



Astrophysical Sources of Stochastic Gravitational-Wave Background

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Stochastic Background

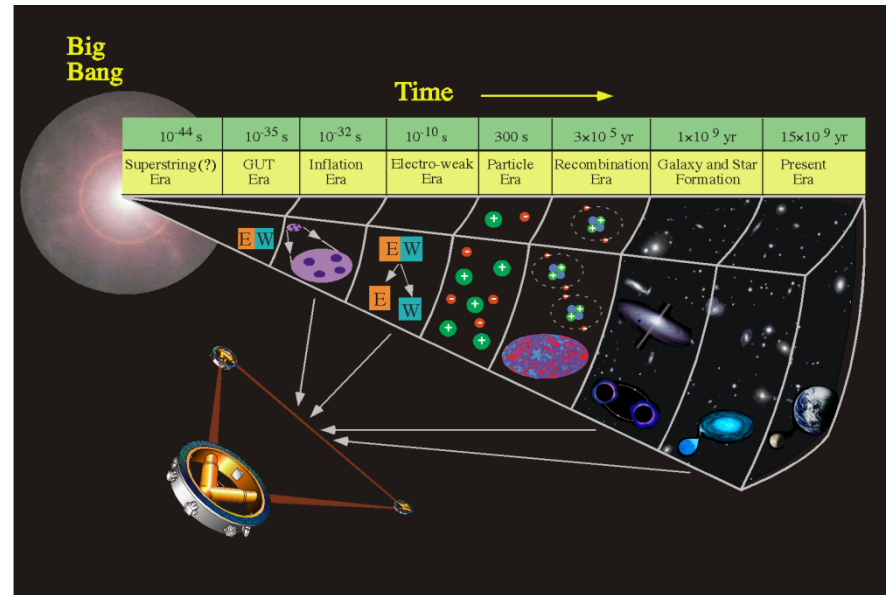
A stochastic background of gravitational waves (SGWB) has resulted from the superposition of a large number of unresolved sources since the Big Bang. We distinguish between two contributions:

➤ **Cosmological SGWB:**

signature of the early Universe
inflation, cosmic strings, phase transitions...

➤ **Astrophysical SGWB:**

sources since the beginning of stellar activity
compact binaries, supernovae, rotating NSs, core-collapse to NSs or BHs, supermassive BHs...



Plan of this talk

- Spectral properties of Astrophysical Backgrounds (AGBs)
- Detection regimes (resolved sources, popcorn, continuous)
- Some predictions
- Astrophysical constraints with advanced detectors

Spectral properties of AGBs

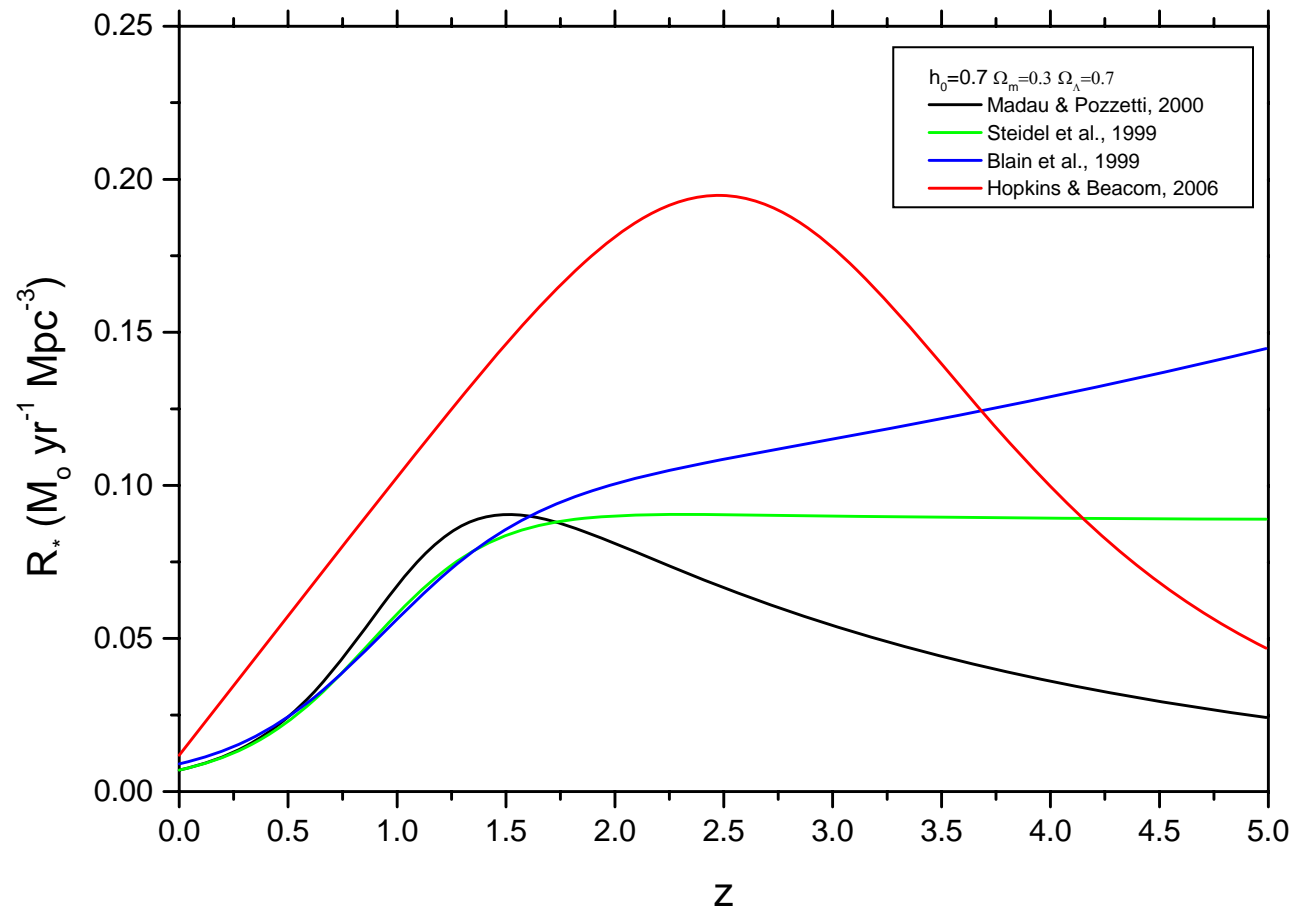
$$\Omega_{\text{gw}}(\nu_o) = \frac{8\pi G}{3c^3 H_0^2} \nu_o \int_0^{z_{\text{sup}}(\nu_o)} \overbrace{\frac{dR^o(z)}{dz}}^{\text{source cosmic rate}} \overbrace{\frac{1}{4\pi r^2(z)(1+z)} \frac{dE_{\text{gw}}}{d\nu}(\nu_o)}^{\text{fluence of single sources}} dz$$

$$\text{where } z_{\text{sup}}(\nu_o) = \begin{cases} \frac{\nu_{\text{max}}}{\nu_o} - 1 & \text{for } \nu_o < \frac{\nu_{\text{max}}}{1+z_{\text{max}}} \\ \nu_o & \\ z_{\text{max}} \sim 6 & \text{otherwise} \end{cases}$$

AGB spectra are determined by:

- the cosmological model ($H_0=70$ km/s/Mpc, $\Omega_m=0.3$, $\Omega_\Lambda=0.7$)
- the star formation history
- the spectral properties of individual sources $dE_{\text{gw}}/d\nu$

Cosmic Star Formation Rate



Detection Regimes

The **nature** of AGBs is characterized by the **duty cycle**, the ratio between the **average event duration** τ^o and the **time interval between successive events** Δt^o .

$$D(z) = \int_0^z \frac{\bar{\tau}^o(z')}{\Delta t^o(z')} dz' \quad \text{where} \quad \begin{cases} \bar{\tau}^o = (1+z')\bar{\tau} \\ \Delta t^o(z') = \left[\frac{dR^o}{dz'}(z') \right]^{-1} \end{cases}$$

➤ **resolved sources ($D \ll 1$):**

burst data analysis, optimal filtering

➤ **popcorn noise ($D \sim 1$)**

Maximum Likelihood statistic (Drasco et al. 2003), Probability Event Horizon (Coward et al. 2005)

