

# **A method for searching for gravitational waves triggered by astronomical observations**

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# Contents

- Gravitational wave search triggered by electro-magnetic observations
- World-wide detector network
- Coherent network analysis
- “RIDGE”--fully coherent network analysis
- Application: monitoring Sco X-1, the strongest X-ray emitted LMXB(low mass X-ray binary).

# Triggered search



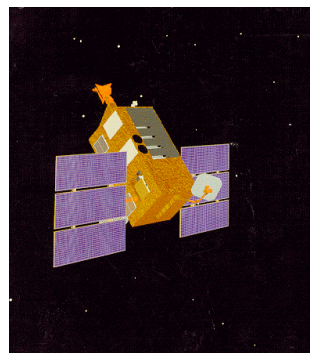
LIGO

+



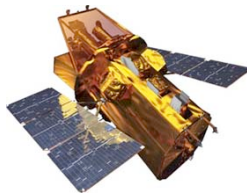
HETE

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RXTE

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SWIFT



Chandra

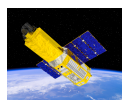


Parkes

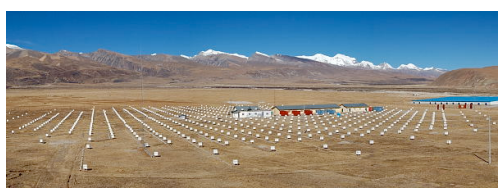
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XMM-Newton

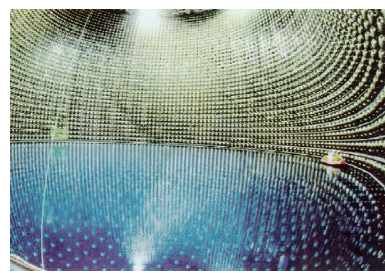


AstroE2



TIBET

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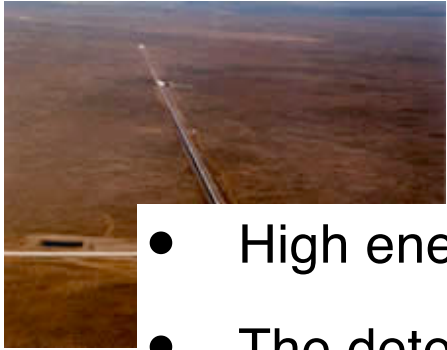
SuperKamiokande

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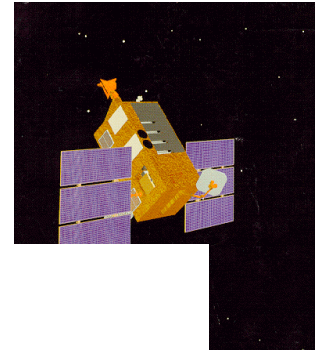


SDSS

# Triggered search

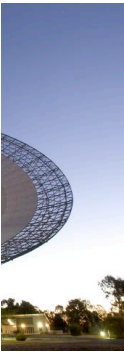


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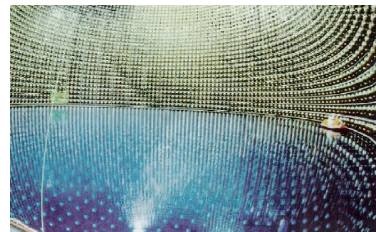
- High energy events are potentially G.W. sources for detection.
- The detection of G.W. can be enhanced by coincidences with electromagnetic observations:  
GRB, SGR, Pulsar glitch, LMXB, Supernova
- Particularly, when a pulsar glitch is observed, we may predict when it occurs next theoretically(Ito(1983))
  - > can adjust the observation schedule to the predicted event.
- Detection efficiency can be increased
  - Time coincidence -- specify data to analyze
    - > sophisticated analysis
  - Source location
    - accurate recovery of waveforms
    - > extract astrophysical parameters-Newton

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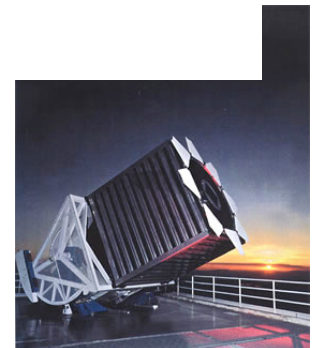
TIBET

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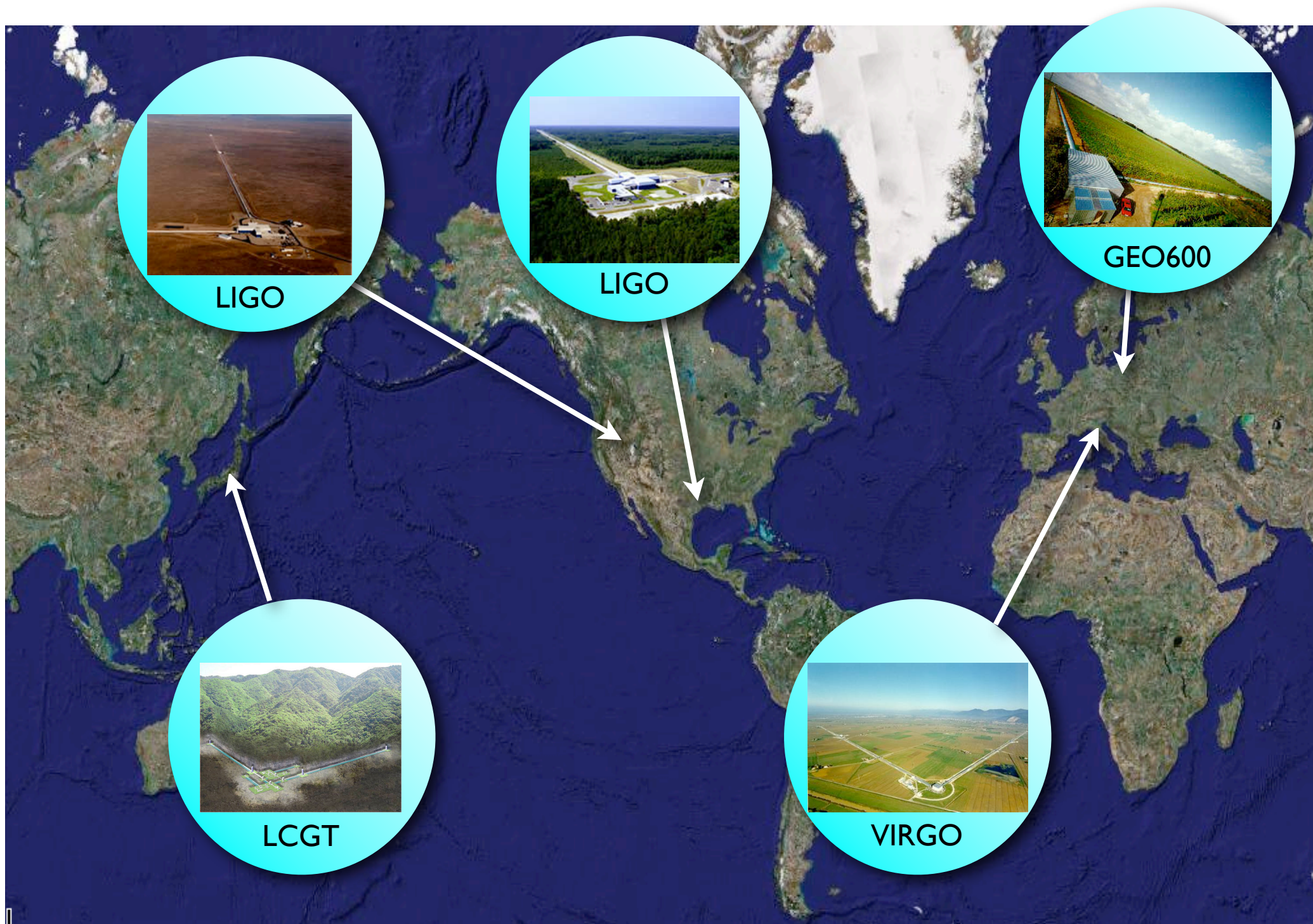
SuperKamiokande

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SDSS

# Gravitational wave detector network



# Gravitational wave detector network



- When gravitational waves arrive at the earth, the signals are encoded into output of each detector.
- For data analysis to extract the signals,
  - how to combine these data streams from the detectors?
  - how to recover the signal waveforms to obtain astronomical information?

