



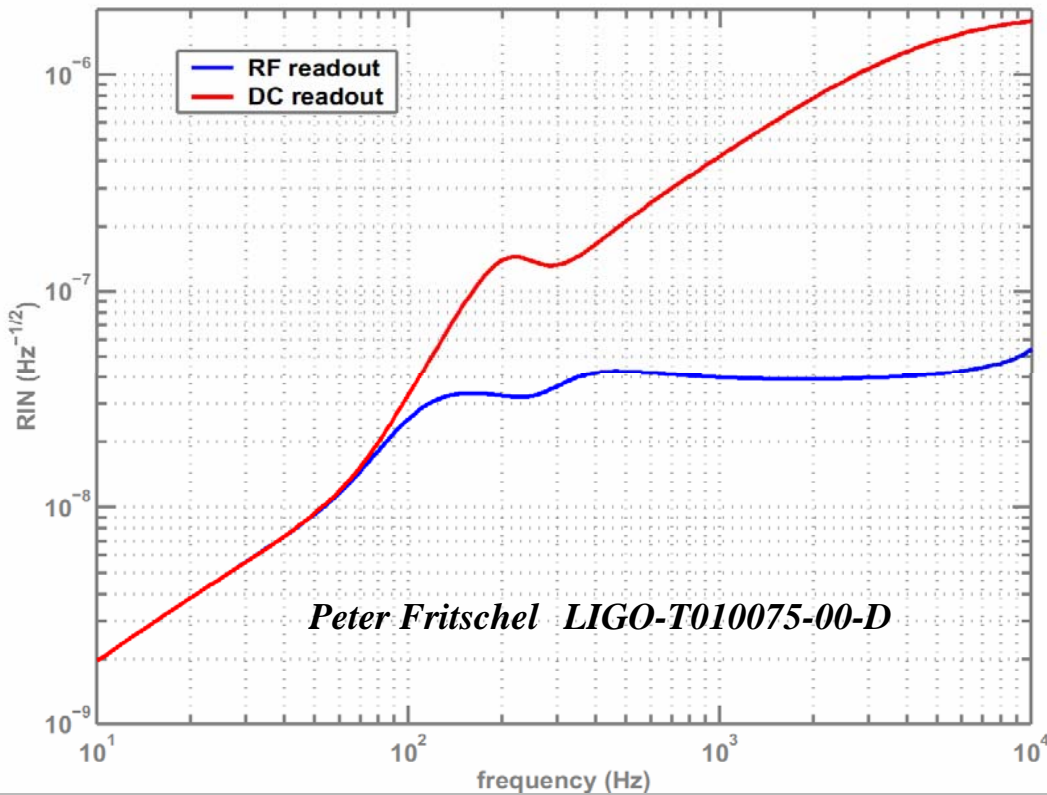
Advanced LIGO EOM Noise

Wan Wu, Rodrigo Delgado, Volker Quetschke,
Guido Mueller, David Reitze and David Tanner