➤ **gaussian stochastic background ($D \gg 1$)**

cross correlation statistic (isotropic/anisotropic)

Models

➤ Core collapse supernovae

- **Neutron star formation:** *Blair & Ju 1996, Coward et al. 2001-02, Howell et al. 2004, Buonanno et al. 2005*
- **Stellar Black Hole formation:** *Ferrari et al. 1999, de Araujo et al. 2000-04*

➤ Neutron stars

- **tri-axial emission:** *Regimbau & de F. Pacheco 2001-06*
- **bar or r-modes:** *Owen et al. 1998, Ferrari et al. 1999, Regimbau 2001*
- **phase transitions:** *Sigl 2006*

➤ Stellar Compact Binaries

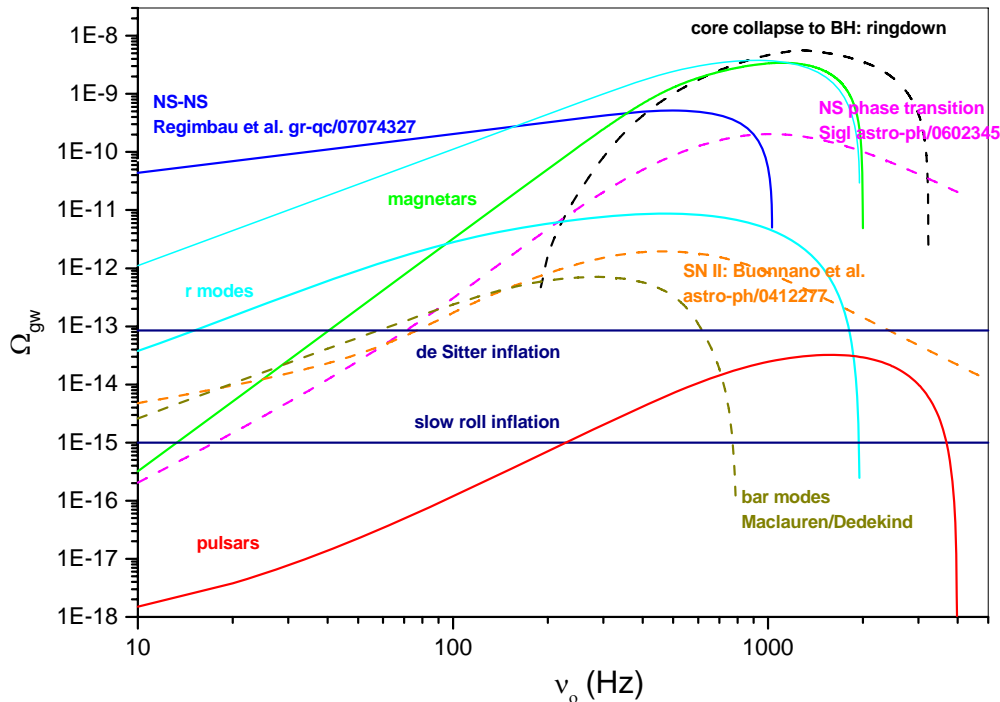
- **near coalescence (NS, BH):** *Regimbau et al. 2006-07, Coward et al. 2005 (BNS), Howell et al. 2007 (BBH)*
- **low frequency inspiral phase:** *Ferrari et al. 2002, Farmer & Phinney 2002, Cooray 2004 (WD-NS)*

➤ Capture of compact objects by SMBHs : *Barack & Cutler 2004*

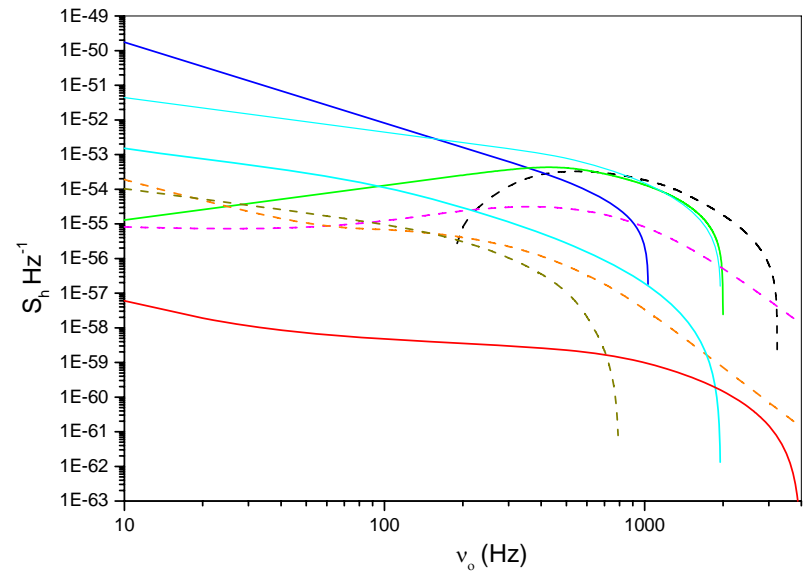
Spectra

The shape of AGBs is characterized by:

- **cutoff** at the maximal emission frequency ν_{\max}
- **maximum** which depends on the shape of the SFR and ν_{\max}
- often well approximated by **power laws at low frequency**



$$\text{spectral energy density: } S_h(\nu_o) = \frac{3H_0^2}{4\pi^2} \nu_o^{-3} \Omega_{gw}(\nu_o)$$



Tri-axial Neutron Stars

➤ source rate:

follows the star formation rate (fast evolution of massive stars)

$$\frac{dR^0}{dz}(z) = \lambda_p \frac{R^*(z)}{(1+z)} \frac{dV}{dz}(z)$$

$$\left\{ \begin{array}{l} \lambda_p = \text{mass fraction of NS progenitors in the range } 8\text{-}40 M_{\odot} \\ R^*(z) = \text{cosmic star formation rate} \end{array} \right.$$

➤ spectral energy density:

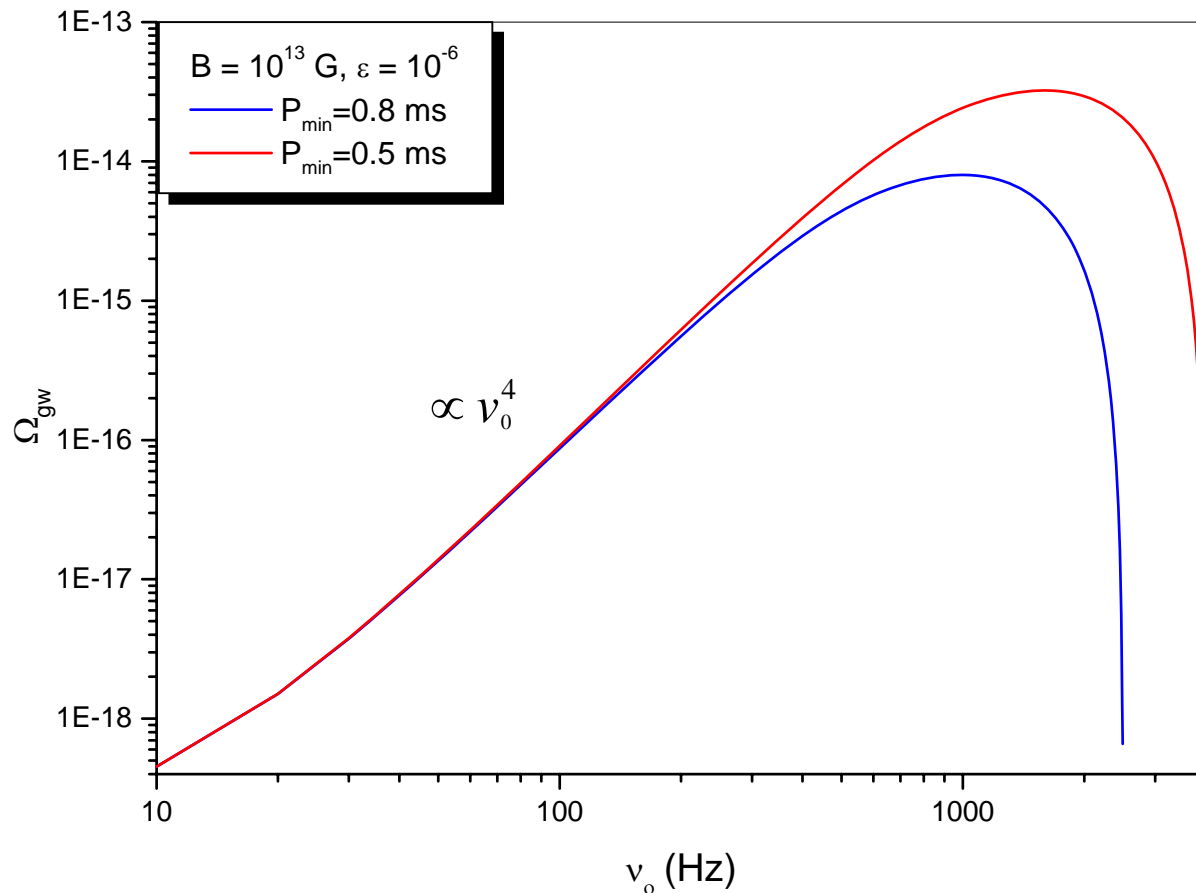
$$\frac{dE_{gw}}{d\nu} = \frac{192\pi^4 G I^3}{5c^2 R^6} \frac{\varepsilon^2}{B_{dip}^2 \sin^2 \alpha} \nu^3 \quad \text{with } \nu \in [0; 2/P_0]$$

