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# **S5 calibration: time dependent coefficients $\alpha, \gamma$**

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[http://blue.ligo-wa.caltech.edu/engrun/Calib\\_Home/](http://blue.ligo-wa.caltech.edu/engrun/Calib_Home/)  
<http://ligo.phys.lsu.edu/sung/Factors/S5/V2/index.html>

# The formulas

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Calibration for Fourier domain:

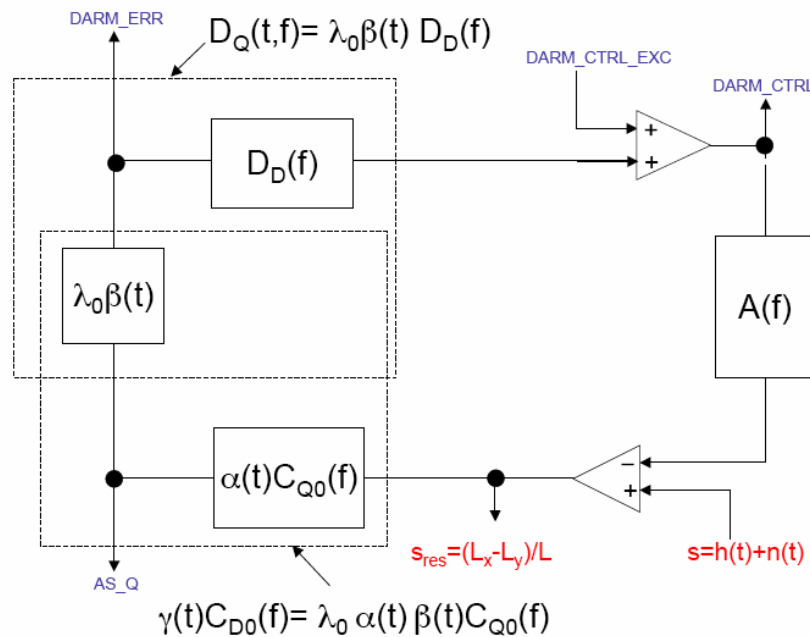
$$h(f) = R(f)GW(f)$$

$$\text{If } GW = ASQ, R_{ASQ}(f) = \frac{1 + \gamma G_0(f)}{\alpha C_{ASQ,0}(f)}$$

$$\text{If } GW = DARM\_ERR, R_{DERR}(f) = \frac{1 + \gamma G_0(f)}{\gamma C_{DERR,0}(f)}$$

Calibration Coefficients are measures of loop gain ( $\gamma$ ) and of sensing gain ( $\alpha$ ) relative to the “reference time”; they vary in time.

# More formulas



$$\gamma = \frac{1}{G_0(f_{cal})} \frac{DCTRL - EXC}{EXC}$$

$$\alpha = \frac{D_0(f_{cal})}{G_0(f_{cal})} \frac{ASQ}{DCTRL}$$

We use X. Siemen's code to get estimates for DARM\_CTRL, DARM\_CTRL\_EXC and AS\_Q at the frequency of the calibration line: by demodulation, we obtain complex time series, sampled at 60 sec sampling time (and 1 sec too).

We “only” need knowledge of open loop gain  $G(f)$  and digital filter  $D(f)$  at the calibration line frequency, at the reference time.

