

*LIGO Laboratory / LIGO Scientific Collaboration*

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**LCGT**  
**bLCGT Recycling Cavity Baffles Conceptual Design**

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LIGO Scientific Collaboration

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T1200176 LCGT- AOS

**Table of Contents**

<b>1</b>	<b>INTRODUCTION.....</b>	<b>5</b>
<b>1.1</b>	<b>Applicable Documents.....</b>	<b>5</b>
<b>2</b>	<b>WEDGE ANGLES.....</b>	<b>5</b>
<b>3</b>	<b>RECYCLING CAVITY BAFFLES.....</b>	<b>5</b>
<b>3.1</b>	<b>Power Recycling Cavity.....</b>	<b>5</b>
3.1.1	PR3.....	5
3.1.2	PR2.....	6
3.1.3	PRM.....	8
<b>3.2</b>	<b>Signal Recycling Cavity.....</b>	<b>9</b>
3.2.1	SR3.....	9
3.2.2	SR2.....	10
3.2.3	SRM.....	11
3.2.4	Output Faraday Isolator.....	11
3.2.5	Output Mode Cleaner.....	12
<b>3.3</b>	<b>Baffle Characteristics.....</b>	<b>13</b>
<b>3.4</b>	<b>Stray Light Noise.....</b>	<b>14</b>
3.4.1	Seismic Motion.....	14
3.4.2	OFI and OMC Suspension Transmissibility.....	15
3.4.3	Beam Dump Surface BRDF.....	16
3.4.4	Recycling Cavity Baffles Scatter.....	17
3.4.4.1	DARM Motion Transfer Functions.....	17
3.4.4.2	PRM Scatter.....	18
3.4.4.3	PR2 Scatter.....	23
3.4.4.4	PR3 Scatter.....	25
3.4.4.5	BS Ghost Beams and SR2 HR Scatter.....	28
3.4.4.6	ITM Ghost Beams Scatter.....	31
3.4.4.7	SRM Scatter.....	33
3.4.4.8	SR2 Scatter.....	35
3.4.4.9	SR3 Scatter.....	38
3.4.4.10	Output Faraday Isolator (OFI) Scatter.....	41
<b>3.5</b>	<b>Optical Interfaces.....</b>	<b>44</b>
<b>4</b>	<b>INTERFACE CONTROL DOCUMENT.....</b>	<b>45</b>

**Table of Figures**

<i>Figure 1: PR3 HR and PR3AR Baffles; POY Pick-off Beam.....</i>	<i>6</i>
<i>Figure 2: PR2 HR, PR2 Scraper Baffle, POB Pick-off Beam.....</i>	<i>7</i>
<i>Figure 3: PRM HR and AR Baffles.....</i>	<i>8</i>
<i>Figure 4: SR3 HR and AR Baffles.....</i>	<i>9</i>
<i>Figure 5: SR2 Scraper Baffle, SR2AR Baffle; POX Pick-off Beam.....</i>	<i>10</i>
<i>Figure 6: SRM, SRM AR Baffles.....</i>	<i>11</i>
<i>Figure 7: Output Faraday Isolator, MMT2 OMC.....</i>	<i>12</i>

*Figure 8: Output Mode Cleaner, MMT1 OMC* ..... 13

*Figure 9: Seismic Ground Noise, m/rtHz* ..... 14

*Figure 10: OFI Transmissibility along beam axis*..... 15

*Figure 11: DARM motion transfer functions*..... 17

**Figure 12: PRM Ghost Beam Scatter** ..... 22

*Figure 13: PR2 Ghost Beam Scatter* ..... 25

*Figure 14: PR3 Ghost Beam Scatter* ..... 28

*Figure 15: BS and SR2 Ghost beams Scatter* ..... 30

*Figure 16: ITM Ghost Beam Scatter* ..... 32

*Figure 17: SRM Ghost Beam Scatter* ..... 35

*Figure 18: SR2 Ghost Beam Scatter*..... 38

*Figure 19: SR3 Ghost Beam Scatter*..... 41

*Figure 20: OFI, OMC, OMC Repl, and output PD scatter*..... 44

## **1 INTRODUCTION**

This document presents a conceptual design for the bLCGT Recycling Cavity Baffles.

### **1.1 Applicable Documents**

## **2 WEDGE ANGLES**

The ITM and BS wedge angles determine the positions of the recycling cavity baffles.

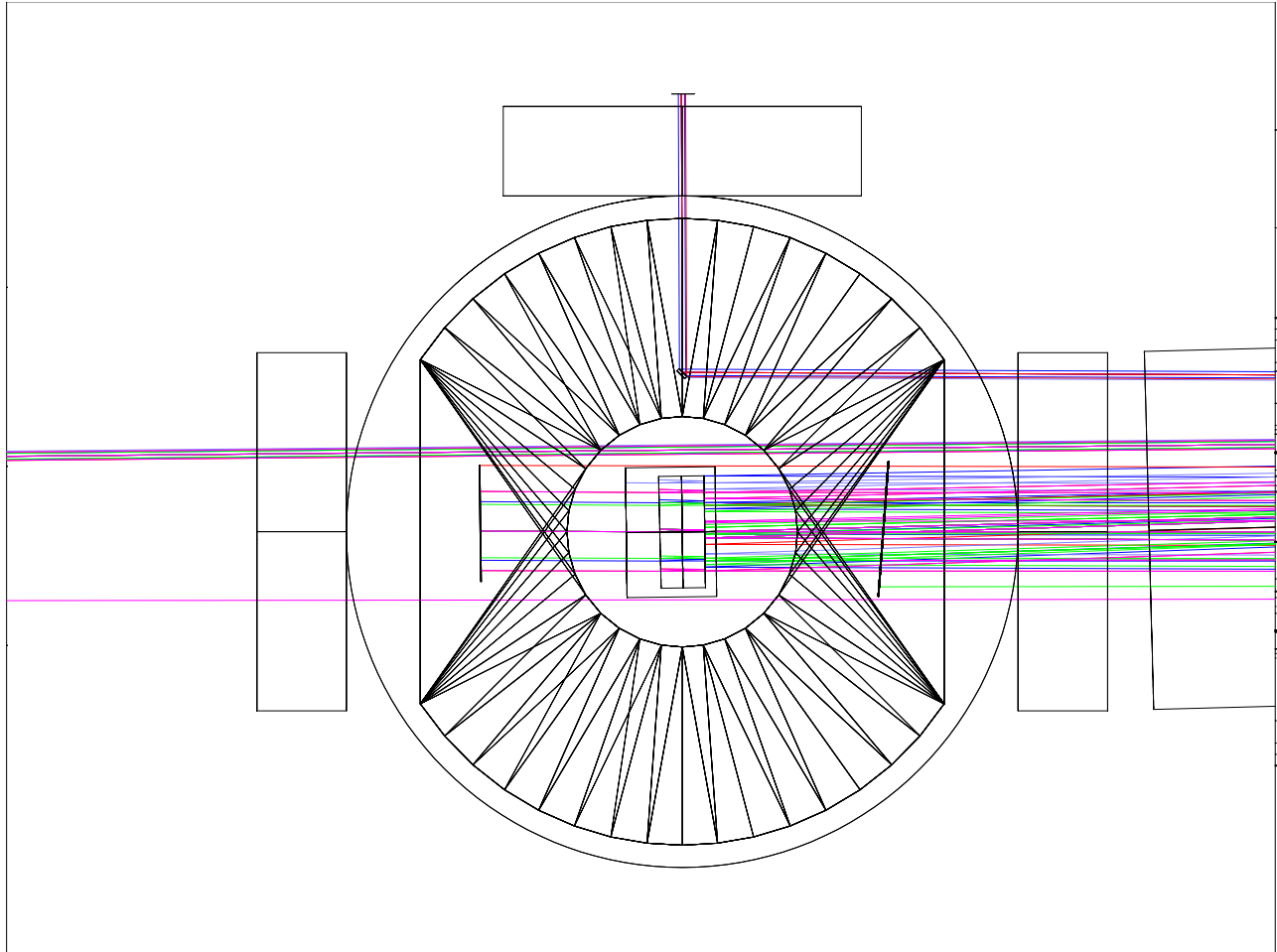
The symmetric BS wedge angle = 0.050 deg is chosen so that the POX beam, which reflects from the AT surface of the BS, will hit the SR3 HR surface and separate from the main IFO beam at the vicinity of SR2, where the POX pick-off mirror will be located. The thick side of the BS mirror faces toward the arms of the IFO.

The ITM wedge angle = 0.025 deg is chosen so that the ITMY GBAR3 hits the PR3 mirror. The thick side of ITMX faces in the  $-Y$  direction; the thick side of ITMY faces in the  $+X$  direction

