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# Controlling Transient Thermal Effects in High-Power Gravitational-Wave Detectors

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# Presentation Outline

- Why high power?
- Transient thermal effects
- The TCS
- Controlling thermal effects
- Models
- Results



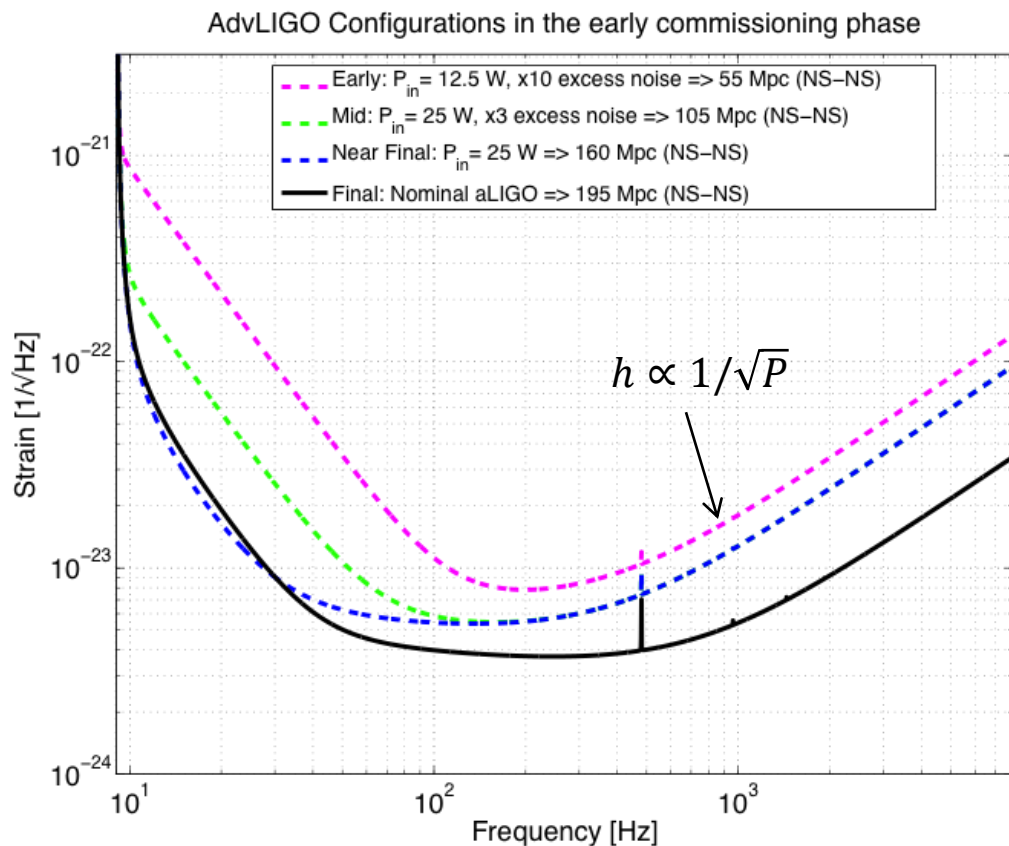
# Why high-powered laser operation?

- High-frequency gravitational-wave emitters (like compact binary mergers) could reveal interesting physics we don't fully understand yet.
- However, detecting high-frequency waves requires overcoming fundamental noise sources that affect the signal.



Credit: NASA / Goddard Space Flight Center

# Why high-powered laser operation?

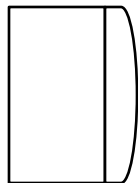


- Above  $\sim 150$  Hz, Advanced LIGO's noise floor is dominated by quantum shot noise.
- Increasing the laser power increases strain sensitivity, but causes self-heating in the test masses that must be addressed & controlled.

# Transient thermal effects

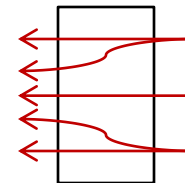
## Thermoelastic effects

- Occur as a result of thermal expansion.
- These lead to surface deformations in the test-mass.



