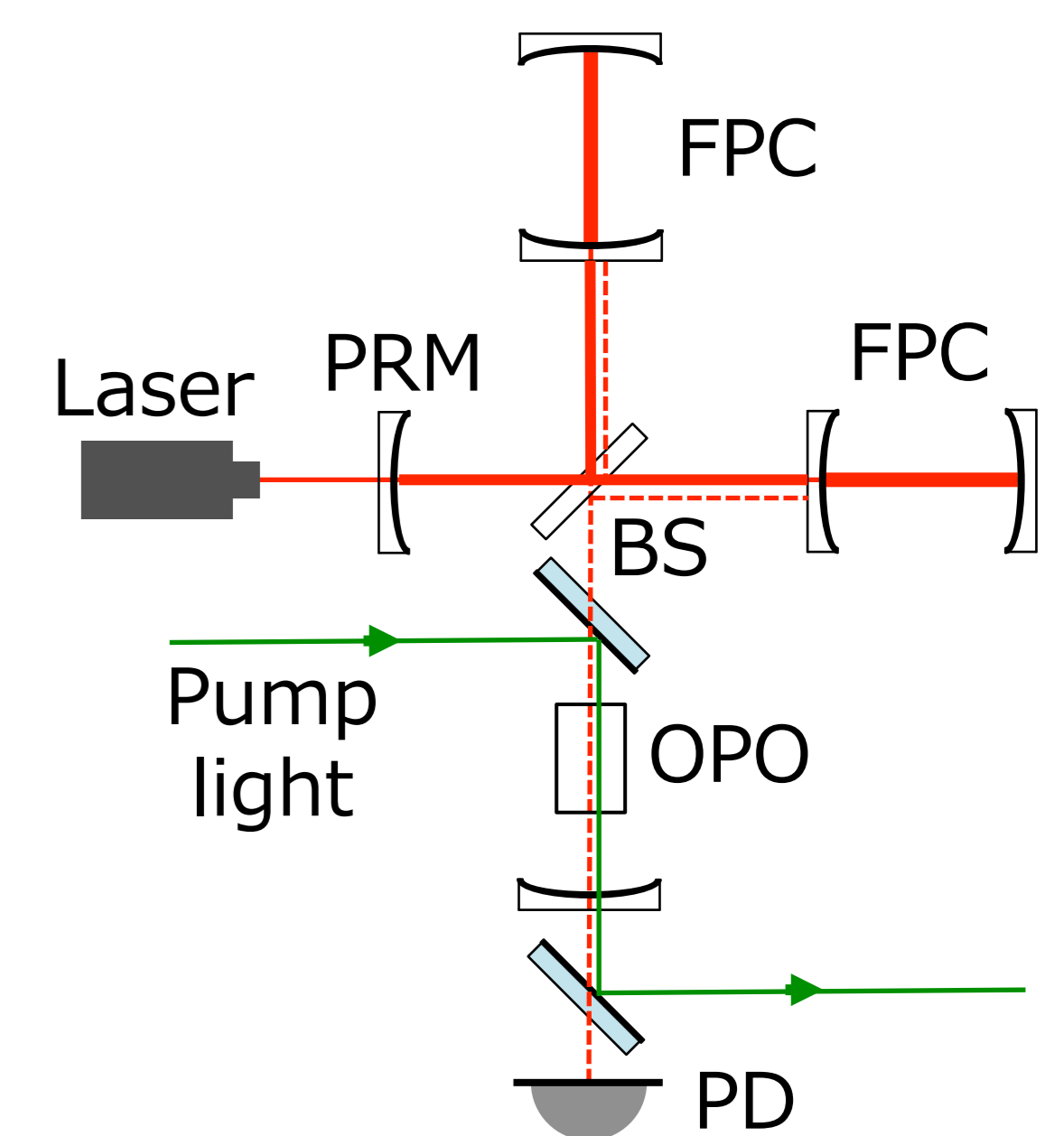
$s$ : squeezing factor

**Green term** – the effectively laser power.  
**Orange term** – intra-cavity squeezing coefficient

**Optical spring with signal amplification exceed a certain frequency by changing the squeezing factor.**

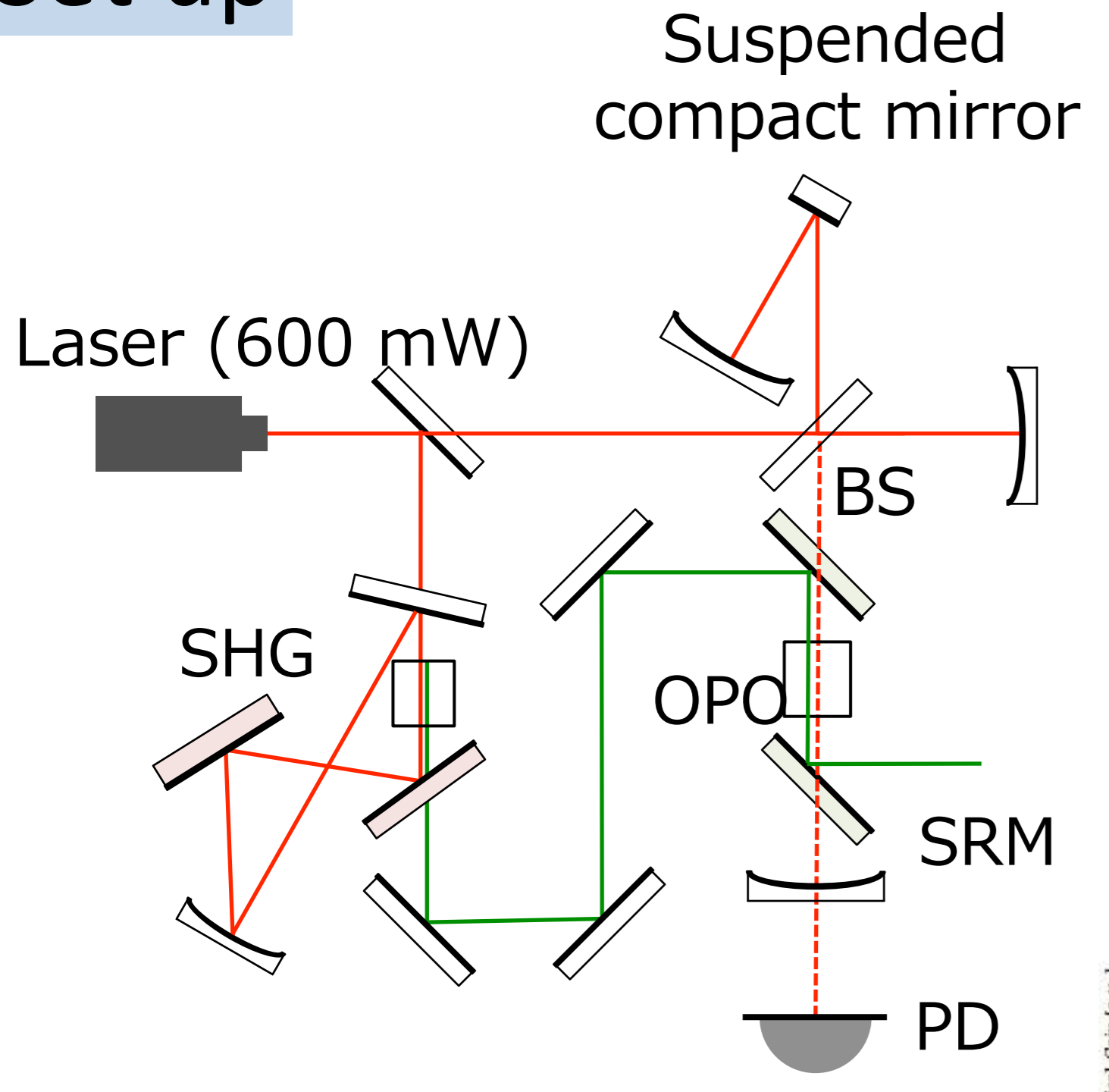
## Signal amplification

In order to realize the signal amplification, we use the OPO (Optical parametric oscillator) which consists of the nonlinear optics and pump light. It is placed inside the SRC. While, the OPO is typically used for reduction of the phase fluctuations, we use the OPO for signal amplification. Signal amplification has similar effects as using the high power laser.