Population synthesis (Regimbau & de F. Pacheco 2000, Faucher-Giguere & Kaspi 2006) :

- **initial period:** normal distribution with $\langle P_0 \rangle \sim 250\text{ -}300\text{ ms}$ and $\sigma \sim 80\text{ -}150\text{ ms}$
- **magnetic field:** log-normal distribution with $\langle \log B \rangle \sim 13\text{ G}$

Energy density spectrum

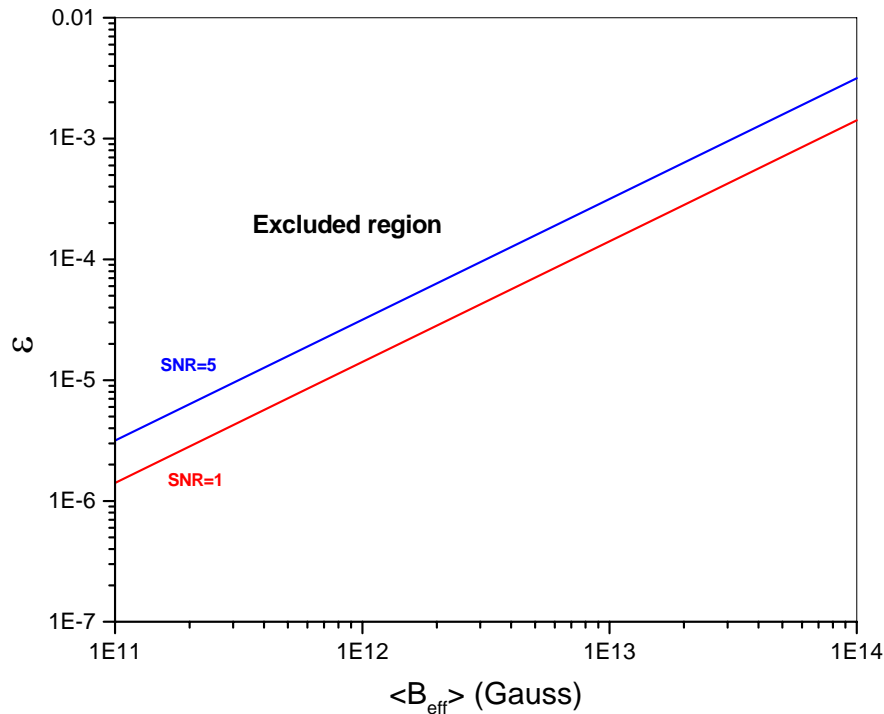
Spectrum from the cosmological population of rotating NSs, assuming initial period and magnetic field distributions derived from population synthesis.



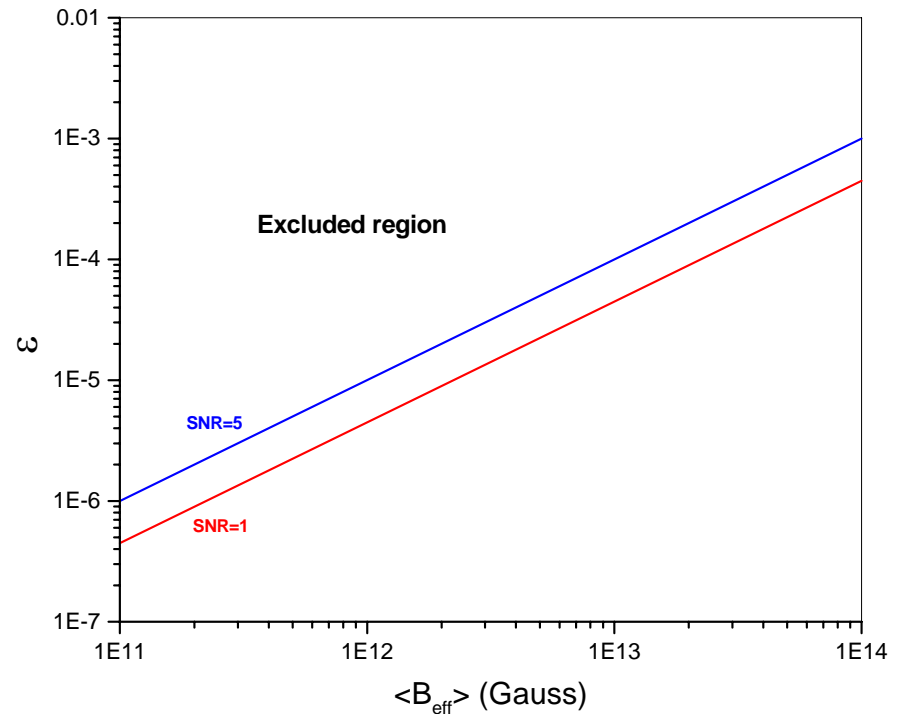
Constraints on ε - B^*

Constraints given by **coaligned and coincident detectors** (ex: H1-H2), for $T=3$ yrs of observation, in the range 10-500 Hz.

Advanced detectors (Ad LIGO sensitivity)



3rd generation detectors (Einstein Telescope)



*2-D projection, assuming the distribution of initial period derived from population synthesis.

Double Neutron Stars

Last thousands seconds before the last stable orbit in [10-1500 Hz]: 96% of the energy released.

➤ source rate:

$$\frac{dR^0}{dz}(z) = f_b \beta_{ns} \lambda_p \int \frac{R^*(t_c - t_d)}{1 + z_f} P(t_d) dt_d \frac{dV}{dz}(z)$$

