

An Interferometric
displacement sensor
for test mass
location.

by Mal Gray

David McClelland

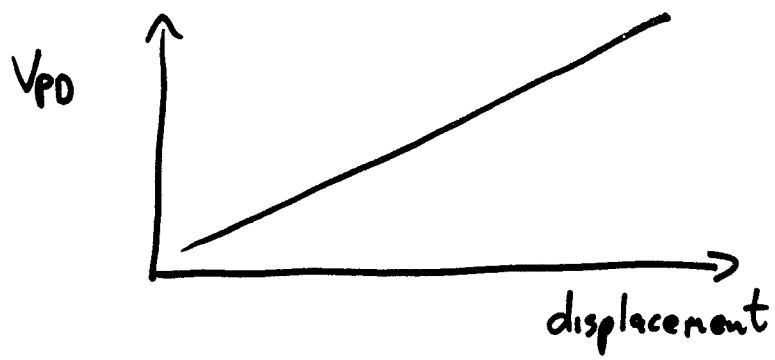
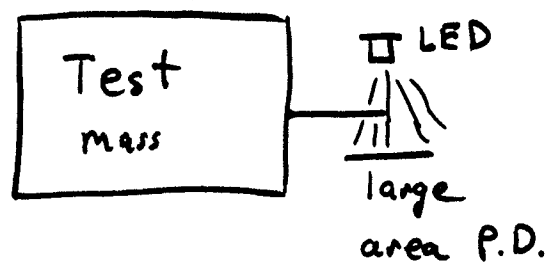
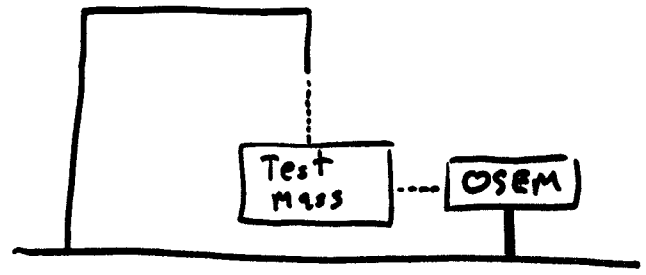
Hans Bachor

ANU Physics Department
5/24/96

LIGO-G960130-00-D

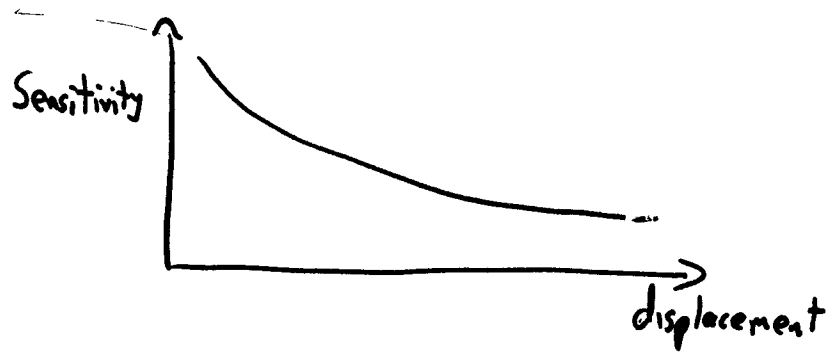
Performance of existing shadow meter

(based on analysis by Alex Abramovici, 5-13-99)