# Complex coefficients

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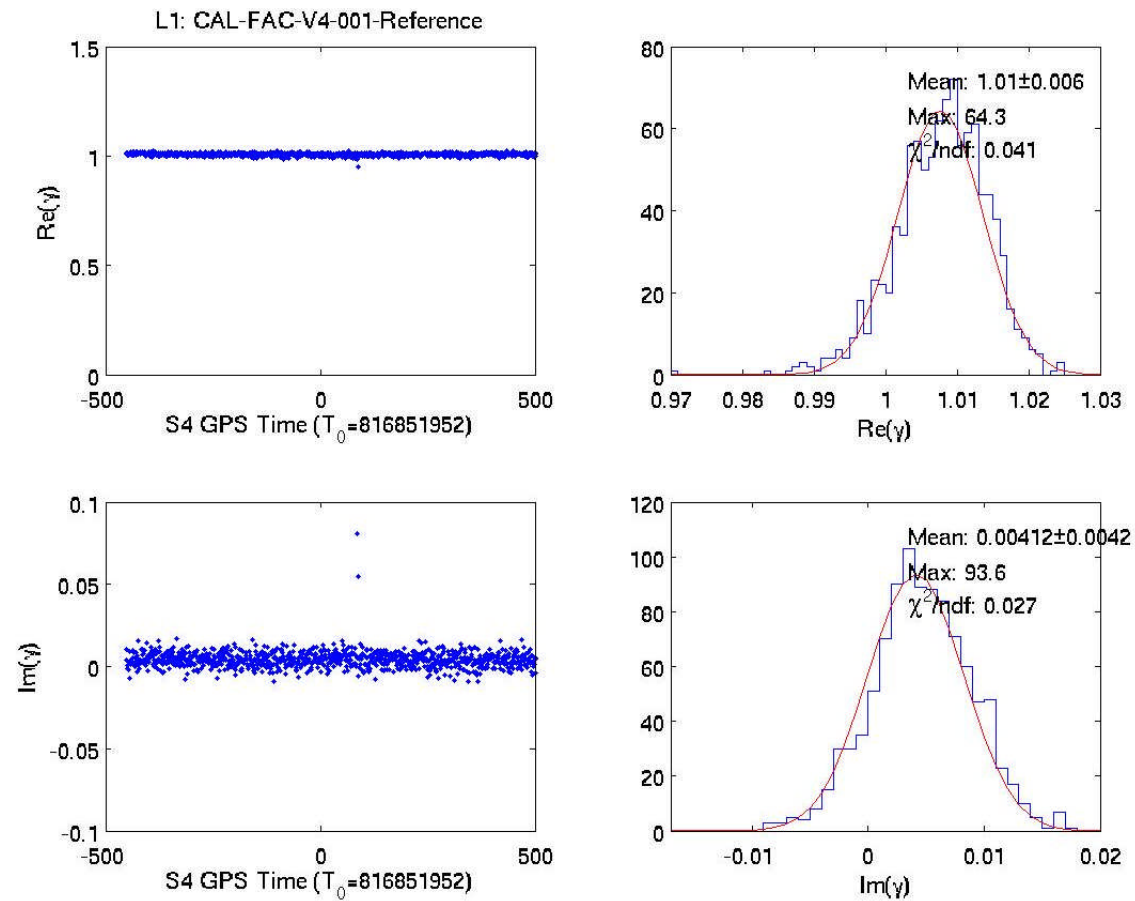
$$\gamma = \frac{1}{g_0} \frac{DCTRL - EXC}{EXC}$$

$$\alpha = \frac{d_0}{g_0} \frac{ASQ}{DCTRL}$$

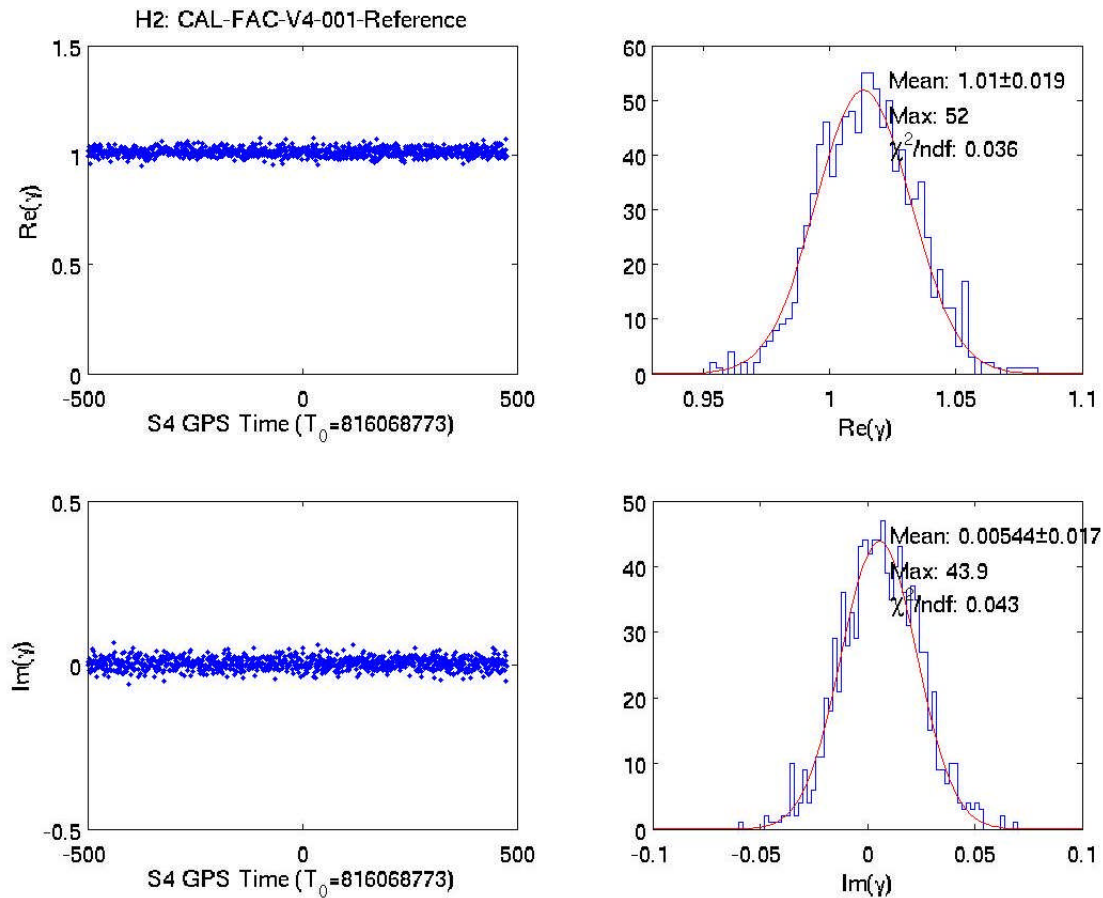
Ideally (no noise in ASQ,  $g_0$  and  $d_0$  perfectly known), coefficients are real, and identically equal to one at the reference time.