## **3 RECYCLING CAVITY BAFFLES**

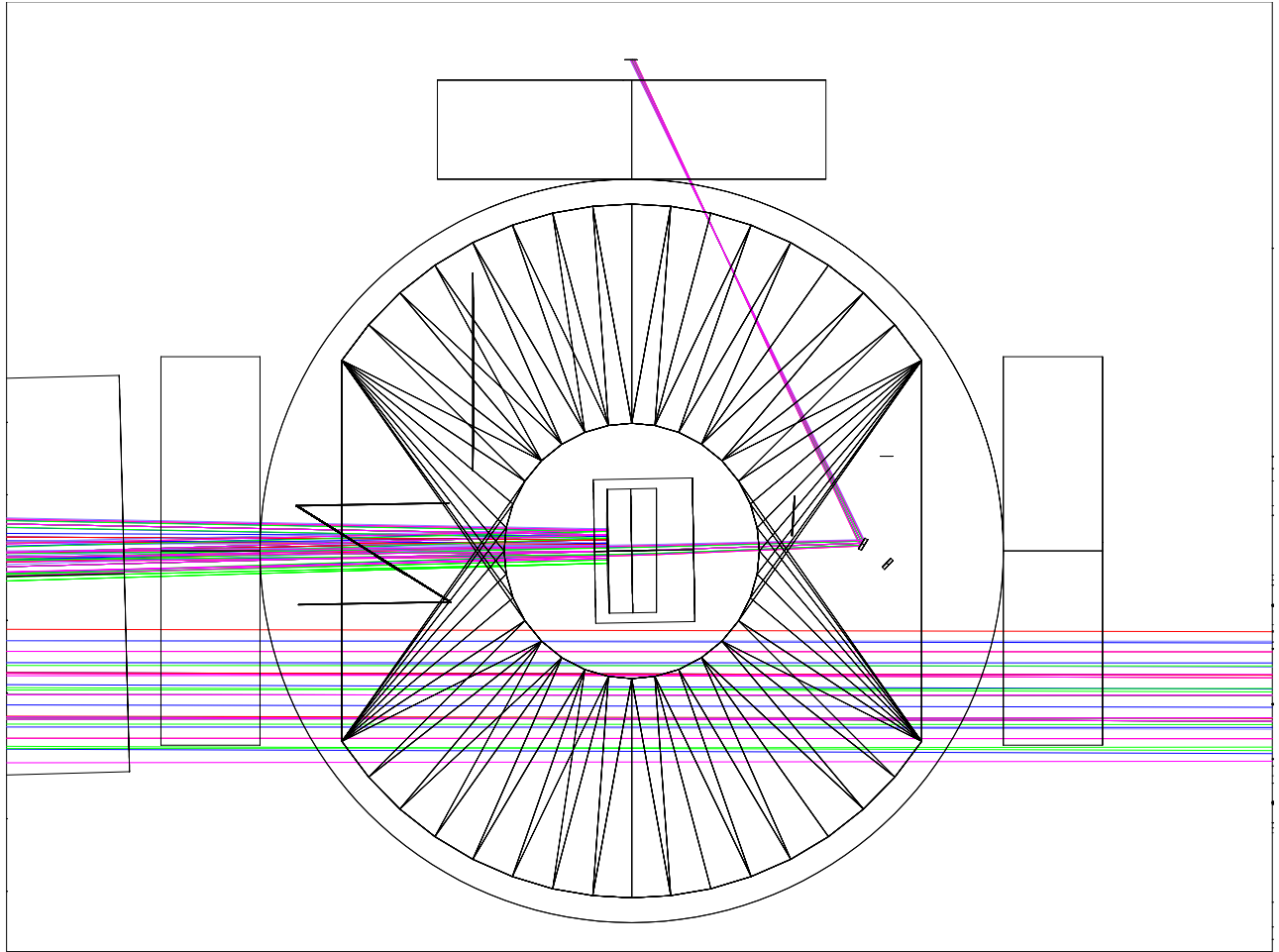
### **3.1 Power Recycling Cavity**

#### **3.1.1 PR3**



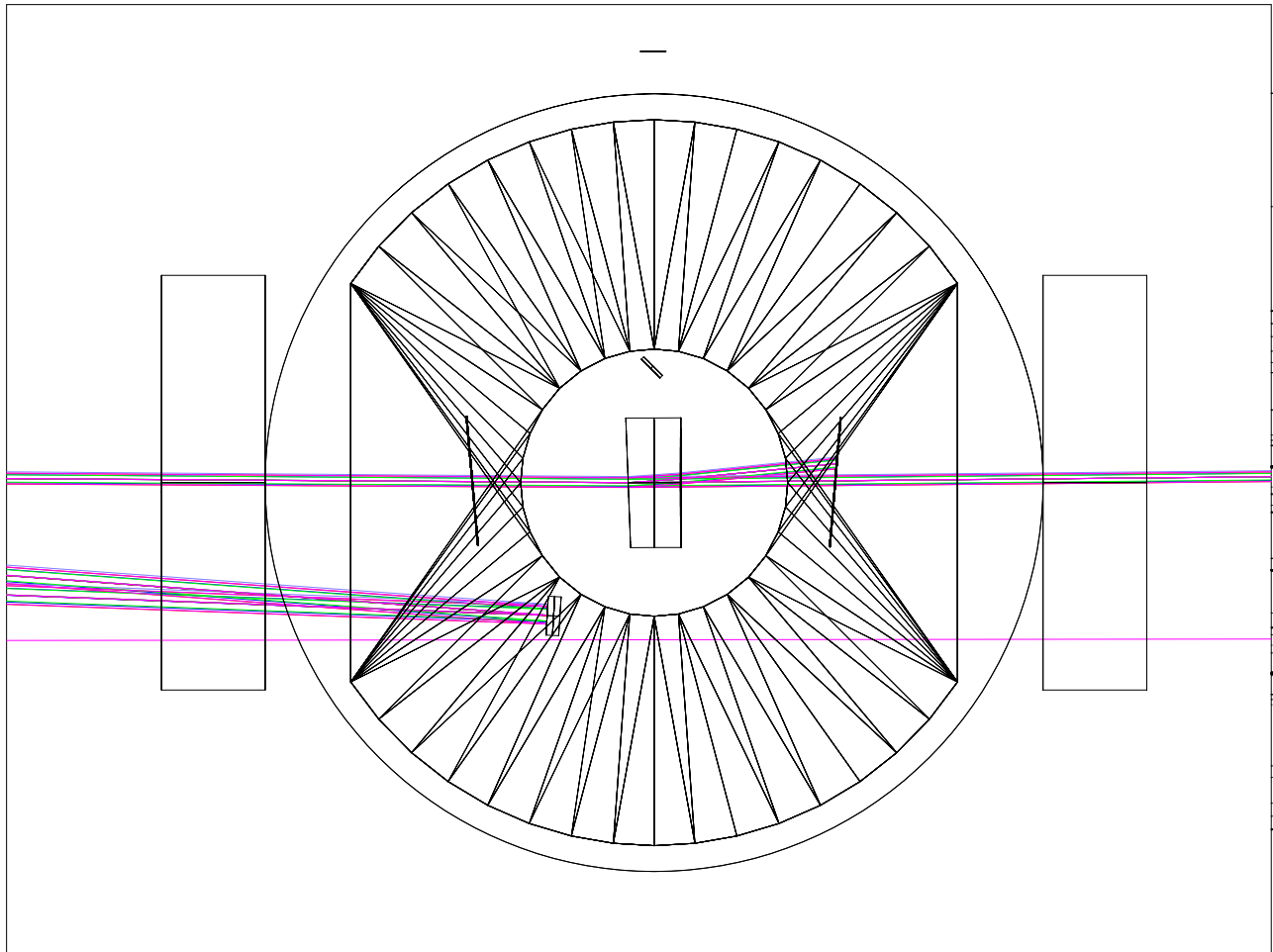
**Figure 1: PR3 HR and PR3AR Baffles; POY Pick-off Beam**

### 3.1.2 PR2



**Figure 2: PR2 HR, PR2 Scraper Baffle, POB Pick-off Beam**

### 3.1.3 PRM

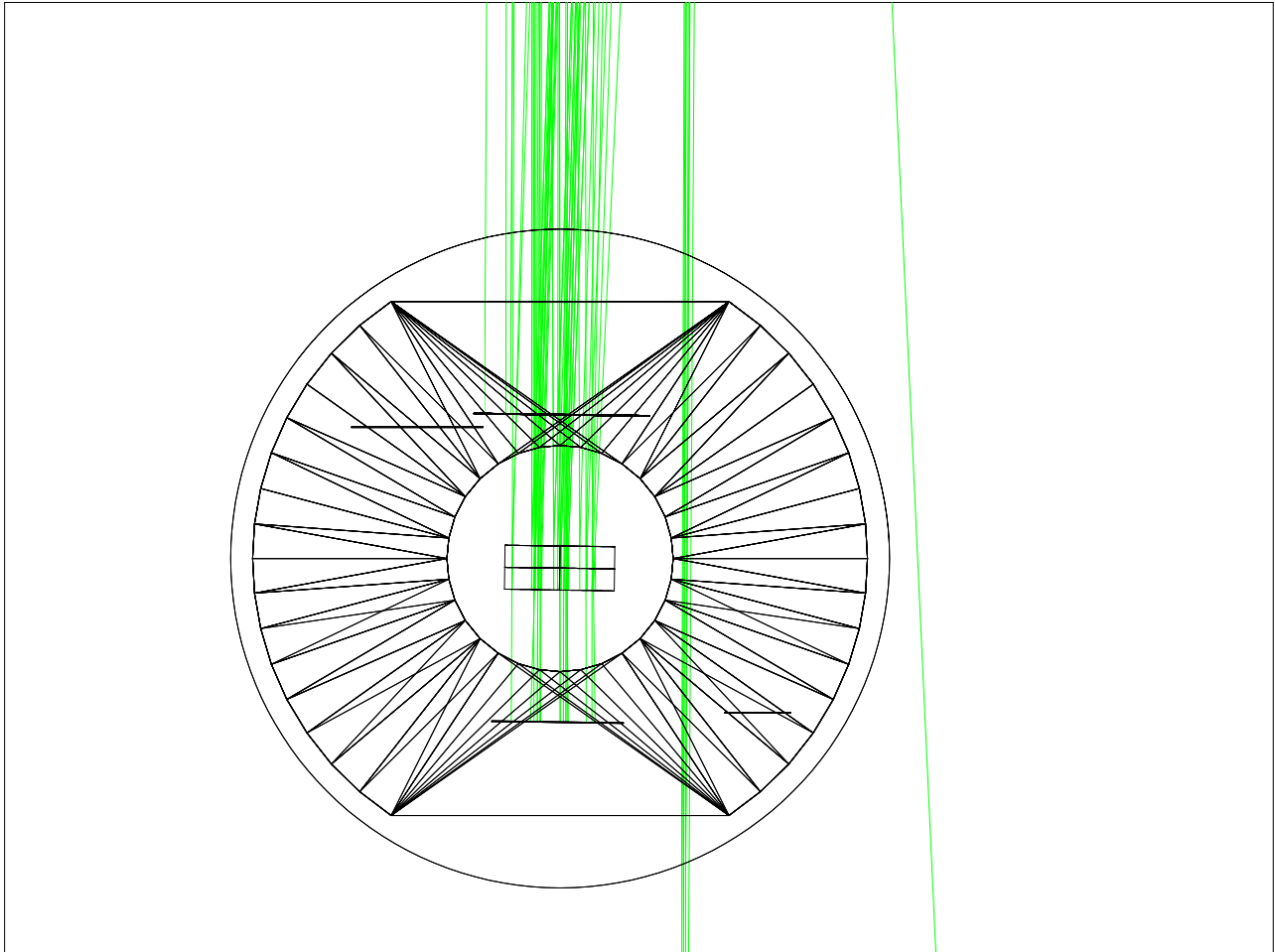


**Figure 3: PRM HR and AR Baffles**



## 3.2 Signal Recycling Cavity

### 3.2.1 SR3



**Figure 4: SR3 HR and AR Baffles**

3.2.2 SR2

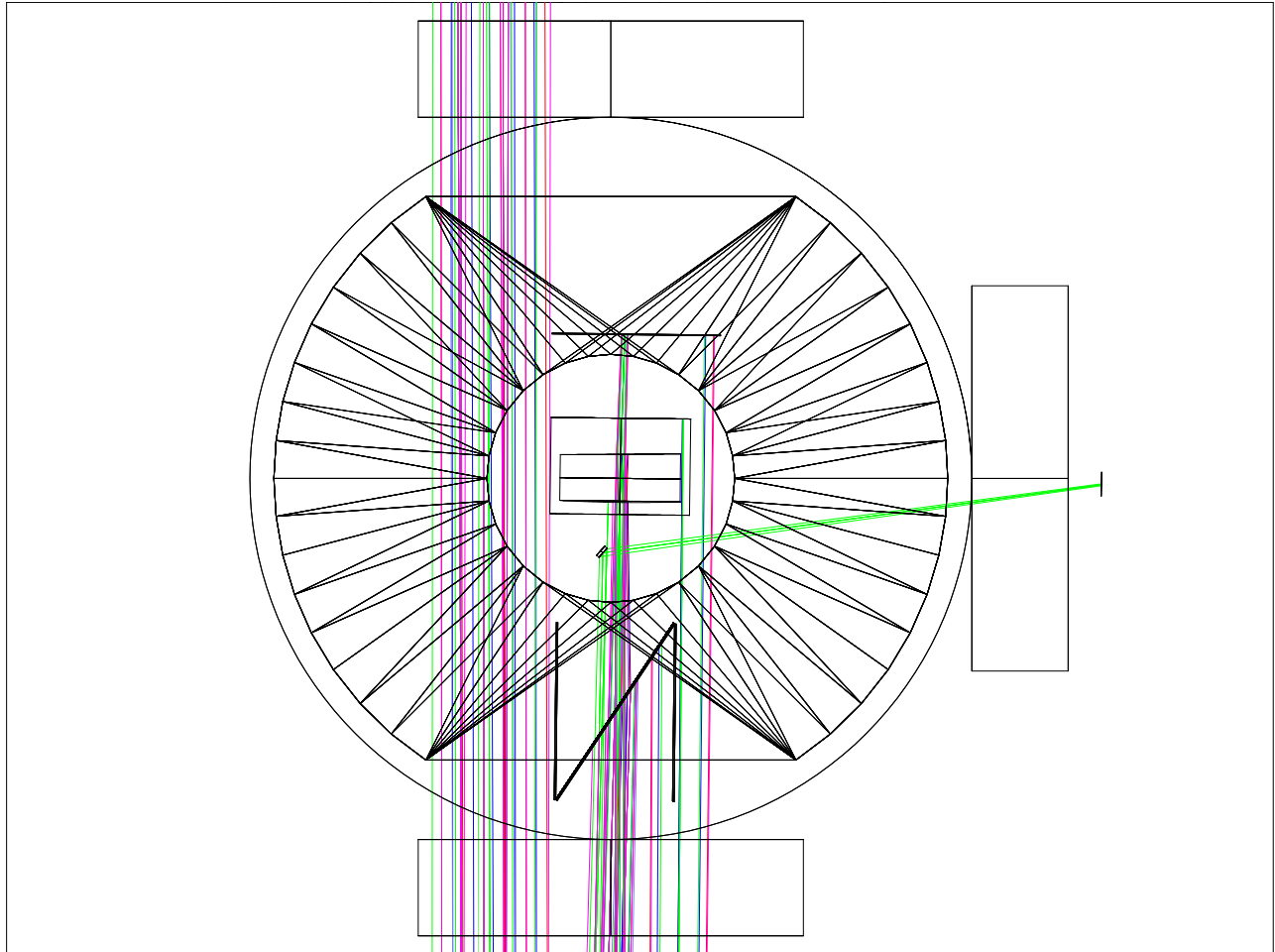
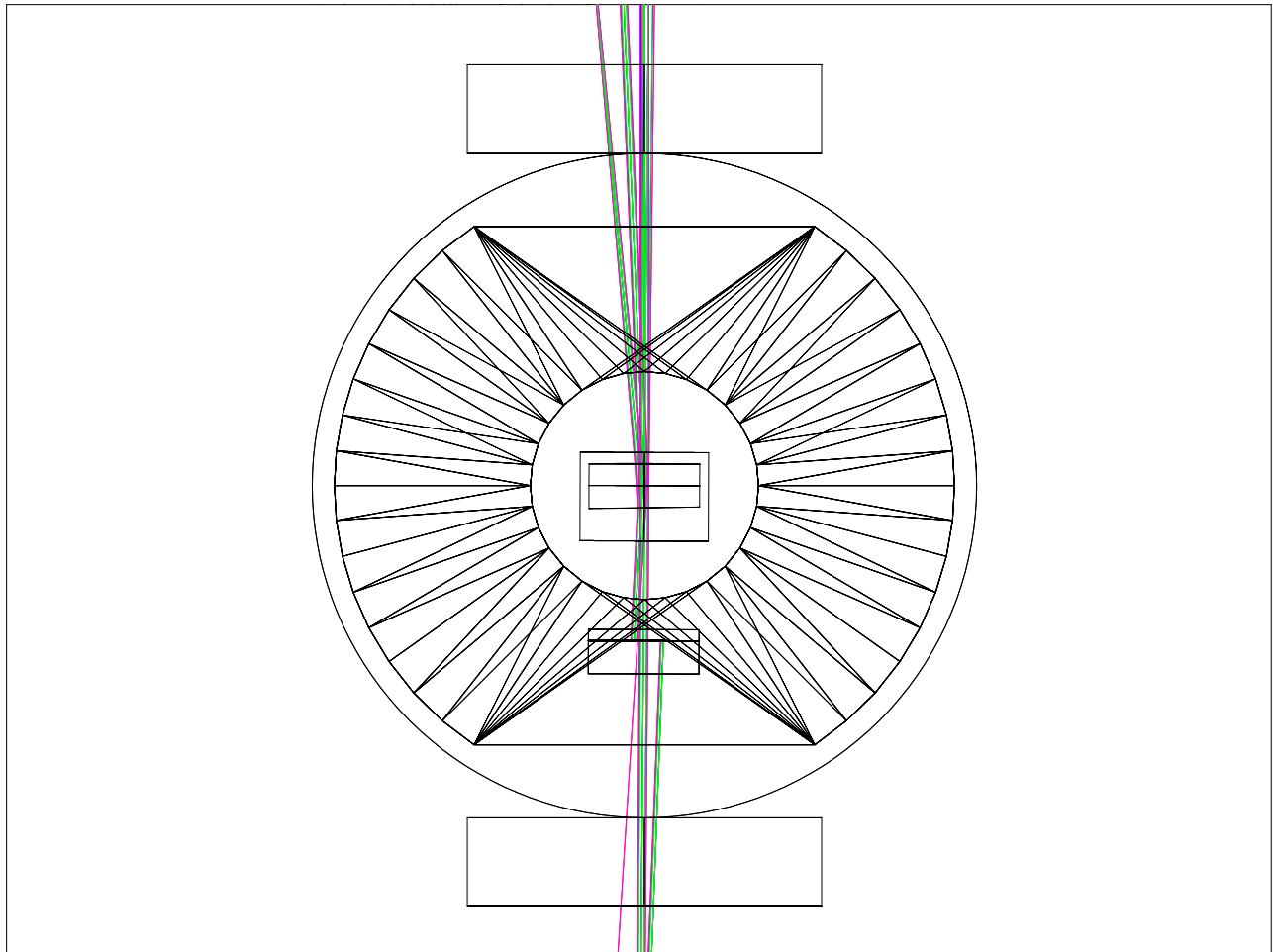