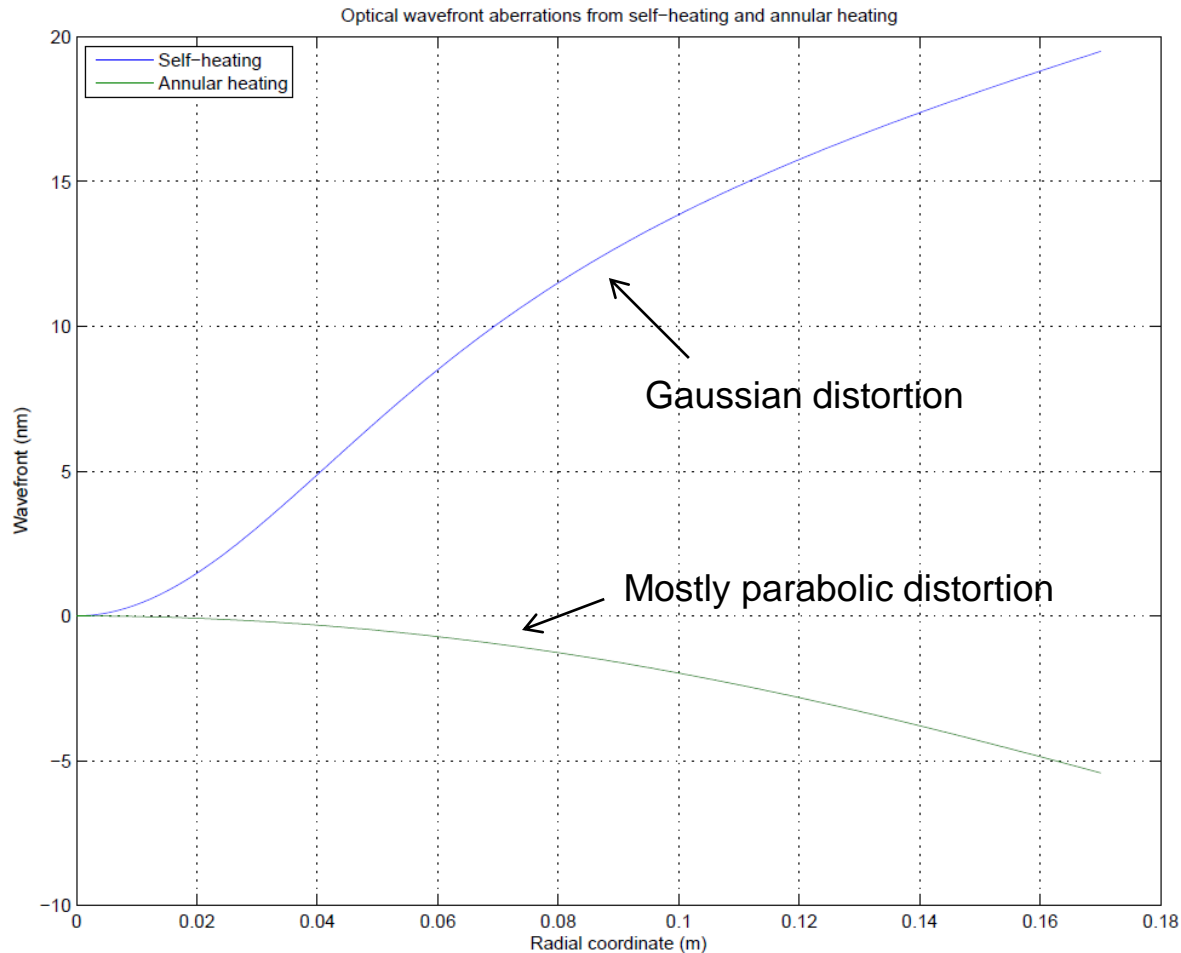
## Thermorefractive effects

- Occur as a result of the thermo-optic effect.
- These lead to spatially-dependent refractive indices.

