

T1300406 Wide Angle Scatter from ITM  
 2/4/11

Displacement noise requirement @ 100 Hz, m/rt Hz	$D_{\text{req}} := 1 \cdot 10^{-21}$
Motion of manifold @ 100 Hz, m/rt Hz	$x_{\text{manifold}} := 8 \cdot 10^{-11}$
ACB displacement @ 100 Hz, m/rtHz	$x_{\text{ACB}} := 1 \cdot 10^{-12}$
ISI optical table displacement @ 100 Hz, m/rtHz	$x_{\text{ISI}} := 3 \cdot 10^{-14}$
Transfer function @ 100 Hz, ITM HR	$TF_{\text{itmhr}} := 1.1 \cdot 10^{-9}$
BRDF of chamber wall, sr <sup>-1</sup>	$BRDF_{\text{wall}} := 0.1$
BRDF of porcelainized steel, sr <sup>-1</sup>	$BRDF_{\text{porc}} := 0.04$
BRDF of black glass, sr <sup>-1</sup>	$BRDF_{\text{bg}} := 1 \cdot 10^{-6}$
BRDF of BD, sr <sup>-1</sup>	$BRDF_{\text{bd}} := 0.030$
BRDF of oxidized un-polished steel, sr <sup>-1</sup>	$BRDF_{\text{oxiunpolish}} := 0.03$
laser wavelength, m	$\lambda := 1.064 \cdot 10^{-6}$
wave number, m <sup>-1</sup>	$k := 2 \cdot \frac{\pi}{\lambda} \quad k = 5.905 \times 10^6$
hemispherical scattering loss fraction TM wide angle(ref: T070089)	$\alpha_{\text{TM}} := 10 \times 10^{-6}$
see T070303 with arm cavity gain = 13000	
arm power, W	$P_a := 8.125 \times 10^5$
input laser power, W	$P_{\text{psl}} := 125$
arm cavity length, m	$L := 4000$

The following data comes from ZEMAX sensor data; see /ALIGO/SLC/ACB/wide angle scatter\_ITMX\_H1\_power.xls

**SCATTER PATH LENGTH**

distance from ITM to WIDE ANGLE BAF TOP LEDGE ITMX, m	$L_{wabtop} := 0.6$
distance from ITM to WIDE ANGLE BAF BOTTOM LEDGE ITMX, m	$L_{wabbot} := 0.4$
distance from WIDE ANGLE BAF PLATE 1 ITMX, m	$L_{wabp1} := 1.3$
distance from WIDE ANGLE BAF PLATE 2 ITMX, m	$L_{wabp2} := 1.1$
distance from WIDE ANGLE BAF PLATE 3 ITMX, m	$L_{wabp3} := 0.9$
distance from WIDE ANGLE BAF PLATE 4 ITMX, m	$L_{wabp4} := 0.8$
distance from WIDE ANGLE BAF SIDE right, m	$L_{wabsr} := 0.7$
distance from WIDE ANGLE BAF SIDE left, m	$L_{wabsl} := 0.4$
distance from WIDE ANGLE Side Extender, m	$L_{wabse} := 0.24$
distance from PLATE above TM, m	$L_{ptm} := 0.24$
distance from SUS ring around TM, m	$L_{rtm} := 0.17$
distance from ACB, m	$L_{acb} := 0.8$
distance from UPPER BSC, m	$L_{upbsc} := 2$
distance from FLOOR BSC, m	$L_{floorbsc} := 0.8$

distance from SPOOL, m	$L_{\text{spool}} := 2.3$
distance from Manifold, m	$L_{\text{mani}} := 5$
distance from ETMX manifold flat baffle, m	$L_{\text{maniflat}} := 2.393$