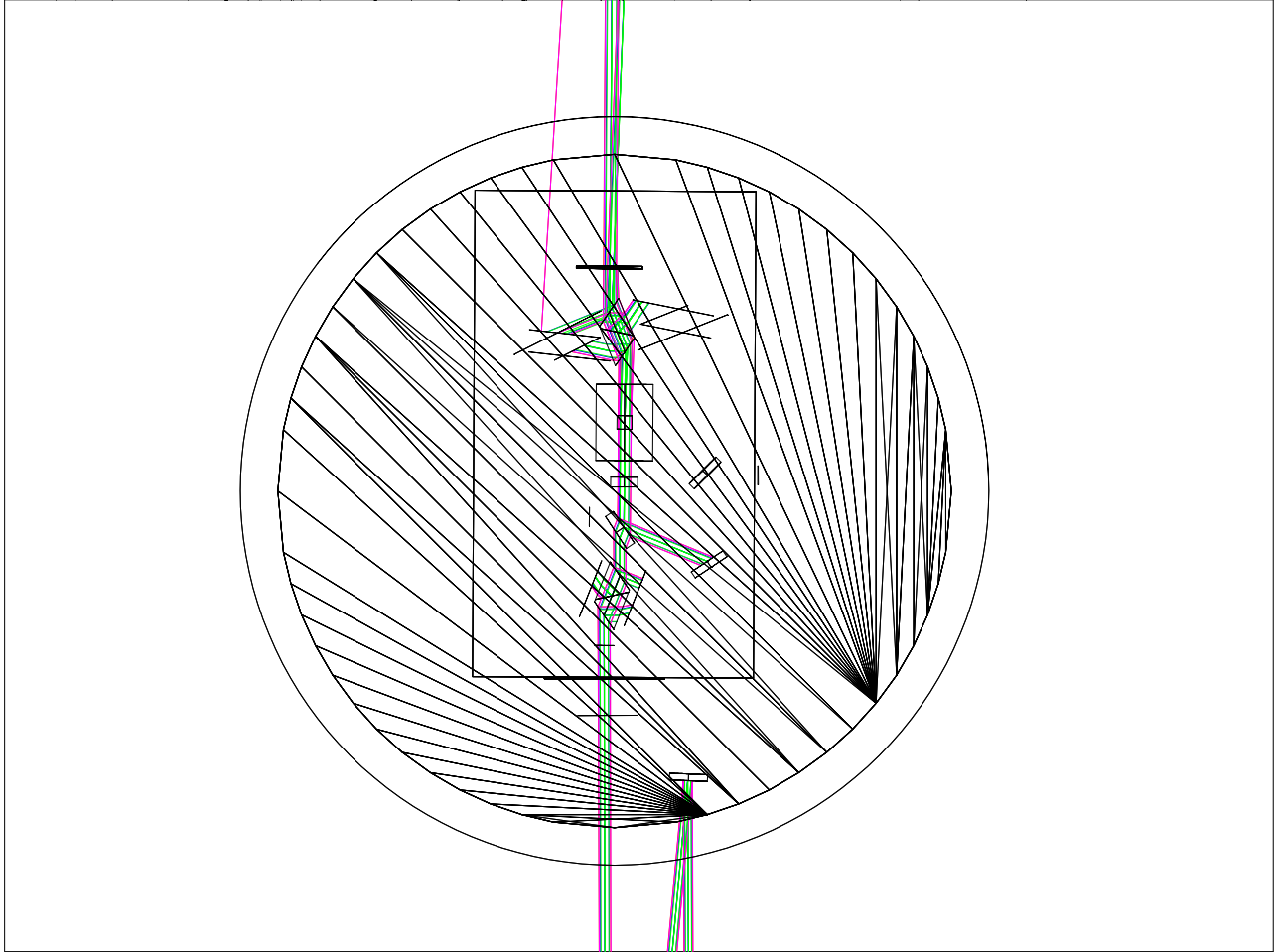
Figure 5: SR2 Scraper Baffle, SR2AR Baffle; POX Pick-off Beam

### 3.2.3 SRM



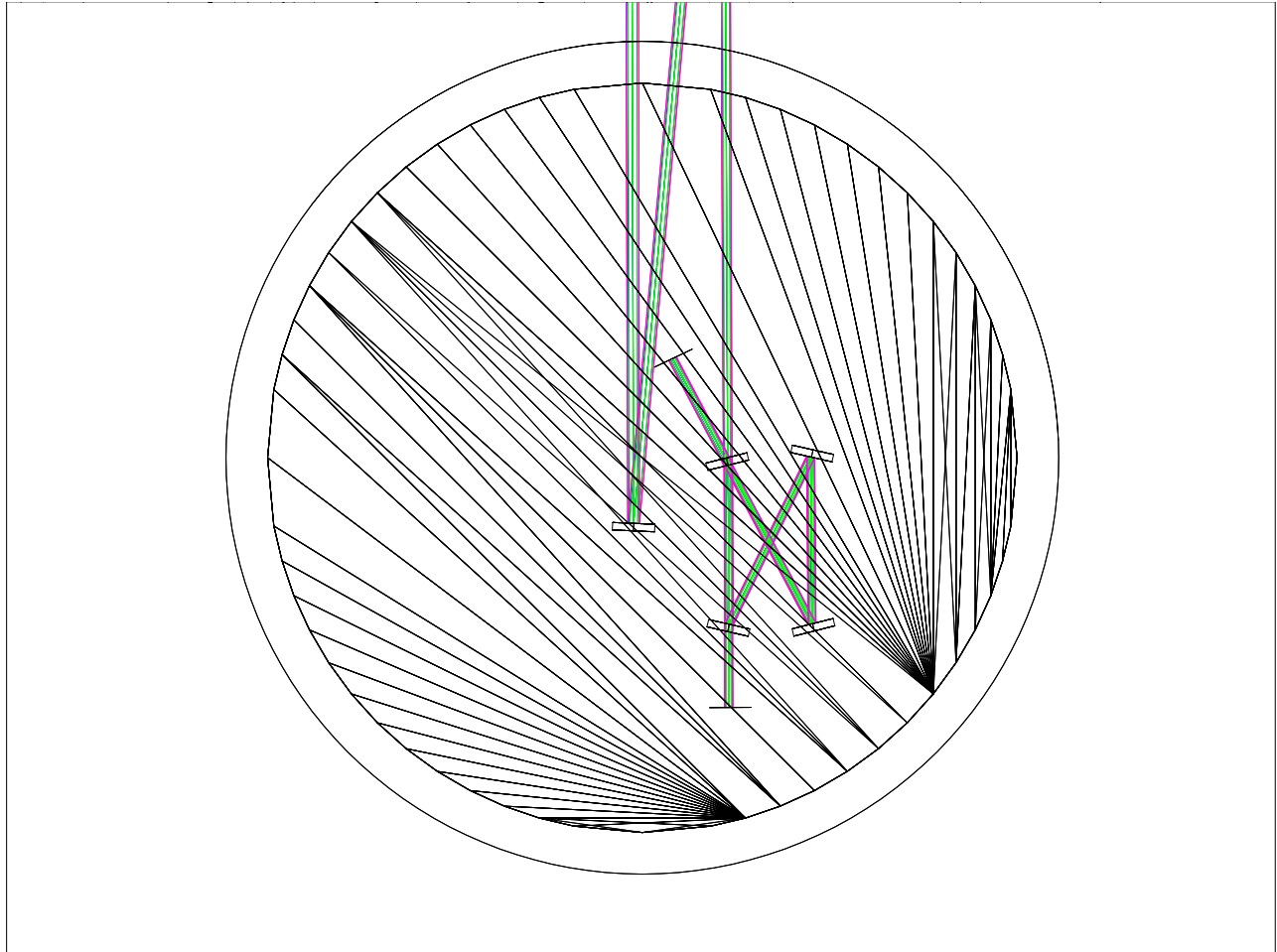
**Figure 6: SRM, SRM AR Baffles**

### 3.2.4 Output Faraday Isolator



**Figure 7: Output Faraday Isolator, MMT2 OMC**

### 3.2.5 Output Mode Cleaner



**Figure 8: Output Mode Cleaner, MMT1 OMC**

### 3.3 Baffle Characteristics

**Table 1: ? Baffle Characteristics**

Parameter	Value
Location	
Suspension	
Inside aperture diameter	

Parameter	Value
Outer diameter	
Material	
BRDF	
Weight	

### 3.4 Stray Light Noise

#### 3.4.1 Seismic Motion

The ground motion is taken from the Kamioka mine data.

The cryoshield seismic motion is measured data.

The seismic motion of the suspended table, which was modeled as 1/10 the seismic ground motion, can be taken as a minimum requirement.

All of the recycling cavity baffles are mounted to a suspended table in the chamber.

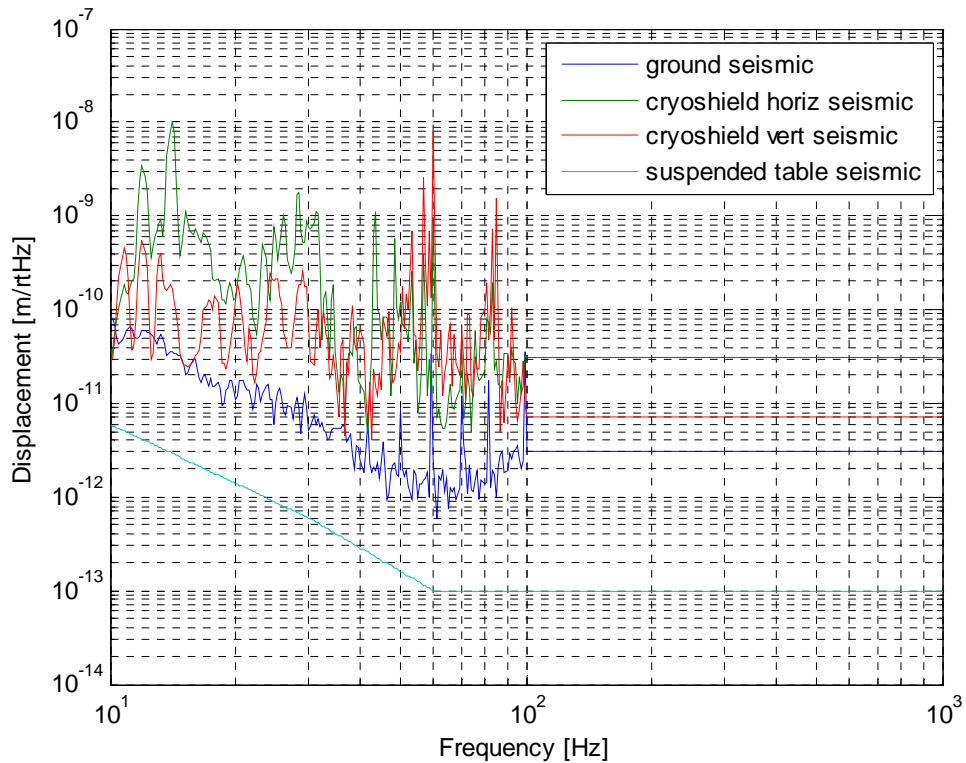
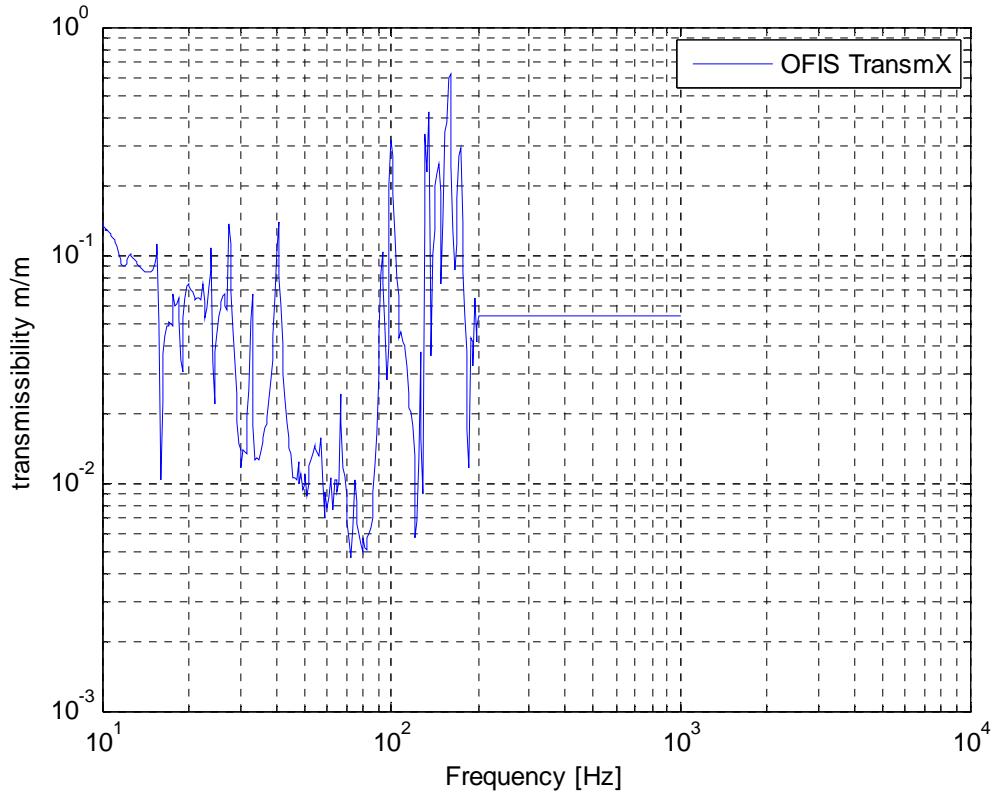


Figure 9: Seismic Ground Noise, m/rtHz

### 3.4.2 OFI and OMC Suspension Transmissibility

The Output Faraday Isolator (OFI) and the output mode cleaner (OMC) are mounted to the suspended table, but must be suspended by an additional suspension structure. The aLIGO OFI suspension transmissibility was used as a SUS model for these calculations.