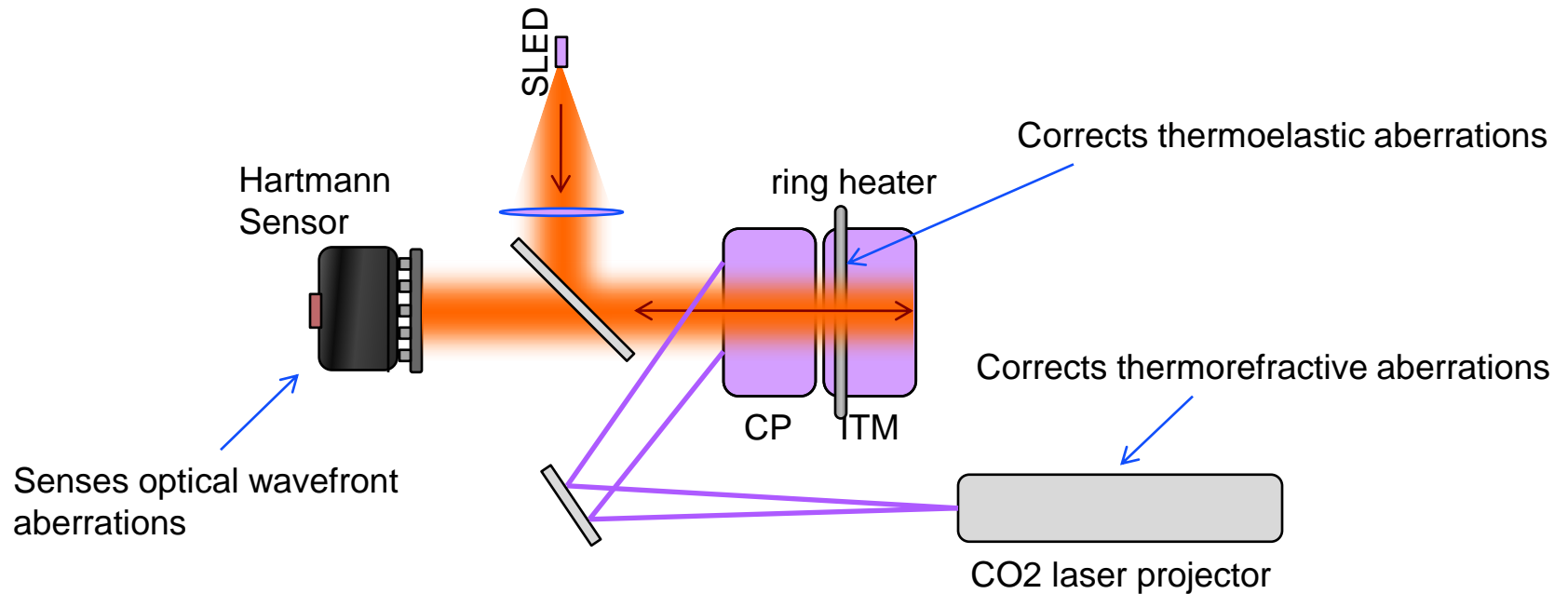


**Both induce optical  
wavefront  
aberrations.**

# Characterizing optical aberrations



# The TCS: A Diagram



Credit: Dr. Aidan Brooks

# TCS controller model

- A PID (proportional-integral-derivative) controller model was developed in MATLAB using finite difference methods to minimize optical aberrations.
- The controller reads an error signal (the defocus) and calculates an actuation (emitted power) which is determined by the given controller gains.