### **COC INCIDENT ANGLE**

incident angle from WIDE ANGLE BAF TOP LEDGE ITMX, rad	$\theta_{\text{wabtop}} := 1.0$
incident angle from WIDE ANGLE BAF BOTTOM LEDGE ITMX, rad	$\theta_{\text{wabbot}} := 0.6$
incident angle from WIDE ANGLE BAF PLATE 1 ITMX, rad	$\theta_{\text{wabp1}} := 1.3$
incident angle from WIDE ANGLE BAF PLATE 2 ITMX, rad	$\theta_{\text{wabp2}} := 1$
incident angle from WIDE ANGLE BAF PLATE 3 ITMX, rad	$\theta_{\text{wabp3}} := 1.2$
incident angle from WIDE ANGLE BAF PLATE 4 ITMX, rad	$\theta_{\text{wabp4}} := 0.6$
incident angle from WIDE ANGLE BAF SIDE right, rad	$\theta_{\text{wabsr}} := 1.05$
incident angle from WIDE ANGLE BAF SIDE left, rad	$\theta_{\text{wabsl}} := 0.53$
incident angle from WIDE ANGLE Side Extender, rad	$\theta_{\text{wabse}} := 1.26$
incident angle from PLATE above TM, rad	$\theta_{\text{ptm}} := 1.4$
incident angle from SUS ring around TM, rad	$\theta_{\text{rtm}} := 1.5$

incident angle from ACB, rad	$\theta_{acb} := 0.32$
incident angle from UPPER BSC, rad	$\theta_{upbsc} := 1.4$
incident angle from FLOOR BSC, rad	$\theta_{floorbsc} := 1.4$
incident angle from SPOOL, rad	$\theta_{spool} := 0.17$
incident angle from Manifold, rad	$\theta_{mani} := 0.08$
incident angle from ETMx manifold flat baffle, rad	$\theta_{maniflat} := 0.08$

**FRACTION of LAMBERTIAN SCATTER FROM COC HITTING SURFACE**

fractional power from WIDE ANGLE BAF TOP LEDGE ITMX	$PF_{wabtop} := 0.077$	<del><math>PF_{wabtop} := 0.083</math></del>
fractional power from WIDE ANGLE BAF BOTTOM LEDGE ITMX	$PF_{wabbot} := 0.21$	<del><math>PF_{wabbot} := 0.22</math></del>
fractional power from WIDE ANGLE BAF PLATE 1 ITMX	$PF_{wabp1} := 0.037$	<del><math>PF_{wabp1} := 0.002</math></del>
fractional power from WIDE ANGLE BAF PLATE 2 ITMX	$PF_{wabp2} := 0.082$	<del><math>PF_{wabp2} := 0.0012</math></del>
fractional power from WIDE ANGLE BAF PLATE 3 ITMX	$PF_{wabp3} := 0.12$	<del><math>PF_{wabp3} := 0.0038</math></del>
fractional power from WIDE ANGLE BAF PLATE 4 ITMX	$PF_{wabp4} := 0.165$	<del><math>PF_{wabp4} := 0.0008</math></del>
fractional power from WIDE ANGLE BAF SIDE right	$PF_{wabsr} := 0.047$	<del><math>PF_{wabsr} := 0.069</math></del>
fractional power from WIDE ANGLE BAF SIDE left	$PF_{wabsl} := 0.16$	<del><math>PF_{wabsl} := 0.24</math></del>
fractional power from WIDE ANGLE Side Extender		$PF_{wabse} := 0.007$
fractional power from PLATE above TM	$FP_{ptm} := 5 \cdot 10^{-3}$	<del><math>FP_{ptm} := 7 \cdot 10^{-3}</math></del>

fractional power from SUS ring around TM	$FP_{rtm} := 8 \cdot 10^{-3}$	$FP_{rtm} := 10 \cdot 10^{-3}$
fractional power from ACB	$PF_{acb} := 0.232$	$PF_{acb} := 0.269$
fractional power from UPPER BSC	$PF_{upbsc} := 0.006$	$PF_{upbsc} := 0.003$
fractional power from FLOOR BSC	$PF_{floorbsc} := 0.002$	$PF_{floorbsc} := 0.007$
fractional power from SPOOL	$PF_{spool} := 0.0095$	$PF_{spool} := 0.045$
fractional power from Manifold	$PF_{mani} := 0.030$	$PF_{mani} := 0.033$
fractional power from ETMx Manifold flat baffle	$PF_{maniflat} := 0.037$	

## INCIDENT POWER

ACB BACK, W

$$P_{acb} := P_a \cdot PF_{acb} \cdot \alpha_{TM} = 2.186 \quad P_a = 8.125 \times 10^5$$