**Figure 10: OFI Transmissibility along beam axis**

### **3.4.3 Beam Dump Surface BRDF**

Most of the baffles are constructed of polished oxidized steel with the first surface inclined at an incidence angle 57 deg. The measured BRDF is  $< 0.03 \text{ sr}^{-1}$ .

The PRM AR & HR baffle is composed of polished silicon carbide, because it also serves as an errant beam baffle and must absorb the 50 W PSL beam without being damaged. Likewise, the PRM HR baffle is composed of polished silicon carbide, because it also serves as an errant beam baffle and must absorb the reflected beam from PR2 without being damaged.

The output mode cleaner (OMC) Refl beam dump must be made of black glass, with BRDF =  $1\text{E-}6 \text{ sr}^{-1}$ , in order to reduce the scattering to an acceptable level.



### 3.4.4 Recycling Cavity Baffles Scatter

#### 3.4.4.1 DARM Motion Transfer Functions

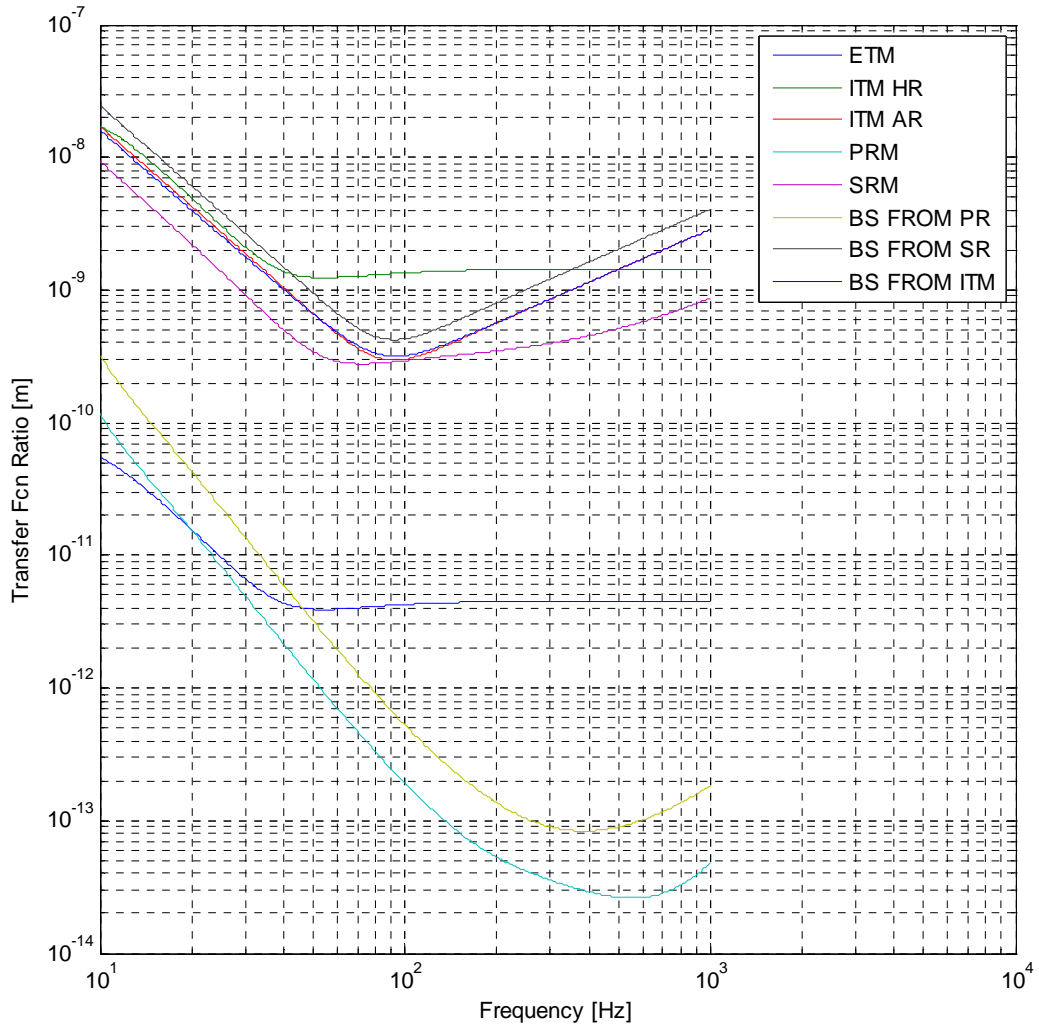


Figure 11: DARM motion transfer functions

### 3.4.4.2 PRM Scatter

#### PRM GBHR3

power incident on PRM HR beam dump from  
PRM GBHR3  
(forward and backward beams), W

$$P_{\text{prmgbhr3}} := 2 \cdot P_{\text{rc}} \cdot T_{\text{prmhr1064}}^2 \cdot R_{\text{prmar}}$$

$$P_{\text{prmgbhr3}} = 8 \times 10^{-4}$$

power scattered from PRM HR3 baffle, W

$$P_{\text{prmgbhr3s}} := P_{\text{prmgbhr3}} \cdot \text{BRDF}_{\text{bd}} \cdot \frac{w_{\text{ifo}}^2}{w_{\text{pr20}}^2} \cdot \Delta_{\text{ifo}} \cdot T_{\text{prmhr1064}}^2 \cdot R_{\text{prmar}}$$

$$P_{\text{prmgbhr3s}} = 7.634 \times 10^{-17}$$

displacement noise @ 100 Hz, m/rtHz

$$\text{DN}_{\text{prmgbhr3}} := \text{TF}_{\text{prbs}} \cdot \left( \frac{P_{\text{prmgbhr3s}}}{P_{\text{psl}}} \right)^{0.5} \cdot x_{\text{sustable}} \cdot 2 \cdot k$$

$$\text{DN}_{\text{prmgbhr3}} = 2.189 \times 10^{-27}$$

**PRM GBAR3**

power incident on PRM AR Baffle (forward and backward beams), W

$$P_{\text{prmgbar3}} := P_{\text{refl}} \cdot R_{\text{prmar}} \cdot R_{\text{prmr1064}} \cdot T_{\text{prmar1064}}$$

$$P_{\text{prmgbar3}} = 4.5 \times 10^{-6}$$

power scattered from PRM AR Baffle, W

$$P_{\text{prmgbar3s}} := P_{\text{prmgbar3}} \cdot \text{BRDF}_{\text{sic}} \cdot \frac{w_{\text{ifo}}^2}{w_{\text{prm0}}^2} \cdot \Delta_{\text{ifo}}$$

$$P_{\text{prmgbar3s}} = 1.184 \times 10^{-10}$$

displacement noise @ 100 Hz, m/rtHz

$$\text{DN}_{\text{prmgbar3}} := \text{TF}_{\text{prm}} \cdot \left( \frac{P_{\text{prmgbar3s}}}{P_{\text{psl}}} \right)^{0.5} \cdot x_{\text{sustable}} \cdot 2 \cdot k$$

$$\text{DN}_{\text{prmgbar3}} = 1.091 \times 10^{-24}$$

**Scatter of IO Reflected beam from input Faraday isolator**

Reflected power from PRM, W

$$P_{\text{refl}} = 0.1$$

power scattered from input Faraday isolator surface, W

$$P_{\text{refls}} := P_{\text{refl}} \cdot \text{BRDF}_{\text{fi}} \cdot \frac{w_{\text{ifo}}^2}{w_{\text{prmm0}}^2} \cdot \Delta_{\text{ifo}} \cdot T_{\text{prmh}} \cdot 10^6$$

$$P_{\text{refls}} = 3.604 \times 10^{-11}$$

displacement noise @ 100 Hz, m/rtHz

$$\text{DN}_{\text{refls}} := \text{TF}_{\text{prm}} \cdot \left( \frac{P_{\text{refls}}}{P_{\text{psl}}} \right)^{0.5} \cdot x_{\text{sustable}} \cdot 2 \cdot k$$

$$\text{DN}_{\text{refls}} = 6.016 \times 10^{-25}$$

**Scatter from dumped IO Reflected beam**

Need SiC surface for beam dump, water cooled

power scattered from Refl Beam Dump, W

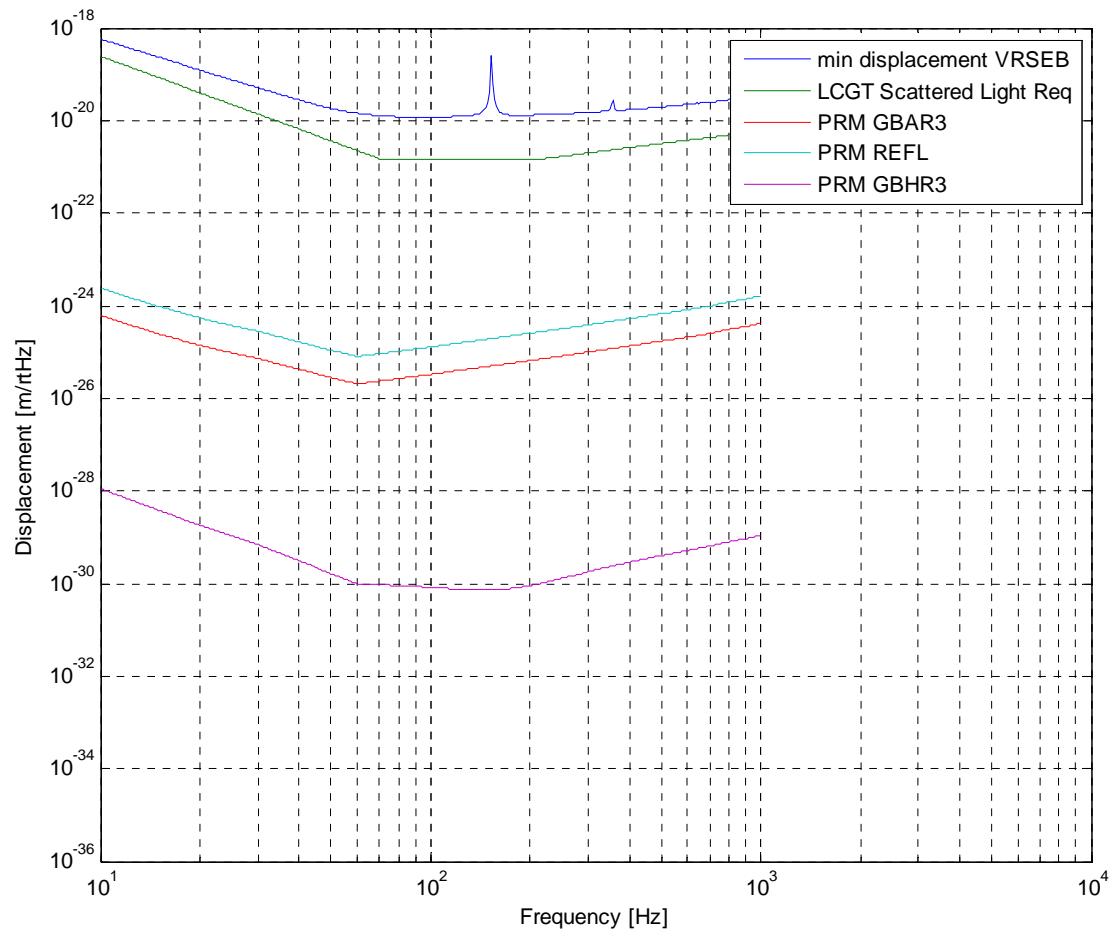
$$P_{\text{refl bds}} := P_{\text{refl}} \cdot \text{BRDF}_{\text{sic}} \cdot \frac{w_{\text{ifo}}^2}{w_{\text{prmm0}}^2} \cdot \Delta_{\text{ifo}}$$

$$P_{\text{refl bds}} = 3.604 \times 10^{-7}$$

displacement noise @ 100 Hz, m/rtHz

$$\text{DN}_{\text{refl bds}} := \text{TF}_{\text{prm}} \cdot \left( \frac{P_{\text{refl bds}}}{P_{\text{psl}}} \right)^{0.5} \cdot x_{\text{sustable}} \cdot 2 \cdot k$$

$$\text{DN}_{\text{refl bds}} = 6.016 \times 10^{-23}$$

**Figure 12: PRM Ghost Beam Scatter**

### 3.4.4.3 PR2 Scatter

#### PR2 GBHR3

power incident on PR2 scraper baffle from  
PR2 GBHR3  
(forward and backward beams), W

$$P_{pr2gbhr3} := 2 \cdot P_{rc} \cdot T_{pr2hr1064}^2 \cdot R_{pr2ar1064}$$

$$P_{pr2gbhr3} = 4 \times 10^{-7}$$

$$BRDF_{bd} = 0.03$$

power scattered from PR2 GBHR3 toward PR3, W

$$P_{pr2gbhr3pr3s} := \frac{P_{pr2gbhr3}}{2} \cdot BRDF_{wall} \cdot \frac{w_{ifo}^2}{w_{pr30}^2} \cdot \Delta_{ifo} \cdot T_{pr2hr1064}^2 \cdot R_{pr2ar1064}$$

$$P_{pr2gbhr3pr3s} = 1.339 \times 10^{-22}$$

power scattered from PR2 GBHR3 toward PRM, W

$$P_{pr2gbhr3prms} := \frac{P_{pr2gbhr3}}{2} \cdot BRDF_{wall} \cdot \frac{w_{ifo}^2}{w_{pr20}^2} \cdot \Delta_{ifo} \cdot T_{pr2hr1064}^2 \cdot R_{pr2ar1064}$$

