

# Inverted pendulum studies for seismic attenuation

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# Introduction

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- Seismic noise is one of the most important noise sources that will affect the detector at low frequencies
- There is the necessity to design an adequate isolation system

An inverted pendulum (IP) is implemented to provide attenuation at frequencies extending down to the micro-seismic peak and to realize a mean to position the entire system without requiring large force

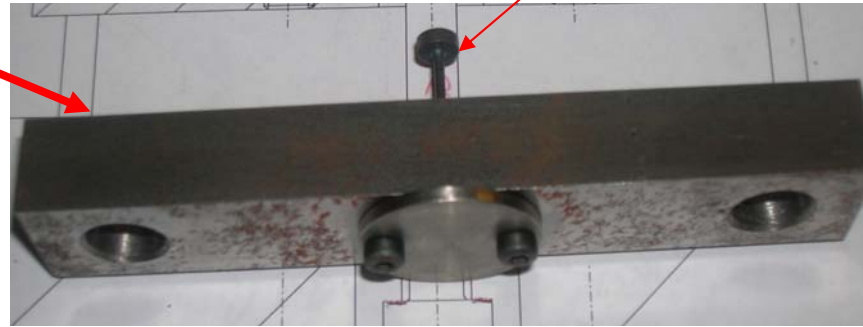
# Inverted Pendulum

IP is a horizontal pre-isolation stage with ultra-low resonant frequency, typically 30 mHz