One approach is coherent network analysis



LCGT

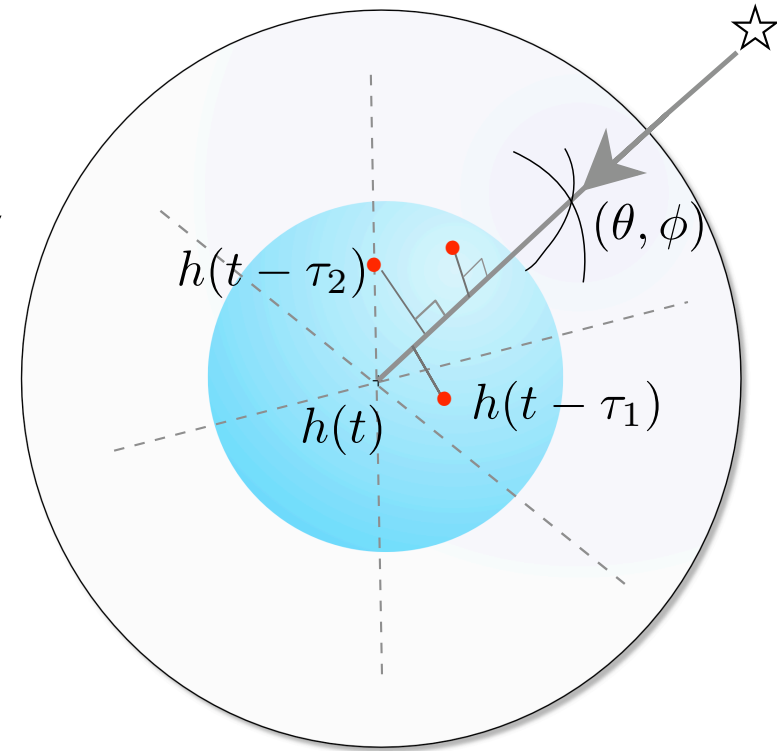


VIRGO

# Coherent network analysis

Natural way to handle networks of detectors

- Use arbitrary # of detectors
- Statistics combines all data streams coherently
- Recovery of polarization waveforms and sky position



$$\begin{bmatrix} x_1(t) \\ \vdots \\ x_d(t) \end{bmatrix} = \begin{bmatrix} F_{1+}(\theta, \phi) & F_{1\times}(\theta, \phi) \\ \vdots & \vdots \\ F_{d+}(\theta, \phi) & F_{d\times}(\theta, \phi) \end{bmatrix} \begin{bmatrix} h_+(t) \\ h_\times(t) \end{bmatrix} + \begin{bmatrix} n_1(t) \\ \vdots \\ n_d(t) \end{bmatrix}$$

**data = response x gw + noise**

$$\text{gw } \xi_i(t) = F_{i+}(\theta, \phi)h_+(t) + F_{i\times}(\theta, \phi)h_\times(t)$$

Changing  $(\theta, \phi)$ , look for

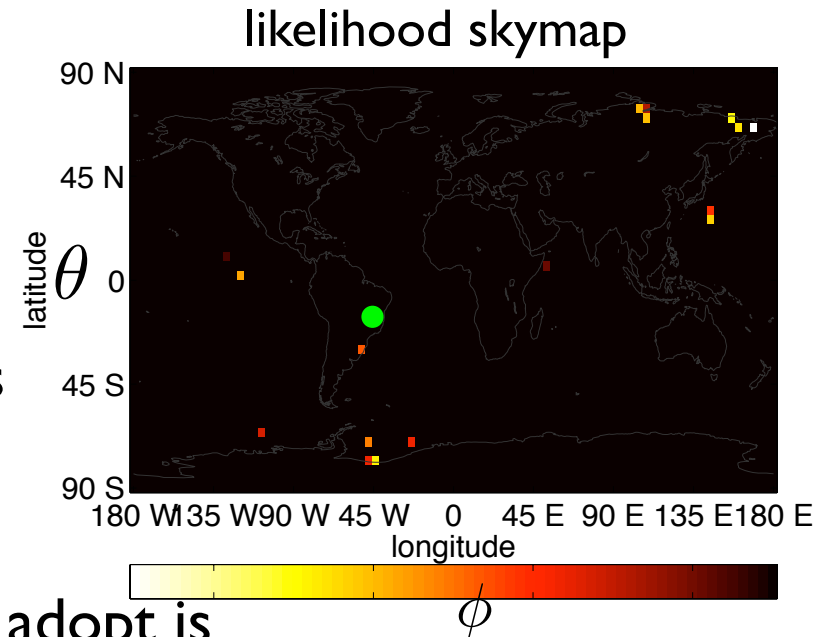
$$L = \sum_{i=1}^d \left( \sum_{t=0}^T \| x_i(t) - \xi_i(t + \tau_i, \theta, \phi) \|^2 \right) \rightarrow \text{minimum}$$

# Tikhonov regularization

$$\begin{bmatrix} x_1(t) \\ \vdots \\ x_d(t) \end{bmatrix} = \begin{bmatrix} F_{1+}(\theta, \phi) & F_{1\times}(\theta, \phi) \\ \vdots & \vdots \\ F_{d+}(\theta, \phi) & F_{d\times}(\theta, \phi) \end{bmatrix} \begin{bmatrix} h_+(t) \\ h_\times(t) \end{bmatrix} + \begin{bmatrix} n_1(t) \\ \vdots \\ n_d(t) \end{bmatrix}$$

$\parallel$                        $\parallel$   
 $F_+(\theta, \phi)$      $F_\times(\theta, \phi)$

- Detection of G.W. is an inverse problem
- Due to the degree of freedom of the response matrix, the problem becomes ill-posed ( When  $F_\times(\theta, \phi) \propto F_+(\theta, \phi)$  , matrix becomes rank deficient.)
- The error in the best-fit solution is amplified



The technique to address this rank deficiency we adopt is

Tikhonov regularization based approach (M. Rakhmanov **CQG 23,S673 (2006)**)

$$L_g = \sum_{i=1}^d \left( \sum_{t=0}^T \| x_i(t) - \xi_i(t, \theta, \phi, \tau_i) \|^2 \right) + g\Omega[h]$$

Impose regulator on standard maximum likelihood statistic

similar approach:

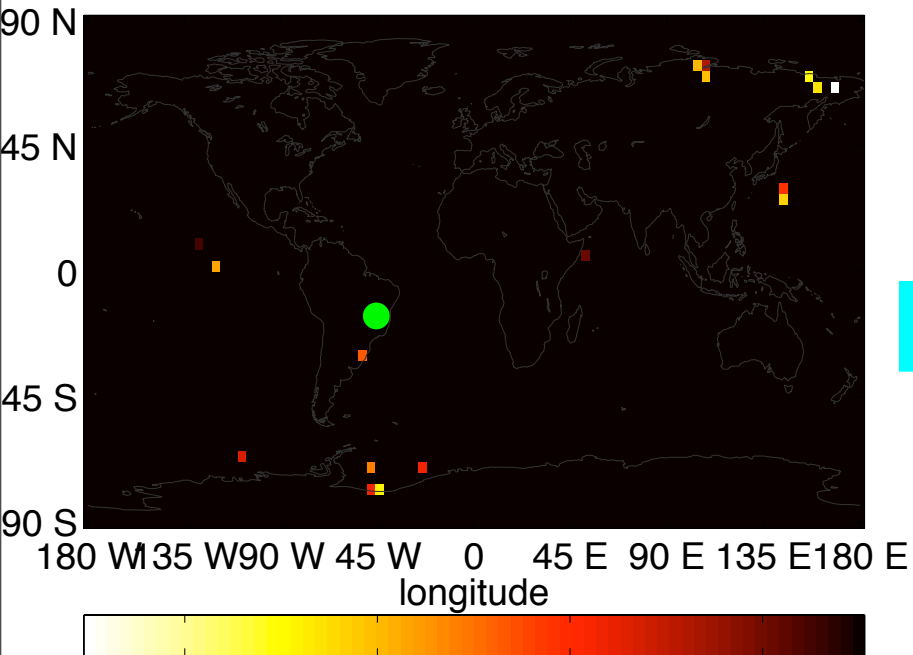
Klimenko et al **PRD 72, 122002 (2005)**

Mohanty et al **CQG 23 (2006)**

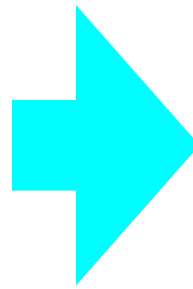
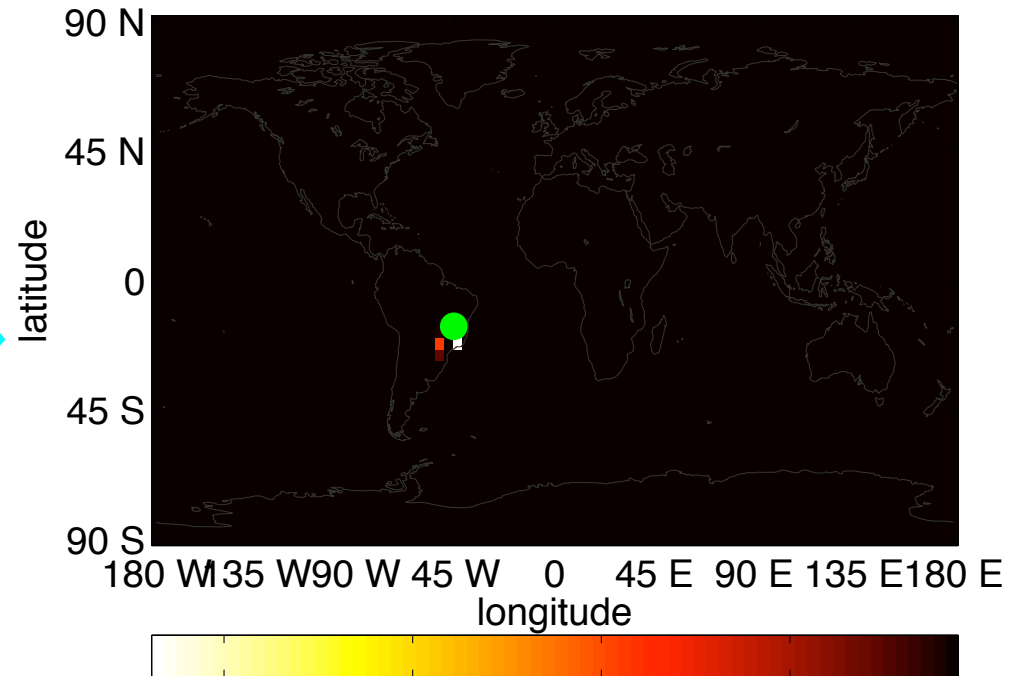


# Effect of regulator

no regulator



with regulator



Without regulator, likelihood values beyond a given threshold are scattered widely.