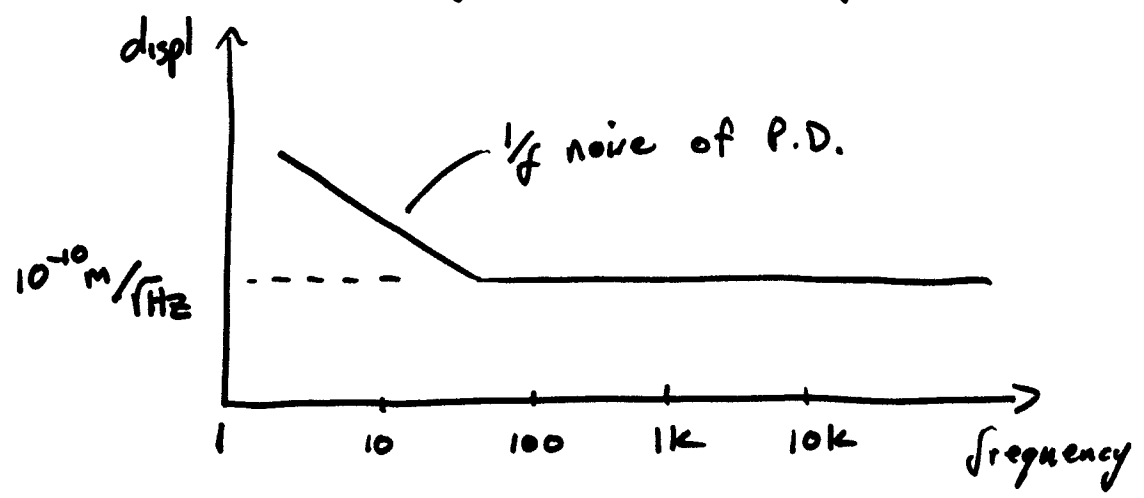


$$\text{Shot noise} \sim \sqrt{V_{pd}}$$

$$\text{Sensitivity} \sim \frac{1}{\sqrt{V_{pd}}}$$



Sensitivity vs frequency



when placed in feedback system, noise floor is attenuated by $\approx 1.3 \times 10^{-10}$

giving a contribution of $\approx 1.3 \times 10^{-20} \text{ m}/\sqrt{\text{Hz}}$ at 100Hz (at actuator).

amplifier output noise contribution $\sim 1.1 \times 10^{-20} \text{ m}/\sqrt{\text{Hz}}$

and LIGO upper limit of $10^{-19} \text{ m}/\sqrt{\text{Hz}}$

sensor displacement noise is a significant noise source in the existing configuration however, it is well within the LIGO limit.

dynamic range of shadow sensor $\approx \frac{10^{-4}}{10^{-10}} = 10^6 \Rightarrow 120 \text{ dB}$

Limits of sensitivity and dynamic range
due to shot noise.

for an optical intensity measurement

$$\text{maximum dynamic range} = \sqrt{\frac{i_{pd}}{2e}}$$

where $i_{dc} = P_{opt} \cdot S$

assuming $S \approx 0.5 \text{ AW} (\text{at } \lambda = 0.8 \mu\text{m})$ and $P_{opt} = 10 \text{ mW}$

$$\begin{aligned} \text{maximum dynamic range} &\approx 1.2 \times 10^8 \\ &\approx 160 \text{ dB} \end{aligned}$$

(or $\approx 170 \text{ dB}$ for $P_{opt} = 100 \text{ mW}$)

implication for sensitivity:

if we require $\Delta L_{max} = 0.1 \text{ mm}$

$$\Rightarrow \text{shot noise floor} = 10^{-12} \text{ m}/\sqrt{\text{Hz}} \text{ (10 mW)}$$

$$\Rightarrow 10^{-11} \text{ m}/\sqrt{\text{Hz}} \text{ for } \Delta L = 1 \text{ mm.}$$

this limit is intrinsically optical

\Rightarrow real devices are usually limited

by electronics dynamic range

Proposed specifications for the
interferometric sensor.

assuming LIGO stage II requires a significantly smaller sensitivity limit than $10^{-19} \text{ m}/\sqrt{\text{Hz}}$.

dynamic range of 1mm
(maximum excursion at $\approx 1 \text{ Hz}$, due to pendulum resonances).

sensitivity of better than $10^{-12} \text{ m}/\sqrt{\text{Hz}}$
at 100 Hz.

sensitivity of better than $10^{-9} \text{ m}/\sqrt{\text{Hz}}$
below 100 Hz.

a non-contact measuring system

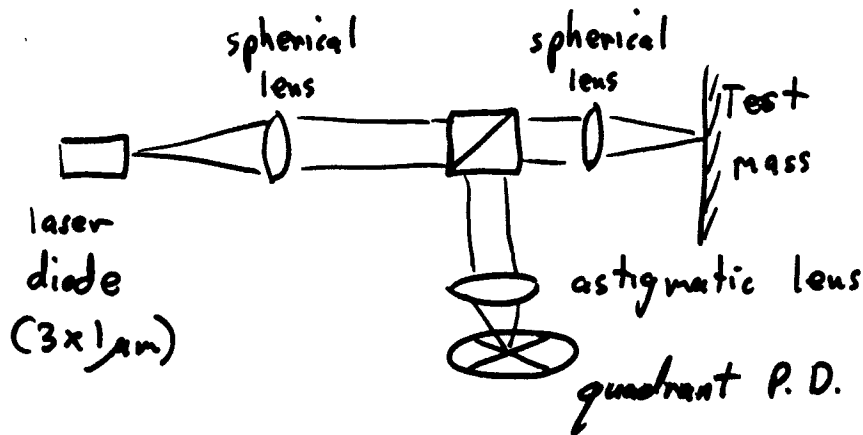
Three proposed methods of meeting these specs:

① astigmatic optical motion sensor

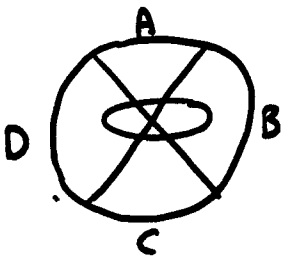
② fringe counting interferometer

③ tracking mirror & interferometer

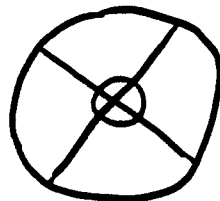
Astigmatic optical motion sensor



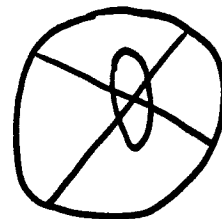
test mass
near side
of focus



test mass
at focus



test mass
far side
of focus



$$\text{signal out} = (A+C) - (B+D)$$

Advantages

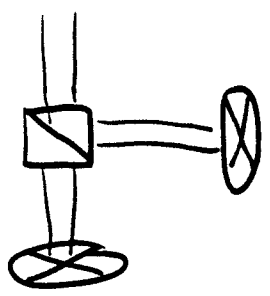
- # simple (non-interferometric) optics
- # gives vertical & horizontal motion as well
(A-C = vert, B-D = hori)
- # difference (balanced) detection \Rightarrow doesn't require a shot noise limited laser.

Disadvantages

- # realistic lasers (single mode diode) limit
power $\approx 100 \text{ nW} \Rightarrow$ dynamic range = 3×10^8
 \Rightarrow noise floor = $3 \times 10^{-12} \text{ m}/\sqrt{\text{Hz}}$
for $\Delta L = 1 \text{ nm}$

non-trivial electronic dynamic range issues

eg:



→ DC coupled for $\Delta L = 1\text{mm}$, low frequency motion (DC ... 100Hz).