- If the amplitude of  $g_0$  is off, we'll notice a deviation from unity  $\gamma$  calculated at the reference time.
- If the phase of  $g_0$  is off, we'll see a systematic imaginary part in  $\gamma$  at all times.
- If there is random noise in ASQ at the calibration line frequency, there will be a random imaginary component in  $\gamma$ .
- The true coefficients are real; we estimate them from the real part of the complex calculated coefficients.
- The imaginary parts are used to estimate systematic and random errors in our estimates.

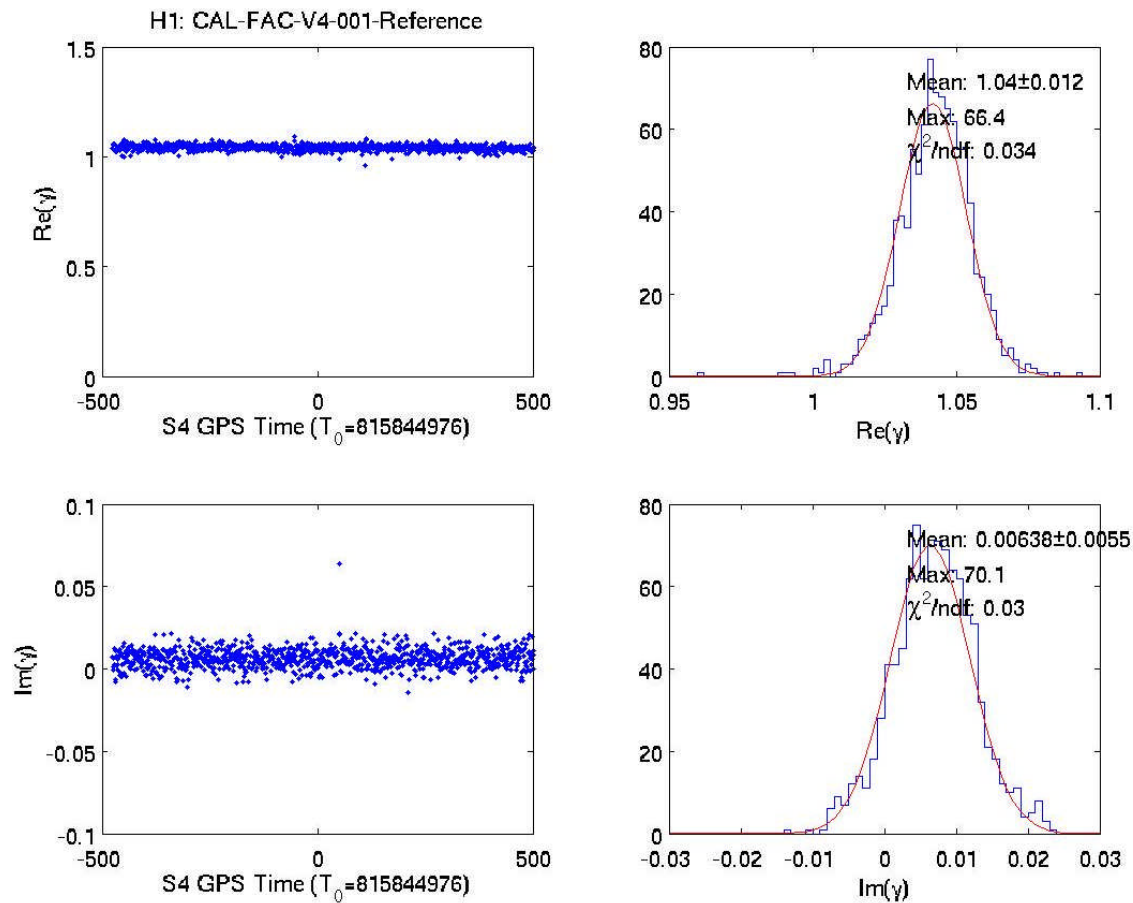
# S5 calibrations: L1 reference time



# S5 calibrations: H2 reference time

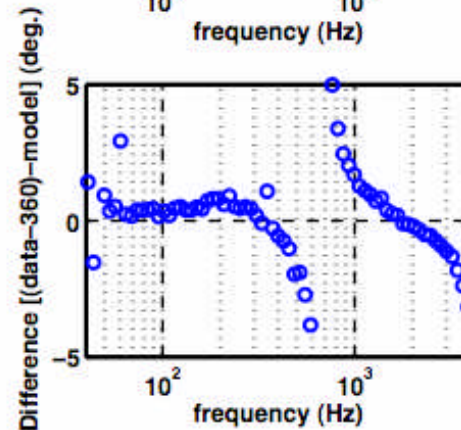
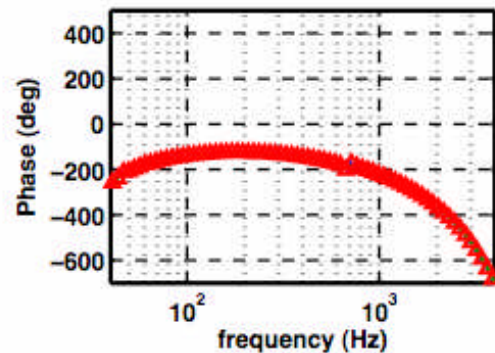
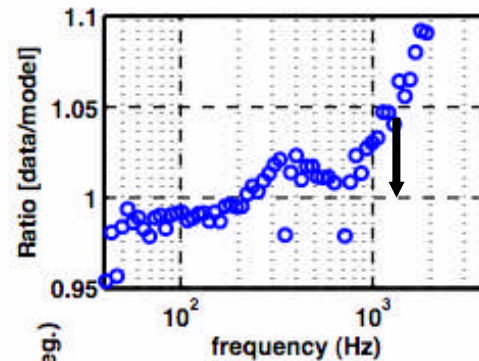
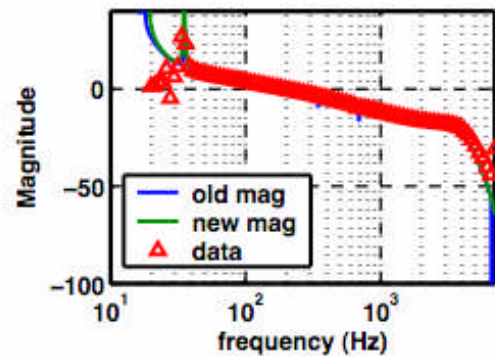