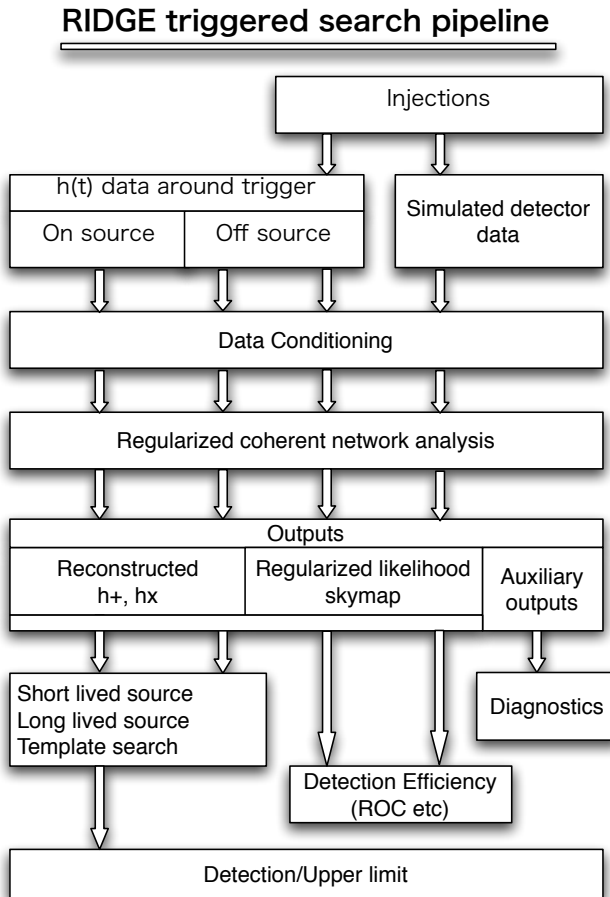
After adding regulator, the values are converged around the true solution.

# RIDGE pipeline

-- *fully coherent network analysis pipeline* --

Project Page: <http://phys.utb.edu/~kazu/RIDGE>

## Flow chart



- Target : triggered/untriggered search
- Pipeline consists of
  - data conditioning
  - coherent network analysis
- The codes have been fully implemented.
- Currently analyzing LIGO/GEO/VIRGO data:
  - Search for G.W. bursts
  - Understanding various glitches

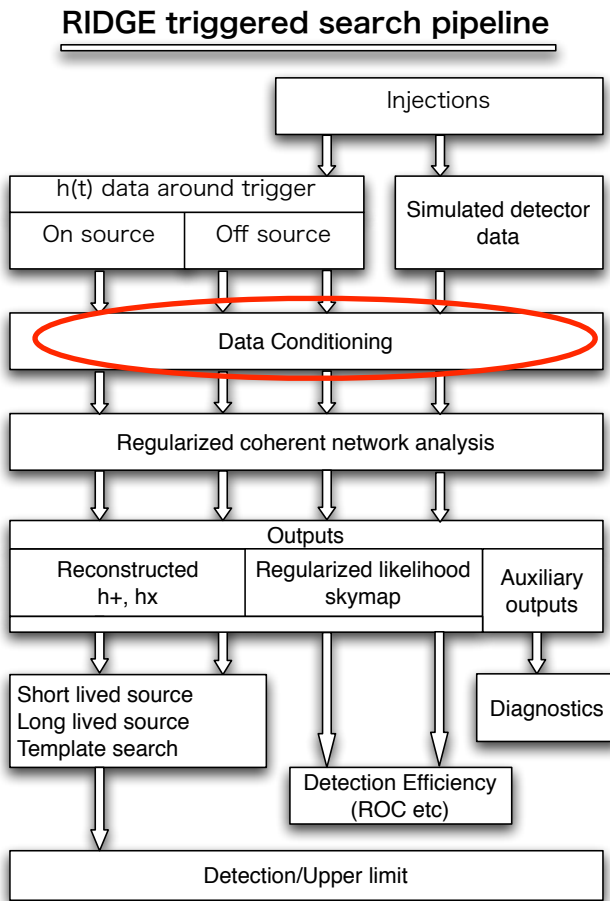
Note:

glitch : A large amplitude noise transient

# RIDGE pipeline

-- *fully coherent network analysis pipeline* --

Project Page: <http://phys.utb.edu/~kazu/RIDGE>



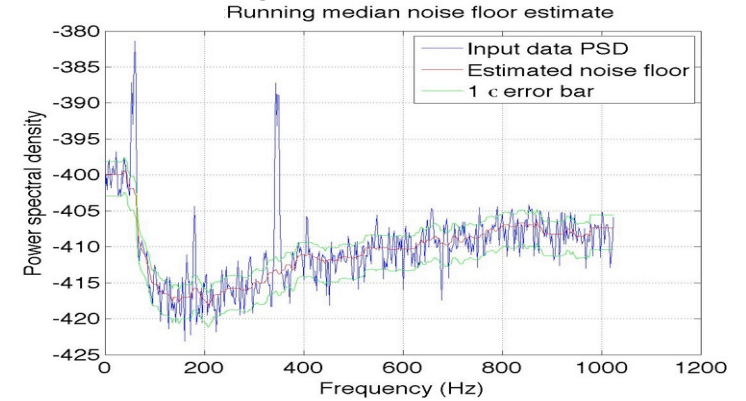
Feature:

- New data conditioning
- Tikhonov-regularized coherent network analysis

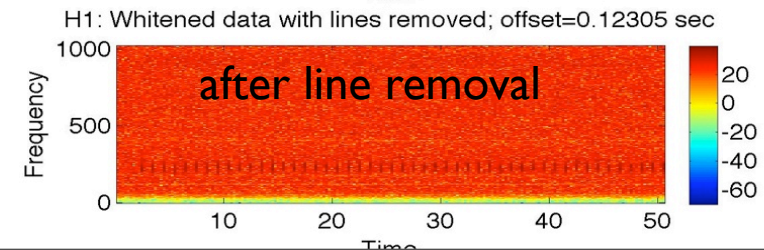
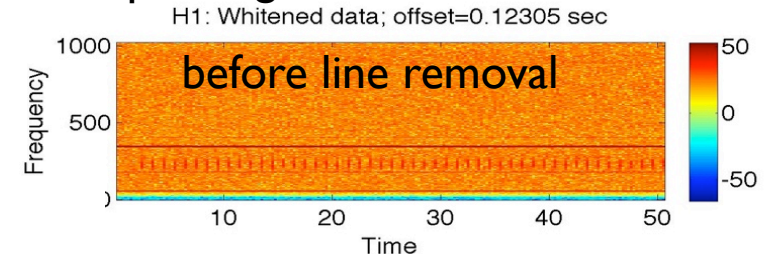
- Time domain noise floor whitening  
**S. Mukherjee CQG 21 (2004) S1783**

- Remove lines by Median Based Line Tracker  
**S. Mohanty CQG 19 (2002) 1513**

Power spectrum of simulated data



Spectrogram



# One application of RIDGE

## Monitoring Sco X-1

-- with some combinations of detectors --

- Sco X-1 is the strongest X-ray source, and has frequent X-ray outbursts
- G.W. observation can derive constraints on accretion or r-mode
- Sensitivities of detectors to Sco X-1 changes in time due to the rotation of the detector antenna patterns.
- Which detector combination is effective for detection?
  - Detection efficiency
  - Signal recovery
  - Here we consider H1-H2-L1, H1-H2-L1-V1, H1-L1-V1-LCGT combination

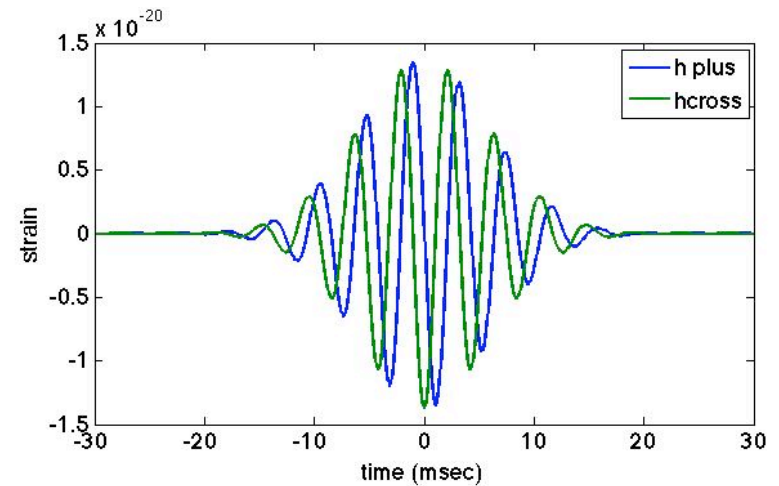
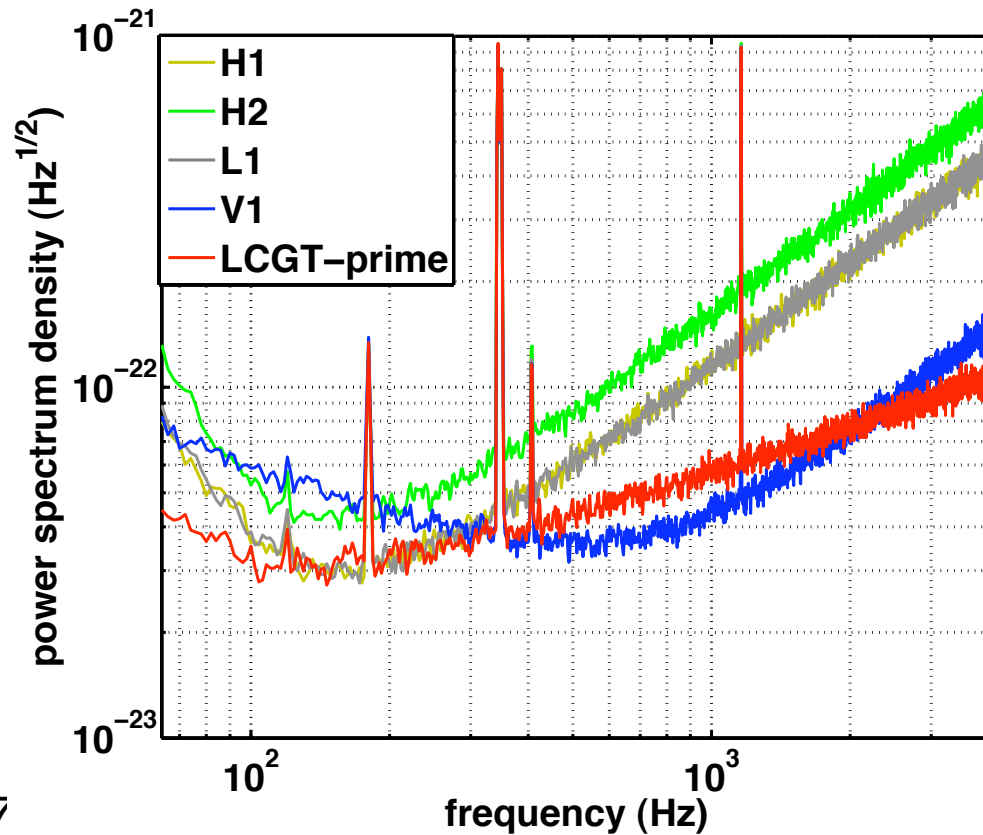
# Monte Carlo Simulation