Noise requirement on the modulation index



Modulation index variation δm



Intensity fluctuation of the carrier light



Radiation pressure noise

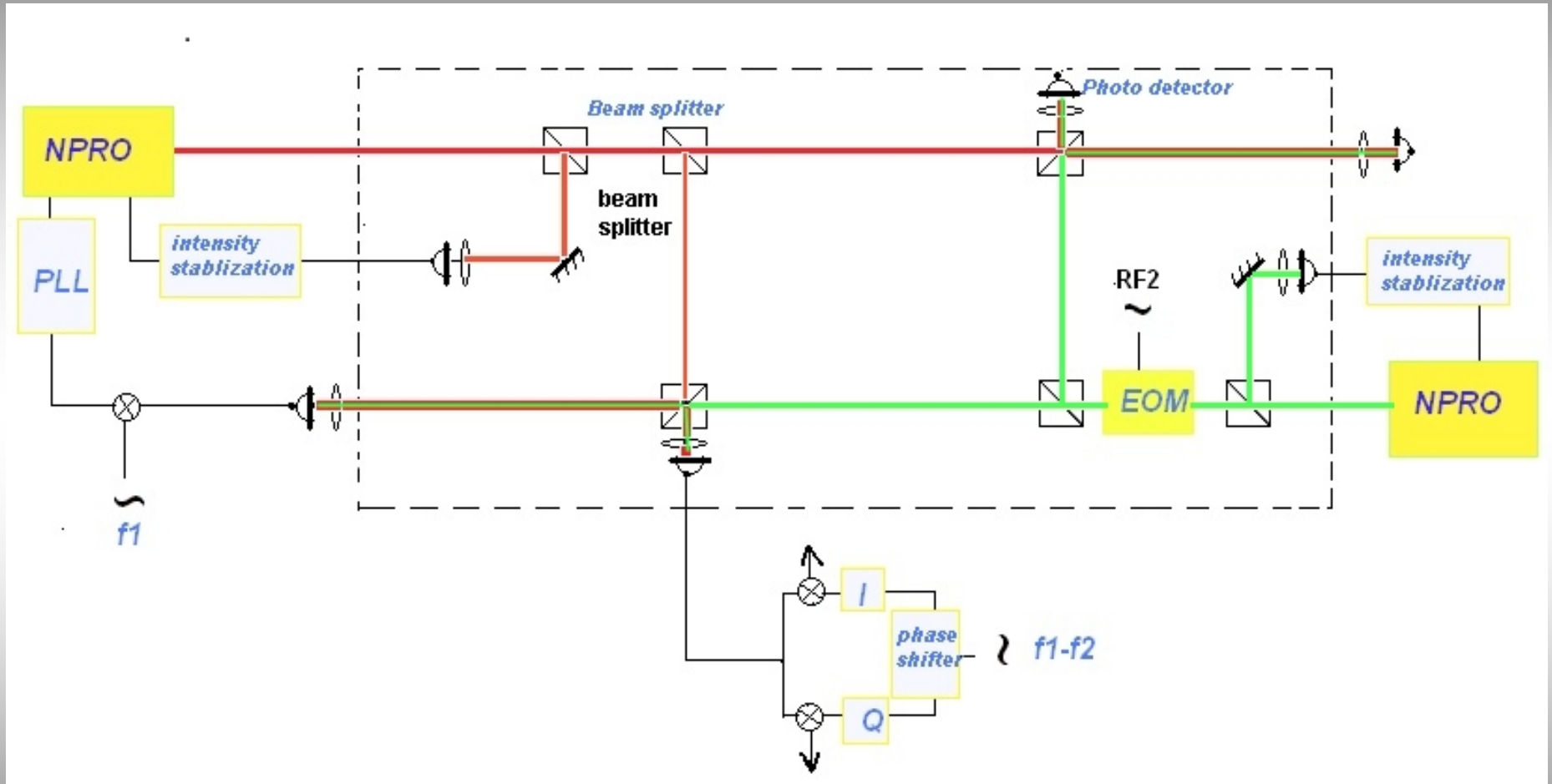
$$E = E_0 e^{i[\varpi t + m \sin(\Omega t + \phi)]} \approx J_0(m) E_0 e^{i\varpi t} + J_1(m) E_0 e^{i[(\varpi + \Omega)t + \phi]} - J_1(m) E_0 e^{i[(\varpi - \Omega)t - \phi]} + \dots$$

For $m = 0.1$, δm must $< 10^{-8} / \sqrt{\text{Hz}}$ at 10 Hz !





Experiment setup



- Phase locking two lasers with a frequency offset
- Intensity stabilization for both lasers
- Measure the beat signal – *Carrier-Carrier, Carrier-Sideband*





Signals we measure

Carrier-sideband beat note ~

$$J_1(m + \delta m(f)) E_1 E_2 (1 + \tilde{A}(f)) \cos(\phi + \delta\phi_{pll}(f) + \delta\phi_{SB}(f))$$

I/Q demodulation to get:

Relative amplitude noise ~

$$\frac{\delta m(f)}{m} + \tilde{A}(f) + \tilde{A}_\Omega(f) + \Delta\phi(\delta\phi_\Omega(f) + \delta\phi_{pll}(f) + \delta\phi_{SB}(f))$$