# S5 calibrations: H1 reference time

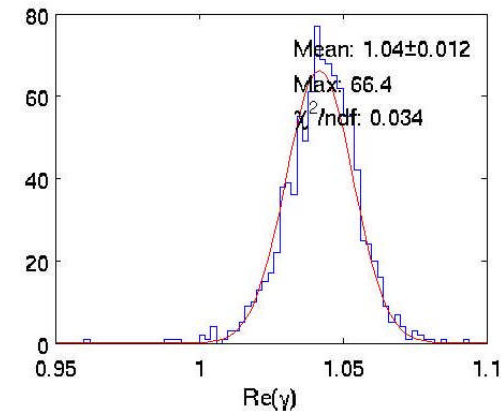


# H1 “features”

H1 OLG comparison:815844976



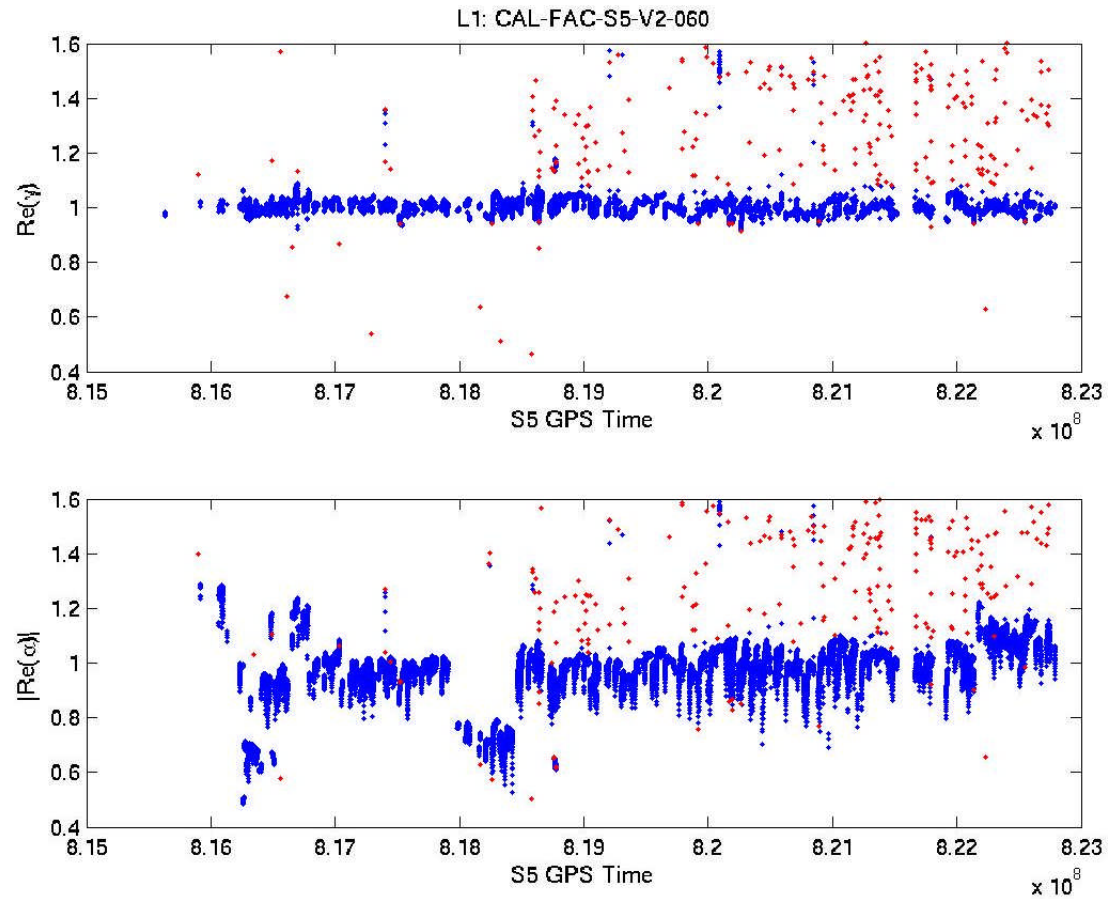
Choose  $g_0 = G_0(f_{cal})$   
from reference model,  
but with a 4%  
correction.



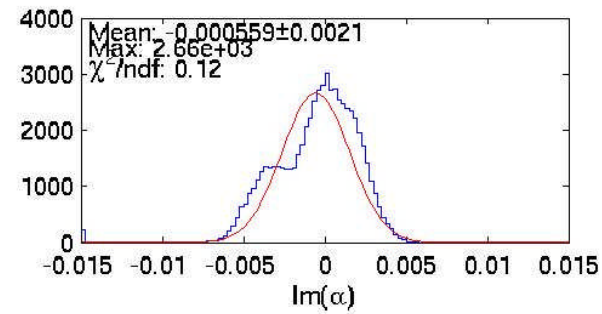
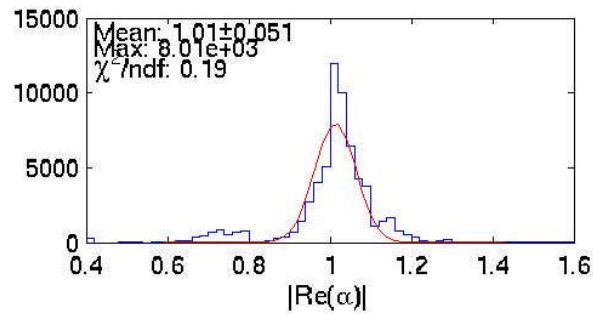
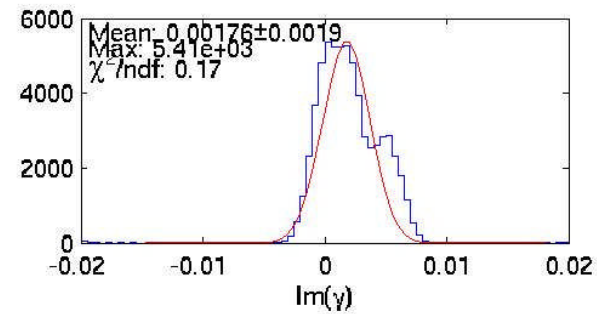
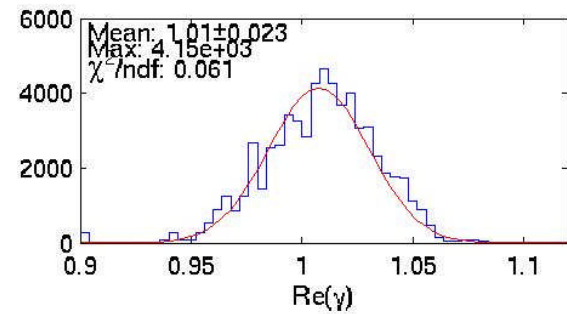
L1, H2 are within 1%: leave them alone.