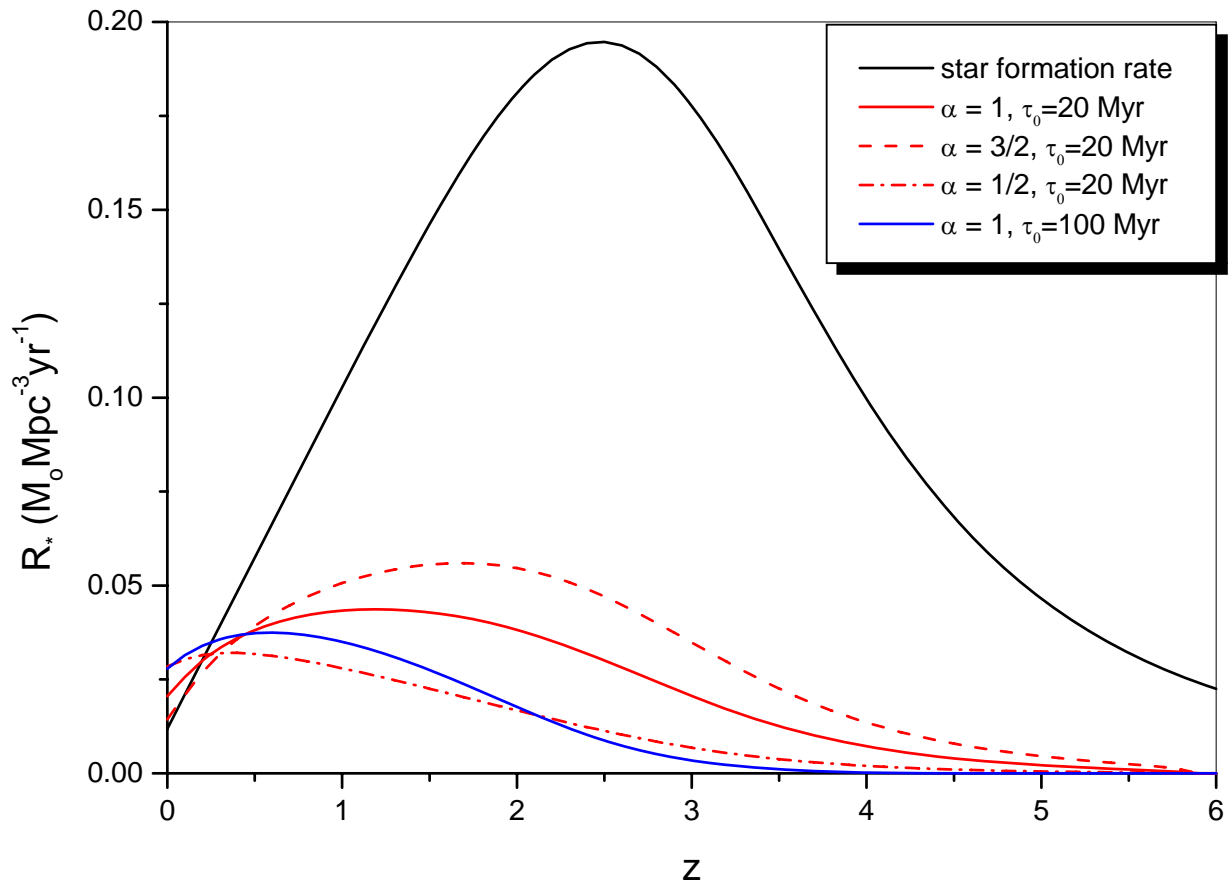
$$\left\{ \begin{array}{l} \lambda_p = \text{mass fraction of NS progenitors in the range } 8\text{-}40 M_{\odot} \\ f_b: \text{fraction of massive binaries formed among all stars} \\ \beta_{NS}: \text{fraction of massive binaries that remain bounded after the second supernova} \\ R^*(z) = \text{cosmic star formation rate} \\ P(t_d): \text{probability for a newly formed NS/NS to coalesce in a timescale } t_d \end{array} \right.$$

➤ spectral energy density:

$$\frac{dE_{gw}}{d\nu} = \frac{(\pi G)^{2/3}}{3} \frac{m_1 m_2}{(m_1 + m_2)^{1/3}} \nu^{-1/3} \text{ with } \nu \in [10 \text{ Hz}; \nu_{lso}]$$

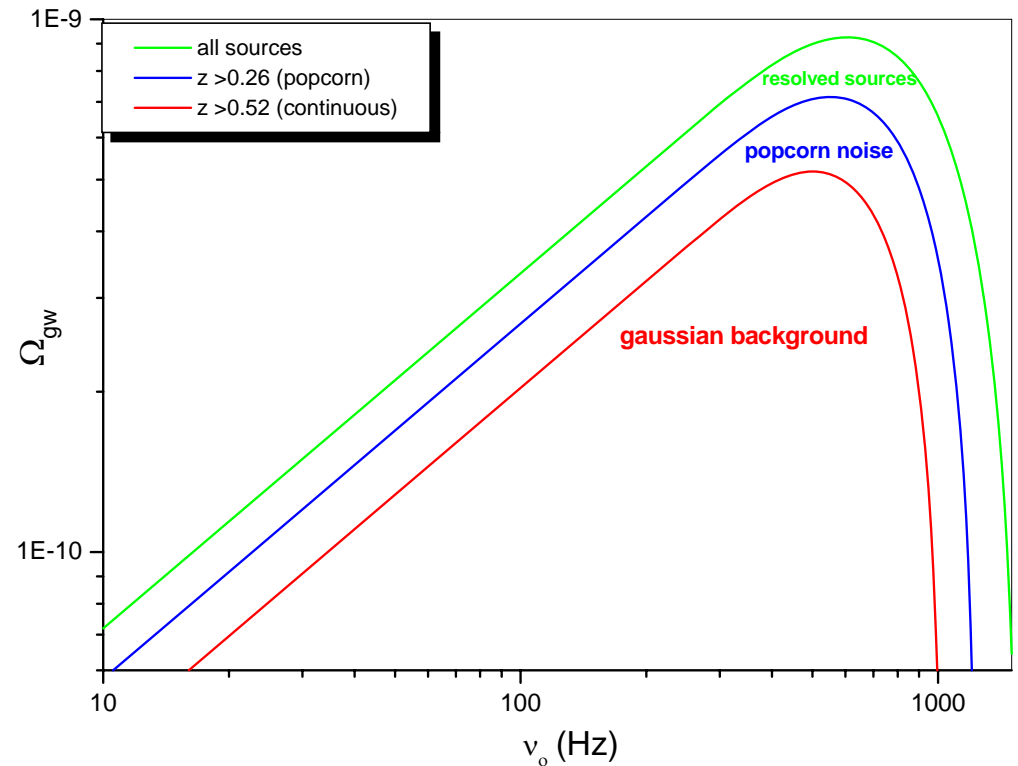
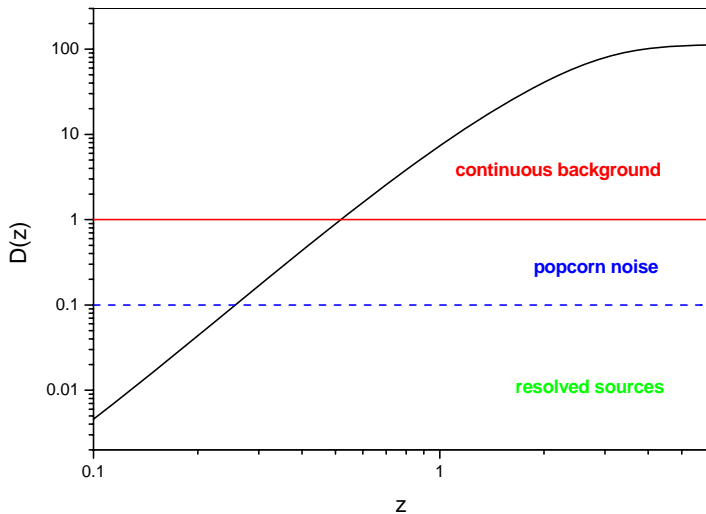
Cosmic coalescence rate

