LASER INTERFEROMETER GRAVITATIONAL WAVE OBSERVATORY - LIGO -CALIFORNIA INSTITUTE OF TECHNOLOGY MASSACHUSETTS INSTITUTE OF TECHNOLOGY

Technical Note LIGO

LIGO-T13003-28-v3

2013/05/14

aLIGO DRMI Sensing Matrices

Lisa Barsotti, Anamaria Effler, Matt Evans, Kiwamu Izumi

This is an internal working note of the LIGO project

California Institute of Technology LIGO Project, MS 18-34 Pasadena, CA 91125 Phone (626) 395-2129 Fax (626) 304-9834 E-mail: info@ligo.caltech.edu

LIGO Hanford Observatory Route 10, Mile Marker 2 Richland, WA 99352 Phone (509) 372-8106 Fax (509) 372-8137 E-mail: info@ligo.caltech.edu Massachusetts Institute of Technology LIGO Project, Room NW17-161 Cambridge, MA 02139 Phone (617) 253-4824 Fax (617) 253-7014 E-mail: info@ligo.mit.edu

> LIGO Livingston Observatory 19100 LIGO Lane Livingston, LA 70754 Phone (225) 686-3100 Fax (225) 686-7189 E-mail: info@ligo.caltech.edu

1 Intro

The purpose of this document is to calculate the length sensing matrices for a few different configurations for the DRMI test at LLO (which should also match the DRMI sensing matrix at LHO). We look at four in particular, DRMI and PRMI, sideband locked and carrier locked. For the purpose of full interferometer locking, the DRMI sideband lock is the necessary configuration.



Figure 1: Diagram of DRMI Model Parameters (not to scale)

Fig. 1 shows the optical parameters used in this calculation. Table 1 shows the common parameters used for all the calculations. We use 5W input power as a reasonable starting point for DRMI commissioning. At each port, there may be RFPDs both in air and in vacuum looking at the same signal, comparable in size.

The modeling doesn't take into account mode matching or contrast defect, so there will be inaccuracies associated with that, especially an underestimate of the DC powers and signal strength at the AS port.

| Input Power | REFL PO | POP PO | AS PO | OMC/AS Split | $\gamma_1 = \gamma_2$ |
|-------------|---------|--------|-------|--------------|-----------------------|
| 5W | 1.25% | 12.5% | 1.25% | 90/10 | 0.1 |

Table 1: Common parameters for all calculations

2 Sensing Matrices

For each configuration we calculate the DC powers reaching our PDs (attenuated), then the RF DC powers at various points in the optical configuration (not attenuated). These tables can be used to initially gauge if we want to change the attenuation level at some port to optimize our sensing. Then we show the sensing matrix for each RFPD I and Q signals, in table form and radar-plot form. In green we point out the elements to be used in the readout scheme.

Script to produce these can be found in the cvs mit iscmodeling repository at *iscmodeling/LentickleAligo/DRMI/*.

2.1 DRMI Carrier Locked

| DC Powers at Ports | | | | |
|--------------------|--------|--|--|--|
| REFL DC | 7.8mW | | | |
| POP DC | 9.1mW | | | |
| AS DC | 26nW | | | |
| OMC DC | 230 nW | | | |

Table 2: Table of the attenuated powers at our ports (carrier lock).

| RF Powers in important places in DRMI | | | | | | |
|---------------------------------------|--------|--------|--------|--------|---------|--------|
| Freq | INPUT | REFL | PRC | SRC | OMC IN | OMC |
| +f2 | 12.4mW | 12.4mW | 91.3uW | 13.7uW | 4.3uW | 13.2nW |
| +f1 | 12.4mW | 12.4mW | 93.8uW | 7.44nW | 2.3nW | 0.12nW |
| carrier | 4.95 W | 0.575W | 290W | 0.73uW | 0.23 uW | 23uW |
| -f1 | 12.4mW | 12.4mW | 93.8uW | 7.44nW | 2.3nW | 0.12nW |
| -f2 | 12.4mW | 12.4mW | 91.3uW | 13.7uW | 4.3uW | 13.2nW |

Table 3: Table of RF DC powers in various places of DRMI.