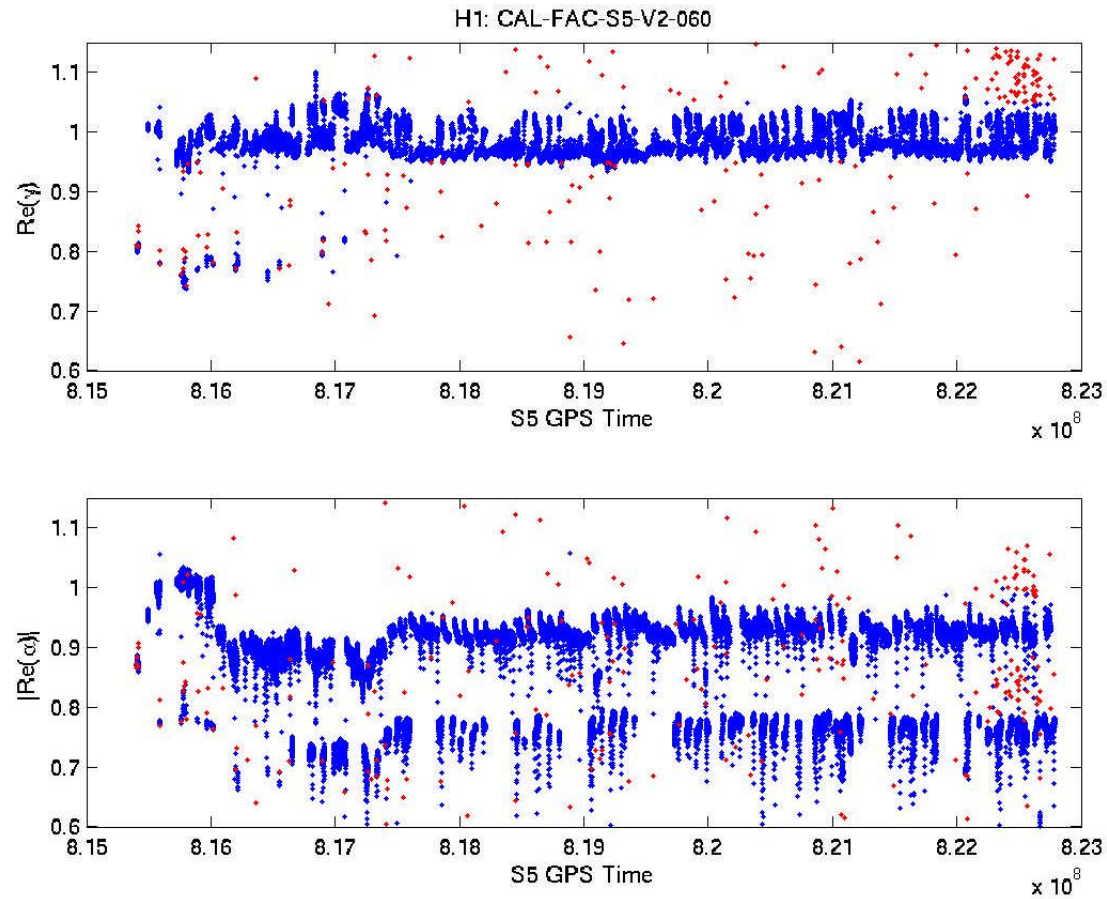
# L1 $\gamma$ , $\alpha$ coefficients S5 up to Feb 1