$P(t_d) \propto t_d^{-\alpha}$ with minimal delay τ_o



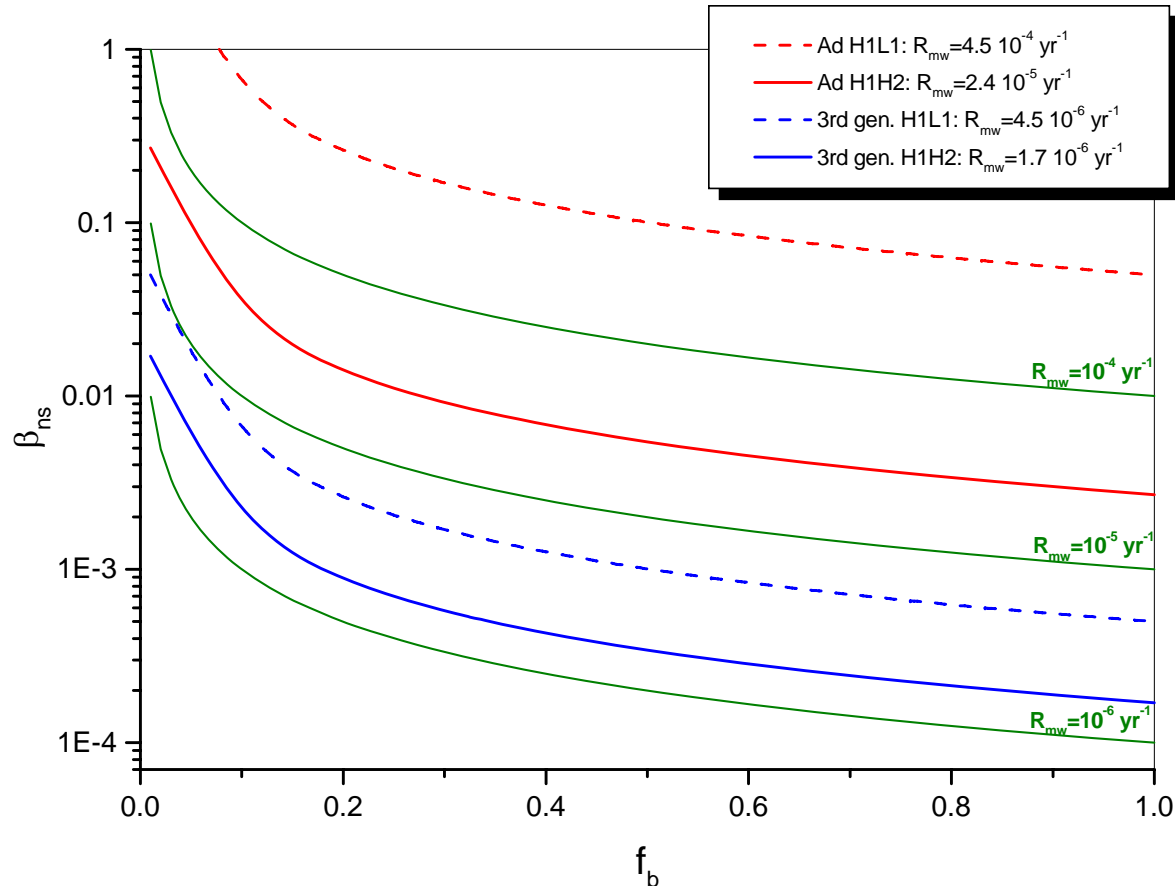
Energy density spectrum

Spectrum for the three regimes (resolved sources, popcorn noise and gaussian background), assuming a galactic coalescence rate $R_{\text{mw}} = 3 \cdot 10^{-5} \text{ yr}^{-1}$ and a coalescence time distribution with parameter $\alpha=1$ and $\tau_0=20\text{Myr}$.



Constraints on $f_b - \beta_{ns}^*$

Constraints given on the fractions f_b and β_{ns} for **T= 3 years** and **SNR=1**.



*2D projection, assuming a coalescence time distribution with parameter $\alpha=1$ and $\tau_0=20\text{Myr}$.

Summary and Conclusions

➤ Why are AGBs important (and need to be modeled accurately)?

- ✓ carry information about the star formation history, the statistical properties of source populations.
- ✓ may be a noise for the cosmological background

➤ How do AGBs differ from the CGB (and need specific detection strategies)?

- ✓ anisotropic in the local universe (directed searches)
- ✓ different regimes: shot noise, **popcorn noise** and gaussian
(maximum likelihood statistic, Drasco et al.; probability event horizon Coward et al.)
- ✓ spectrum characterized by a **maximum** and a cutoff frequency

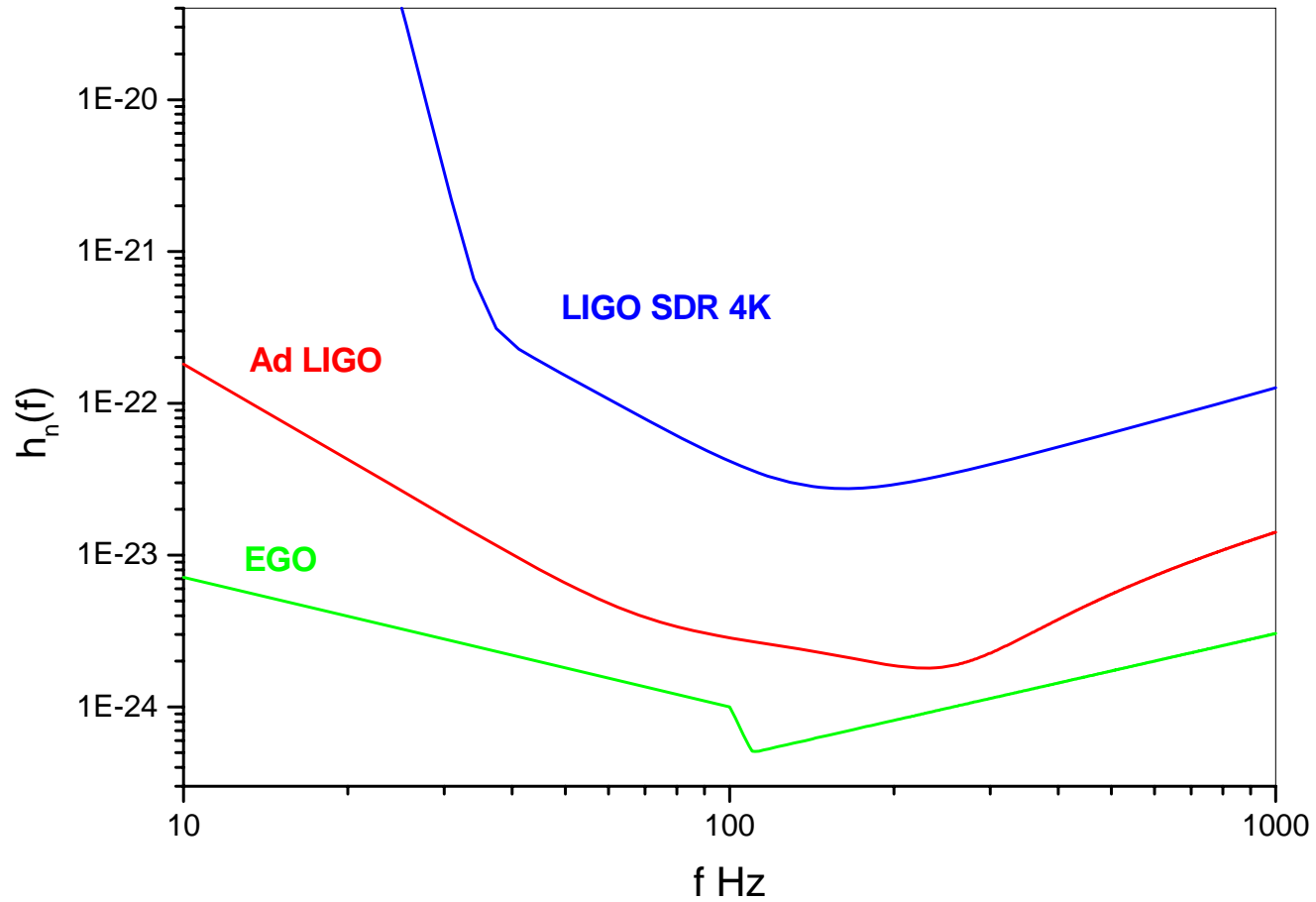
➤ Advanced detectors may be able to put interesting constraints

- ✓ NS ellipticity, magnetic field, initial period
- ✓ rate of compact binaries

....