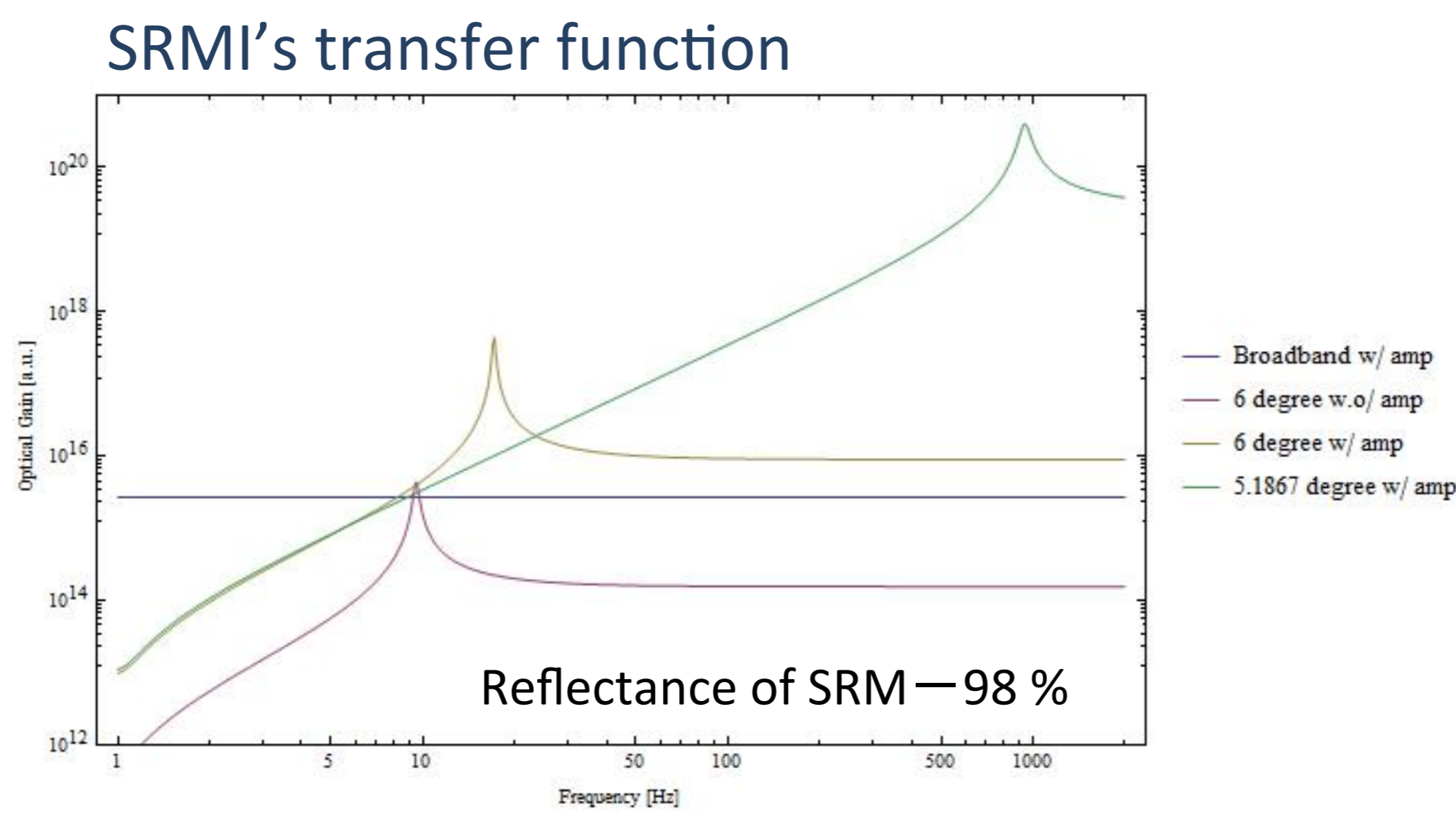


## Experiment

### Set up

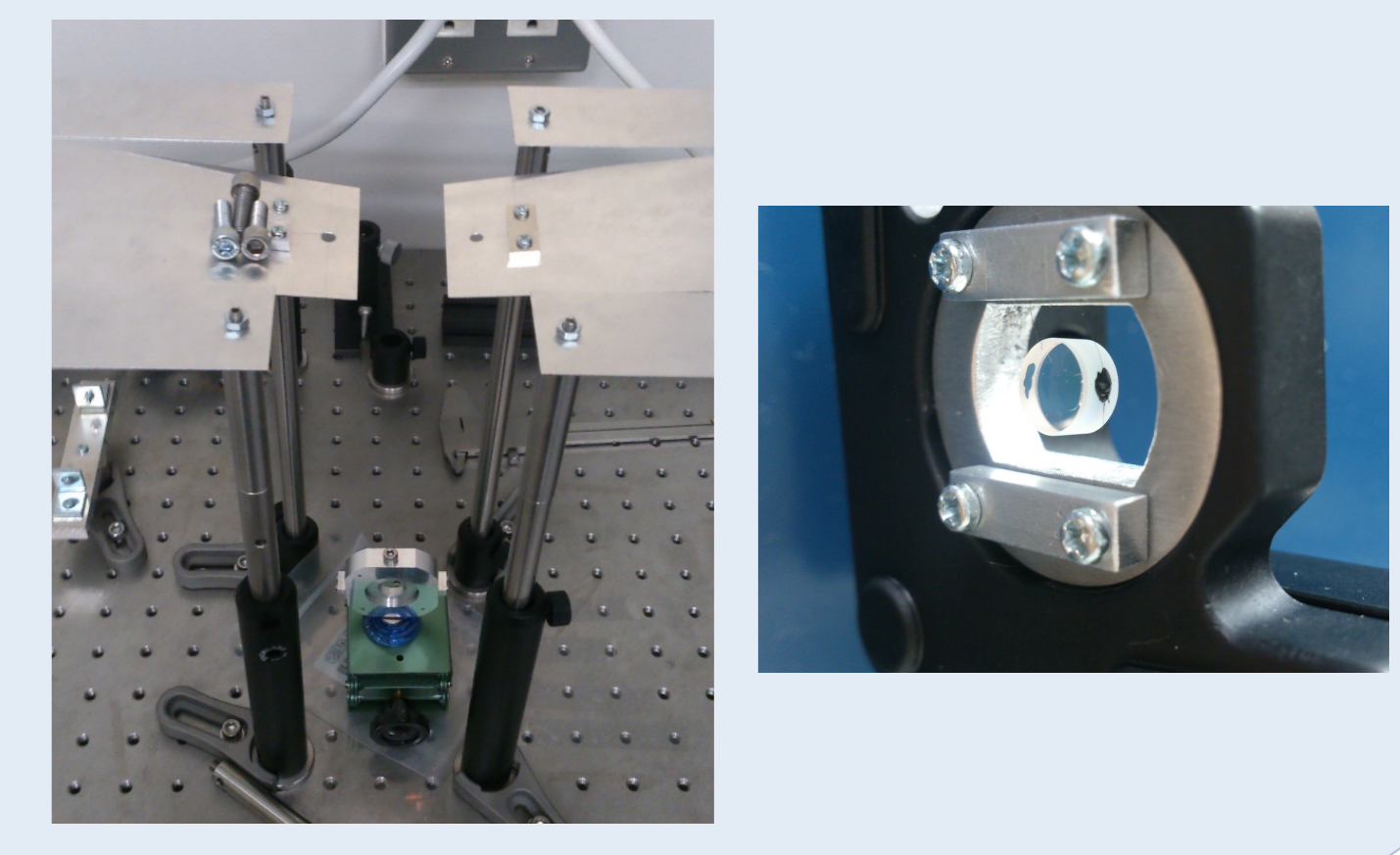


MI – locked  
SRC – locked  
SHG – constructing  
OPO – tested



### Suspended compact mirror

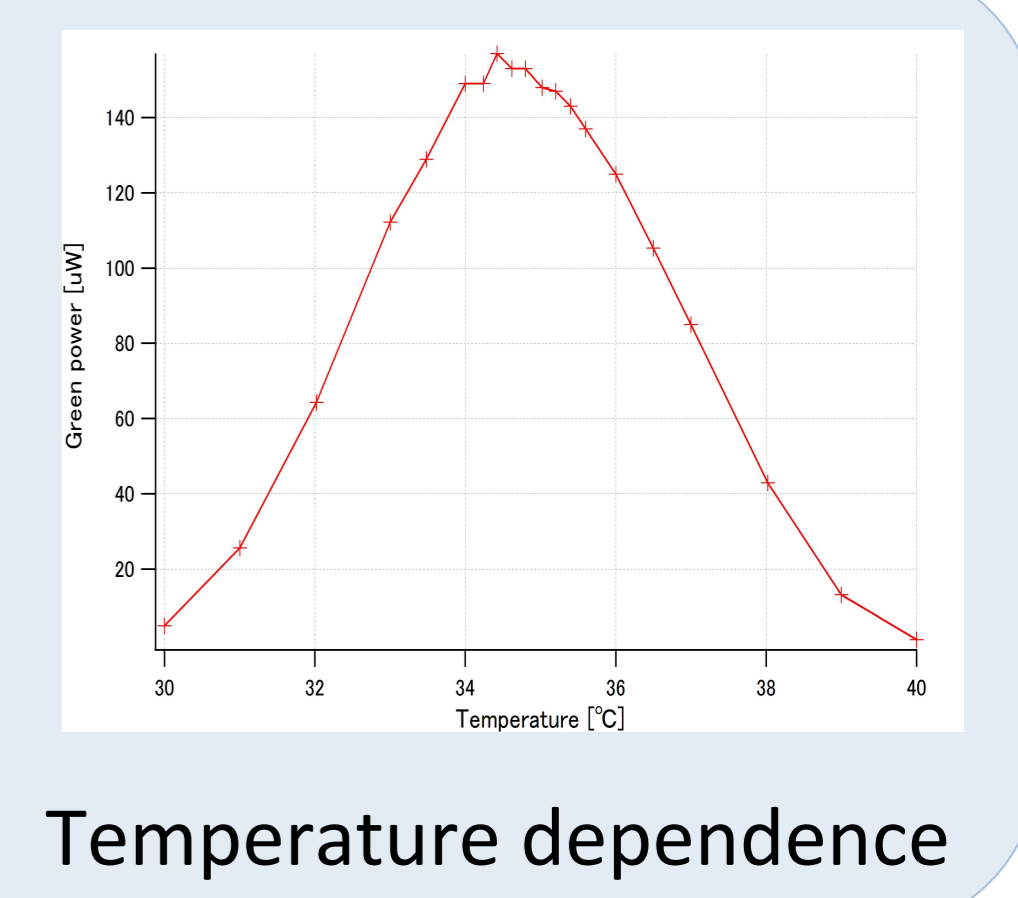
Mass – 200 mg  
Resonant frequency  
longitudinal – 23 Hz  
pitch, yaw – 33 Hz  
Wire Material – tungsten



### Nonlinear optics

Material – PPKTP  
Conversion efficiency (one-pass)

$$E_{NL} = \frac{P_{SHG}}{P_0^2} \sim 0.005 W^{-1}$$



## Future work

- Stabilize the control system to see the optical spring.
- Improve the SHG efficiency to generate higher power pump light to realize the signal amplification.
- Combine two experiments and measure the shift of the optical spring resonance by using the signal amplification.