WIDE ANGLE BAF TOP LEDGE, W

$$P_{wabtop} := P_a \cdot PF_{wabtop} \cdot \alpha_{TM} = 0.674$$

WIDE ANGLE BAF BOTTOM LEDGE, W

$$P_{wabbot} := P_a \cdot PF_{wabbot} \cdot \alpha_{TM} = 1.787$$

WIDE ANGLE BAF PLATE 1 ITMX, W

$$P_{wabp1} := P_a \cdot PF_{wabp1} \cdot \alpha_{TM} = 0.016$$

WIDE ANGLE BAF PLATE 2 ITMX, W

$$P_{wabp2} := P_a \cdot PF_{wabp2} \cdot \alpha_{TM} = 9.75 \times 10^{-3}$$

WIDE ANGLE BAF PLATE 3 ITMX, W

$$P_{wabp3} := P_a \cdot PF_{wabp3} \cdot \alpha_{TM} = 0.031$$

WIDE ANGLE BAF PLATE 4 ITMX, W

$$P_{\text{wabp4}} := P_a \cdot PF_{\text{wabp4}} \cdot \alpha_{\text{TM}} = 6.5 \times 10^{-3}$$

WIDE ANGLE BAF SIDE right, W

$$P_{\text{wabsr}} := P_a \cdot PF_{\text{wabsr}} \cdot \alpha_{\text{TM}} = 0.561$$

WIDE ANGLE BAF SIDE left, W

$$P_{\text{wabsl}} := P_a \cdot PF_{\text{wabsl}} \cdot \alpha_{\text{TM}} = 1.95$$

WIDE ANGLE BAF SIDE Extender, W

$$P_{\text{wabse}} := P_a \cdot PF_{\text{wabse}} \cdot \alpha_{\text{TM}} = 0.057$$

PLATE above TM, W

$$P_{\text{ptm}} := P_a \cdot FP_{\text{ptm}} \cdot \alpha_{\text{TM}} = 0.057$$

SUS ring around TM, W

$$P_{\text{rtm}} := P_a \cdot FP_{\text{rtm}} \cdot \alpha_{\text{TM}} = 0.081$$

UPPER BSC, W

$$P_{\text{upbsc}} := P_a \cdot PF_{\text{upbsc}} \cdot \alpha_{\text{TM}} = 0.024$$

FLOOR BSC, W

$$P_{\text{floor}} := P_a \cdot PF_{\text{floorbsc}} \cdot \alpha_{\text{TM}} = 0.057$$

SPOOL, W

$$P_{\text{spool}} := P_a \cdot PF_{\text{spool}} \cdot \alpha_{\text{TM}} = 0.366$$

MANIFOLD, W

$$P_{\text{mani}} := P_a \cdot PF_{\text{mani}} \cdot \alpha_{\text{TM}} = 0.268$$

ETMX MANIFOLD FLAT BAF, W

$$P_{\text{maniflat}} := P_a \cdot PF_{\text{maniflat}} \cdot \alpha_{\text{TM}} = 0.301$$

**POWER SCATTERED INTO IFO MODE**

$$P_{inc} := 1$$

$$w_{ifo} := 1$$

$$BRDF_s := 1$$

$$\theta_{inc} := 1$$

$$P_{sTM} := P_{inc} \cdot BRDF_s \cdot \frac{\pi \cdot w_{ifo}^2}{L^2} \quad P_{sTMifo} := P_{inc} \cdot BRDF_s \cdot \frac{\alpha_{TM}}{\pi \cdot L^2} \cdot \lambda^2 \cdot \cos(\theta_{inc})$$

$$P_{sTMifo} := P_{sTM} \cdot \frac{\alpha_{TM}}{\pi} \cdot \cos(\theta_{inc}) \cdot \frac{\lambda^2}{(\pi \cdot w_{ifo}^2)}$$

$$P_{acb} = 2.186$$

ACB BACK, W

$$P_{acbifo} := \sqrt{4} \cdot P_{acb} \cdot \left( \alpha_{TM} \cdot \frac{\lambda^2}{\pi \cdot L_{acb}^2} \cdot BRDF_{oxiunpolish} \cdot \cos(\theta_{acb}) \right)$$