5 simulated data

- H1,H2,L1,V1 design sensitivity
- LCGT-prime: x10 worse than design
- Gaussian noise
- 16384Hz sampling
- 2000sec
- Lines are at same position for all ifo

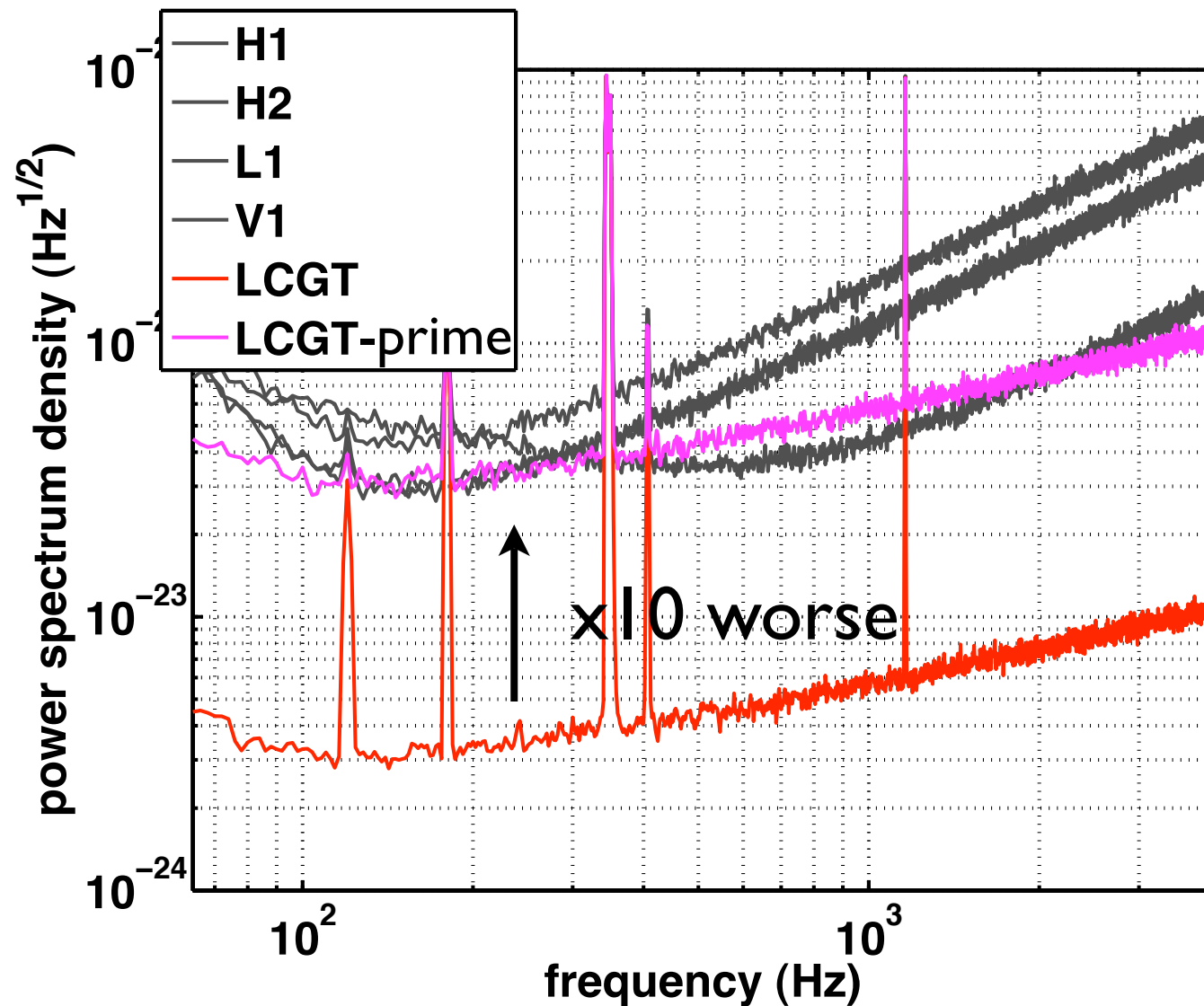
Injected signal:

- SineGaussian(235Hz)
- Skylocation: ScoX1
- hrss= $2 \times 10^{-21} \text{ Hz}^{-1/2}$



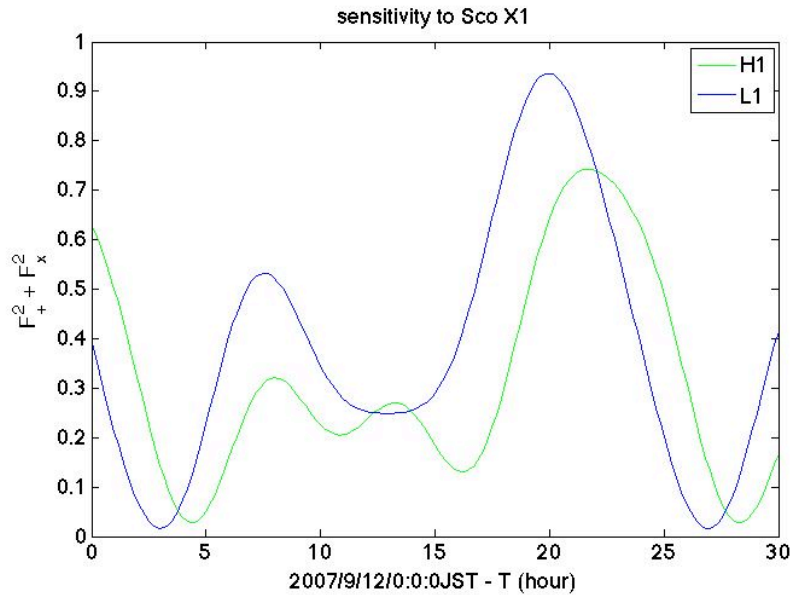
# Monte Carlo Simulation

To focus on importance of detector location, use sensitivity  $\times 10$  worse than the design sensitivity of LCGT.



# Sensitivity to Sco X-1

## HI - LI



y-axis:

detector response :  $F_+(\theta_s, \phi_s)^2 + F_x(\theta_s, \phi_s)^2$   
to the location of Sco X-1( $\theta_s, \phi_s$ )

x-axis:

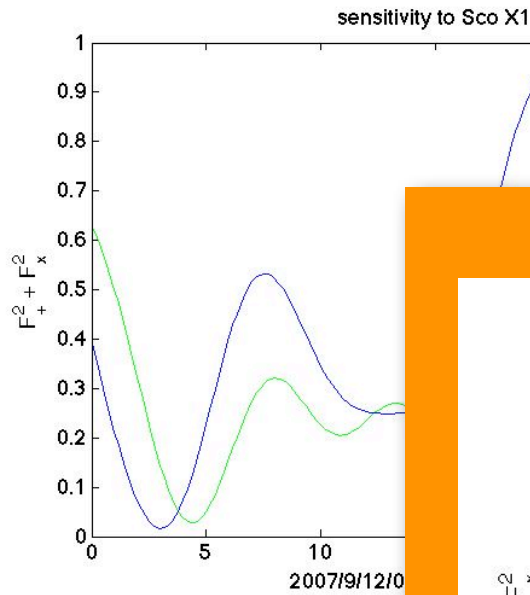
hour from 0:00(JST), today

Due to the rotation of the earth, the response function is 24hr-periodic function.