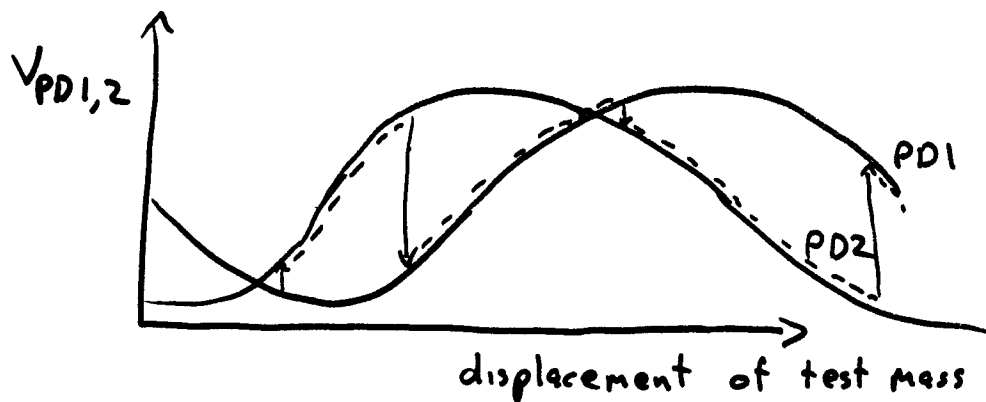
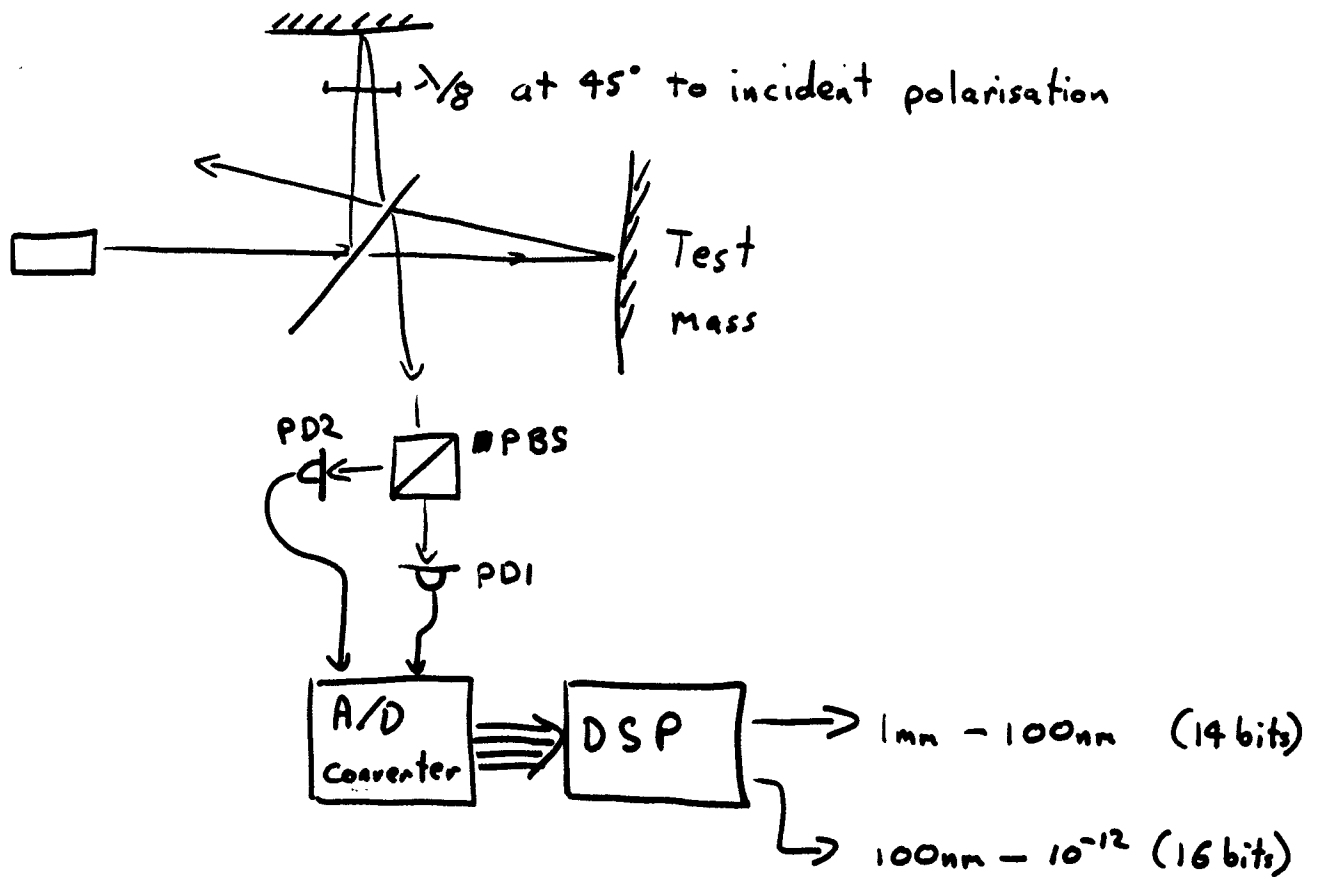
→ AC coupled for high sensitivity, high frequency response (100 ... 10kHz).

how to combine these 2 signals to give a useful feedback signal without reducing dynamic range?

⇒ cross-over network of some sort.

finalised optical design and all optics are in-house at ANU.

Fringe Counting Interferometer



PD1 & PD2
are 90°
out of phase.