DRMI Carrier Lock



Figure 2: Radar representation of the sensing matrix: MICH blue, PRCL red, SRCL green.

| Sensing Matrix in W/m | | | | | | |
|-----------------------|------|---------------------|-------|--|--|--|
| Probe | MICH | PRCL | SRCL | | | |
| REFL 9I | 115 | 4.3×10^{6} | 38 | | | |
| REFL 9Q | 106 | 2 | 4 | | | |
| REFL 45I | 330 | 4.3×10^{6} | 68 | | | |
| REFL 45Q | 599 | 51 | 2 | | | |
| POP 9I | 0.5 | 5330 | 0.08 | | | |
| POP 9Q | 0.2 | 56 | 0.005 | | | |
| POP 45I | 2 | 5250 | 7 | | | |
| POP 45Q | 43 | 272 | 0.3 | | | |
| AS 45I | 0.01 | 0.9 | 0.4 | | | |
| AS 45Q | 3270 | 1 | 0.01 | | | |
| REFL 27I | 627 | 2.84×10^4 | 17 | | | |
| REFL 27Q | 75 | 1 | 1 | | | |
| REFL 135I | 3 | 144 | 80 | | | |
| REFL 135Q | 236 | 0.02 | 1 | | | |

Table 4: Sensing matrix for carrier lock.

2.2 DRMI sideband locked

| DC Powers at Ports | | |
|--------------------|-------|--|
| REFL DC | 62mW | |
| POP DC | 56uW | |
| AS DC | 20uW | |
| OMC DC | 456nW | |

Table 5: Table of the attenuated powers at our ports (sideband lock).

| RF Powers in important places in DRMI | | | | | | |
|---------------------------------------|--------|-------|-------|------|--------|-------|
| Freq | INPUT | REFL | PRC | SRC | OMC IN | OMC |
| +f2 | 12.4mW | 1.8mW | 152mW | 23mW | 7.2mW | 22uW |
| +f1 | 12.4mW | 1.4mW | 726mW | 58uW | 18uW | 890nW |
| carrier | 4.95 W | 4.95W | 37mW | 94pW | 30pW | 3nW |
| -f1 | 12.4mW | 1.4mW | 726mW | 58uW | 18uW | 890nW |
| -f2 | 12.4mW | 1.8mW | 152mW | 23mW | 7.2mW | 22uW |

Table 6: Table of RF DC powers in various places of DRMI (sideband lock).

DRMI Sideband Lock





Figure 3: Radar representation of the sensing matrix: MICH blue, PRCL red, SRCL green.

| Sensing Matrix in W/m | | | | | |
|-----------------------|---------------------|---------------------|---------------------|--|--|
| Probe | MICH | PRCL | SRCL | | |
| REFL 9I | 2.1×10^4 | 4.3×10^{6} | 817 | | |
| REFL 9Q | 8080 | 58 | 23 | | |
| REFL 45I | 2970 | 9.1×10^5 | 1.1×10^{5} | | |
| REFL 45Q | 6.4×10^{5} | 17 | 910 | | |
| POP 9I | 27 | 5340 | 1 | | |
| POP 9Q | 10 | 83 | 0.01 | | |
| POP 45I | 57 | 1110 | 136 | | |
| POP 45Q | 803 | 84 | 9 | | |
| AS 45I | 0.02 | 6 | 0.7 | | |
| AS 45Q | 1520 | 0.5 | 0.07 | | |
| REFL 27I | 537 | 2.4×10^4 | 125 | | |
| REFL 27Q | 918 | 1 | 10 | | |
| REFL 135I | 3 | 1140 | 136 | | |
| REFL 135Q | 801 | 0.02 | 1 | | |

 Table 7: Sensing matrix for sideband lock.