LIGO only network has sensitivity at the region  $T = 17-24$ hr.  
However,  $T=2-5$ hr,  $10-16$ hr, the sensitivity worsens

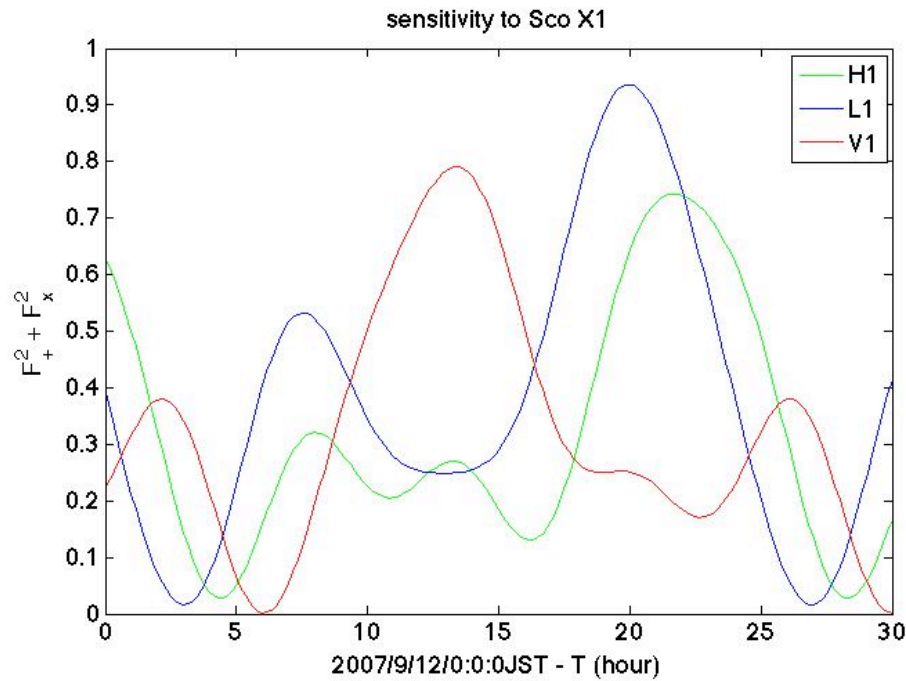
# Sensitivity to Sco X-1

## H1,H2 - L1



Adding VIRGO to the LIGO network, the sensitivity at the region  $T=10-16$ hr is improved.

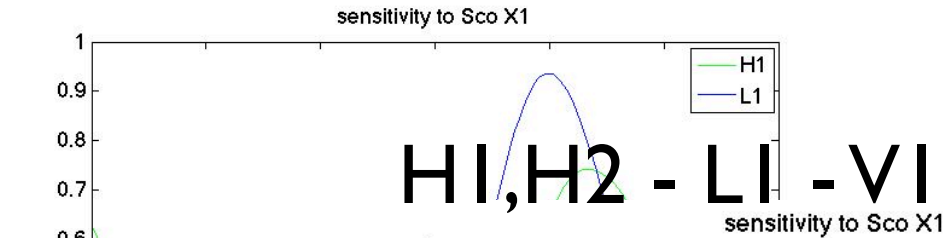
## H1,H2 - L1 - V1





# Sensitivity to Sco X-1

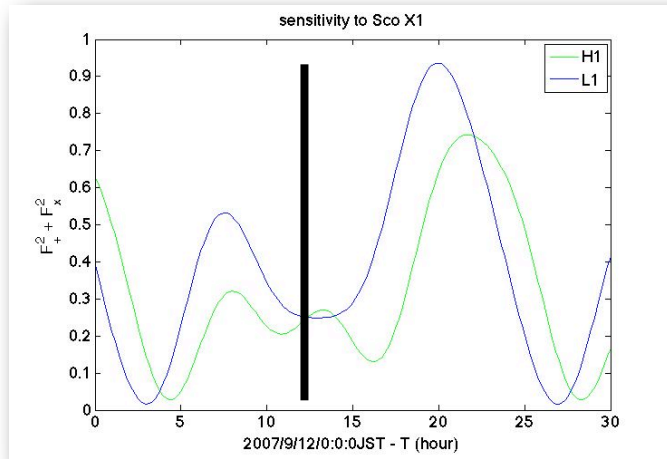
## HI, H2 - LI



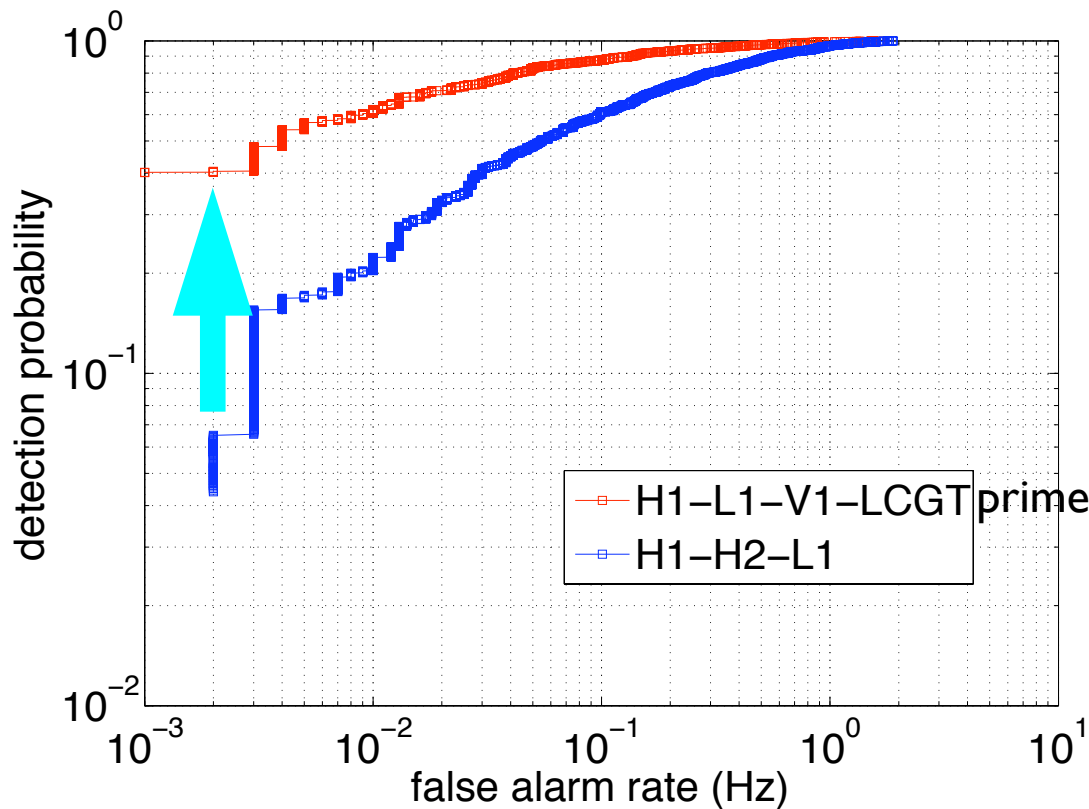
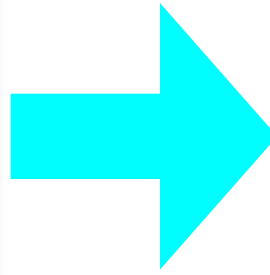
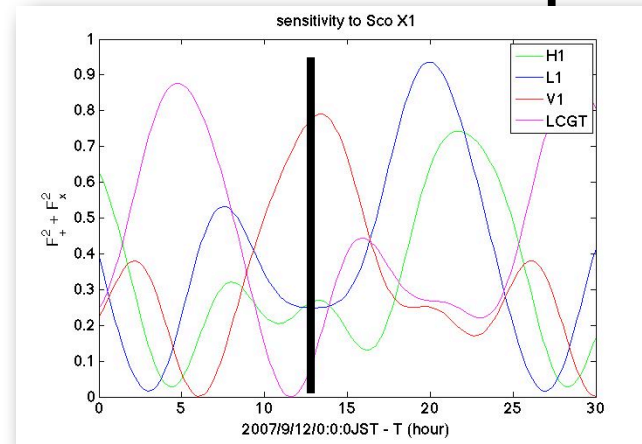
The network covers all region.

# Detection efficiency

## H1+H2+L1



## H1+L1+V1+LCGT-prime



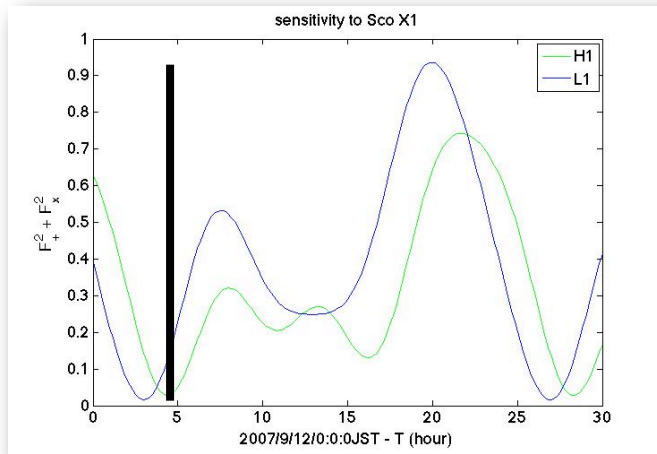
VIRGO compensate the low sensitivity region for LIGO network.