$$u(t) = K_p e(t) + K_i \int_0^t e(t) dt + K_d \frac{d(e(t))}{dt}$$

Power to be emitted

Contributes the bulk of output change

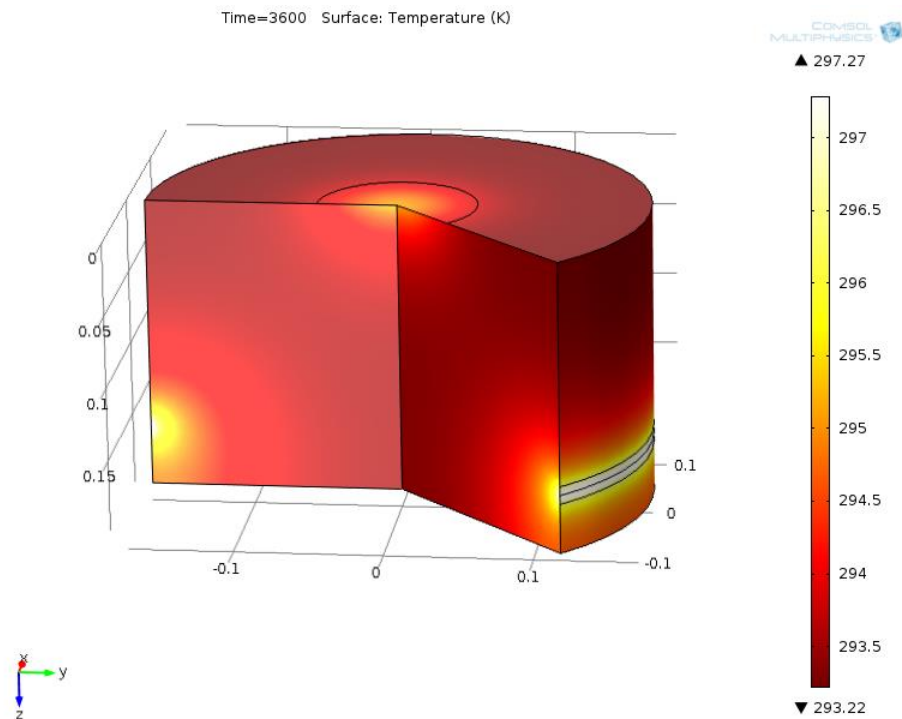
Corrects steady-state error

Decreases settling time



# Finite element model

- A finite element model was developed in COMSOL to simulate the thermal effects in the ITM/ETM.
- The model includes self-heating and ring heater thermal effects.