# L1 $\gamma$ , $\alpha$ coefficients S5 up to Feb 1

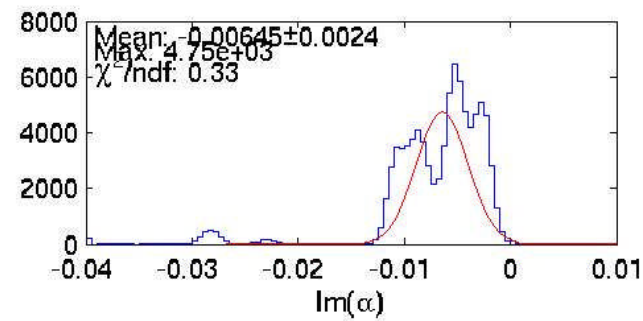
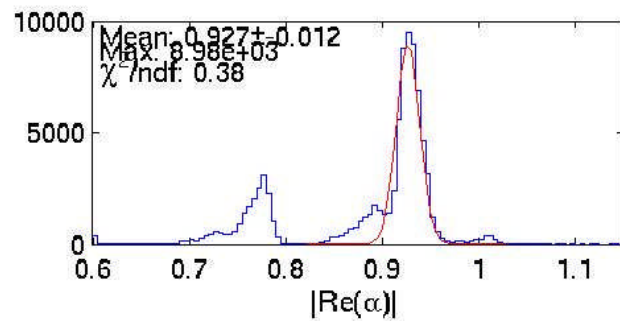
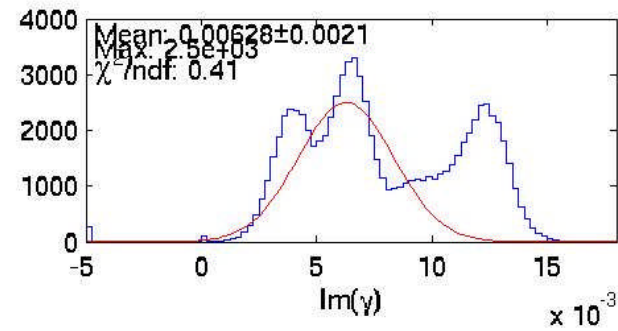
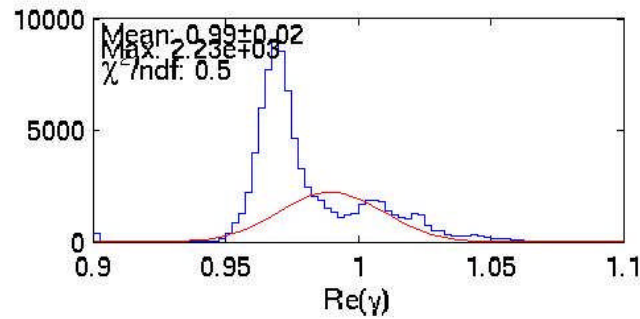