Detection probability  
@false alarm rate 0.01Hz

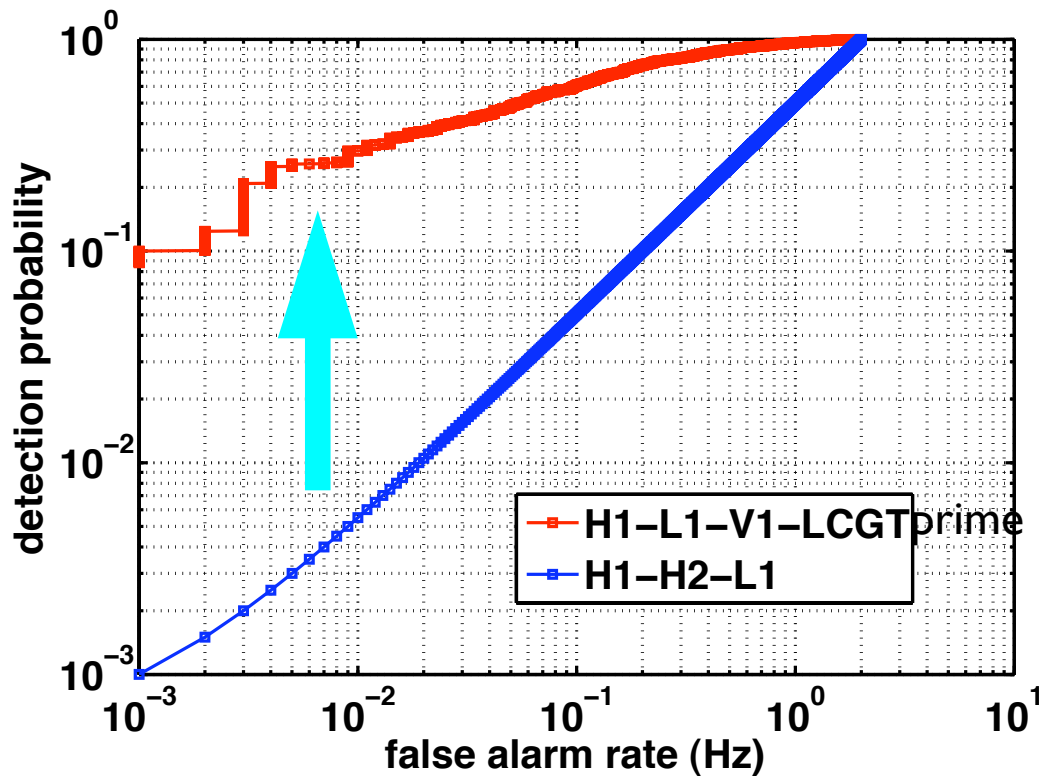
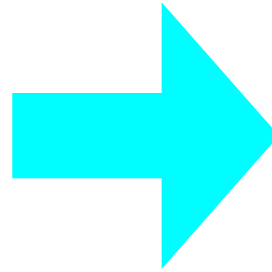
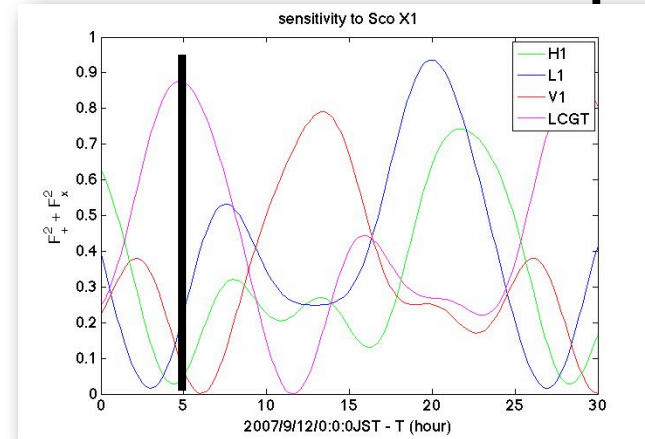
20% -----> 60%

# Detection efficiency

## H1+H2+L1



## H1+L1+V1+LCGT-prime



LCGT compensates the low sensitivity region for LIGO-VIRGO network.

Detection probability  
@false alarm rate 0.2Hz

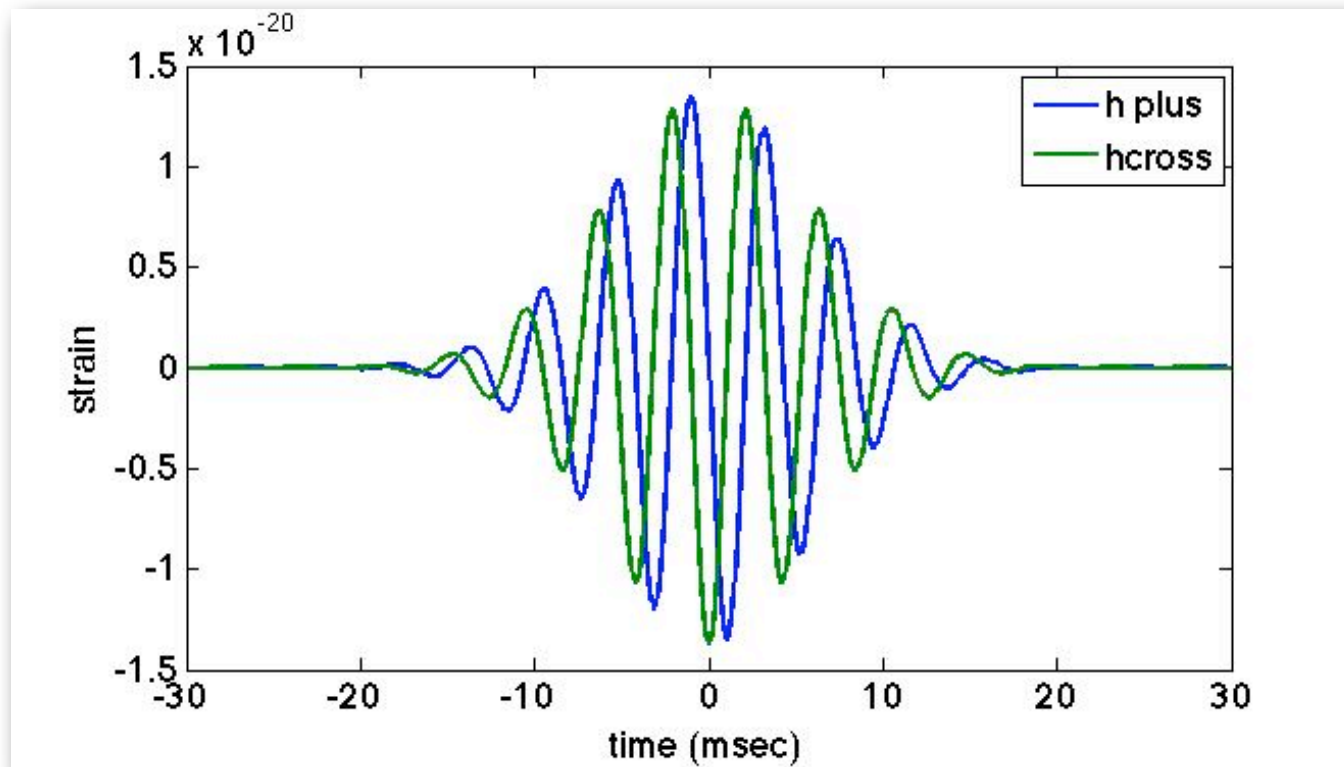
less 10% -----> 80%

# Reconstruction of G.W. waveforms

Injected signal:

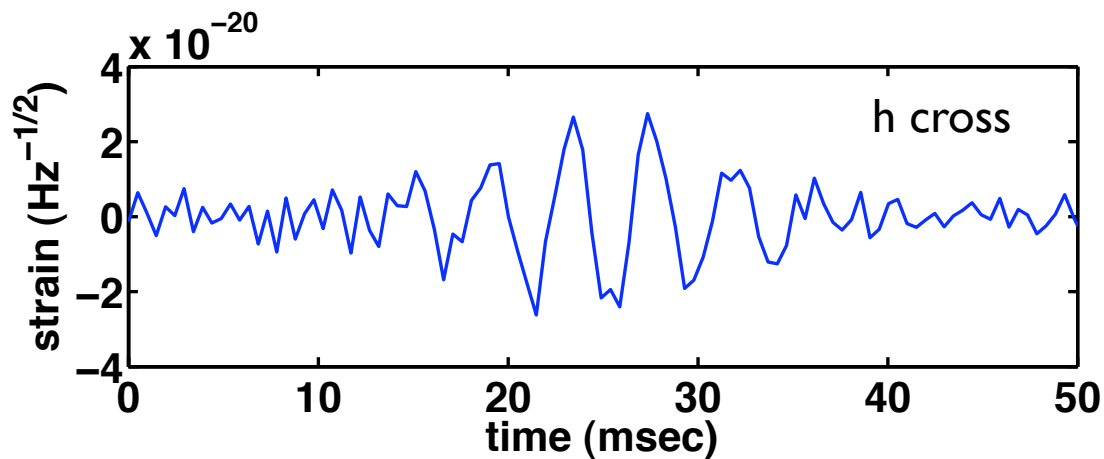
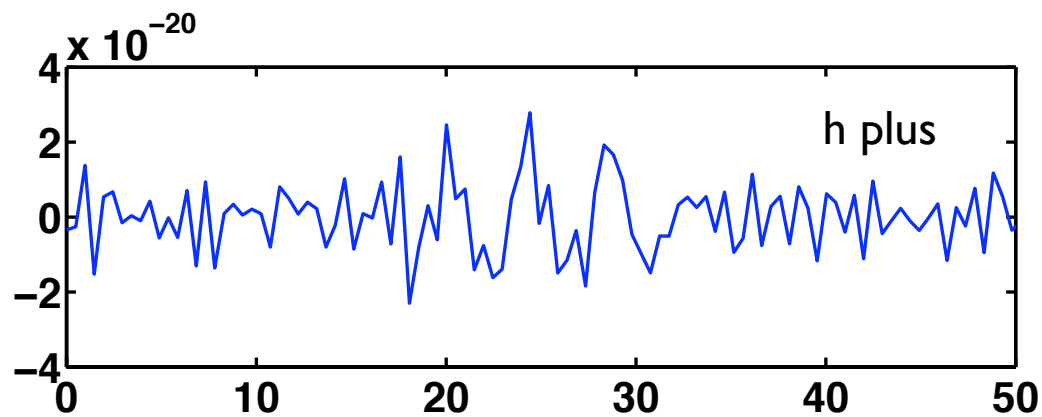
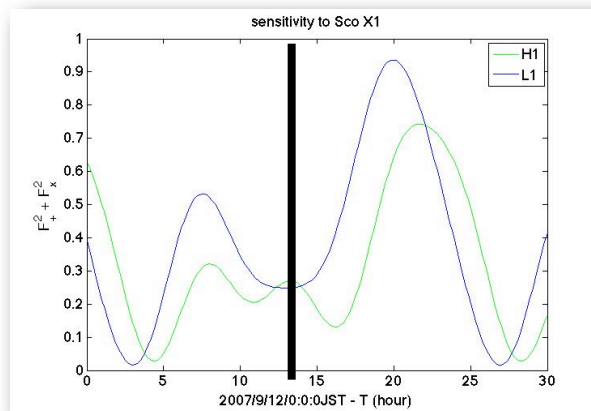
• Sine Gaussian of the central frequency 235Hz