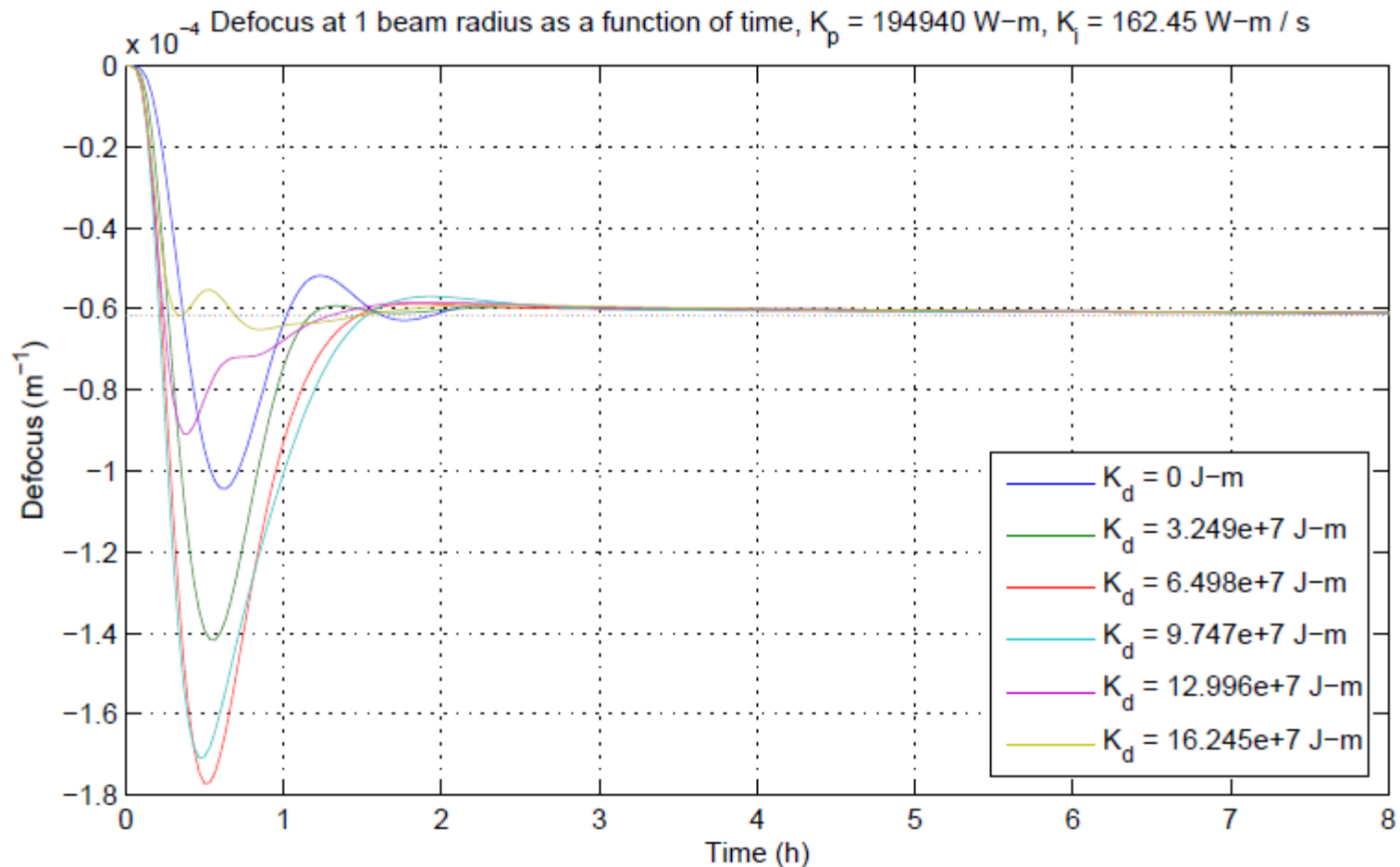


# Controlling optical aberrations

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- Combining the controller model with the finite element heating model allows for a dynamic simulation of transient thermal effects in the test mass.
  - » COMSOL model simulates thermal effects in the test mass.
  - » MATLAB controller model calculates defocus & actuation.
  - » Actuation power passed to the COMSOL model; cycle repeats.
- However, communication overhead between MATLAB and COMSOL limits applicability; other methods should be tried.

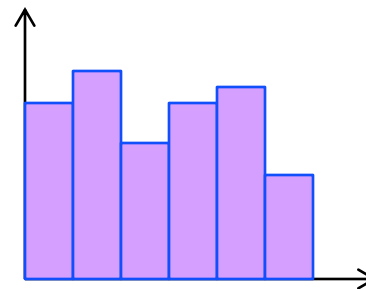
# Controlling optical aberrations



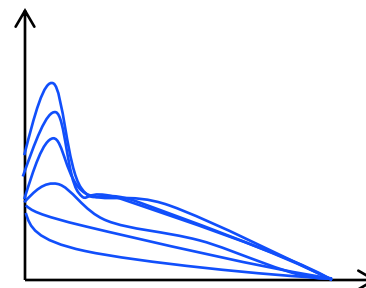
# Wavefront predictor

- The predictor uses the principle of superposition and the digital nature of the actuation to recreate a digital signal response from unit rectangle signal response data.
- It does not require finite element analysis, and is extremely time-efficient (~ 300 times faster than COMSOL+MATLAB model!)
- *It approximates nonlinear thermal behavior, namely radiation, as linear.*