$$P_{acbifo} = 7.009 \times 10^{-19}$$

WIDE ANGLE BAF TOP LEDGE, W

$$P_{wabtopifo} := \sqrt{4} \cdot P_{wabtop} \cdot \left( \alpha_{TM} \cdot \frac{\lambda^2}{\pi \cdot L_{wabtop}^2} \cdot BRDF_{oxiunpolish} \cdot \cos(\theta_{wabtop}) \right)$$

$$P_{wabtopifo} = 2.188 \times 10^{-19}$$

WIDE ANGLE BAF BOTTOM LEDGE, W

$$P_{\text{wabbotifo}} := \sqrt{4} \cdot P_{\text{wabbot}} \cdot \left( \alpha_{\text{TM}} \cdot \frac{\lambda^2}{\pi \cdot L_{\text{wabbot}}^2} \cdot \text{BRDF}_{\text{oxiunpolish}} \cdot \cos(\theta_{\text{wabbot}}) \right)$$

$$P_{\text{wabbotifo}} = 1.994 \times 10^{-18}$$

WIDE ANGLE BAF SIDE right, W

$$P_{\text{wabsrifo}} := \sqrt{4} \cdot P_{\text{wabsr}} \cdot \left( \alpha_{\text{TM}} \cdot \frac{\lambda^2}{\pi \cdot L_{\text{wabsr}}^2} \cdot \text{BRDF}_{\text{oxiunpolish}} \cdot \cos(\theta_{\text{wabsr}}) \right)$$

$$P_{\text{wabsrifo}} = 1.231 \times 10^{-19}$$

WIDE ANGLE BAF SIDE left, W

$$P_{\text{wabslifo}} := \sqrt{4} \cdot P_{\text{wabsl}} \cdot \left( \alpha_{\text{TM}} \cdot \frac{\lambda^2}{\pi \cdot L_{\text{wabsl}}^2} \cdot \text{BRDF}_{\text{oxiunpolish}} \cdot \cos(\theta_{\text{wabsl}}) \right)$$

$$P_{\text{wabslifo}} = 2.274 \times 10^{-18}$$

WIDE ANGLE BAF SIDE Extender, W

$$P_{\text{wabseifo}} := \sqrt{4} \cdot P_{\text{wabse}} \cdot \left( \alpha_{\text{TM}} \cdot \frac{\lambda^2}{\pi \cdot L_{\text{wabse}}^2} \cdot \text{BRDF}_{\text{oxiunpolish}} \cdot \cos(\theta_{\text{wabse}}) \right)$$

$$P_{\text{wabseifo}} = 6.529 \times 10^{-20}$$

TOTAL WIDE ANGLE BAF SIDE, W



$$P_{\text{wabstifo}} := \left( P_{\text{wabsrifo}}^2 + P_{\text{wabslifo}}^2 + P_{\text{wabseifo}}^2 \right)^{0.5}$$

$$P_{\text{wabstifo}} = 2.278 \times 10^{-18}$$

TOTAL ACB BACK AND BOX, W

$$P_{\text{wacbboxifo}} := \left( P_{\text{acbifo}}^2 + P_{\text{wabtopifo}}^2 + P_{\text{wabbotifo}}^2 + P_{\text{wabsrifo}}^2 + P_{\text{wabslifo}}^2 + P_{\text{wabseifo}}^2 \right)^{0.5}$$

$$P_{\text{wacbboxifo}} = 3.115 \times 10^{-18}$$

WIDE ANGLE BAF PLATE 1 ITMX, W

$$P_{\text{wabp1ifo}} := \sqrt{4} \cdot P_{\text{wabp1}} \cdot \left( \alpha_{\text{TM}} \cdot \frac{\lambda^2}{\pi \cdot L_{\text{wabp1}}^2} \cdot \text{BRDF}_{\text{oxiunpolish}} \cdot \cos(\theta_{\text{wabp1}}) \right)$$

$$P_{\text{wabp1ifo}} = 5.561 \times 10^{-22}$$

WIDE ANGLE BAF PLATE 2 ITMX, W

$$P_{\text{wabp2}} = 9.75 \times 10^{-3}$$

$$P_{\text{wabp2ifo}} := \sqrt{4} \cdot P_{\text{wabp2}} \cdot \left( \alpha_{\text{TM}} \cdot \frac{\lambda^2}{\pi \cdot L_{\text{wabp2}}^2} \cdot \text{BRDF}_{\text{oxiunpolish}} \cdot \cos(\theta_{\text{wabp2}}) \right)$$