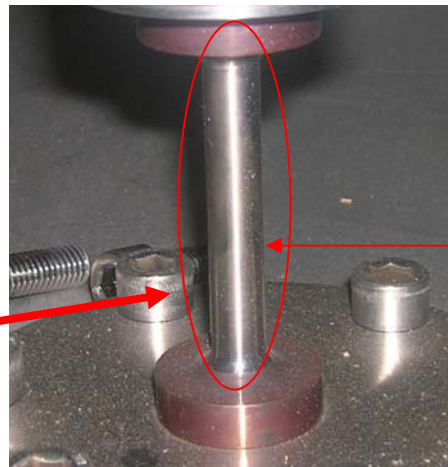


LIGO-G05

Small flex joint

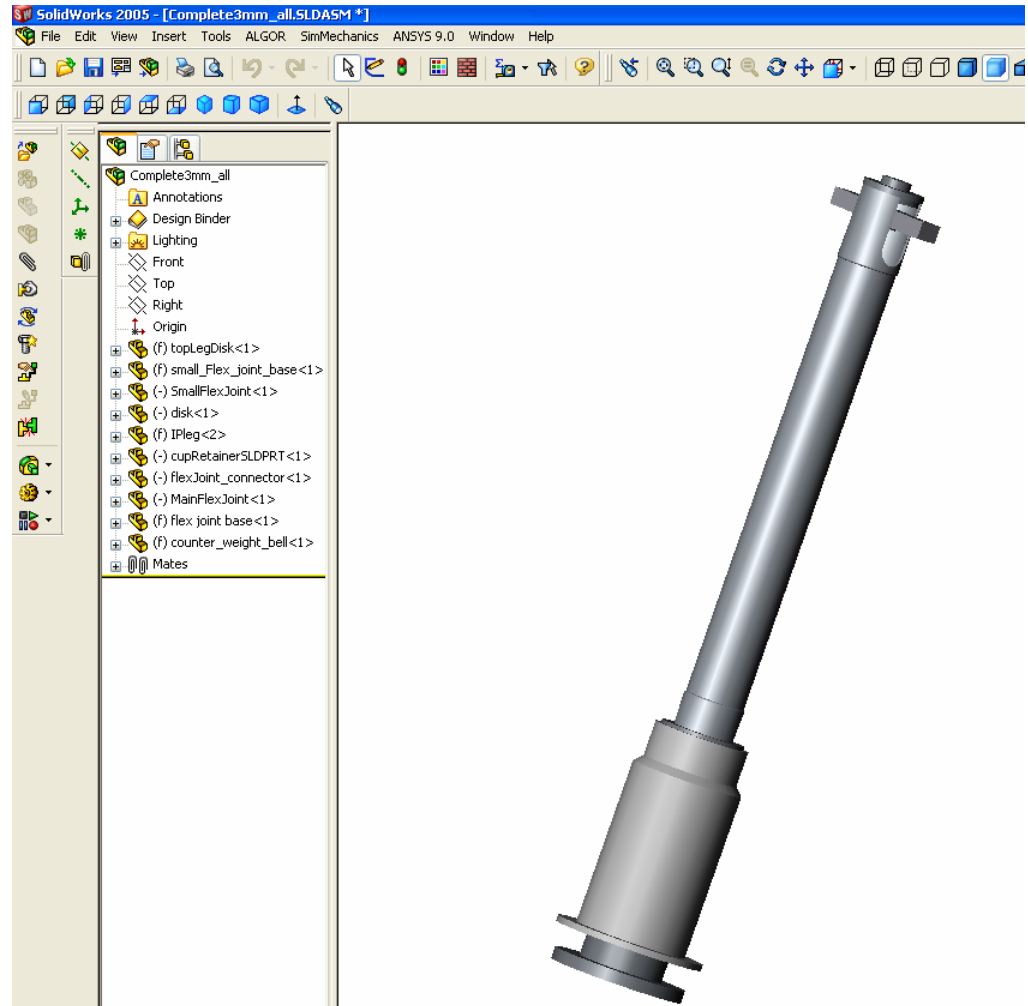
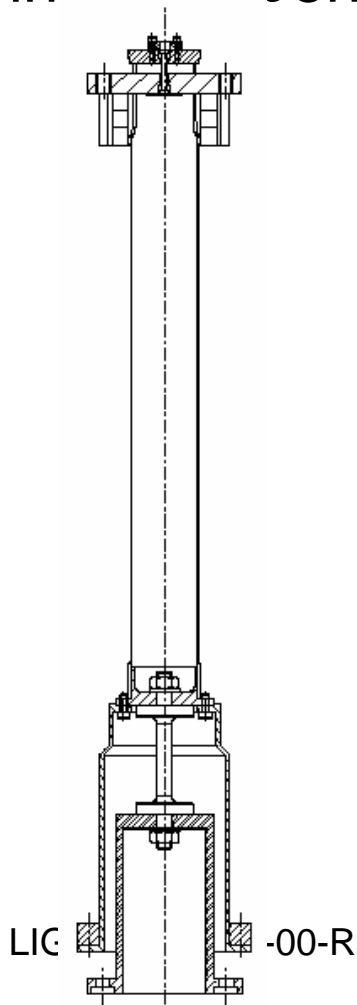


Main flex joint



# IP in ANSYS: First step

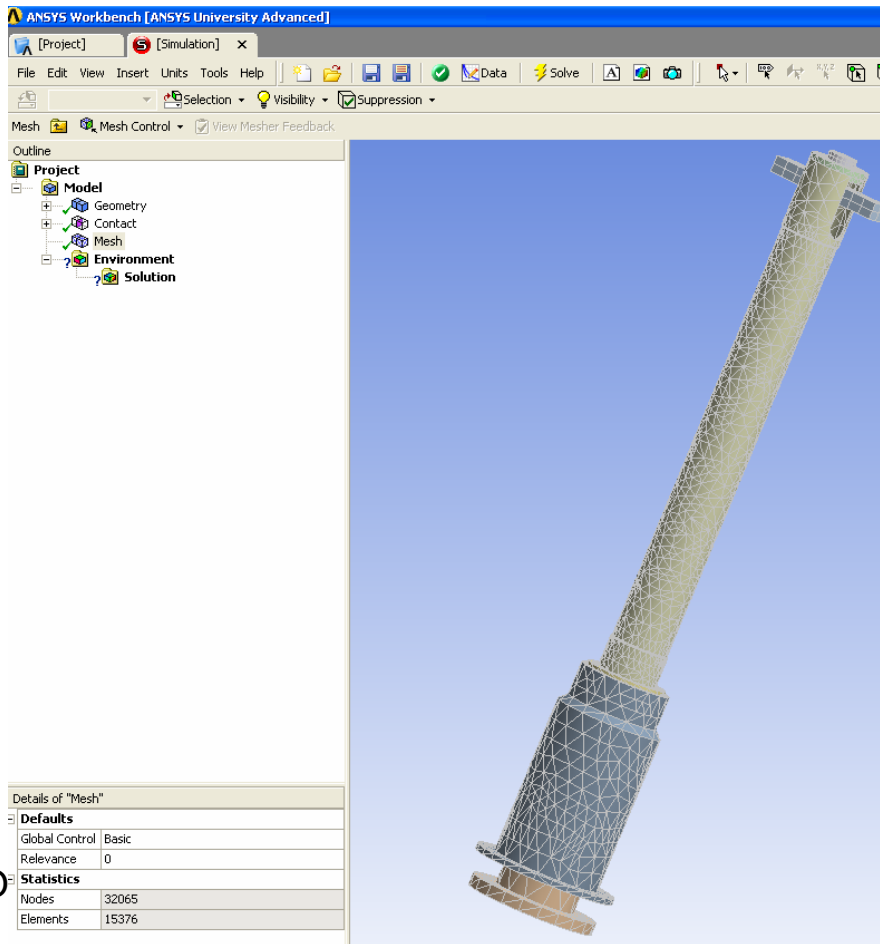
- Draw in each detail the individual legs of the inverted pendulum in Solid Solid Works<sup>©</sup>