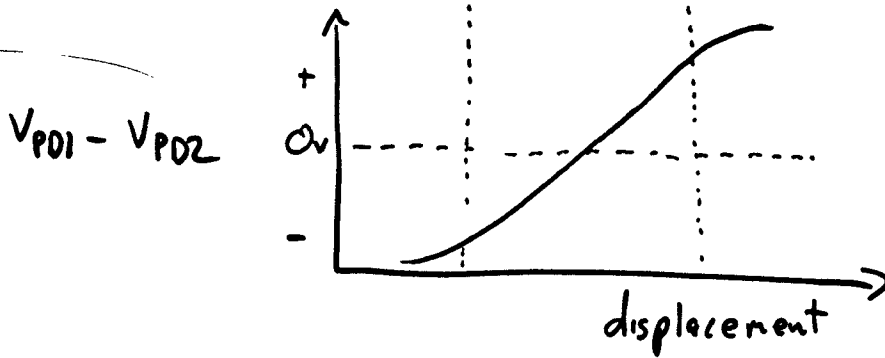
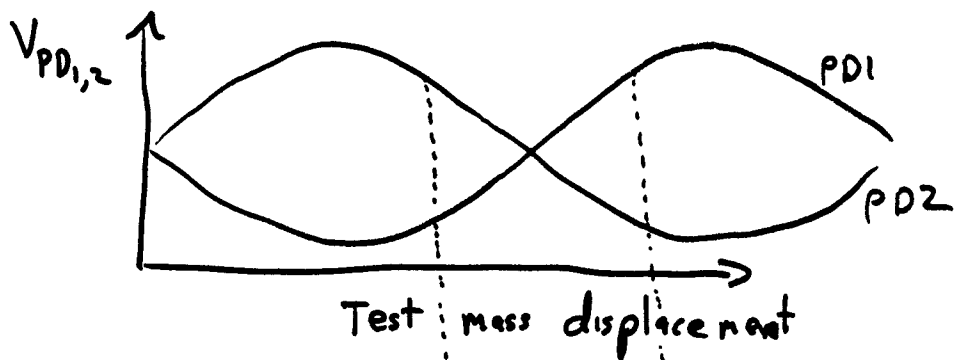
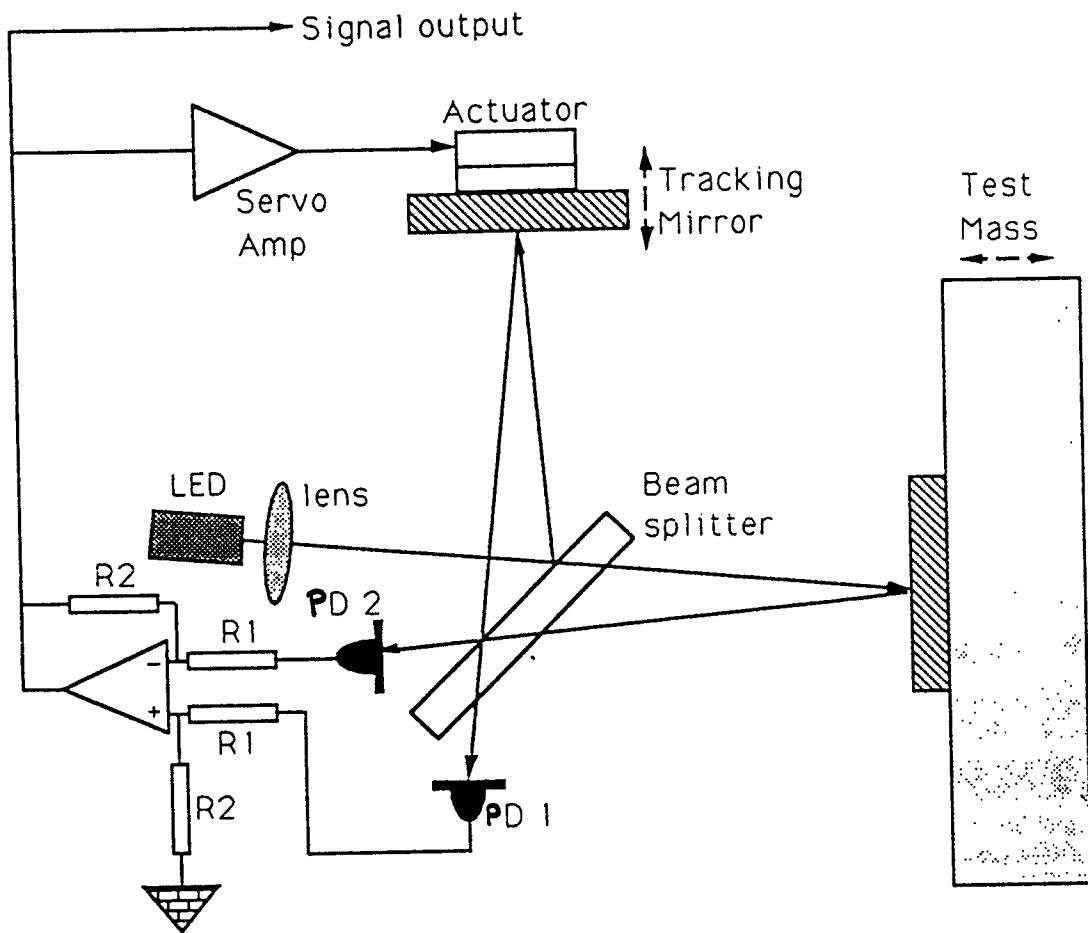
Advantages