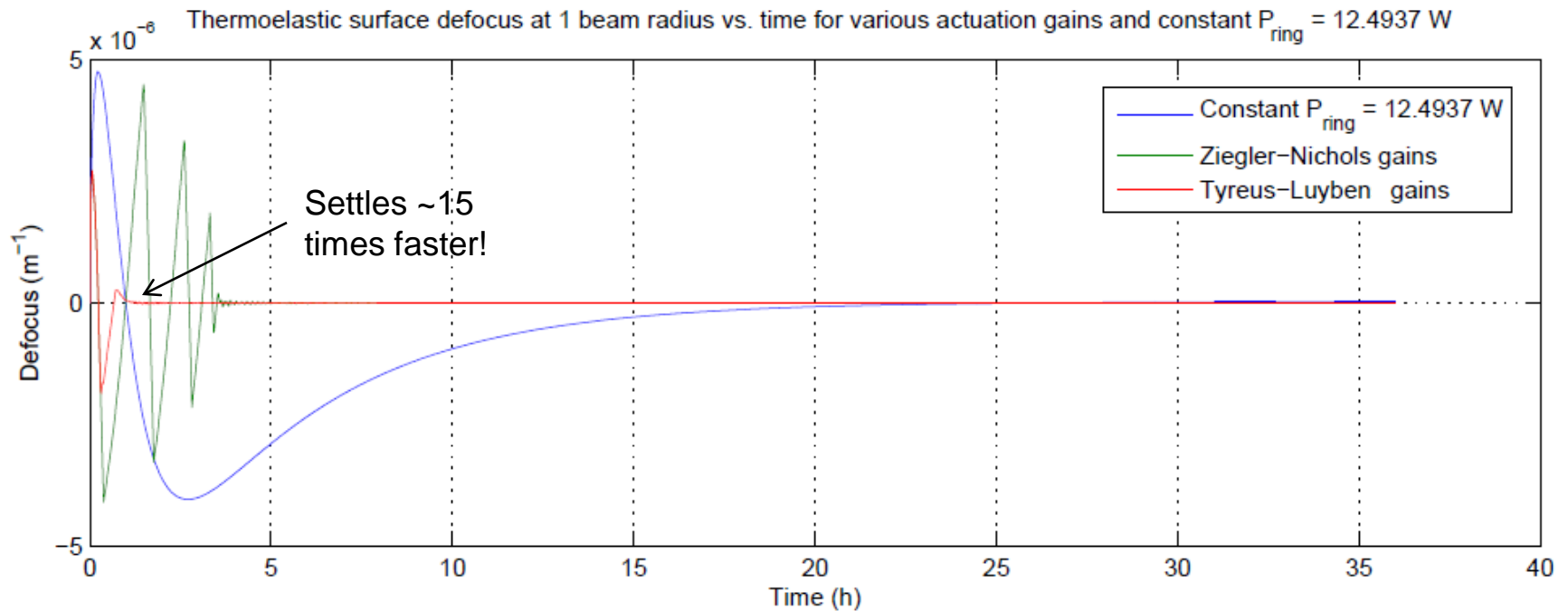
From a rectangle signal...



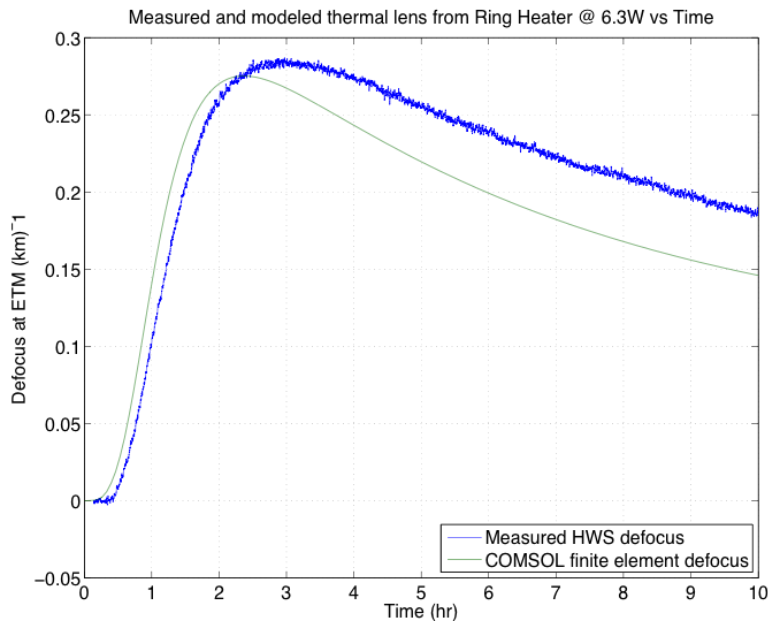
To a digital one!