•  $h_{rss} = 2.8 \times 10^{-21} \text{ Hz}^{1/2}$



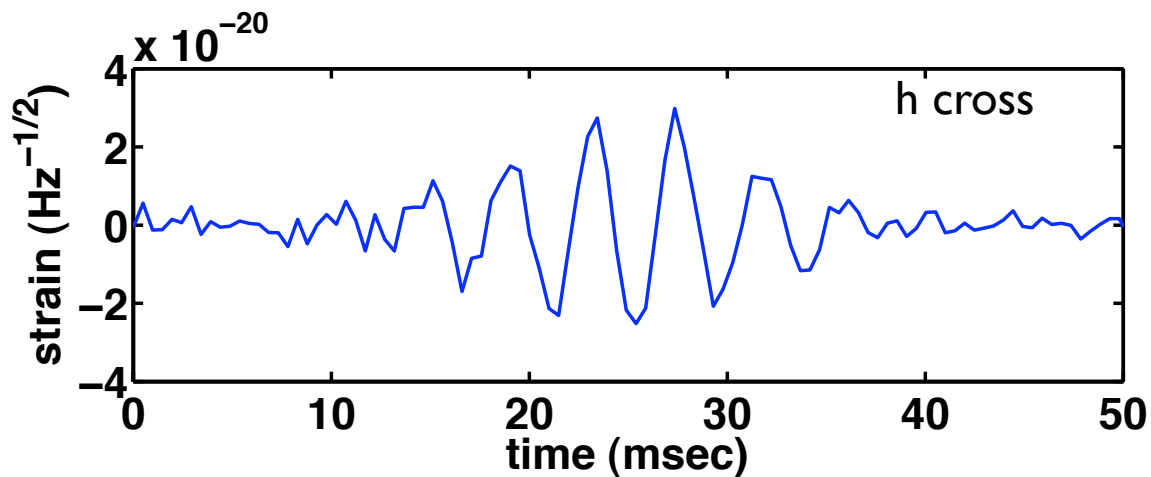
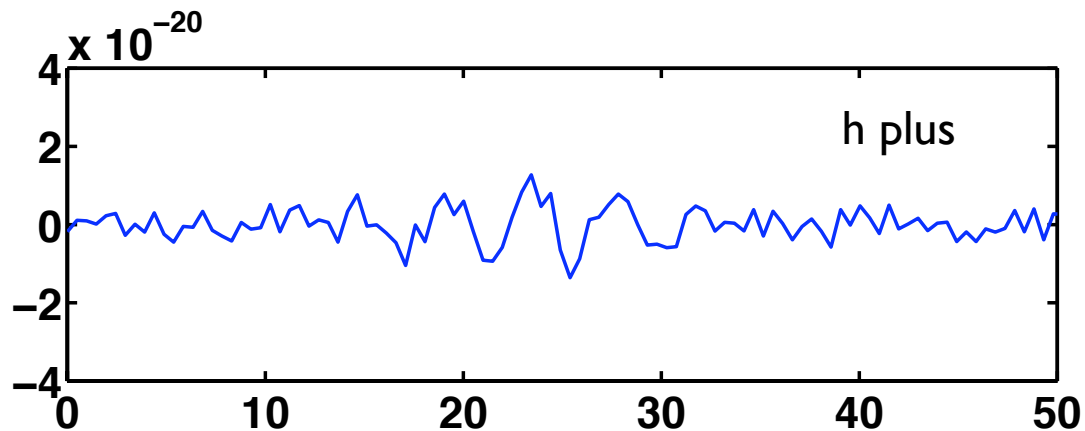
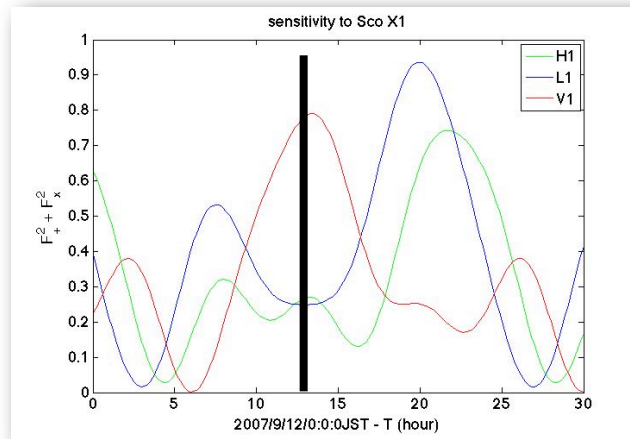
# Reconstruction of G.W. waveforms

H1+H2+L1



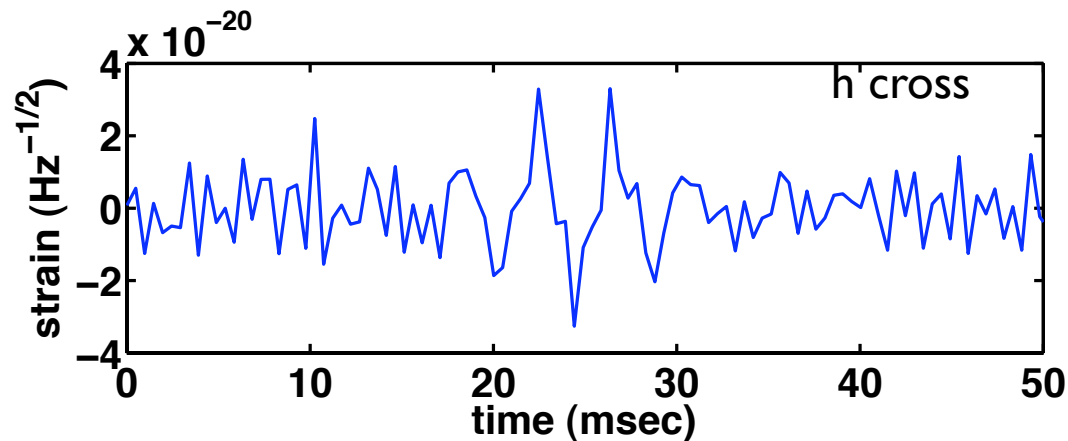
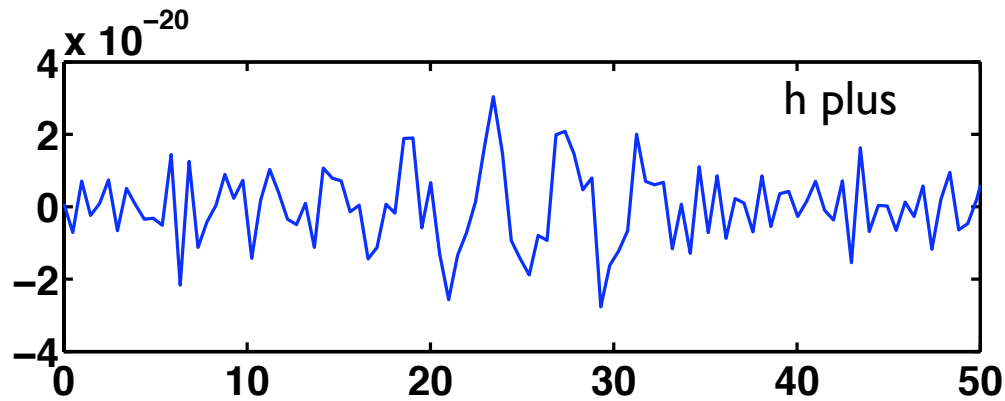
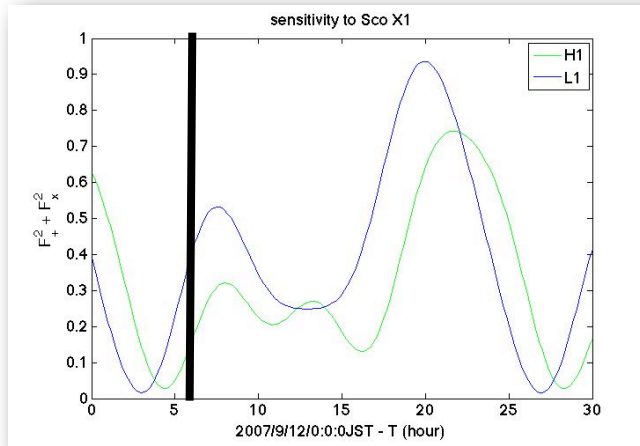
# Reconstruction of G.W. waves