$$P_{pr2gbhr3prms} = 3.181 \times 10^{-23}$$

total power scattered from PR2 GBHR3

$$P_{pr2gbhr3s} := P_{pr2gbhr3pr3s} + P_{pr2gbhr3prms}$$

$$P_{pr2gbhr3s} = 1.657 \times 10^{-22}$$

displacement noise @ 100 Hz, m/rtHz

$$DN_{pr2gbhr3} := TF_{prbs} \cdot \left( \frac{P_{pr2gbhr3s}}{P_{psl}} \right)^{0.5} \cdot x_{sustainable} \cdot 2 \cdot k$$

$$DN_{pr2gbhr3} = 3.225 \times 10^{-30}$$

**PR2 GBAR1 (POB)**

power incident on PR2 AR Baffle (forward beam), W

$$P_{\text{pr2gbar1}} := P_{\text{rc}} \cdot T_{\text{pr2hr1064}} \cdot T_{\text{pr2ar1064}}$$

$$P_{\text{pr2gbar1}} = 0.4$$

**PR2 GBAR3**

power incident on PR2 AR Baffle (forward and backward beams), W

$$P_{\text{pr2gbar3}} := 2 \cdot P_{\text{rc}} \cdot T_{\text{pr2hr1064}} \cdot R_{\text{pr2ar1064}} \cdot R_{\text{pr2hr1064}} \cdot T_{\text{pr2ar1064}}$$

$$P_{\text{pr2gbar3}} = 7.988 \times 10^{-4}$$

power scattered from PR2 GBAR3 toward PR3, W

$$P_{\text{pr2gbar3pr3s}} := \frac{P_{\text{pr2gbar3}}}{2} \cdot \text{BRDF}_{\text{bd}} \cdot \frac{w_{\text{ifo}}^2}{w_{\text{pr30}}^2} \cdot \Delta_{\text{ifo}} \cdot T_{\text{pr2hr1064}} \cdot R_{\text{pr2ar1064}} \cdot R_{\text{pr2hr1064}} \cdot T_{\text{pr2ar1064}}$$

$$P_{\text{pr2gbar3pr3s}} = 1.602 \times 10^{-16}$$

power scattered from PR2 GBAR3 toward PRM, W

$$P_{\text{pr2gbar3prms}} := \frac{P_{\text{pr2gbar3}}}{2} \cdot \text{BRDF}_{\text{bd}} \cdot \frac{w_{\text{ifo}}^2}{w_{\text{pr20}}^2} \cdot \Delta_{\text{ifo}} \cdot T_{\text{pr2hr1064}} \cdot R_{\text{pr2ar1064}} \cdot R_{\text{pr2hr1064}} \cdot T_{\text{pr2ar1064}}$$

$$P_{\text{pr2gbar3prms}} = 3.806 \times 10^{-17}$$

total power scattered from PR2 GBAR3

$$P_{\text{pr2gbar3s}} := P_{\text{pr2gbar3pr3s}} + P_{\text{pr2gbar3prms}}$$

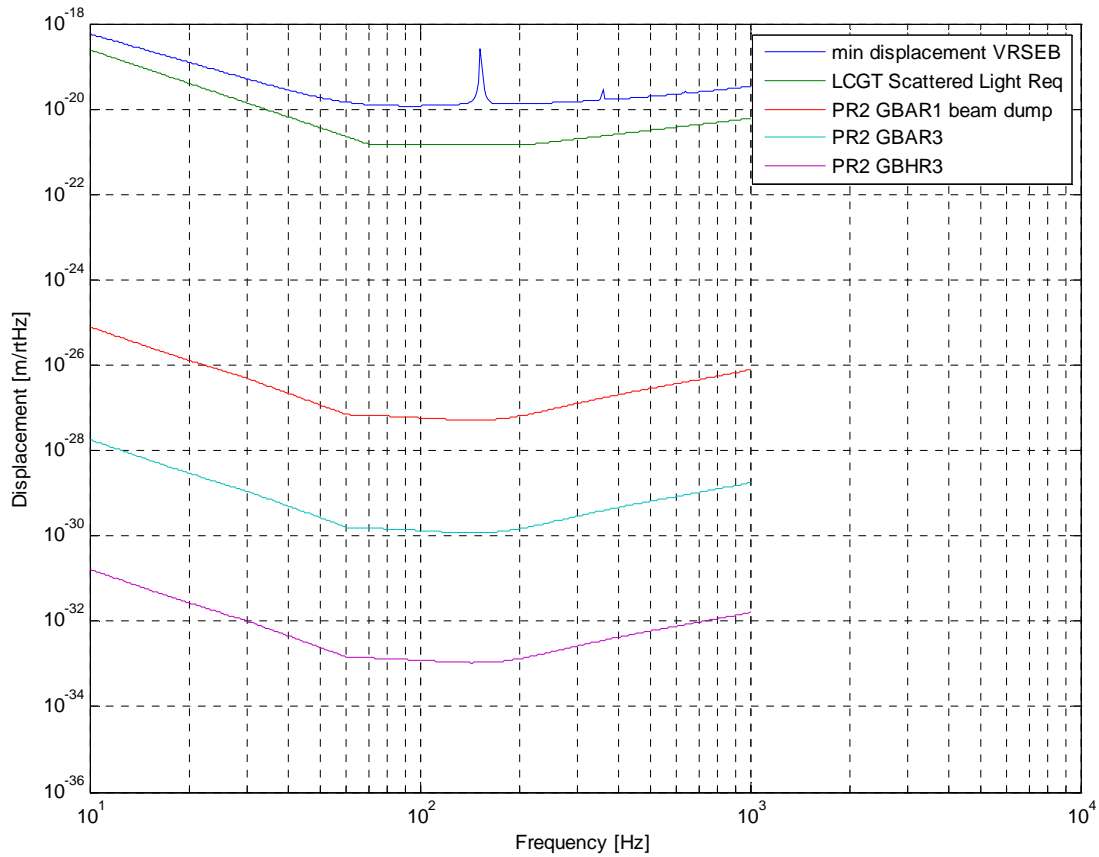
$$P_{\text{pr2gbar3s}} = 1.983 \times 10^{-16}$$



displacement noise @ 100 Hz, m/rtHz

$$DN_{pr2gbar3} := TF_{prbs} \cdot \left( \frac{P_{pr2gbar3s}}{P_{psl}} \right)^{0.5} \cdot x_{sustable} \cdot 2 \cdot k$$

$$DN_{pr2gbar3} = 3.528 \times 10^{-27}$$



**Figure 13: PR2 Ghost Beam Scatter**

### 3.4.4.4 PR3 Scatter

**PR3 GBHR3**

power incident on chamber wall from PR3  
GBHR3  
(forward and backward beams), W

$$P_{pr3gbhr3} := 2 \cdot P_{rc} \cdot T_{pr3hr1064}^2 \cdot R_{pr3ar1064}$$

$$P_{pr3gbhr3} = 4 \times 10^{-9}$$

$$BRDF_{wall} = 0.1$$

power scattered from chamber wall by  
PR3 GBHR3 toward BS, W

$$P_{pr3gbhr3bss} := \frac{P_{pr3gbhr3}}{2} \cdot BRDF_{wall} \cdot \Delta_{ifo} \cdot T_{pr3hr1064}^2 \cdot R_{pr3ar1064}$$

$$P_{pr3gbhr3bss} = 8.338 \times 10^{-31}$$

power scattered from chamber wall  
by  
PR3 GBHR3 toward PR2, W

$$P_{pr3gbhr3pr2s} := \frac{P_{pr3gbhr3}}{2} \cdot BRDF_{wall} \cdot \Delta_{ifo} \cdot \frac{w_{ifo}^2}{w_{pr30}^2} \cdot T_{pr3hr1064}^2 \cdot R_{pr3ar1064}$$

$$P_{pr3gbhr3pr2s} = 1.339 \times 10^{-26}$$

total power scattered from chamber wall by  
PR3 GBHR3

$$P_{pr3gbhr3s} := P_{pr3gbhr3bss} + P_{pr3gbhr3pr2s}$$

$$P_{pr3gbhr3s} = 1.339 \times 10^{-26}$$

displacement noise @ 100 Hz, m/rtHz

$$DN_{pr3gbhr3} := TF_{prbs} \cdot \left( \frac{P_{pr3gbhr3s}}{P_{psl}} \right)^{0.5} \cdot x_{sustable} \cdot 2 \cdot k$$

$$DN_{pr3gbhr3} = 2.899 \times 10^{-32}$$

**PR3 GBAR1**

power incident on PR3 AR Baffle  
(forward and backward beams), W

$$P_{\text{pr3argbar1}} := 2 \cdot P_{\text{rc}} \cdot T_{\text{pr3hr1064}} \cdot T_{\text{pr3ar1064}}$$

$$P_{\text{pr3argbar1}} = 0.0799$$

power scattered from PR3 AR Baffle toward BS, W

$$P_{\text{pr3argbar1bss}} := \frac{P_{\text{pr3argbar1}}}{2} \cdot \text{BRDF}_{\text{bd}} \cdot \Delta_{\text{ifo}} \cdot T_{\text{pr3hr1064}} \cdot T_{\text{pr3ar1064}}$$

$$P_{\text{pr3argbar1bss}} = 9.986 \times 10^{-17}$$

power scattered from PR3 AR Baffle toward PR3 W

$$P_{\text{pr3argbar1pr2s}} := \frac{P_{\text{pr3argbar1}}}{2} \cdot \text{BRDF}_{\text{bd}} \cdot \Delta_{\text{ifo}} \cdot \frac{w_{\text{ifo}}^2}{w_{\text{pr30}}^2} \cdot T_{\text{pr3hr1064}} \cdot T_{\text{pr3ar1064}}$$

$$P_{\text{pr3argbar1pr2s}} = 1.604 \times 10^{-12}$$

total power scattered from PR3 AR Baffle, W

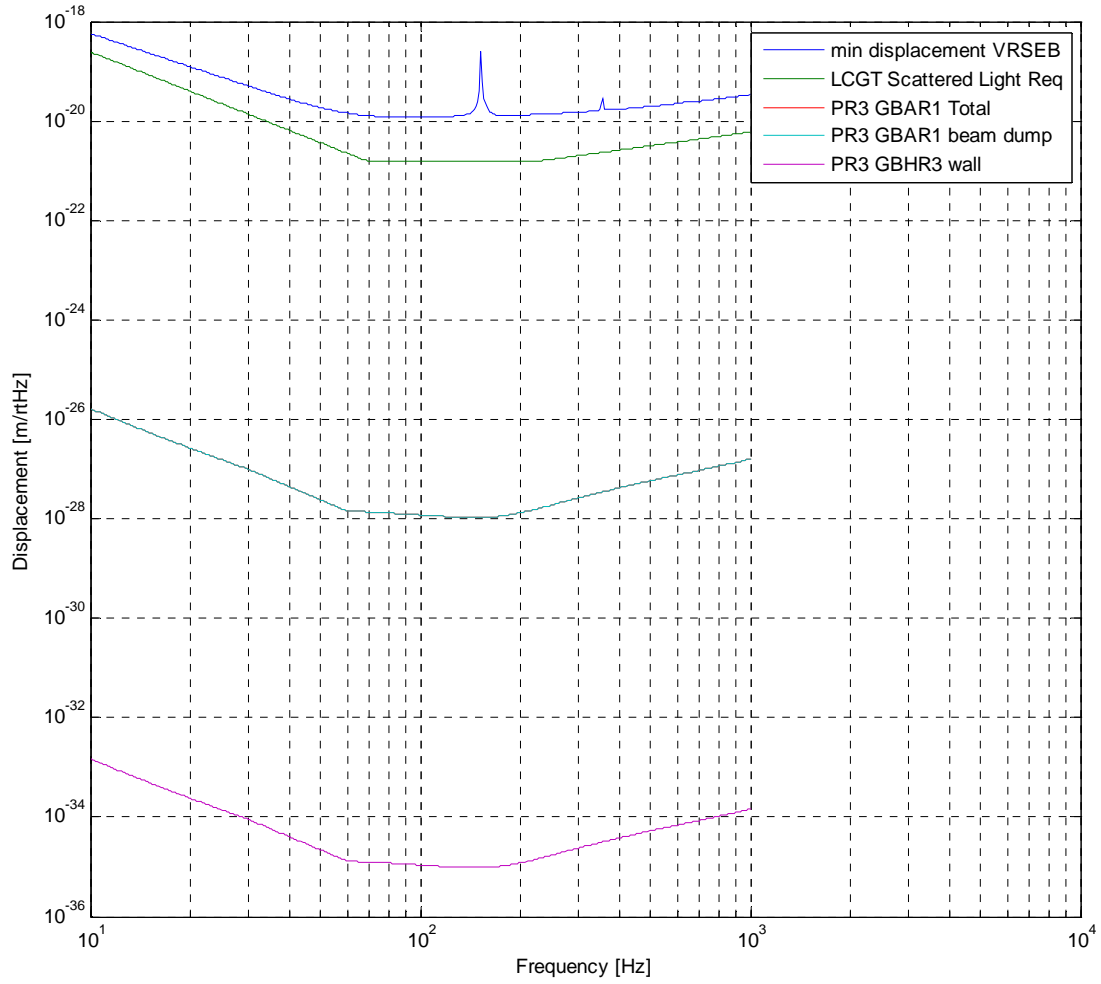
$$P_{\text{pr3argbar1s}} := P_{\text{pr3argbar1bss}} + P_{\text{pr3argbar1pr2s}}$$