$$P_{\text{wabp2ifo}} = 9.413 \times 10^{-22}$$

WIDE ANGLE BAF PLATE 3 ITMX, W

$$P_{\text{wabp3ifo}} := \sqrt{4} \cdot P_{\text{wabp3}} \cdot \left( \alpha_{\text{TM}} \cdot \frac{\lambda^2}{\pi \cdot L_{\text{wabp3}}^2} \cdot \text{BRDF}_{\text{oxiunpolish}} \cdot \cos(\theta_{\text{wabp3}}) \right)$$

$$P_{\text{wabp3ifo}} = 2.986 \times 10^{-21}$$

WIDE ANGLE BAF PLATE 4 ITMX, W

$$P_{\text{wabp4ifo}} := \sqrt{4} \cdot P_{\text{wabp4}} \cdot \left( \alpha_{\text{TM}} \cdot \frac{\lambda^2}{\pi \cdot L_{\text{wabp4}}^2} \cdot \text{BRDF}_{\text{oxiunpolish}} \cdot \cos(\theta_{\text{wabp4}}) \right)$$

$$P_{\text{wabp4ifo}} = 1.812 \times 10^{-21}$$

PLATE above TM, W

$$P_{\text{ptmifo}} := \sqrt{4} \cdot P_{\text{ptm}} \cdot \left( \alpha_{\text{TM}} \cdot \frac{\lambda^2}{\pi \cdot L_{\text{ptm}}^2} \cdot \text{BRDF}_{\text{wall}} \cdot \cos(\theta_{\text{ptm}}) \right)$$

$$P_{\text{ptmifo}} = 1.21 \times 10^{-19}$$

SUS ring around TM, W

$$P_{\text{rtmifo}} := \sqrt{4} \cdot P_{\text{rtm}} \cdot \left( \alpha_{\text{TM}} \cdot \frac{\lambda^2}{\pi \cdot L_{\text{rtm}}^2} \cdot \text{BRDF}_{\text{wall}} \cdot \cos(\theta_{\text{rtm}}) \right)$$

$$P_{\text{rtmifo}} = 1.433 \times 10^{-19}$$

TOTAL SUS, W

$$P_{\text{susifo}} := \left( P_{\text{ptmifo}}^2 + P_{\text{rtmifo}}^2 \right)^{0.5}$$

$$P_{\text{susifo}} = 1.875 \times 10^{-19}$$

TOTAL WIDE ANGLE BAF PLATE  
 ITMX, W

$$P_{\text{wabptifo}} := \left( P_{\text{wabp1ifo}}^2 + P_{\text{wabp2ifo}}^2 + P_{\text{wabp3ifo}}^2 + P_{\text{wabp4ifo}}^2 \right)^{0.5}$$

$$P_{\text{wabptifo}} = 3.66 \times 10^{-21}$$

UPPER BSC, W

$$P_{\text{upbscifo}} := \sqrt{4} \cdot P_{\text{upbsc}} \cdot \left( \alpha_{\text{TM}} \cdot \frac{\lambda^2}{\pi \cdot L_{\text{upbsc}}^2} \cdot \text{BRDF}_{\text{wall}} \cdot \cos(\theta_{\text{upbsc}}) \right)$$

$$P_{\text{upbscifo}} = 7.465 \times 10^{-22}$$

FLOOR BSC, W

$$P_{\text{floorbscifo}} := \sqrt{4} \cdot P_{\text{floor}} \cdot \left( \alpha_{\text{TM}} \cdot \frac{\lambda^2}{\pi \cdot L_{\text{floorbsc}}^2} \cdot \text{BRDF}_{\text{wall}} \cdot \cos(\theta_{\text{floorbsc}}) \right)$$

$$P_{\text{floorbscifo}} = 1.089 \times 10^{-20}$$

SPOOL, W

$$P_{\text{spoolifo}} := \sqrt{4} \cdot P_{\text{spool}} \cdot \left( \alpha_{\text{TM}} \cdot \frac{\lambda^2}{\pi \cdot L_{\text{spool}}^2} \cdot \text{BRDF}_{\text{wall}} \cdot \cos(\theta_{\text{spool}}) \right)$$