Extra Slides

Sensitivity



Magnetars

- about **10-20%** of the radio pulsar population
- super-strong crustal **magnetic fields** ($B_{\text{dip}} \sim 10^{14} - 10^{16} \text{ G}$) formed by dynamo action in proto neutron stars with **millisecond rotation period** $P_0 \sim 0.6 - 3 \text{ ms}$ (break up limit - convective overturn).
- strong magnetic fields can induce significant **equatorial deformation**
 - **pure poloidal field** (Bonazzola 1996)

$$\varepsilon_B = g \frac{R^8 B^2 \sin^2 \alpha}{4GI^2} \approx 3.7 \times 10^{-4} g_{100} R_{10}^8 I_{45}^{-2} B_{15}^2$$

The distortion parameter g depends on both the EOS and the geometry of the magnetic field:
 $g \sim 1-10$ (non-superconductor), $g \sim 100-1000$ (type I superconductor), $g > 1000-10000$ (type II superconductor, counter rotating electric current)

- **internal field dominated by the toroidal component** (Cutler 2002, dall'Osso et al. 2007):

$$\varepsilon_B \sim -1.6 \times 10^{-4} \langle B_{t,16}^2 \rangle^2 \quad \text{when } B_t \gg B_p$$

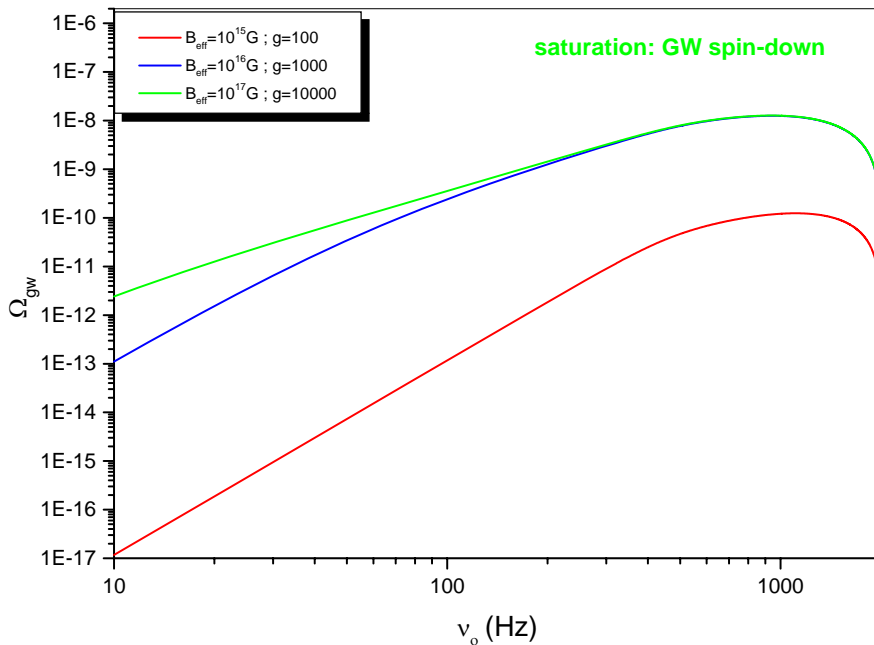
- **spectral energy density**

$$\frac{dE_{\text{gw}}}{d\nu} = K\nu^3 \left[1 + \frac{K}{\pi^2 I} \nu^2 \right]^{-1} \quad \text{where } K \sim \begin{cases} 3.9 \times 10^{37} g_{100}^2 B_{15}^2 & \text{(pure poloidal field)} \\ 7.1 \times 10^{36} B_{t,16}^4 B_{15}^{-2} & \text{(toroidal internal field)} \end{cases}$$

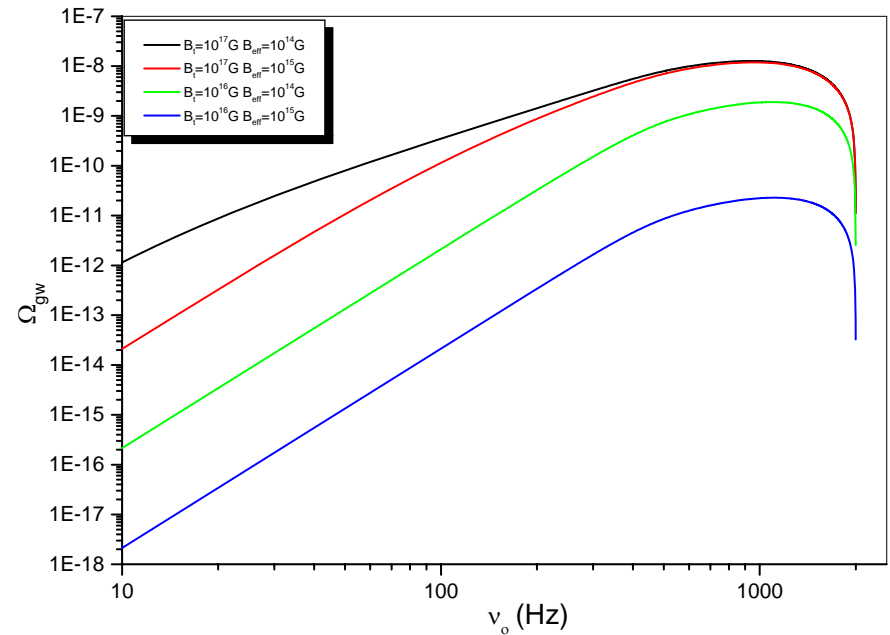
Energy density spectrum

Spectrum from the cosmological population of magnetars, assuming an initial period $P_i = 1$ ms and a galactic rate $R_{\text{mw}} = 0.1$ per century.

pure poloidal magnetic field



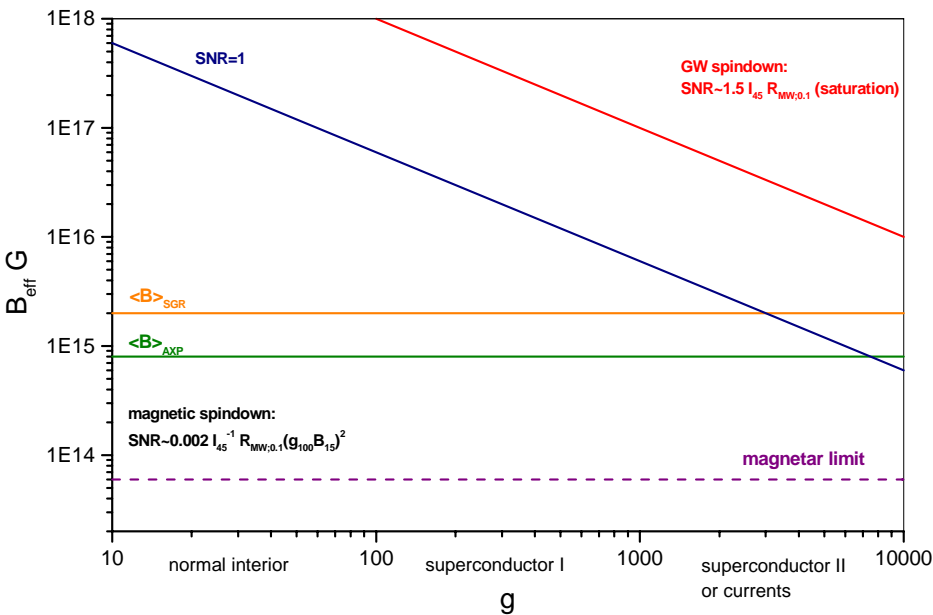
toroidal internal magnetic field



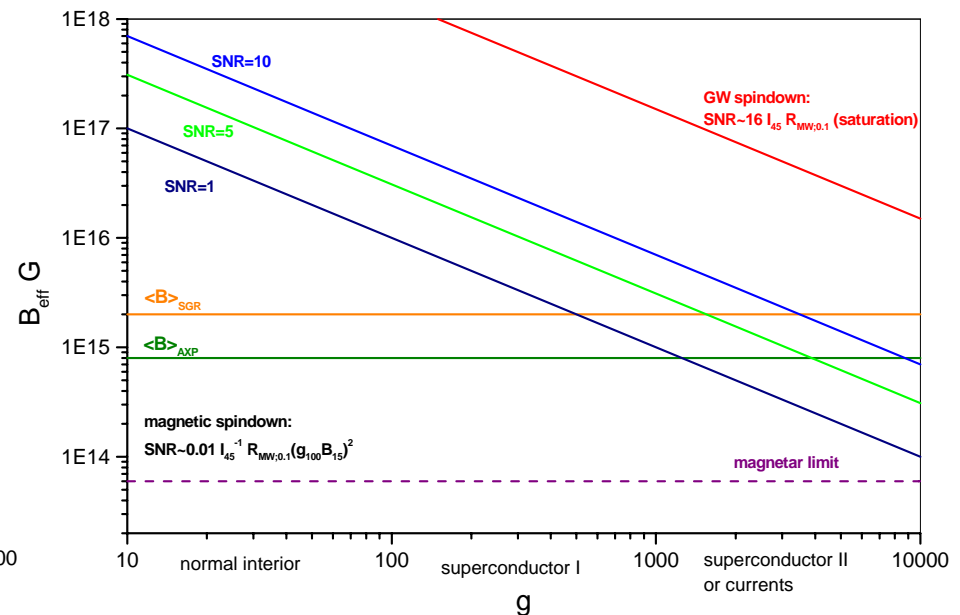
Constraints on g-B

Constraints given by **coaligned and coincident detectors (H1-H2)**, for T=3 yrs of observation, , in the range 10-500 Hz.