$$P_{\text{pr3argbar1s}} = 1.604 \times 10^{-12}$$

displacement noise @ 100 Hz, m/rtHz

$$\text{DN}_{\text{pr3gbar1}} := \text{TF}_{\text{prbs}} \cdot \left( \frac{P_{\text{pr3argbar1s}}}{P_{\text{psl}}} \right)^{0.5} \cdot x_{\text{sustainable}} \cdot 2 \cdot k$$

$$\text{DN}_{\text{pr3gbar1}} = 3.173 \times 10^{-25}$$



**Figure 14: PR3 Ghost Beam Scatter**

**3.4.4.5 BS Ghost Beams and SR2 HR Scatter**

**BS\_GBAR1 (POX)**

power incident on SR2 Scraper Baffle from X arm, W

$$P_{\text{bsar1sr2baf}} := \frac{P_{\text{rc}}}{2} \cdot R_{\text{bsar}}$$

$$P_{\text{bsar1sr2baf}} = 0.02$$

power scattered from SR2 Scraper Baffle, W

$$P_{\text{bsar1sr2bafs}} := P_{\text{bsar1sr2baf}} \cdot \text{BRDF}_{\text{bd}} \cdot \frac{w_{\text{ifo}}^2}{w_{\text{sr30}}^2} \cdot \Delta_{\text{ifo}} \cdot R_{\text{bsar}}$$

$$P_{\text{bsar1sr2bafs}} = 8.318 \times 10^{-13}$$

displacement noise @ 100 Hz, m/rtHz

$$\text{DN}_{\text{bsar1sr2bafs}} := \text{TF}_{\text{itmar}} \cdot \left( \frac{P_{\text{bsar1sr2bafs}}}{P_{\text{psl}}} \right)^{0.5} \cdot x_{\text{sustainable}} \cdot 2 \cdot k$$

$$\text{DN}_{\text{bsar1sr2bafs}} = 1.371 \times 10^{-22}$$

**BS\_GBAR3P**

The stray light from both arms are almost anti-resonant, and the wavefronts overlap; their coherent sum is reduced by the square of the asymmetry coefficient for common mode field rejection

power incident on SR2 Scraper Baffle from both arms, W

$$P_{\text{bsar3sr2baf}} := \frac{P_{\text{rc}}}{2} \cdot \left[ (1 - R_{\text{bsar}}) \cdot R_{\text{bshr}} \cdot R_{\text{bsar}} + (1 - R_{\text{bshr}}) \cdot R_{\text{bsar}} \right] \cdot (1 - R_{\text{bsar}}) \cdot C_{\text{assy}}^2$$

$$P_{\text{bsar3sr2baf}} = 8.249 \times 10^{-6}$$

power scattered from SR2 Scraper Baffle, W

$$P_{\text{bsar3sr2bafs}} := P_{\text{bsar3sr2baf}} \cdot \text{BRDF}_{\text{bd}} \cdot \frac{w_{\text{ifo}}^2}{w_{\text{sr30}}^2} \cdot \Delta_{\text{ifo}} \cdot [(1 - R_{\text{bsar}}) \cdot R_{\text{bshr}} \cdot R_{\text{bsar}} + (1 - R_{\text{bshr}}) \cdot R_{\text{bsar}}] \cdot (1 - R_{\text{bsar}}) \cdot C_{\text{assy}}^2$$

$$P_{\text{bsar3sr2bafs}} = 1.415 \times 10^{-19}$$

displacement noise @ 100 Hz, m/rtHz

$$\text{DN}_{\text{bsar3sr2baf}} := \text{TF}_{\text{itmar}} \left( \frac{P_{\text{bsar3sr2bafs}}}{P_{\text{psl}}} \right)^{0.5} \cdot x_{\text{sustable}} \cdot 2 \cdot k$$

$$\text{DN}_{\text{bsar3sr2baf}} = 5.655 \times 10^{-26}$$

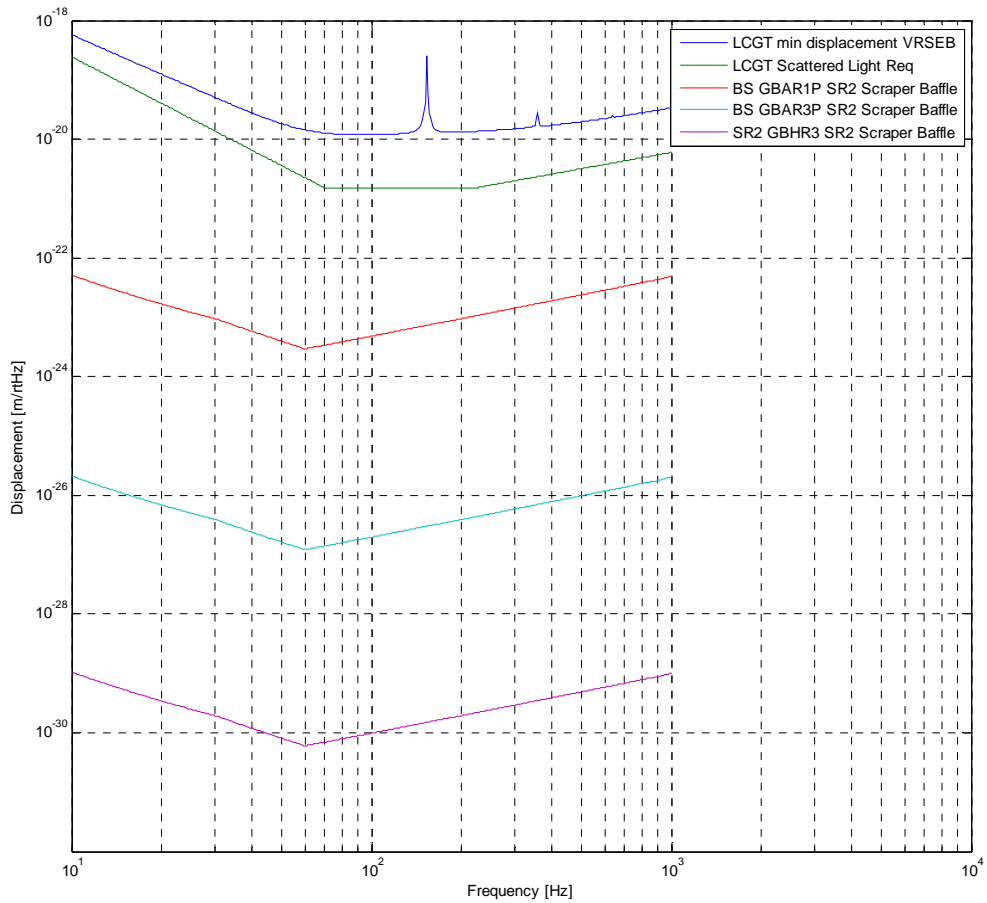


Figure 15: BS and SR2 Ghost beams Scatter

### 3.4.4.6 ITM Ghost Beams Scatter

#### ITMX\_GBAR1\_BD

Part of the ITMX\_GBAR1 is caught by the ITMX elliptical baffle, part reflects from SR2 back through BS and is caught by ITMY ACB.

Power of ITMX GBAR1, W

$$P_{itmar1} := P_{rc} \cdot R_{itmar}$$

$$P_{itmar1} = 0.04$$

#### ITMY\_GBAR1\_BD

Part of the ITMY\_GBAR1 merges with the POX beam and POY beam at PR2, part of it is caught by the PR3 HR baffle

#### ITMY\_GBAR3\_POY

Power incident on POY PO mirror, W

$$P_{itmar3PO} := \frac{P_{rc}}{2} \cdot R_{bshr} \cdot R_{itmhr}^2 \cdot R_{itmar} \cdot (1 - R_{itmar})^2$$

$$P_{itmar3PO} = 9.919 \times 10^{-3}$$

#### ITMY\_GBAR4

2nd order beam can be ignored. Part of the GBAR4 beam is caught on the ITMY Elliptical baf, part is caught on PR2 scraper baffle

#### ITMX\_GBAR3\_BD

power incident on PR2 Scraper Baffle, W

$$P_{itm3bd} := \frac{P_{rc}}{2} \cdot (1 - R_{bshr}) \cdot R_{itmhr}^2 \cdot R_{itmar} \cdot (1 - R_{itmar})^2$$

$$P_{itm3bd} = 9.9192 \times 10^{-3}$$

power scattered from PR2 Scraper Baffle, W

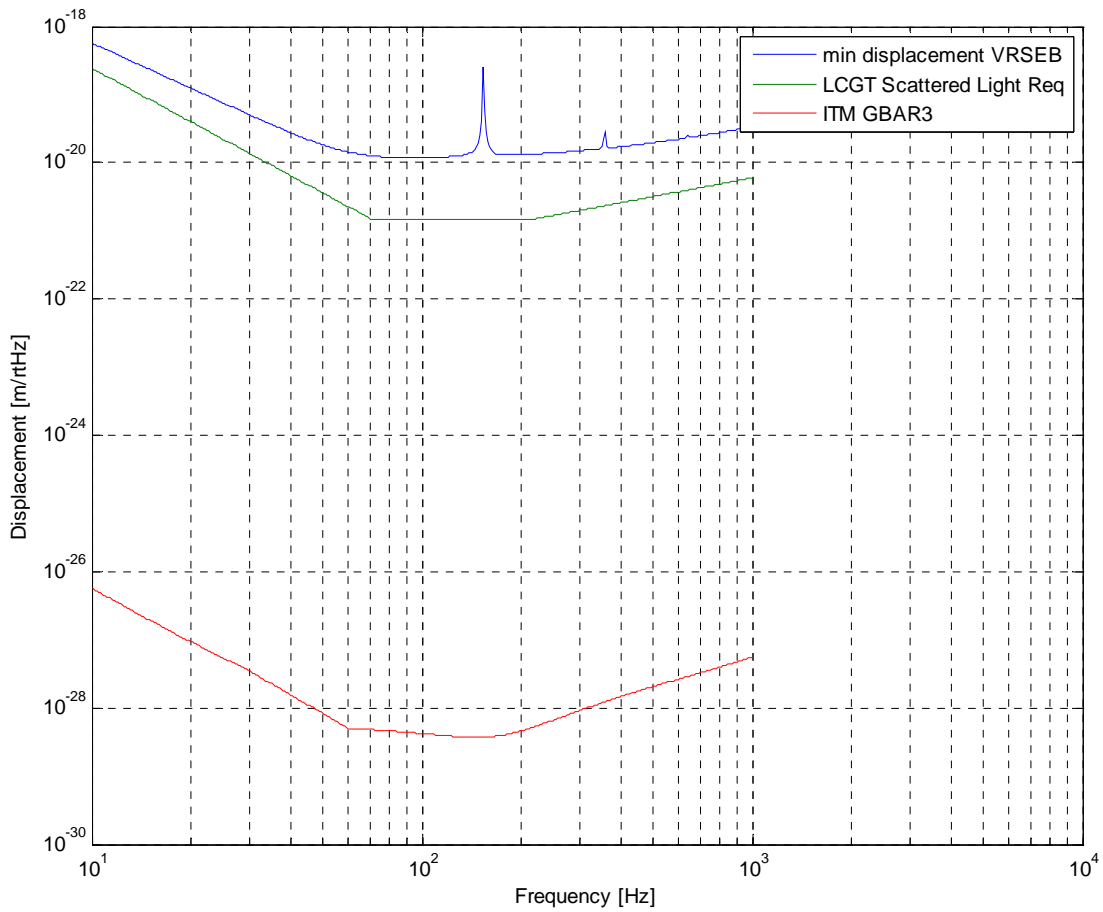
$$P_{itm3bds} := P_{itm3bd} \cdot BRDF_{bd} \cdot \frac{w_{ifo}^2}{w_{pr30}^2} \cdot \Delta_{ifo} \cdot (1 - R_{bshr}) \cdot R_{itmhr}^2 \cdot R_{itmar} \cdot (1 - R_{itmar})^2$$

$$P_{itm3bds} = 1.976 \times 10^{-13}$$

displacement noise @ 100 Hz, m/rtHz

$$DN_{itm\,xar\,3bd} := TF_{prbs} \cdot \left( \frac{P_{itm\,xar\,3bds}}{P_{psl}} \right)^{0.5} \cdot x_{sustainable} \cdot 2 \cdot k$$

$$DN_{itm\,xar\,3bd} = 1.114 \times 10^{-25}$$



**Figure 16: ITM Ghost Beam Scatter**



### 3.4.4.7 SRM Scatter

#### SRM\_GBHR3

power incident on SRM HR baffle, W

$$P_{\text{srmhrbaf}} := P_{\text{srm}} \cdot R_{\text{srmr1064}} \cdot T_{\text{srmhr1064}}$$

$$P_{\text{srmhrbaf}} = 3.893 \times 10^{-7}$$

power scattered from SRM HR baffle, W

$$P_{\text{srmhrbafs}} := P_{\text{srmhrbaf}} \cdot \text{BRDF}_{\text{bd}} \cdot \frac{w_{\text{ifo}}^2}{w_{\text{sr20}}^2} \cdot \Delta_{\text{ifo}} \cdot R_{\text{srmr1064}} \cdot T_{\text{srmhr1064}}$$

$$P_{\text{srmhrbafs}} = 3.658 \times 10^{-18}$$

displacement noise @ 100 Hz, m/rtHz

$$\text{DN}_{\text{srmhrbafs}} := \text{TF}_{\text{srm}} \cdot \left( \frac{P_{\text{srmhrbafs}}}{P_{\text{psl}}} \right)^{0.5} \cdot x_{\text{sustainable}} \cdot 2 \cdot k$$

$$\text{DN}_{\text{srmhrbafs}} = 2.875 \times 10^{-25}$$

**SRM\_GBAR3**

power incident on SRM AR Baffle, W

$$P_{\text{srmabaf}} := P_{\text{srm}} \cdot R_{\text{srmr1064}} R_{\text{srmhr1064}} T_{\text{srmr1064}}$$