$$P_{\text{spoolifo}} = 4.91 \times 10^{-20}$$

MANIFOLD, W

$$P_{\text{maniifo}} := \sqrt{4} \cdot P_{\text{mani}} \cdot \left( \alpha_{\text{TM}} \cdot \frac{\lambda^2}{\pi \cdot L_{\text{mani}}^2} \cdot \text{BRDF}_{\text{wall}} \cdot \cos(\theta_{\text{mani}}) \right)$$

$$P_{\text{maniifo}} = 7.705 \times 10^{-21}$$

MANIFOLD FLAT  
BAF, W

$$P_{\text{maniflatifo}} := \sqrt{2} \cdot P_{\text{maniflat}} \cdot \left( \alpha_{\text{TM}} \cdot \frac{\lambda^2}{\pi \cdot L_{\text{maniflat}}^2} \cdot \text{BRDF}_{\text{bd}} \cdot \cos(\theta_{\text{maniflat}}) \right)$$

$$P_{\text{maniflatifo}} = 8.001 \times 10^{-21}$$

**DISPLACEMENT NOISE @ 100 Hz, m/rtHz**

$$\theta_t := 0 \quad x_s := 1$$

Displacement Noise Requirement @ 100 Hz, m/rt Hz

$$D_{\text{req}} = 1 \times 10^{-21}$$

$$DN_s := TF_{\text{itmhr}} \cdot \left( \frac{P_{\text{sTMifo}}}{P_{\text{psl}}} \right)^{0.5} \cdot \frac{2 \cdot k \cdot x_s}{\sqrt{2}}$$

**Wide Angle Baffle top**

$$DN_{\text{wabtop}} := TF_{\text{itmhr}} \cdot \left( \frac{P_{\text{wabtopifo}}}{P_{\text{psl}}} \right)^{0.5} \cdot x_{\text{ACB}} \cdot \frac{2}{\sqrt{2}} \cdot k$$

$$DN_{\text{wabtop}} = 3.844 \times 10^{-25}$$

**Wide Angle Baffle bottom**

$$DN_{\text{wabbot}} := TF_{\text{itmhr}} \cdot \left( \frac{P_{\text{wabbotifo}}}{P_{\text{psl}}} \right)^{0.5} \cdot x_{\text{ACB}} \cdot \frac{2}{\sqrt{2}} \cdot k$$

$$DN_{\text{wabbot}} = 1.16 \times 10^{-24}$$

**Wide Angle Baffle Sides**

$$DN_{\text{wabst}} := TF_{\text{itmhr}} \cdot \left( \frac{P_{\text{wabstifo}}}{P_{\text{psl}}} \right)^{0.5} \cdot x_{\text{ACB}} \cdot \frac{2}{\sqrt{2}} \cdot k$$

$$DN_{\text{wabst}} = 1.24 \times 10^{-24}$$

### Wide Angle Plate Total

$$DN_{\text{wabpt}} := TF_{\text{itmhr}} \cdot \left( \frac{P_{\text{wabptifo}}}{P_{\text{psl}}} \right)^{0.5} \cdot x_{\text{manifold}} \cdot \frac{2}{\sqrt{2}} \cdot k$$

$$DN_{\text{wabpt}} = 3.977 \times 10^{-24}$$

### SUS

$$DN_{\text{sus}} := TF_{\text{itmhr}} \cdot \left( \frac{P_{\text{susifo}}}{P_{\text{psl}}} \right)^{0.5} \cdot x_{\text{ISI}} \cdot \frac{2}{\sqrt{2}} \cdot k$$

$$DN_{\text{sus}} = 1.067 \times 10^{-26}$$

### ACB BACK

$$DN_{\text{acb}} := TF_{\text{itmhr}} \cdot \left( \frac{P_{\text{acbifo}}}{P_{\text{psl}}} \right)^{0.5} \cdot x_{\text{ACB}} \cdot \frac{2}{\sqrt{2}} \cdot k$$

$$DN_{\text{acb}} = 6.879 \times 10^{-25}$$

### ACB BACK & BOX

$$DN_{\text{acb\_box}} := TF_{\text{itmhr}} \cdot \left( \frac{P_{\text{wacbboxifo}}}{P_{\text{psl}}} \right)^{0.5} \cdot x_{\text{ACB}} \cdot \frac{2}{\sqrt{2}} \cdot k$$