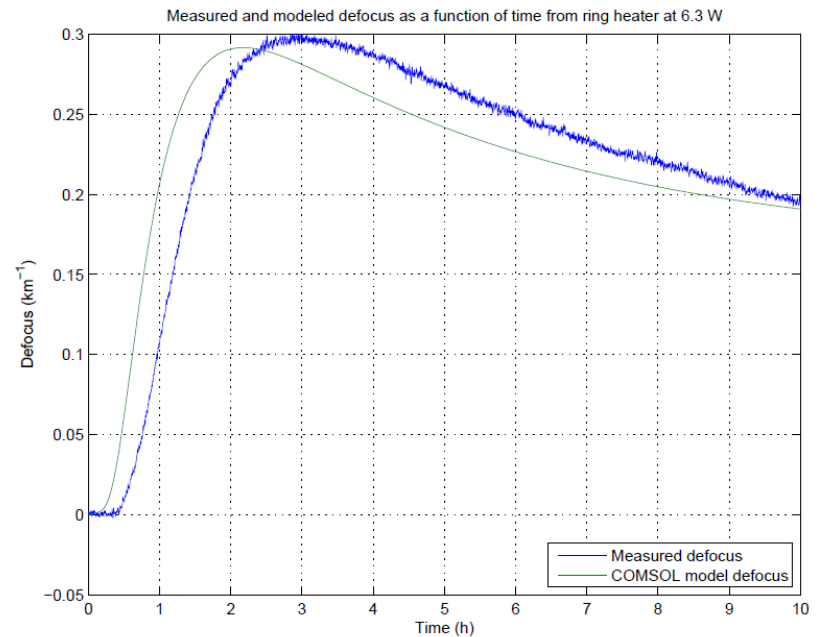
# Results: Active vs. passive correction



# Results: Experiment vs. Models



Aidan's model...

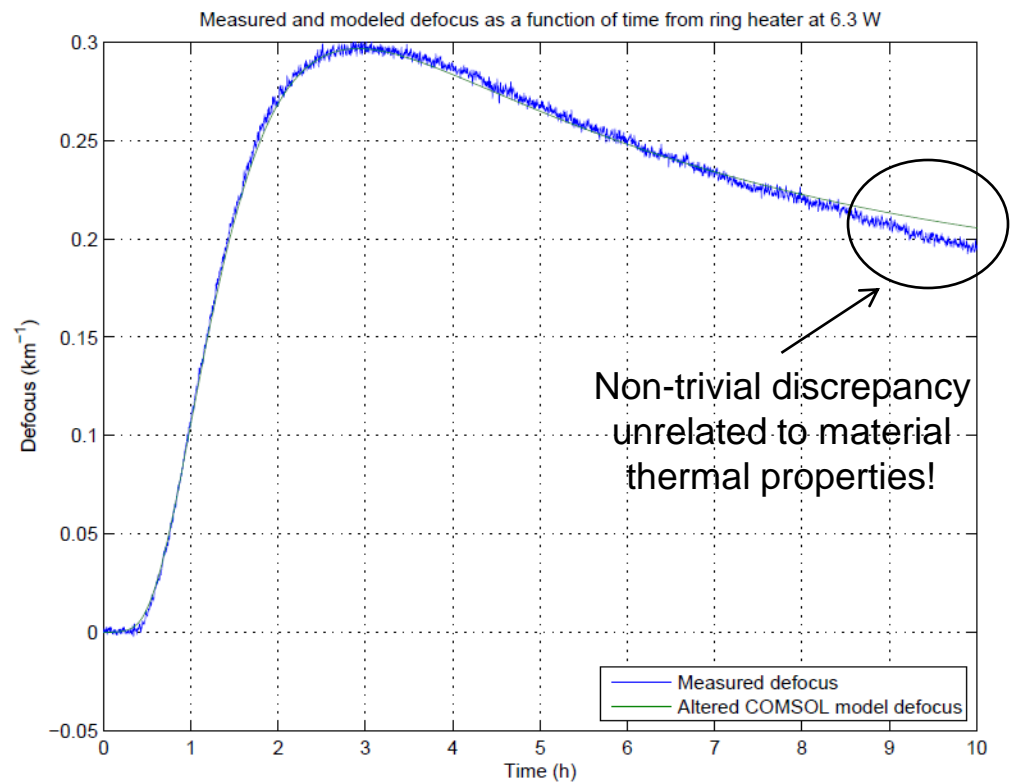


...and my model!

Both models show a similar deviation from experiment.