Advanced detectors (Ad LIGO sensitivity)



3rd generation detectors (Einstein Telescope)

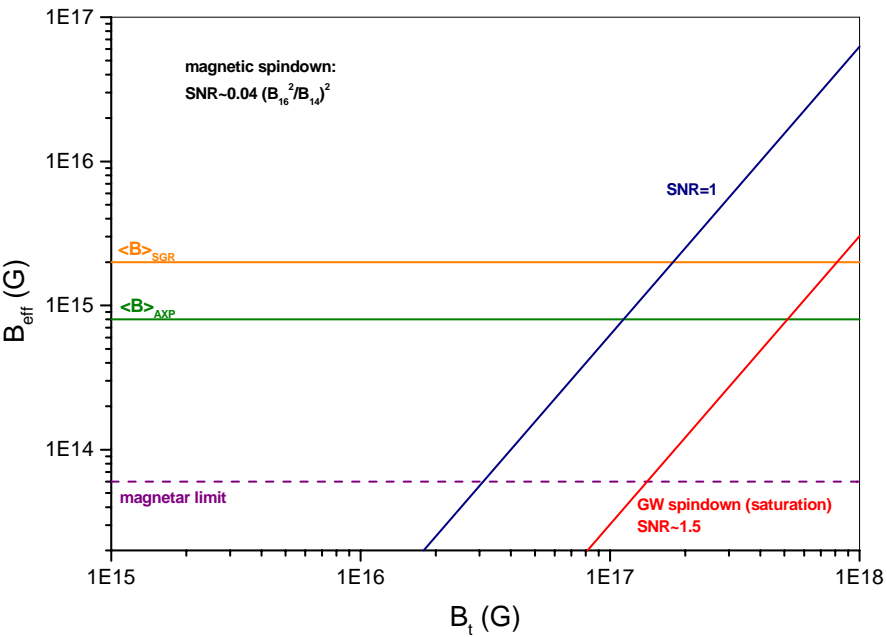


If no detection, we can rule out the model of spindown dominated by GW emission

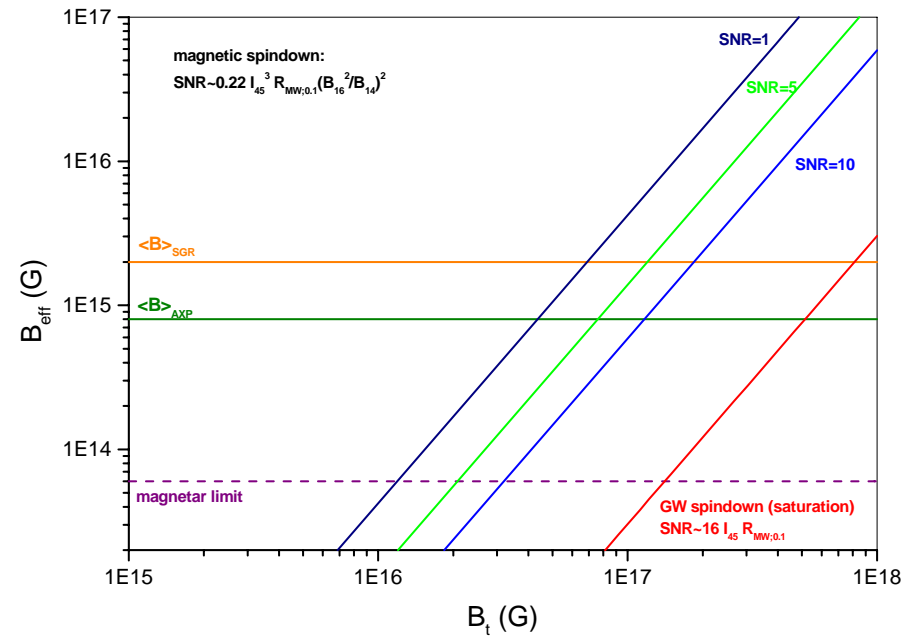
Constraints on $B_t - B$

Constraints given by **coaligned and coincident detectors** (ex: H1-H2), for $T=3$ yrs of observation, in the range 10-500 Hz.

Advanced detectors (Ad LIGO sensitivity)



3rd generation detectors (Einstein Telescope)



If no detection, we can rule out the model of spindown dominated by GW emission

NS Initial Instabilities

➤ source rate:

Only the small fraction of NS born fast enough to enter the instability window:

$$\frac{dR^0}{dz}(z) = \xi \lambda_p \frac{R^*(z)}{(1+z)} \frac{dV}{dz}(z)$$

$$\left\{ \begin{array}{l} \lambda_p = \text{mass fraction of NS progenitors in the range } 40\text{-}100 M_{\odot} \\ \xi = \text{fraction of newborn NS that enter the instability } (\xi = \int_{P_{\min}}^{P_{\max}} g(P_0) dP_0) \\ R^*(z) = \text{cosmic star formation rate} \end{array} \right.$$

Population synthesis ((Regimbau & de F. Pacheco 2000, Faucher-Giguere & Kaspi 2006) :

- **initial period:** normal distribution with $\langle P_0 \rangle \sim 250\text{-}300\text{ ms}$ and $\sigma \sim 80\text{-}150\text{ ms}$

➤ spectral energy density:

$$\frac{dE}{d\nu} = \frac{2E_0}{v_{\text{sup}}^2} v \left\{ \begin{array}{l} \text{r-modes: } E_0 = \Delta E_K \\ \text{bar-modes: } E_0 = E_{\text{MacLauren}} - E_{\text{Dedekind}} \end{array} \right.$$

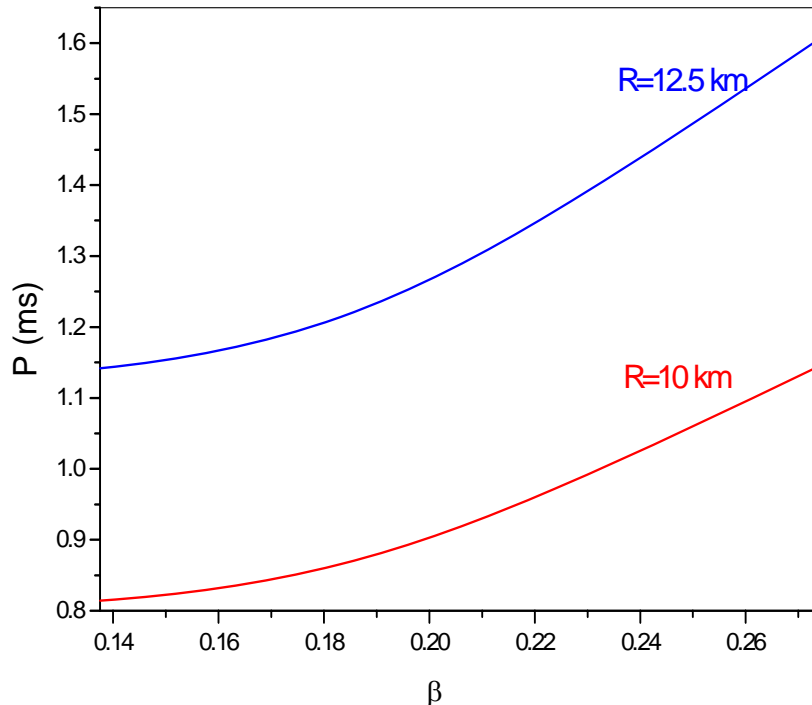
Instability windows

Bar modes:

secular instability: $0.14 < \beta < 0.27$

-R=10 km: $P_o \sim 0.8-1.1$ ms ($\xi \sim 2e-5$)