$$P_{\text{srmabaf}} = 2.145 \times 10^{-6}$$

power scattered from SRM AR Baffle, W

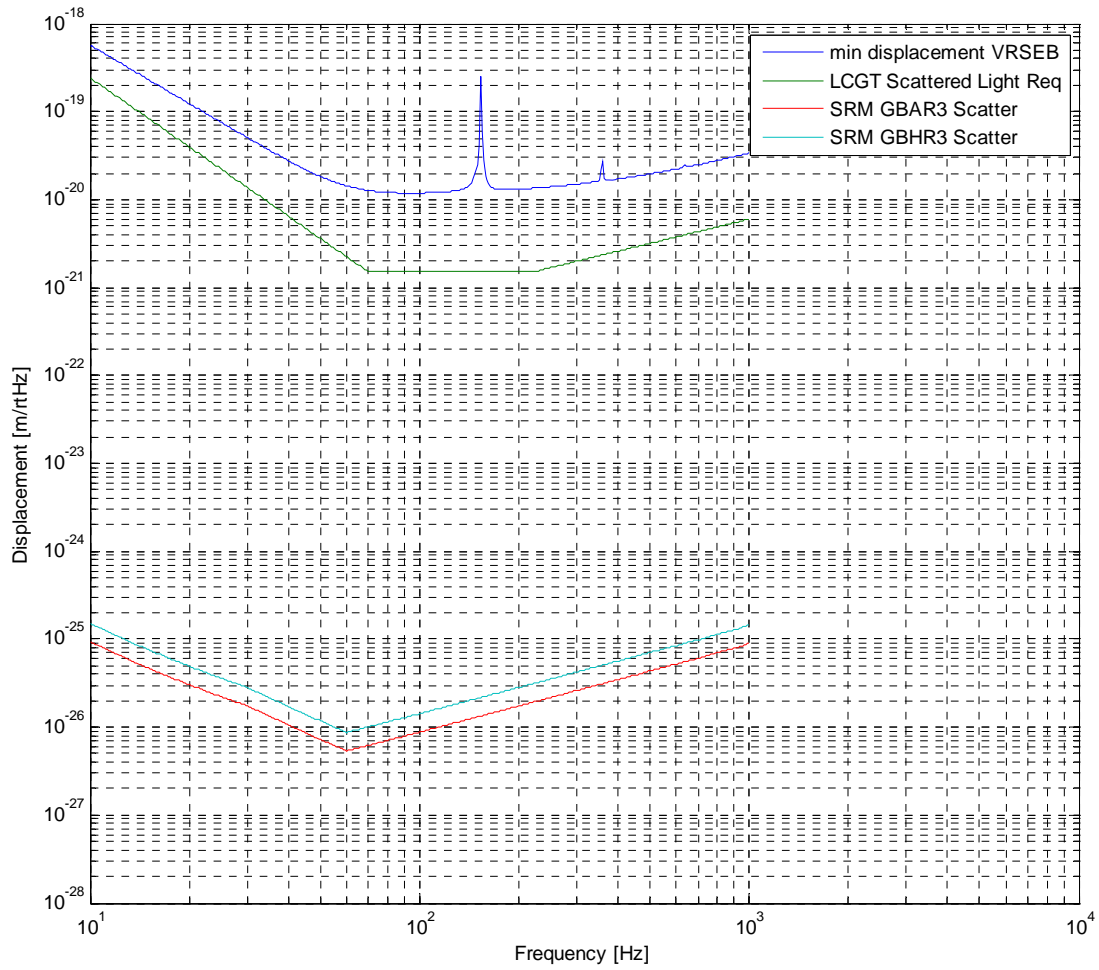
$$P_{\text{srmabafs}} := P_{\text{srmabaf}} \cdot \text{BRDF}_{\text{bd}} \cdot \frac{w_{\text{ifo}}^2}{w_{\text{srm0}}^2} \cdot \Delta_{\text{ifo}} \cdot R_{\text{srmr1064}} R_{\text{srmhr1064}} T_{\text{srmr1064}}$$

$$P_{\text{srmabafs}} = 1.387 \times 10^{-18}$$

displacement noise @ 100 Hz, m/rtHz

$$\text{DN}_{\text{srmabafs}} := \text{TF}_{\text{srm}} \left( \frac{P_{\text{srmabafs}}}{P_{\text{psl}}} \right)^{0.5} \cdot x_{\text{sustable}} \cdot 2 \cdot k$$

$$\text{DN}_{\text{srmabafs}} = 1.771 \times 10^{-25}$$



**Figure 17: SRM Ghost Beam Scatter**

### 3.4.4.8 SR2 Scatter

#### SR2 GBHR3

power incident on SR2 scraper baffle from  
SR2 GBHR3  
(forward and backward beams), W

$$P_{sr2gbhr3} := 2 \cdot P_{src} \cdot T_{sr2hr1064} R_{sr2ar1064} T_{sr2hr1064}$$

$$P_{sr2gbhr3} = 1.65 \times 10^{-10}$$

power scattered from SR2 GBHR3 toward SR3, W

$$P_{sr2gbhr3sr3s} := \frac{P_{sr2gbhr3}}{2} \cdot BRDF_{bd} \cdot \frac{w_{ifo}^2}{w_{sr30}^2} \cdot \Delta_{ifo} \cdot T_{sr2hr1064} R_{sr2ar1064} T_{sr2hr1064}$$

$$P_{sr2gbhr3sr3s} = 1.716 \times 10^{-26}$$

power scattered from SR2 GBHR3 toward SRM, W

$$P_{sr2gbhr3srms} := \frac{P_{sr2gbhr3}}{2} \cdot BRDF_{bd} \cdot \frac{w_{ifo}^2}{w_{srm0}^2} \cdot \Delta_{ifo} \cdot T_{sr2hr1064} R_{sr2ar1064} T_{sr2hr1064}$$

$$P_{sr2gbhr3srms} = 3.153 \times 10^{-28}$$

total power scattered from SR2 GBHR3

$$P_{sr2gbhr3s} := P_{sr2gbhr3sr3s} + P_{sr2gbhr3srms}$$

$$P_{sr2gbhr3s} = 1.747 \times 10^{-26}$$

displacement noise @ 100 Hz, m/rtHz

$$DN_{sr2gbhr3} := TF_{srbs} \cdot \left( \frac{P_{sr2gbhr3s}}{P_{psl}} \right)^{0.5} \cdot x_{sustable} \cdot 2 \cdot k$$

$$DN_{sr2gbhr3} = 2.649 \times 10^{-29}$$

**SR2 GBAR1**

SR2 GBAR1 power incident on SR2 AR Baffle  
(backward beam), W

$$P_{\text{sr2gbar1baf}} := P_{\text{src}} \cdot T_{\text{sr2hr1064}} \cdot T_{\text{sr2ar1064}}$$

$$P_{\text{sr2gbar1baf}} = 1.648 \times 10^{-4}$$

power scattered from SR3 AR Baffle, W

$$P_{\text{sr2gbar1bafs}} := P_{\text{sr2gbar1baf}} \cdot \text{BRDF}_{\text{bd}} \cdot \frac{w_{\text{ifo}}^2}{w_{\text{sr20}}^2} \cdot \Delta_{\text{ifo}} \cdot T_{\text{sr2hr1064}} \cdot T_{\text{sr2ar1064}}$$

$$P_{\text{sr2gbar1bafs}} = 1.007 \times 10^{-13}$$

displacement noise @ 100 Hz, m/rtHz

$$\text{DN}_{\text{sr2gbar1baf}} := \text{TF}_{\text{srbs}} \cdot \left( \frac{P_{\text{sr2gbar1bafs}}}{P_{\text{psl}}} \right)^{0.5} \cdot x_{\text{sustainable}} \cdot 2 \cdot k$$

$$\text{DN}_{\text{sr2gbar1baf}} = 6.361 \times 10^{-23}$$

**SR2 GBAR3**

SR2 GBAR3 power incident on SR2 AR Baffle  
(forward and backward beams), W

$$P_{\text{sr2gbar3baf}} := 2 \cdot P_{\text{src}} \cdot T_{\text{sr2hr1064}} \cdot R_{\text{sr2ar1064}} \cdot R_{\text{sr2hr1064}} \cdot T_{\text{sr2ar1064}}$$

$$P_{\text{sr2gbar3baf}} = 3.295 \times 10^{-7}$$

power scattered from SR3 AR Baffle, W

$$P_{\text{sr2gbar3bafs}} := P_{\text{sr2gbar3baf}} \cdot \text{BRDF}_{\text{bd}} \cdot \frac{w_{\text{ifo}}^2}{w_{\text{sr20}}^2} \cdot \Delta_{\text{ifo}} \cdot (T_{\text{sr2hr1064}} \cdot R_{\text{sr2ar1064}} \cdot R_{\text{sr2hr1064}} \cdot T_{\text{sr2ar1064}})$$

$$P_{\text{sr2gbar3bafs}} = 2.013 \times 10^{-19}$$

displacement noise @ 100 Hz, m/rtHz

$$DN_{sr2gbar3baf} := TF_{srbs} \cdot \left( \frac{P_{sr2gbar3bafs}}{P_{psl}} \right)^{0.5} \cdot x_{sustable} \cdot 2 \cdot k$$

$$DN_{sr2gbar3baf} = 8.992 \times 10^{-26}$$

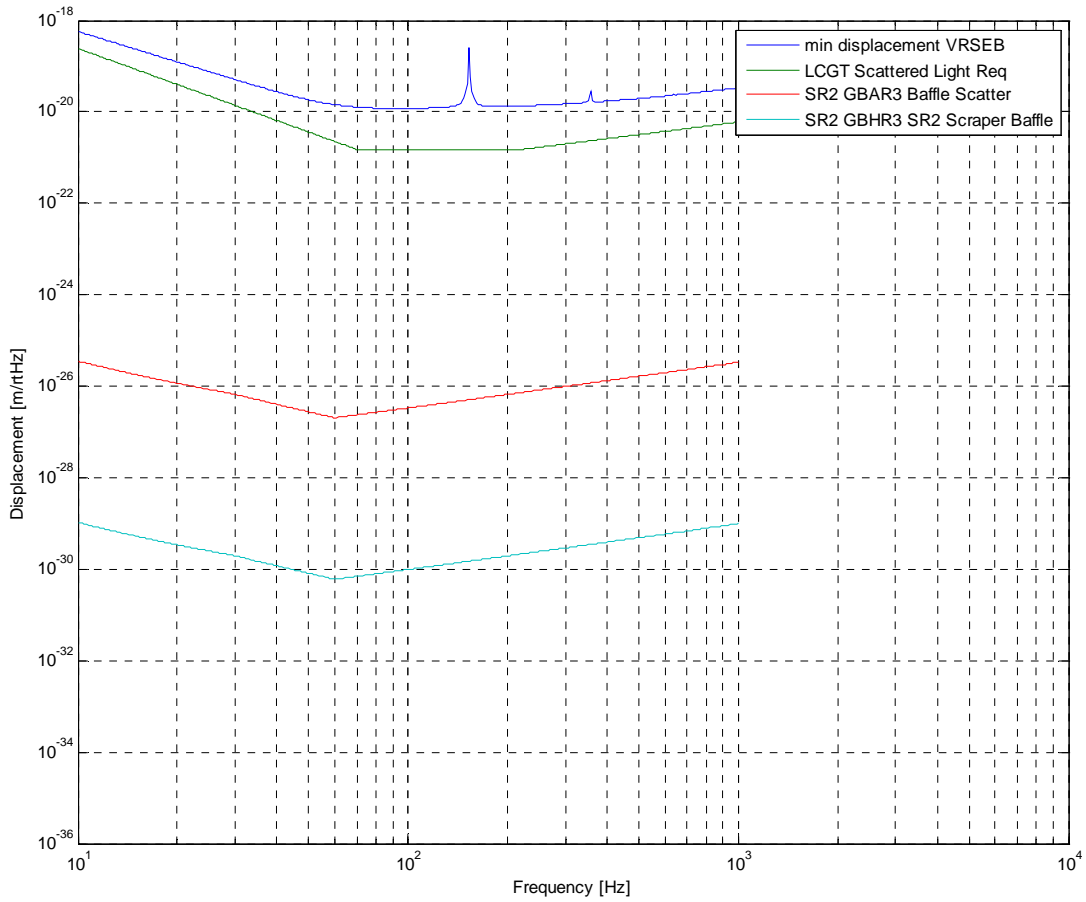


Figure 18: SR2 Ghost Beam Scatter

### 3.4.4.9 SR3 Scatter

**SR3 GBHR3**

power incident on wall from SR3 GBHR3 (forward and backward beams), W

$$P_{\text{sr3gbhr3}} := 2 \cdot P_{\text{src}} \cdot T_{\text{sr3hr1064}}^2 \cdot R_{\text{sr3ar1064}}$$

$$P_{\text{sr3gbhr3}} = 1.65 \times 10^{-12}$$

power scattered from wall by SR3 GBHR3 toward BS, W

$$P_{\text{sr3gbhr3bss}} := \frac{P_{\text{sr3gbhr3}}}{2} \cdot \text{BRDF}_{\text{wall}} \cdot \Delta_{\text{ifo}} \cdot T_{\text{sr3hr1064}}^2 \cdot R_{\text{sr3ar1064}}$$

$$P_{\text{sr3gbhr3bss}} = 3.439 \times 10^{-34}$$

power scattered from wall by SR3 GBHR3 toward SR2 W

$$P_{\text{sr3gbhr3sr2s}} := \frac{P_{\text{sr3gbhr3}}}{2} \cdot \text{BRDF}_{\text{wall}} \cdot \Delta_{\text{ifo}} \cdot \frac{w_{\text{ifo}}^2}{w_{\text{sr30}}^2} \cdot \left( T_{\text{sr3hr1064}}^2 \cdot R_{\text{sr3ar1064}} \right)$$