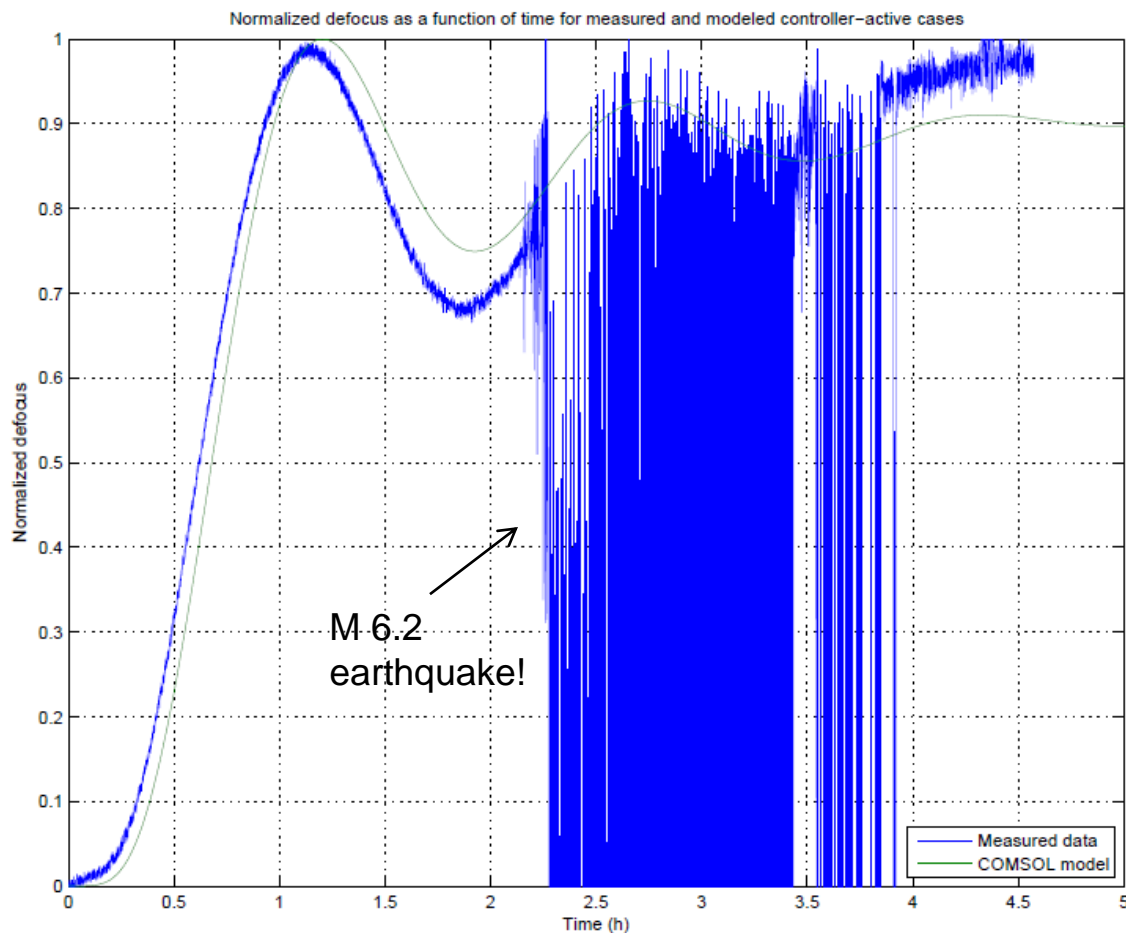
# Results: Experiments vs. Models

- In an attempt to diagnose the problem, a thermal parameter study was conducted to trace the root of the discrepancy.
- By adding a turn-on time constant of  $\sim 1200$  s to the ring heater and lowering the thermal conductivity  $\sim 5\%$ , we get...



# Results: Experiments vs. Models

- A full comparison was done for a controller-active case.
- Experiment appears to react quicker than the altered COMSOL model; some data corrupted from earthquake.
- Clear discrepancy: needs to be further studied.





# Future Work

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- Conclusively identify source of model/experiment discrepancy.
- Include CO<sub>2</sub> laser projector & compensation plate into heating model; simulate full TCS.
- Quantify higher-order mode losses and compare to experiment.
- Investigate how TCS affects other control systems' performance (ACS, etc.).

# Acknowledgements

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- My fellow SURFs
- Caltech
- LIGO Scientific Collaboration
- NSF

# References

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