# LIGO LASER INTERFEROMETER GRAVITATIONAL WAVE OBSERVATORY

# LIGO Laboratory / LIGO Scientific Collaboration

LIGO-E1100684-v1

Surface figure measurement of ETM04

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#### 1 Introduction

The purpose of this note is to memorialize the results of figure measurement of ETM04.

### 2 Method

This is the average of eight measurements taken every 45 degrees, the optic under test is rotated. See T1100370-v2 for more detail.

## 2.1 Uncertainty

The final uncertainty in the measurement of ETM04 is estimated to be of order 0.4nm rms over 300mm and 0.1nm rms over 160mm. This uncertainty is the combination of environmental and RDF errors. See T1100370-v2.

#### 3 Results

ETM04 is measured every 45 degrees in 8 orientations. The final map is the average of all 8 datasets rotated to one orientation (arrow up.) The RDF is subtracted from each data set before averaging. While the error found in this analysis is sufficient for analysis of ETM04, we expect the RDF to be refined by further measurement. A key to the coefficients listed on data images is found in figure 1; for instance coef 4 corresponds to term# 4 in the list of Zernike polynomials.

## Zernike Polynomials Table

In this table,  $\phi$  = polar coordinate angle, and  $\rho$  = radius (normalized to 1 at the edge of the aperture). The numbers in columns m and n are the indices for Zernike polynomials

n	m	Term #	Polynomial	Meaning
0	0	0	1	Piston or Bias
1	+1	1	ρ cos φ	Tilt X
	-1	2	ρsinφ	Tilt Y
	0	3	$2\rho^2-1$	Power
2	+2	4	$\rho^2 \cos 2 \phi$	Astigmatism X
	-2	5	$\rho^2 \sin 2 \phi$	Astigmatism Y
	+1	6	(3ρ <sup>2</sup> -2)ρ cos φ	Coma X
	-1	7	$(3\rho^2-2)\rho \sin \phi$	Coma Y
	0	8	$6\rho^4$ - $6\rho^2$ + 1	Primary Spherical
3	+3	9	ρ <sup>3</sup> cos3 φ	Trefoil X
	-3	10	$\rho^3 \sin 3 \phi$	Trefoil Y
	+2	11	$(4\rho^2-3)\rho^2\cos 2\phi$	Secondary Astigmatism X
	-2	12	$(4\rho^2-3)\rho^2\sin^2\phi$	Secondary Astigmatism Y
	+1	13	$(10\rho^4-12\rho^2+3)\rho\cos\phi$	Secondary Coma X
	-1	14	$(10\rho^4-12\rho^2+3)\rho \sin \phi$	Secondary Coma Y
	0	15	$20\rho^6-30\rho^4+12\rho^2-1$	Secondary Spherical

# 3.1 High Frequency data

Data have been taken at 0.4mm/pixel (full aperture), 0.192mm/pixel, 0.047mm/pixel and 0.023mm/pixel. As of this writing there is no calibration file in place for these apertures, these data will be post processed when a calibration file is available.