# Second step

- Import the pendulum in Ansys<sup>©</sup>

First operation: meshing

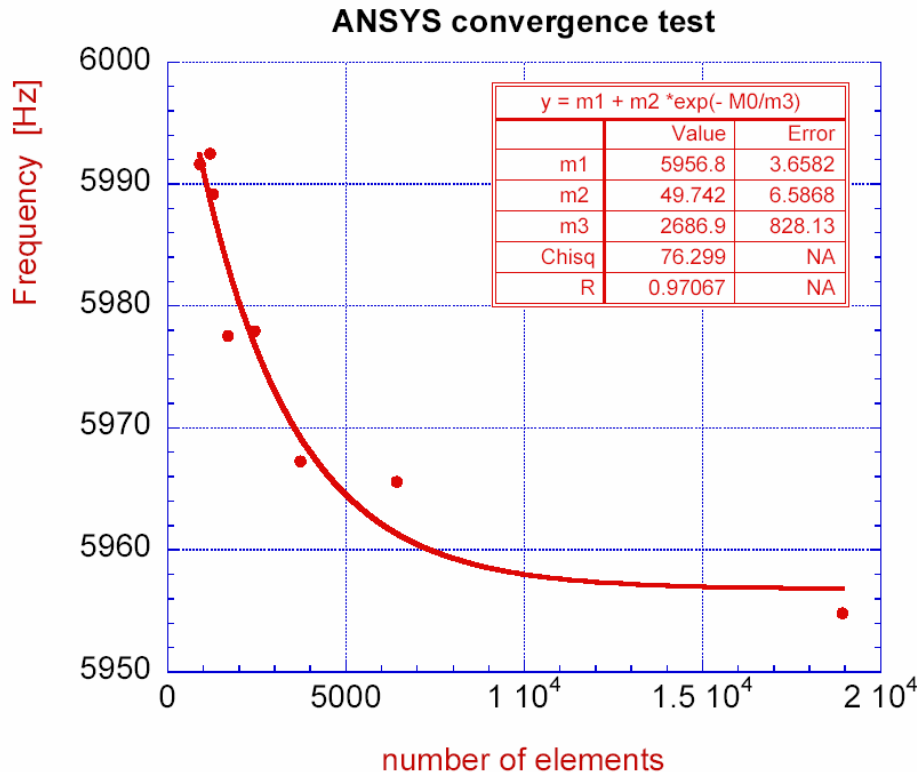


- Ansys is a general purpose finite element modeling
- The body can be sub-divided up into small discrete regions known as **finite elements**
- Calculate stress and strain propagated through the mesh

# Second step

- Import the pendulum in Ansys<sup>©</sup>

Second operation: convergence test to check that the model finds stable resonance frequencies