$$P_{\text{sr3gbhr3sr2s}} = 5.719 \times 10^{-30}$$

total power scattered from SR2 scraper baffle by from SR3 GBHR3

$$P_{\text{sr3gbhr3s}} := P_{\text{sr3gbhr3bss}} + P_{\text{sr3gbhr3sr2s}}$$

$$P_{\text{sr3gbhr3s}} = 5.719 \times 10^{-30}$$

displacement noise @ 100 Hz, m/rtHz

$$\text{DN}_{\text{sr3gbhr3}} := \text{TF}_{\text{srbs}} \cdot \left( \frac{P_{\text{sr3gbhr3s}}}{P_{\text{psl}}} \right)^{0.5} \cdot x_{\text{sustable}} \cdot 2 \cdot k$$

$$\text{DN}_{\text{sr3gbhr3}} = 4.793 \times 10^{-31}$$

**SR3 AR Baffle**

power incident on SR3 AR Baffle  
(forward and backward beams), W

$$P_{sr3arbfaf} := 2 \cdot P_{src} \cdot T_{sr3hr1064} \cdot T_{sr3ar1064}$$

$$P_{sr3arbfaf} = 3.297 \times 10^{-5}$$

power scattered from SR3 AR Baffle toward BS, W

$$P_{sr3arbfafbs} := \frac{P_{sr3arbfaf}}{2} \cdot BRDF_{bd} \cdot \Delta_{ifo} \cdot T_{sr3hr1064} \cdot T_{sr3ar1064}$$

$$P_{sr3arbfafbs} = 4.119 \times 10^{-20}$$

power scattered from SR3 AR Baffle toward SR2, W

$$P_{sr3arbfafsr2s} := \frac{P_{sr3arbfaf}}{2} \cdot BRDF_{bd} \cdot \Delta_{ifo} \cdot \frac{w_{ifo}^2}{w_{sr30}^2} \cdot (T_{sr3hr1064} \cdot T_{sr3ar1064})$$

$$P_{sr3arbfafsr2s} = 6.849 \times 10^{-16}$$

total power scattered from SR3 AR Baffle, W

$$P_{sr3arbafs} := P_{sr3arbfafbs} + P_{sr3arbfafsr2s}$$

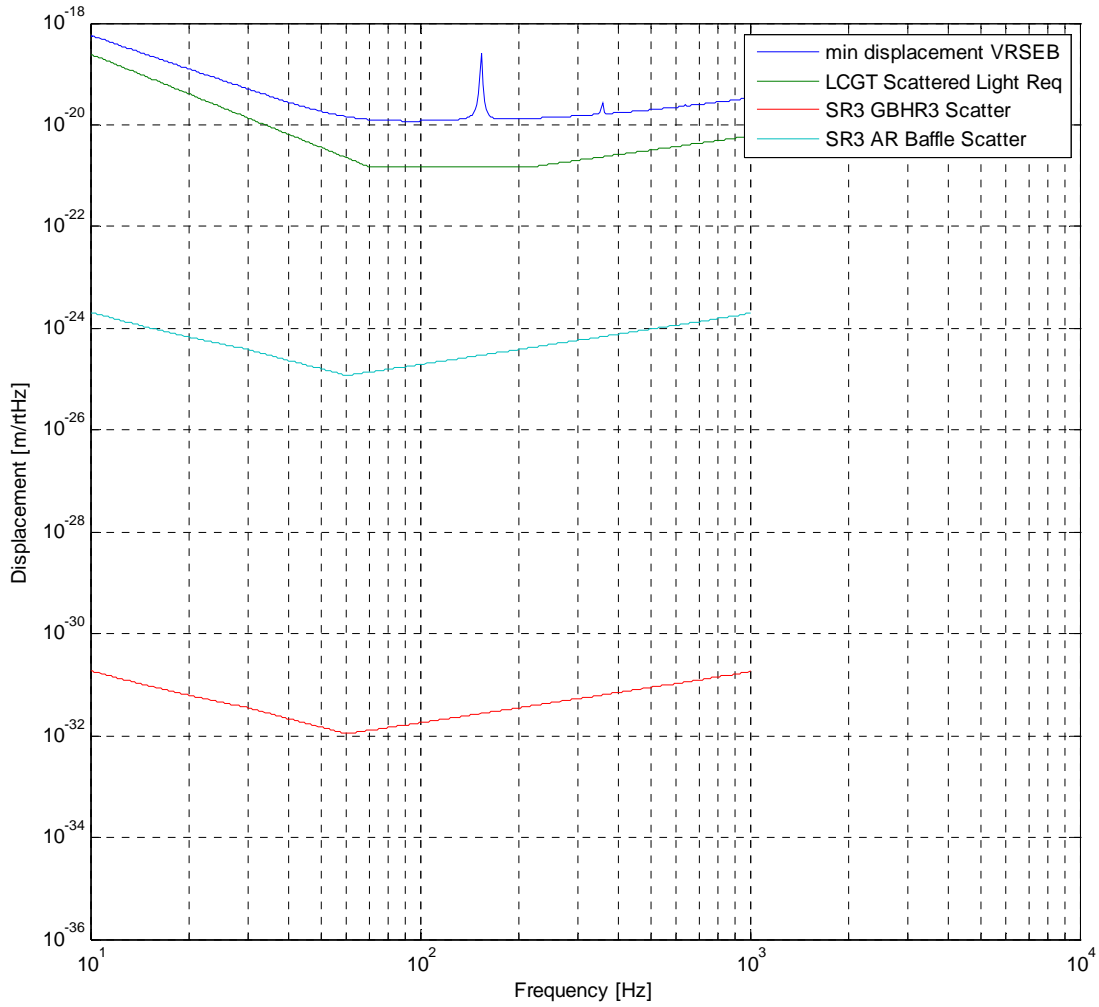
$$P_{sr3arbafs} = 6.849 \times 10^{-16}$$

displacement noise @ 100 Hz, m/rtHz

$$DN_{sr3arbfaf} := TF_{srbs} \cdot \left( \frac{P_{sr3arbafs}}{P_{psl}} \right)^{0.5} \cdot x_{sustable} \cdot 2 \cdot k$$

$$DN_{sr3arbfaf} = 5.246 \times 10^{-24}$$





**Figure 19: SR3 Ghost Beam Scatter**

### 3.4.4.10 Output Faraday Isolator (OFI) Scatter

#### Output Faraday Isolator

power incident on Output Faraday Isolator, W

$$P_{\text{ofi}} := P_{\text{src}} \cdot T_{\text{srmhr106}}$$

$$P_{\text{ofi}} = 0.051$$

$$\text{BRDF}_{\text{fi}} = 1 \times 10^{-4}$$

$$\Delta_{\text{ifo}} = 1.668 \times 10^{-9}$$

power scattered from OFI, W

$$P_{\text{ofis}} := N_{\text{fi}} \cdot P_{\text{ofi}} \cdot \text{BRDF}_{\text{fi}} \cdot \frac{w_{\text{ifo}}^2}{w_{\text{srm0}}^2} \cdot \Delta_{\text{ifo}} \cdot T_{\text{srmr}} \cdot 10^6$$

$$P_{\text{ofis}} = 1.808 \times 10^{-11}$$

displacement noise @ 100 Hz, m/rtHz

$$\text{DN}_{\text{ofis}} := \text{TF}_{\text{srm}} \cdot \left( \frac{P_{\text{ofis}}}{P_{\text{psl}}} \right)^{0.5} \cdot x_{\text{sustable}} \cdot 2 \cdot k$$

$$\text{DN}_{\text{ofis}} = 6.391 \times 10^{-22}$$

### Output Mode Cleaner

TEM00 power incident on Output mode cleaner, W

$$P_{\text{omc}} := P_{\text{srctem00}} \cdot T_{\text{srmhr}} \cdot 10^6$$

$$P_{\text{omc}} = 0.015$$

power scattered from OMC W

$$P_{\text{omcs}} := P_{\text{omc}} \cdot \alpha_{\text{omc}} \cdot G_{\text{omc}} \cdot \frac{w_{\text{ifo}}^2}{w_{\text{omcmm0}}^2} \cdot \Delta_{\text{ifo}} \cdot T_{\text{srmr}} \cdot 10^6$$

$$P_{\text{omcs}} = 2.767 \times 10^{-8}$$

displacement noise @ 100 Hz, m/rtHz

$$\text{DN}_{\text{omcs}} := \text{TF}_{\text{srm}} \cdot \left( \frac{P_{\text{omcs}}}{P_{\text{psl}}} \right)^{0.5} \cdot A_{\text{ofi}} \cdot x_{\text{sustable}} \cdot 2 \cdot k$$

$$\text{DN}_{\text{omcs}} = 2.501 \times 10^{-23}$$

**Output Mode Cleaner Refl**

power reflected from Output mode cleaner, W

$$R_{\text{omc}} := 0.95$$

$$P_{\text{omcrefl}} := P_{\text{srctemxx}} \cdot T_{\text{srmhr1064}}$$

$$P_{\text{omcrefl}} = 0.035$$

$$\text{BRDF}_{\text{blackglass}} := 1 \cdot 10^{-6}$$

power scattered from OMC Refl BD, W

$$P_{\text{omcrefls}} := P_{\text{omcrefl}} \cdot \text{BRDF}_{\text{blackglass}} \cdot \frac{w_{\text{ifo}}^2}{w_{\text{omcmm0}}^2} \cdot \Delta_{\text{ifo}} \cdot R_{\text{omc}} \cdot T_{\text{srmhr1064}}$$

$$P_{\text{omcrefls}} = 1.26 \times 10^{-12}$$

displacement noise @ 100 Hz, m/rtHz

$$\text{DN}_{\text{omcrefls}} := \text{TF}_{\text{srm}} \cdot \left( \frac{P_{\text{omcrefls}}}{P_{\text{psl}}} \right)^{0.5} \cdot x_{\text{sustable}} \cdot 2 \cdot k$$

$$\text{DN}_{\text{omcrefls}} = 1.688 \times 10^{-22}$$

**Output Photodetector**

power incident on output photodetector, W

$$P_{\text{opd}} := P_{\text{srctem00}} \cdot T_{\text{srmhr1064}} \cdot T_{\text{omc}}$$

$$P_{\text{opd}} = 0.015$$

power scattered from PD, W

$$P_{\text{opds}} := P_{\text{opd}} \cdot \text{BRDF}_{\text{pd}} \cdot \frac{w_{\text{ifo}}^2}{w_{\text{opd0}}^2} \cdot \Delta_{\text{ifo}} \cdot T_{\text{srmhr1064}}$$

$$P_{\text{opds}} = 5.535 \times 10^{-8}$$

displacement noise @ 100 Hz, m/rtHz

$$DN_{opds} := TF_{srm} \cdot \left( \frac{P_{opds}}{P_{psl}} \right)^{0.5} \cdot A_{ofi} \cdot x_{sustable} \cdot 2 \cdot k$$

$$DN_{opds} = 3.537 \times 10^{-23}$$

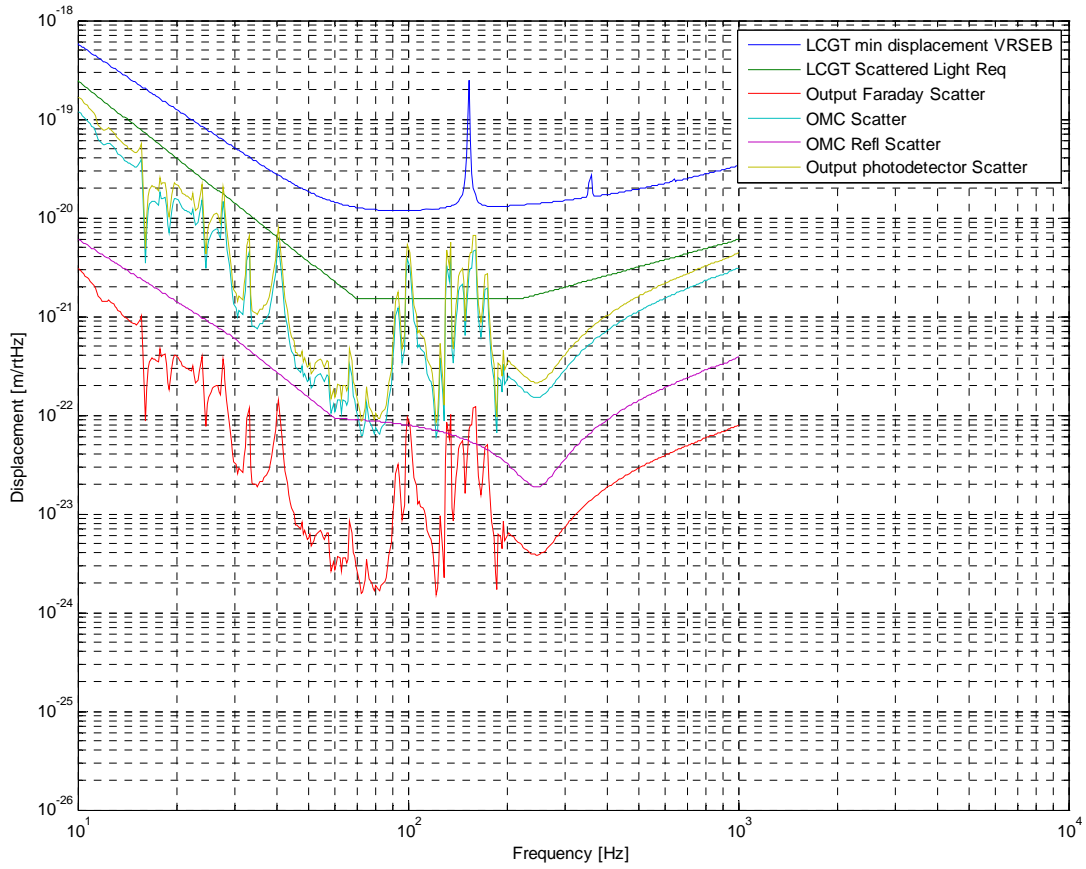


Figure 20: OFI, OMC, OMC Refl, and output PD scatter

### 3.5 Optical Interfaces

## **4 INTERFACE CONTROL DOCUMENT**

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