2.3 PRMI Carrier Locked (with SRM misaligned)

| DC Powers at Ports | | | | |
|--------------------|-------|--|--|--|
| REFL DC | 7.8mW | | | |
| POP DC | 9mW | | | |
| AS DC | 20nW | | | |
| OMC DC | 9nW | | | |

Table 8: Table of the attenuated powers at our ports.

| RF Powers in important places in DRMI | | | | | | | |
|---------------------------------------|--------|--------|--------|-------|--------|-------|--|
| Freq | INPUT | REFL | PRC | SRC | OMC IN | OMC | |
| +f2 | 12.4mW | 12.4mW | 93.5uW | 546nW | 172nW | 0.5nW | |
| +f1 | 12.4mW | 12.4mW | 93.8uW | 22nW | 7nW | 0.3nW | |
| carrier | 4.95 W | 575mW | 290W | 29nW | 9nW | 912nW | |
| -f1 | 12.4mW | 12.4mW | 93.8uW | 22nW | 7nW | 0.3nW | |
| -f2 | 12.4mW | 12.4mW | 93.5uW | 546nW | 172nW | 0.5nW | |

Table 9: Table of RF DC powers in various places of PRMI.

PRMI Carrier Locked





Figure 4: Radar representation of the sensing matrix: MICH blue, PRCL red.

| Sensing Matrix in W/m | | | | | |
|-----------------------|------|---------------------|--|--|--|
| Probe | MICH | PRCL | | | |
| REFL 9I | 33 | 4.3×10^{6} | | | |
| REFL 9Q | 152 | $1.4 x 10^4$ | | | |
| REFL 45I | 41 | 4.3×10^{6} | | | |
| REFL 45Q | 824 | 8.1×10^4 | | | |
| POP 9I | 0.04 | 5330 | | | |
| POP 9Q | 0.7 | 55 | | | |
| POP 45I | 0.1 | 5320 | | | |
| POP 45Q | 3 | 274 | | | |
| AS 45I | 2.6 | 0.5 | | | |
| AS 45Q | 65.4 | 0.007 | | | |
| REFL 27I | 43.8 | 2.66×10^4 | | | |
| REFL 27Q | 279 | 3340 | | | |
| REFL 135I | 106 | 1890 | | | |
| REFL 135Q | 146 | 1370 | | | |

Table 10: Sensing matrix (PRMI carrier lock).

2.4 PRMI Sideband Locked (with SRM misaligned)

| DC Powers at Ports | | | |
|--------------------|-------|--|--|
| REFL DC | 62mW | | |
| POP DC | 82uW | | |
| AS DC | 3uW | | |
| OMC DC | 0.1uW | | |

Table 11: Table of the attenuated powers at our ports.

| RF Powers in important places in DRMI | | | | | | |
|---------------------------------------|--------|-------|--------|-------|--------|-------|
| Freq | INPUT | REFL | PRC | SRC | OMC IN | OMC |
| +f2 | 12.4mW | 445uW | 569mW | 3.3mW | 1mW | 3uW |
| +f1 | 12.4mW | 1.4mW | 719mW | 168uW | 53uW | 2.6uW |
| carrier | 4.95 W | 575mW | 37.4mW | 3.7pW | 1pW | 118pW |
| -f1 | 12.4mW | 1.4mW | 719mW | 168uW | 53uW | 2.6uW |
| -f2 | 12.4mW | 445uW | 569mW | 3.3mW | 1mW | 3uW |

Table 12: Table of RF DC powers in various places of PRMI.

PRMI Sideband Locked





Figure 5: Radar representation of the sensing matrix: MICH blue, PRCL red.

| Sensing Matrix in W/m | | |
|-----------------------|----------------------|---------------------|
| Probe | MICH | PRCL |
| REFL 9I | 414 | 4.3×10^{6} |
| REFL 9Q | 3.27×10^4 | $5x10^{4}$ |
| REFL 45I | 2460 | 3.4×10^{6} |
| REFL 45Q | 1.30×10^{5} | 6.4×10^4 |
| POP 9I | 0.8 | 5280 |
| POP 9Q | 41 | 99 |
| POP 45I | 14.5 | 4150 |
| POP 45Q | 162 | 372 |
| AS 45I | 3.4 | 0.9 |
| AS 45Q | 58 | 0.04 |
| REFL 27I | 42 | 2.66×10^4 |
| REFL 27Q | 269 | 3340 |
| REFL 135I | 92 | 3470 |
| REFL 135Q | 132 | 2420 |

Table 13: Sensing matrix (PRMI sideband lock).