Phase noise ~

$$\delta\phi_\Omega(f) + \delta\phi_{pll}(f) + \delta\phi_{SB}(f)$$





Noise that limits the measurement sensitivity

- **Amplitude noise**

Laser intensity noise A

Mode mismatching noise due to beam jitter

Amplitude noise of the local oscillator A_Ω

- **Phase noise**

Local oscillator phase noise $\delta\phi_\Omega$,

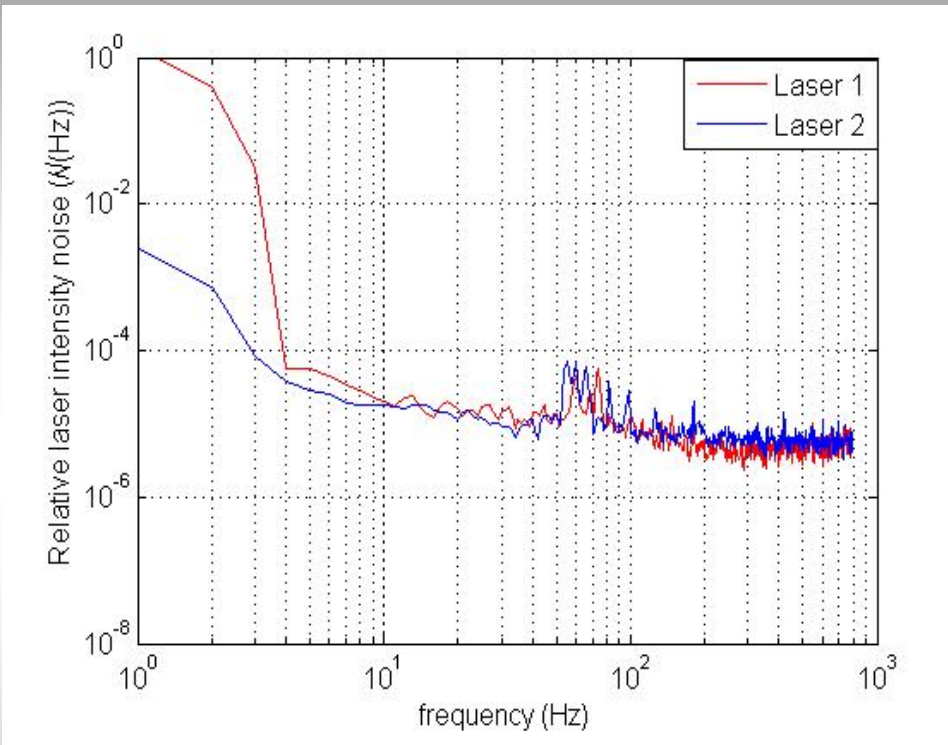
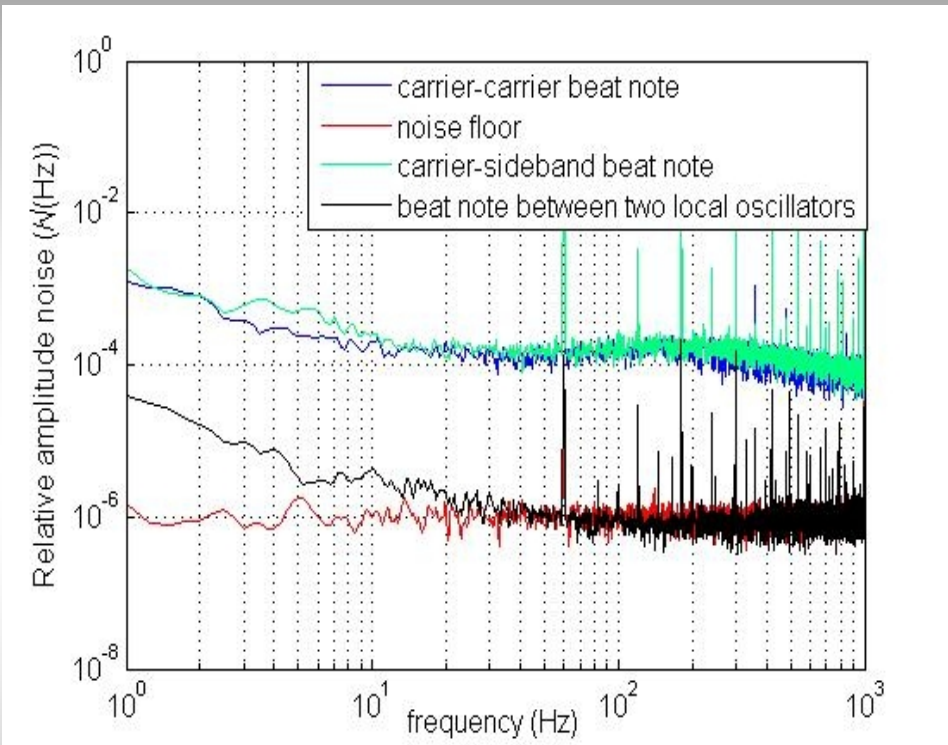
Phase locking noise between two lasers $\delta\phi_{PLL}$,