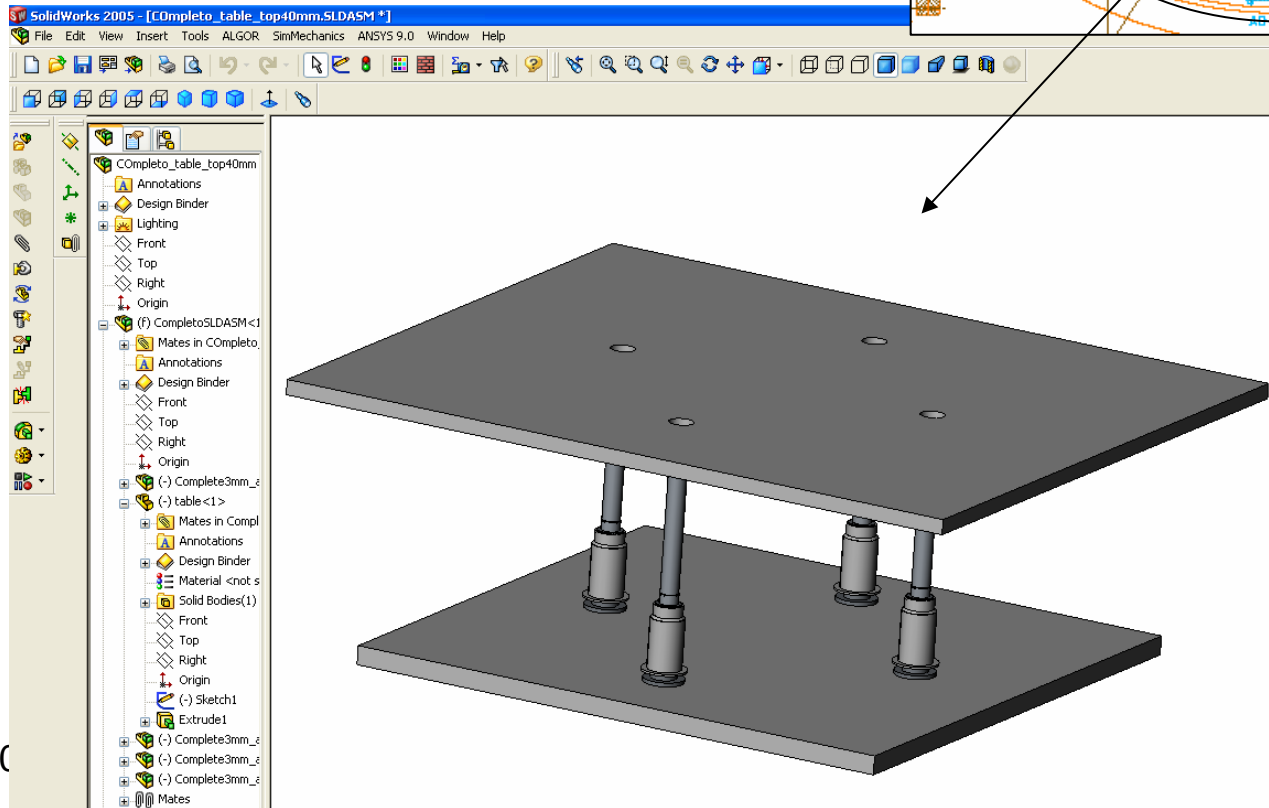
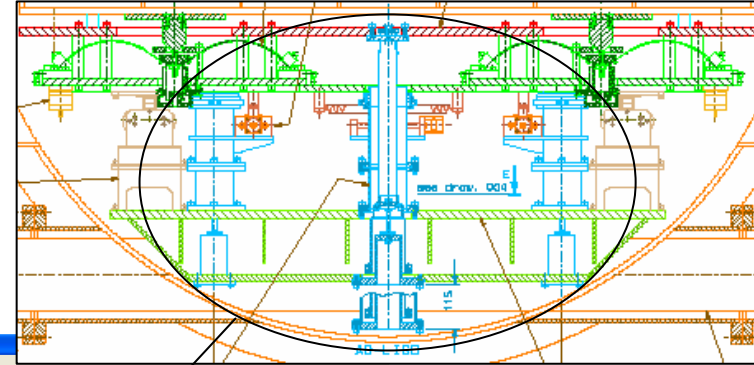