H1+H2+L1+V1



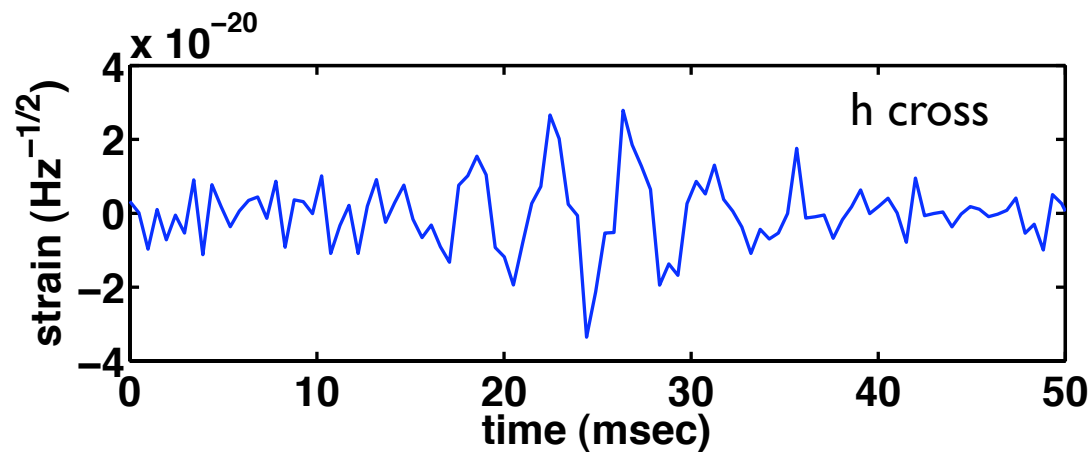
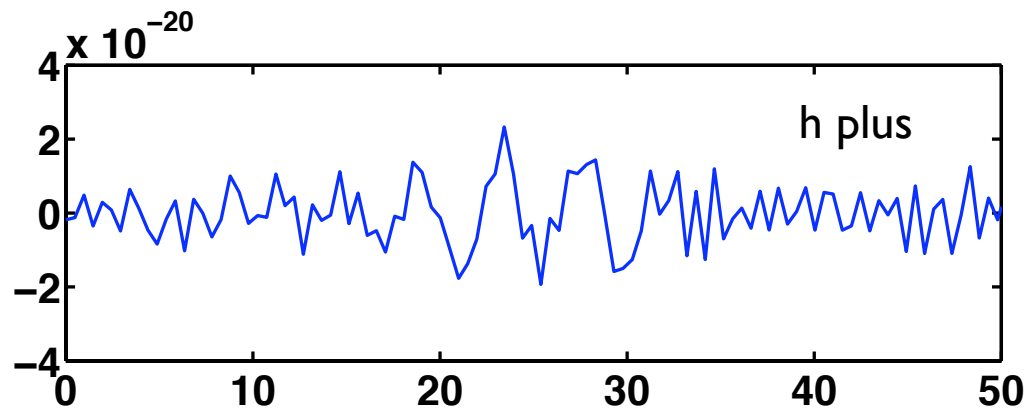
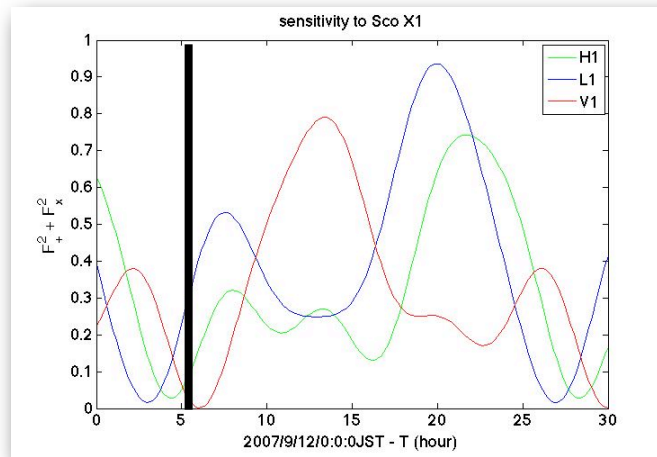
# Reconstruction of G.W. waves

H1+H2+L1



# Reconstruction of G.W. waves

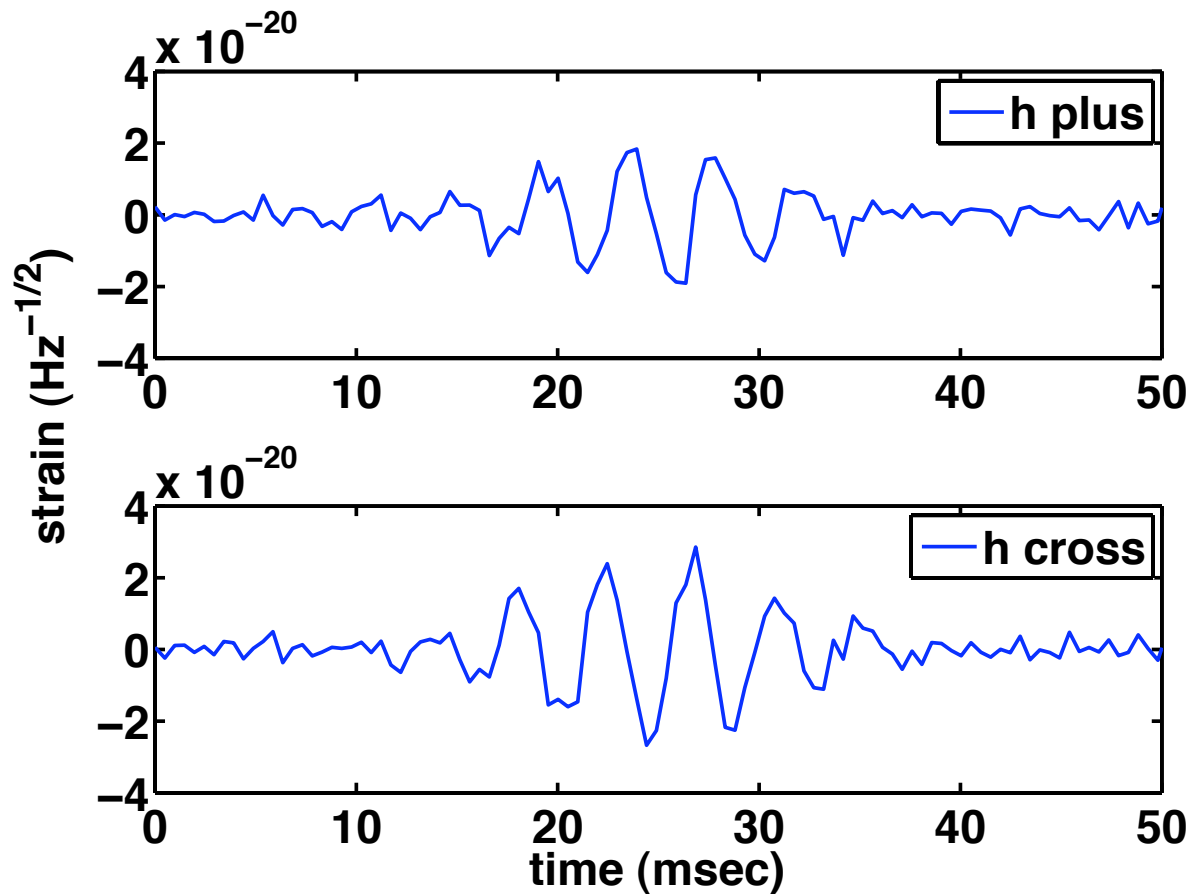
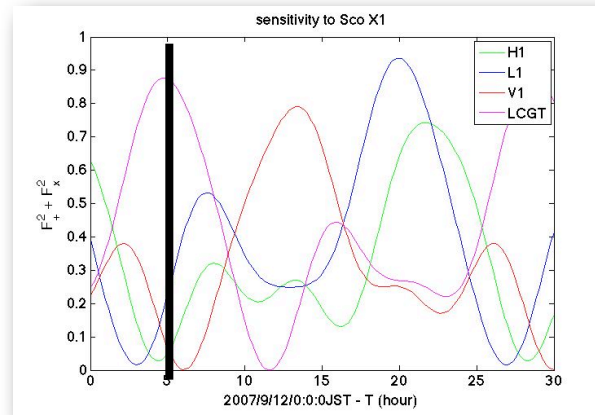
H1+H2+L1+V1





# Reconstruction of G.W. waves

HI+LI+VI+LCGT-prime



G070616-00-Z

# Summary, current status and future plan

## Summary

- The fully coherent network analysis pipeline called “RIDGE” has been developed.
- Coincidence analysis with electro-magnetic observations give us
  - timing information --> more sophisticated analysis
  - source location --> accurate signal recovery and constrain astrophysical parameters
- Sensitivities of some detector combinations and signal recovery are presented

## Current status

- Pulsar glitches during S5 are being analyzed
- Start monitoring Sco X-1
- Various detector noise transients are being analyzed

## Future plan

- Set upper limit on some sources
- Understand detector-originated glitches
- Collaboration with various astronomers needed
- Building alert system which enables quick analysis.

***END***