Sideband phase noise $\delta\phi_{SB}$



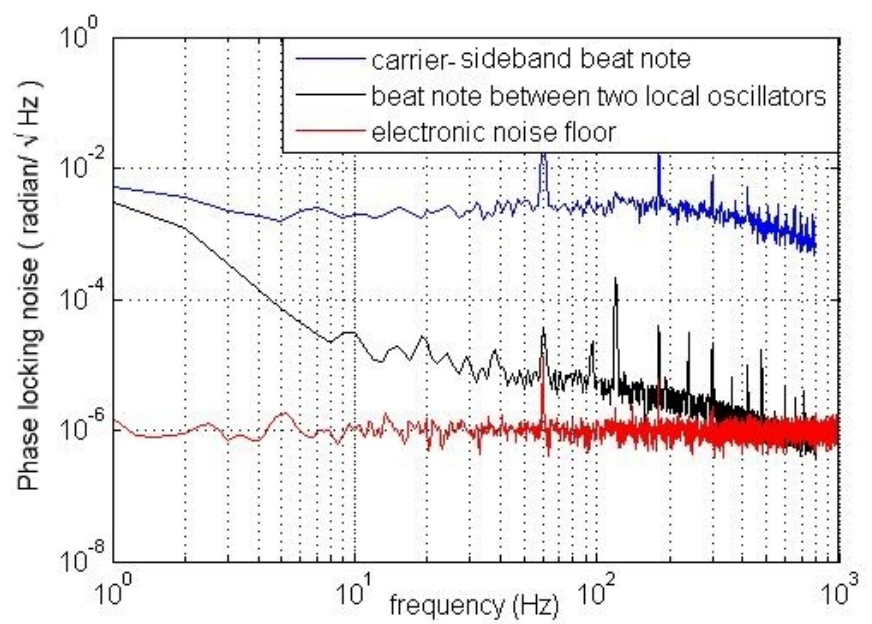
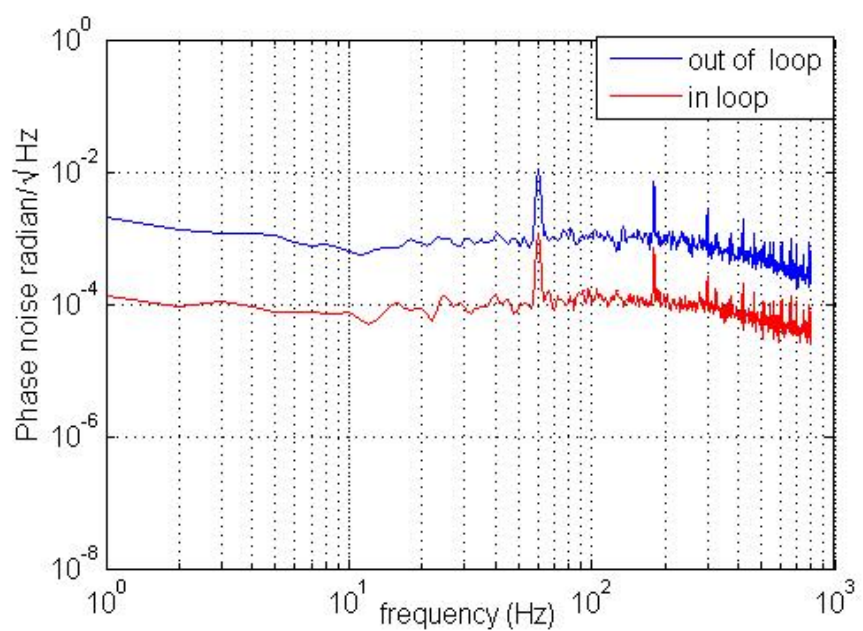


Amplitude noise





Phase noise



The phase noise – amplitude noise coupling is determined by the demodulation phase offset $\Delta\phi$ $\delta\phi(f)$