$$DN_{\text{acb\_box}} = 1.45 \times 10^{-24}$$

### Upper BSC

$$DN_{\text{upbsc}} := TF_{\text{itmhr}} \cdot \left( \frac{P_{\text{upbscifo}}}{P_{\text{psl}}} \right)^{0.5} \cdot x_{\text{manifold}} \cdot \frac{2}{\sqrt{2}} \cdot k$$

$$DN_{\text{upbsc}} = 1.796 \times 10^{-24}$$

**Floor BSC**

$$DN_{\text{floorbsc}} := TF_{\text{itmhr}} \cdot \left( \frac{P_{\text{floorbscifo}}}{P_{\text{psl}}} \right)^{0.5} \cdot x_{\text{manifold}} \cdot \frac{2}{\sqrt{2}}$$

$$DN_{\text{floorbsc}} = 6.858 \times 10^{-24}$$

**Spoolpiece**

$$DN_{\text{spool}} := TF_{\text{itmhr}} \cdot \left( \frac{P_{\text{spoolifo}}}{P_{\text{psl}}} \right)^{0.5} \cdot x_{\text{manifold}} \cdot \frac{2}{\sqrt{2}} \cdot k$$

$$DN_{\text{spool}} = 1.456 \times 10^{-23}$$

**Manifold**

$$DN_{\text{mani}} := TF_{\text{itmhr}} \cdot \left( \frac{P_{\text{maniifo}}}{P_{\text{psl}}} \right)^{0.5} \cdot x_{\text{manifold}} \cdot \frac{2}{\sqrt{2}} \cdot k$$

$$DN_{\text{mani}} = 5.77 \times 10^{-24}$$

**Manifold Flat Baf**

$$DN_{\text{maniflat}} := TF_{\text{itmhr}} \cdot \left( \frac{P_{\text{maniflatifo}}}{P_{\text{psl}}} \right)^{0.5} \cdot x_{\text{manifold}} \cdot \frac{2}{\sqrt{2}}$$

$$DN_{\text{maniflat}} = 5.879 \times 10^{-24}$$

**DIFFUSE SCATTERING FROM PEEK AND CABLING**

length of cabling, m

$$l_c := 2$$

diameter of cabling, m

$$d_c := 0.006$$

frontal area of cabling, m<sup>2</sup>

$$A_c := l_c \cdot d_c = 0.012$$

diameter of peek end cap, m

$$d_{pc} := .025$$

number of peek end caps

$$N_{pc} := 4$$

total area of scattering surfaces, m<sup>2</sup>

$$A_{tpc} := A_c + N_{pc} \cdot \frac{\pi}{4} \cdot d_{pc}^2$$

$$A_{tpc} = 0.014$$

frontal area of ACB, m<sup>2</sup>

$$A_{acb} := 0.7$$

### Incident Power, W

PEEK AND CABLING, W

$$P_{ipc} := P_a \cdot PF_{acb} \cdot \frac{A_{tpc}}{A_{acb}} \cdot \alpha_{TM} = 0.044$$

### Power Scattered into IFO Mode, W

PEEK AND CABLING, W

$$P_{pcifo} := \sqrt{4} \cdot P_{ipc} \cdot \left( \alpha_{TM} \cdot \frac{\lambda^2}{\pi \cdot L_{acb}^2} \cdot BRDF_{wall} \cdot \cos(\theta_{acb}) \right)$$

$$P_{pcifo} = 4.66 \times 10^{-20}$$

### Displacement Noise @ 100 Hz, m/rHz

PEEK AND CABLING, W

$$DN_{pc} := TF_{itmhr} \cdot \left( \frac{P_{pcifo}}{P_{psl}} \right)^{0.5} \cdot x_{ACB} \cdot \frac{2}{\sqrt{2}} \cdot k$$

$$DN_{pc} = 1.774 \times 10^{-25}$$

H:\ADLIGO\SLC\Arm Cavity Baffle  
\T1300406\_ITM\_wide-  
angle\_scatter\_AC\_ZEMAX.xmcd



k

k