# H1 $\gamma$ , $\alpha$ coefficients S5 up to Feb 1

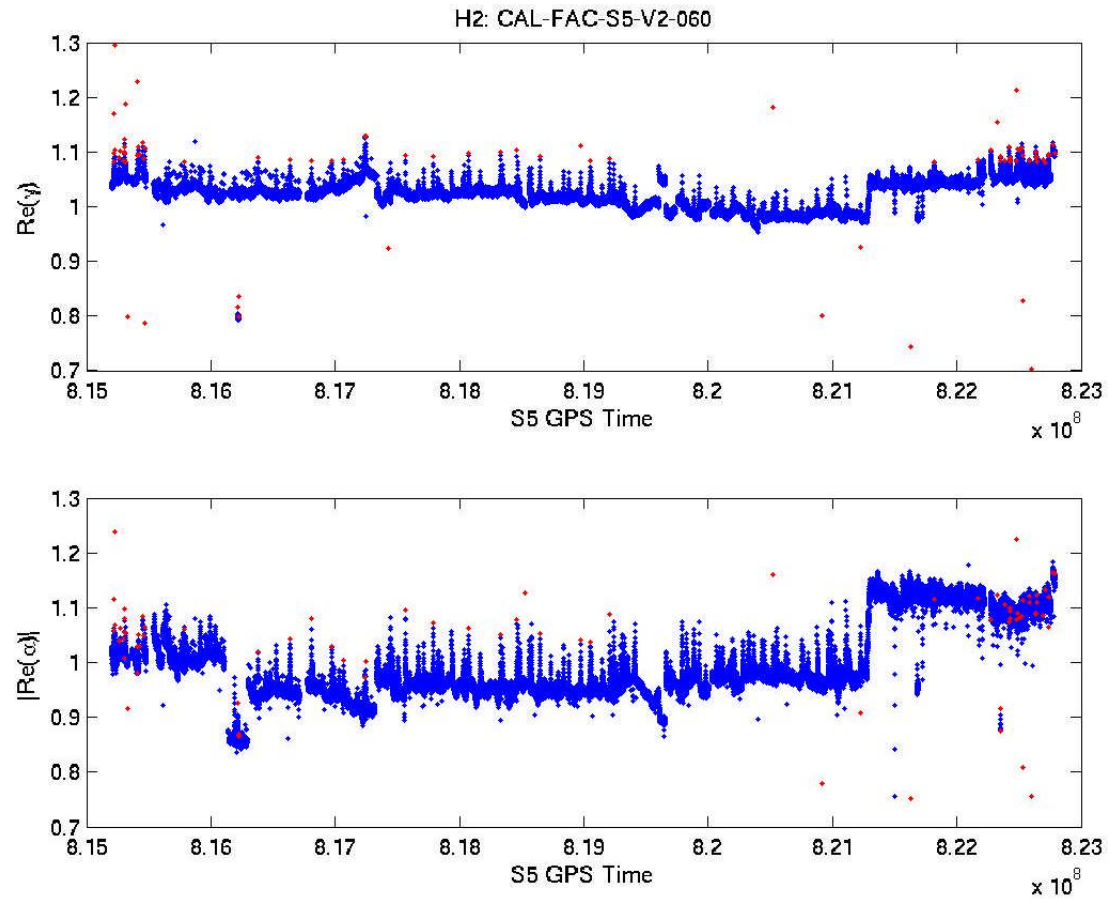


# H1 $\gamma$ , $\alpha$ coefficients

## S5 up to Feb 1

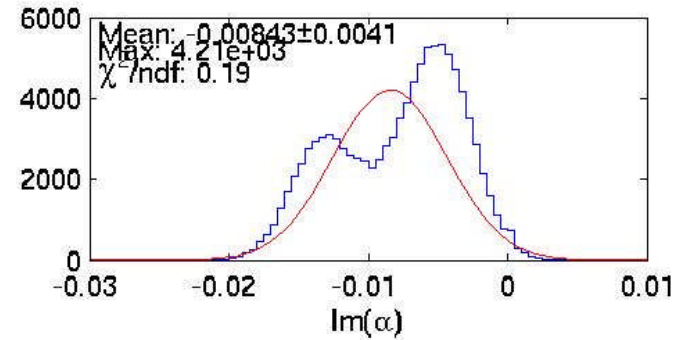
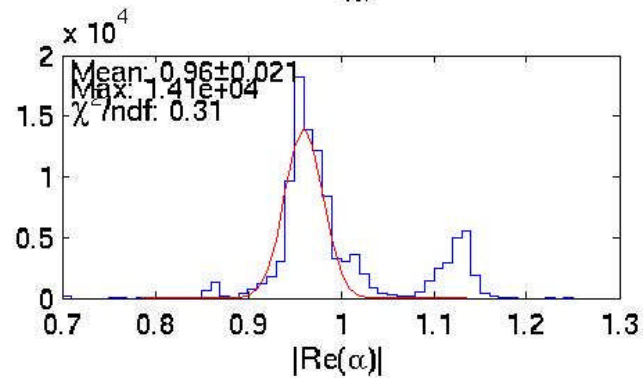
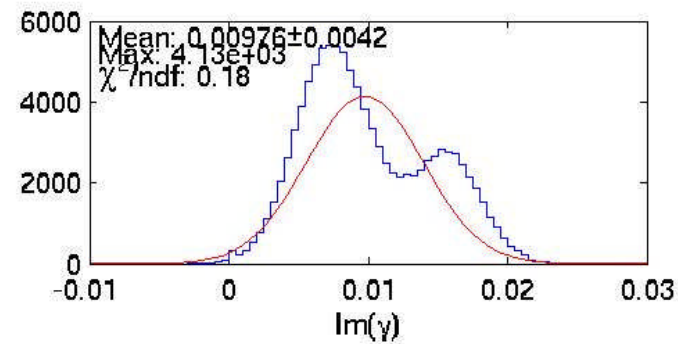
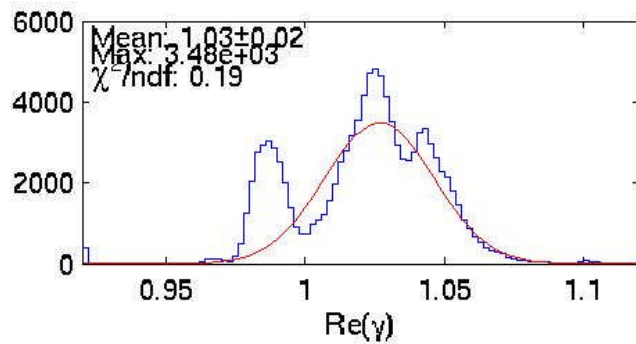


# H2 $\gamma$ , $\alpha$ coefficients S5 up to Feb 1



# H2 $\gamma$ , $\alpha$ coefficients

## S5 up to Feb 1



# How different is $\gamma$ from unity?

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- H1 :
  - » From estimates: median=0.97, std=2%
  - » Error in estimates: 0.6% systematic, 0.2% random
- H2:
  - » From estimates: median=1.02, std=3%
  - » Error in estimates: 1% systematic, 0.4% random
- L1:
  - » From estimates: median=1.01, std=3%
  - » Error in estimates: 0.2% systematic, 0.2% random



# What's next?

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- DQ flags have been produced, most at ends of segments.
- We are investigating some noticeable changes in coefficient values and errors.
- Will regenerate coefficients when a better loop model is available (hopefully without ad hoc corrections)
- Will generate coefficients for Feb 1 onwards. Files will be weeks to months long.
- Hope to generate 16 Hz time series to find fast fluctuations (if any)
- Will explore spectral content of time variations.