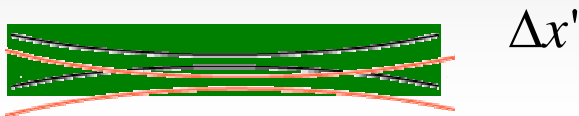
Phase offset drift need to be investigated





$$U_{00} = \hat{U}_{00} - \left(\frac{\Delta x}{\omega_0} + i \frac{\pi \omega_0}{\lambda} \Delta \theta \right) (\hat{U}_{10} + \hat{U}_{01})$$

$$\text{RIN} \sim 4 \left(\frac{\pi \omega_0}{\lambda} \right)^2 \Delta \theta \delta \theta + 4 \frac{\Delta x}{\omega_0^2} \delta x$$



For a 0.1 mm waist,

1 μm displacement offset plus $1 \mu\text{m} / \sqrt{\text{Hz}}$ displacement noise

OR

0.1 mrad tilt angle offset plus 10^{-5} radian / $\sqrt{\text{Hz}}$ tilt noise

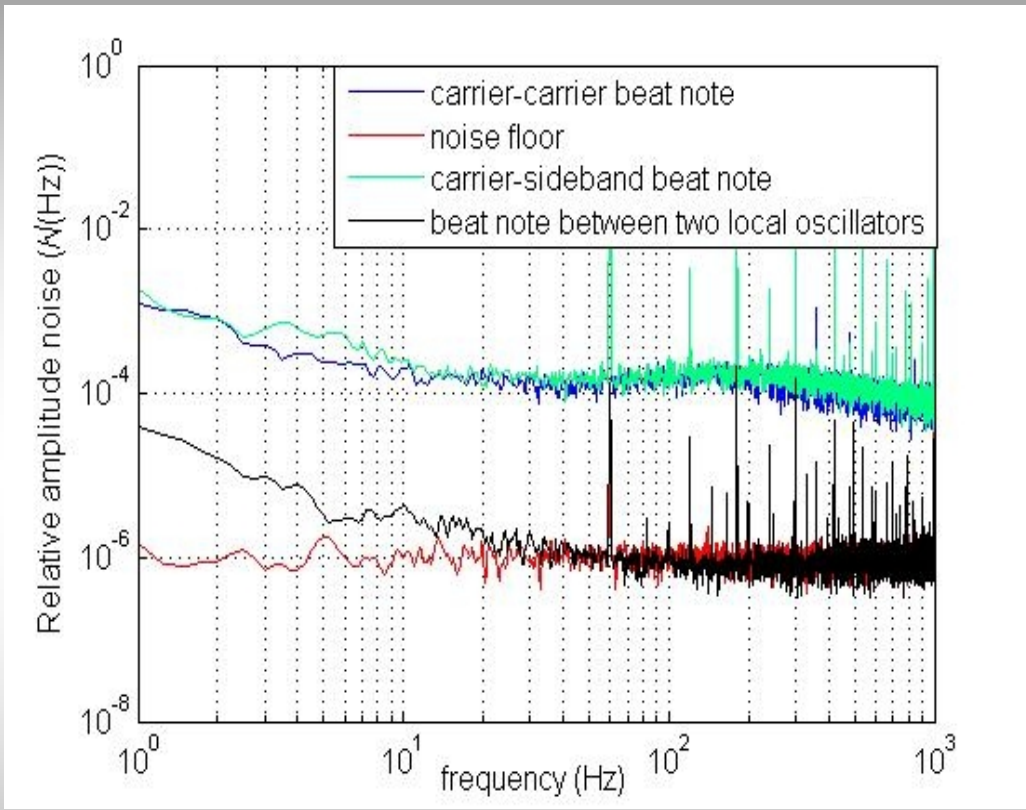


$10^{-4} / \sqrt{\text{Hz}}$ **Relative amplitude noise**





Common mode noise



Common mode noise rejection :





Difficulties to be overcome

- Electronic noise (mixer, phase shifter, etc) hunting
- Phase offset drift, phase locking
- Laser intensity stabilization

Feedback control using the power adjustment port of the Light Wave NPRO will strongly affect the laser frequency and break the phase locking

***Solution:** Control the laser power through the AOM*

- Beam jitter reduction

***Solution:** Characterize the beam jitter and feedback control using prism deflector*

- Application of low noise local oscillators

***Relative amplitude noise** $< 10^{-8} / \sqrt{\text{Hz}}$*





Summary

- *Experiment has been set up. Noise sources are analyzed.*
- *Need more precise noise characterization*
- *Need further test to verify the solutions for noise reduction*