- # arbitrary dynamic range
- # no internal feedback system

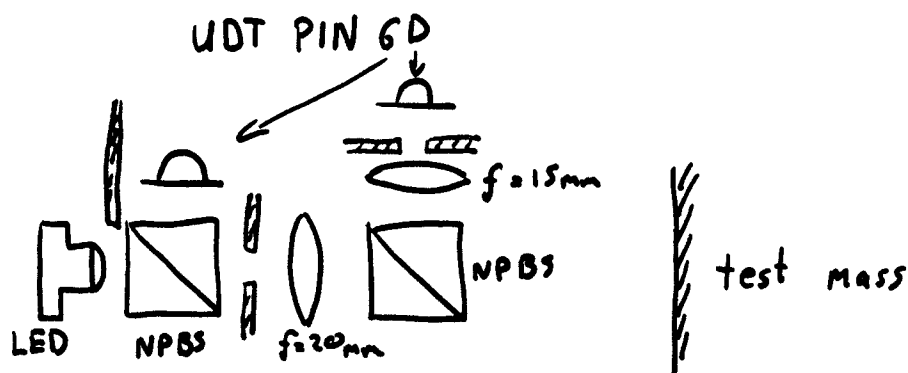
Disadvantages

- # require a stable laser ($\Delta \nu \leq 100 \text{MHz}$).
- # complex DSP task.
- # relative motion only.

Tracking mirror interferometer



Actual Optical Design



tracking mirror

image active area of LED onto end mirrors,
and LED can onto photo diodes.

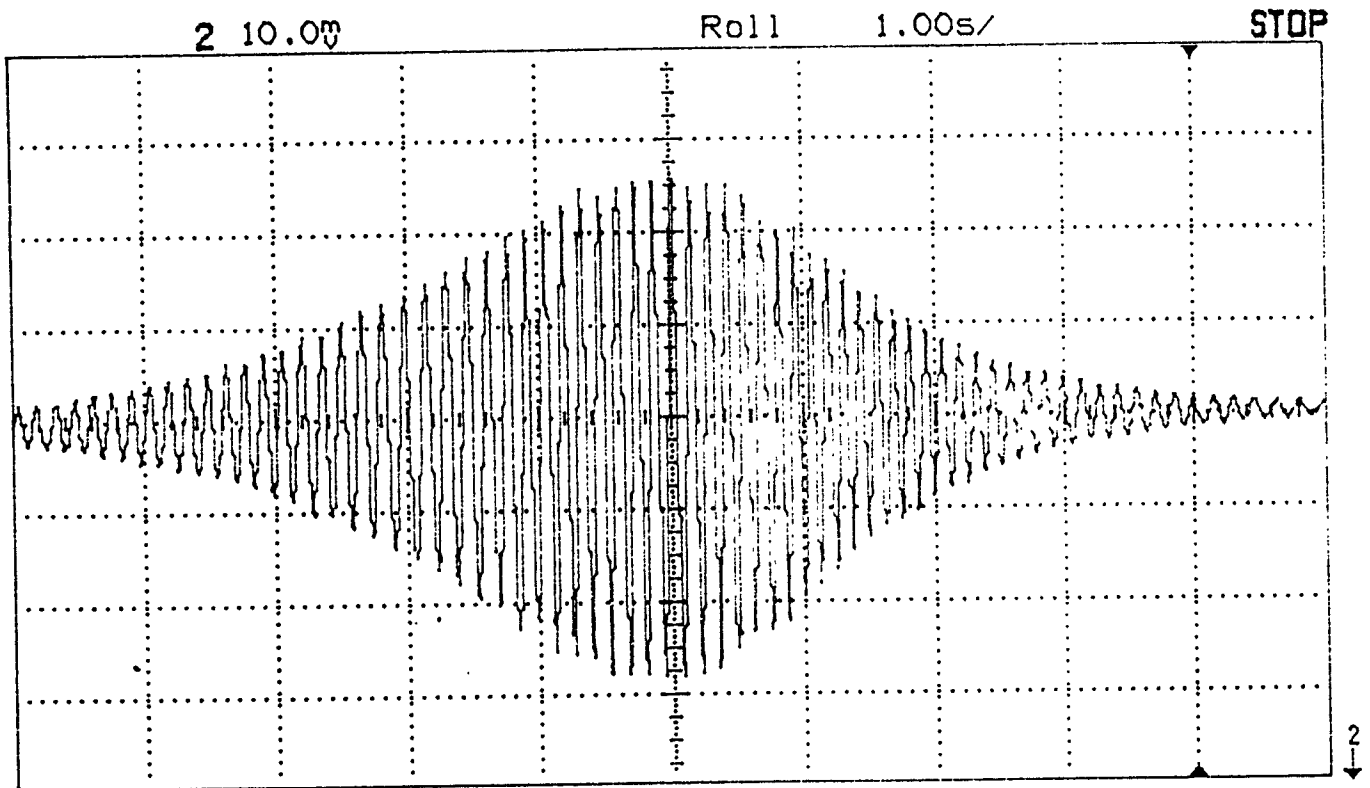
LED used is a Hitachi HE8807FL
giving $\approx 10\text{mW}$ at 880nm ($\pm 30\text{nm}$) for $i=100\text{mA}$