-R=12.5 km: $P_o \sim 1.1-1.6$ ms ($\xi \sim 3e-5$)

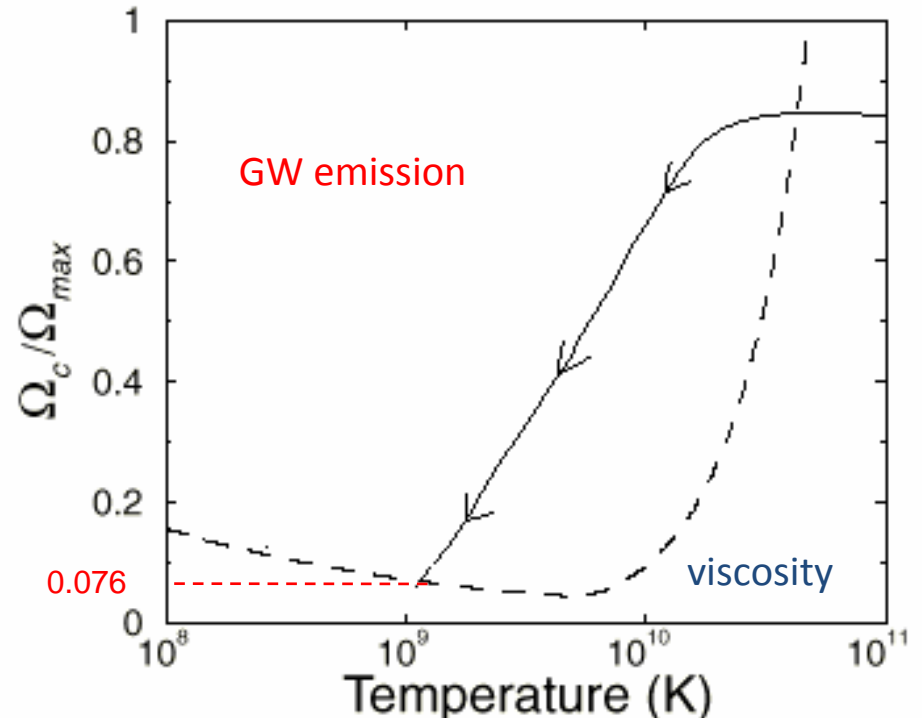


R modes:

$$|\tau_{\text{gw}}(\Omega)| < \tau_v(\Omega, T)$$

-R=10 km: $P_o \sim 0.7-9$ ms ($\xi \sim 5e-4$)

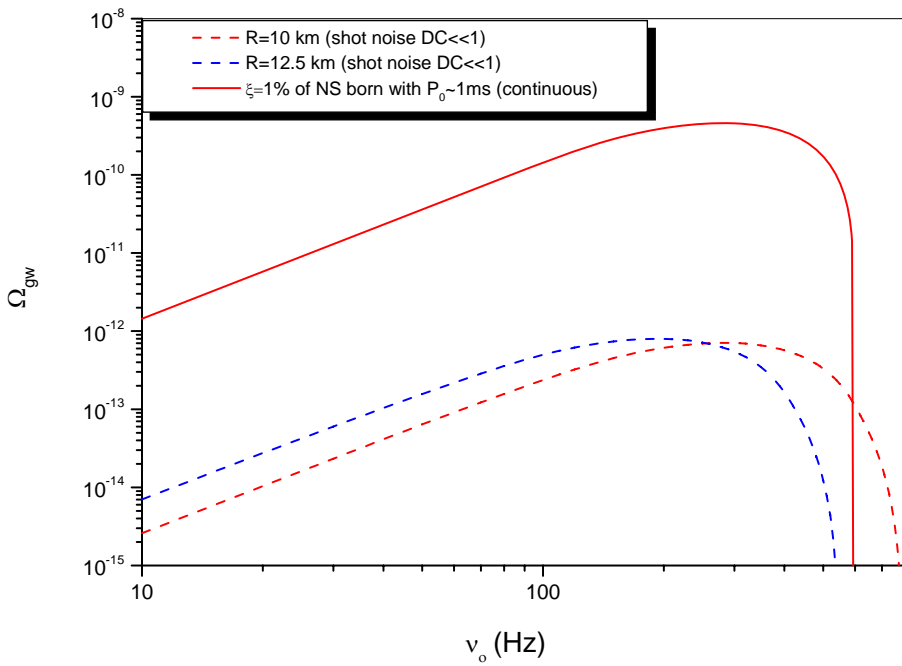
-R=12.5 km: $P_o \sim 1-12$ ms ($\xi \sim 8e-4$)



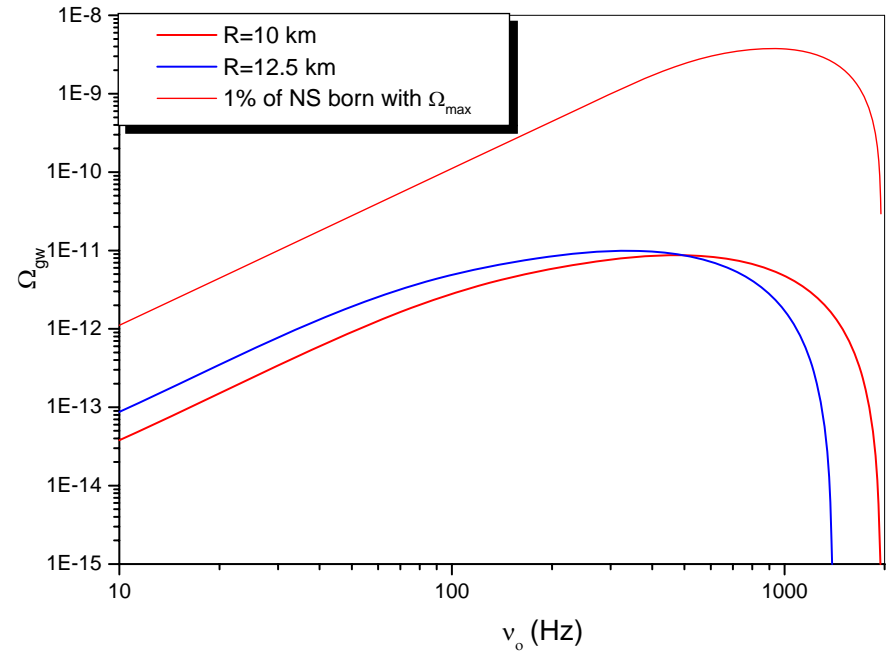
Energy density spectrum

Spectrum from the cosmological population of newborn NSs that enter the bar and r-modes instability windows.

Bar modes:



R modes:



Constraints on ξ

Constraints on the fraction of NS that enter the instability window of **bar modes** and **R modes** near the Keplerian velocity for **T= 3 years** and **SNR=1-5**.

Bar modes:

sensitivity	H1L1	H1H2
Advanced	-	2-4%
3 rd gen.	4-9%	0.2-0.4%

R modes:

sensitivity	H1L1	H1H2
Advanced	-	2-5%
3 rd gen.	4-10%	0.2-0.5%

Core collapse to BH (ringdown)

➤ source rate:

follows the star formation rate (fast evolution of massive stars)

$$\frac{dR^0}{dz}(z) = \lambda_p \frac{R^*(z)}{(1+z)} \frac{dV}{dz}(z)$$

$$\left\{ \begin{array}{l} \lambda_p = \text{mass fraction of NS progenitors in the range } 40\text{-}100 M_{\odot} \\ R^*(z) = \text{cosmic star formation rate} \end{array} \right.$$

➤ spectral energy density:

All the energy is emitted at the same frequency (Thorne, 1987)

$$\frac{dE_{gw}}{d\nu} = \varepsilon M_c c^2 \delta(\nu - \nu_*(M_c)) \text{ with } \nu_*(\text{kHz}) \sim 13 / M_c (M_{\odot})$$

mass of the BH: $M_c = \alpha M_p$ with $\alpha \sim 10 - 20\%$

efficiency: $\varepsilon < 7 \times 10^{-4}$

Energy density spectrum

Spectrum from the cosmological population of newborn distorted BHs. The resulted background is not gaussian but rather a **shot noise** with a duty cycle $DC \sim 0.01$.