LED has a builtin lens, output is \approx colimated
(large active area \Rightarrow family of output angles).

fringe visibility ≈ 0.7 at both detectors

apertures reduce effective power to
 $\approx 100\mu\text{watts}$. \Rightarrow 140dB dynamic range possible
 \Rightarrow best sensitivity $\approx 2 \times 10^{-14} \text{ m}^2/\text{Hz}$

Autocorrelation of HE 8807FL

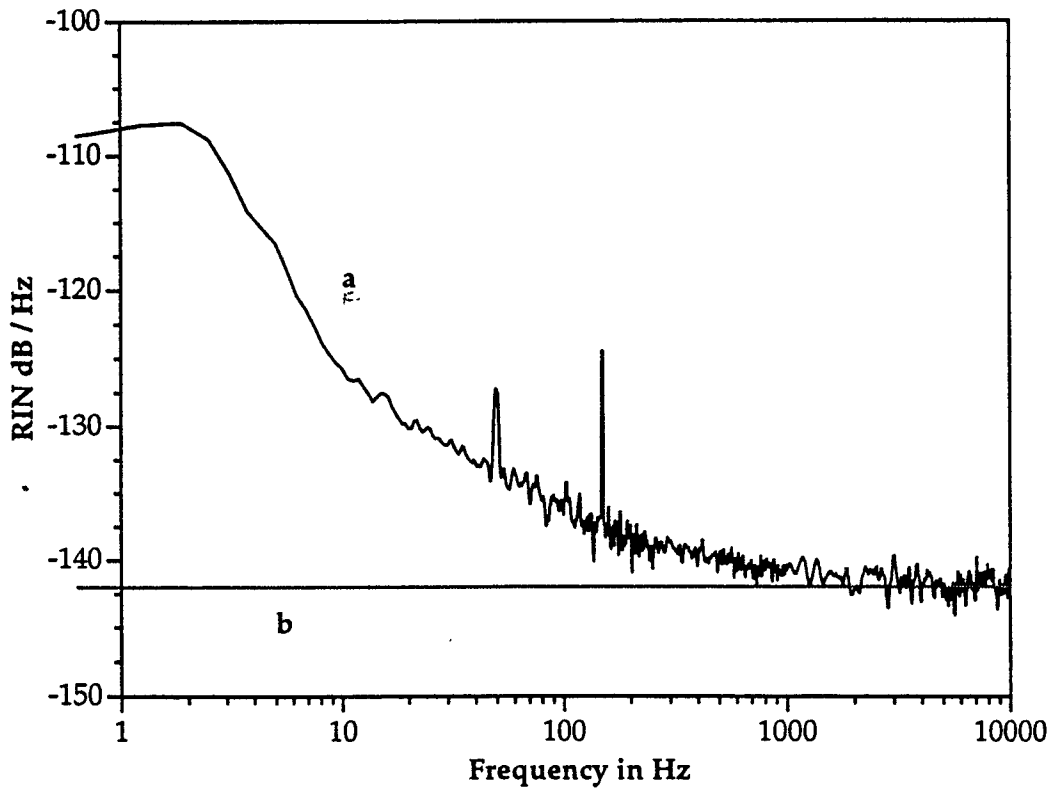


Fringe pattern of the HE8807FL: The pattern is obtained by monitoring the intensity at the antisymmetric port of the rigid Michelson interferometer while scanning the length of one arm through the fringe pattern. The vertical scale is in 10mV/div while the horizontal scale is 1sec/div and is proportional to the arm length difference in the Michelson interferometer.

free of structure and \approx Gaussian
 $\Rightarrow 880 \pm 30\text{nm}$ Gaussian spectrum

using a comparator \Rightarrow absolute length reference.

RIN of LED HE8807fl

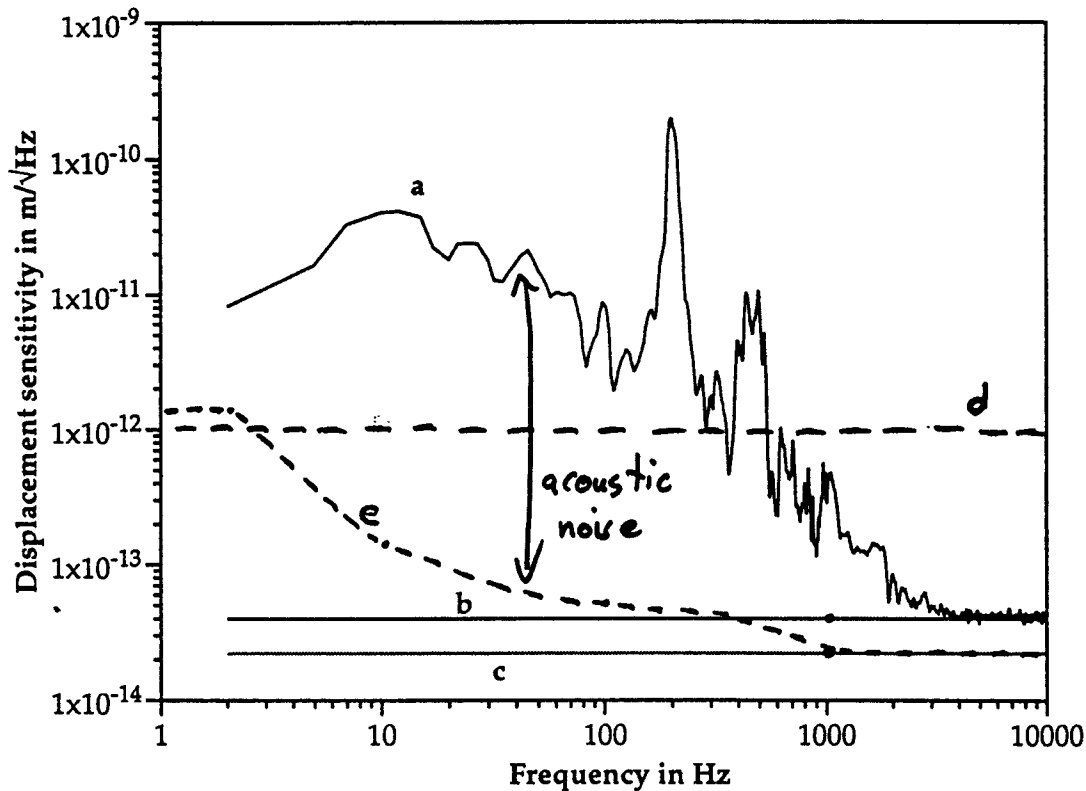


a: LED RIN experimental curve,

b: shot noise limit for the measurement in "a".

shot noise limited above ≈ 1 kHz

Free running sensitivity of LED sensor



- a:** free running noise floor of the LED sensor using a single detector,
- b:** predicted sensitivity based on optical power (shot noise) and electronic noise measurements,
- c:** predicted sensitivity based on optical power (shot noise) measurements alone,
- d:** initial sensitivity specification
- e:** sensitivity limit due to measured RIN

need to improve mechanical isolation of measurement.

Progress to date

- 1/ Build rigid interferometer, photodiode and LED circuits. Ensure free running system meets sensitivity specs.
(\approx 2 weeks to completion)
- 2/ Build tracking mirror / actuator system.
Test for closed loop sensitivity.
(designed, several mock-ups made, yet to start construction).
- 3/ Packaging / vacuum compatibility
(yet to be addressed)
- 4/ Testing on LIGO suspension system
(mid '97)