Convergence test for the first 6 frequencies up to 22 MHz

☺ NO problem of convergence

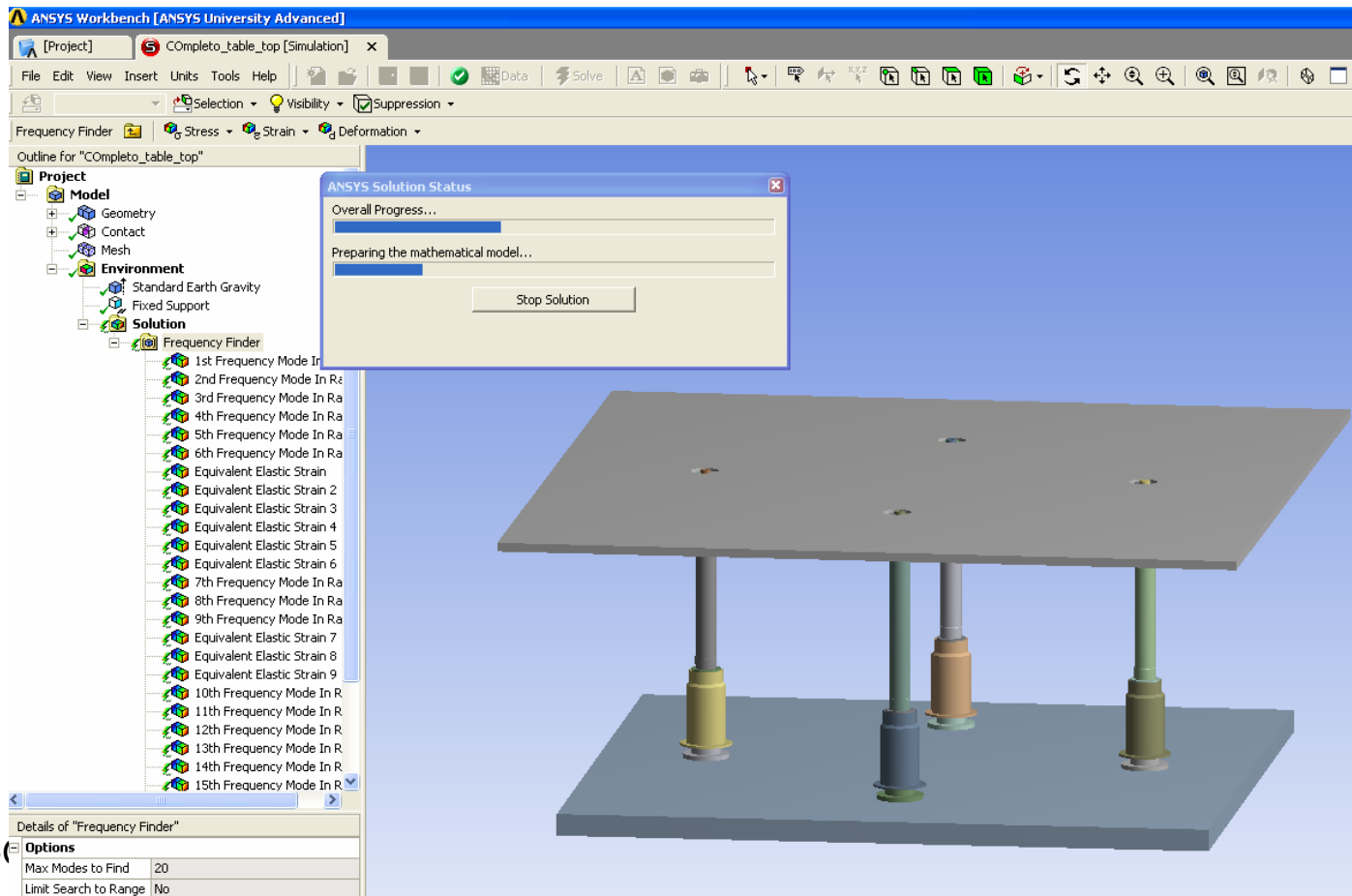
# Third step

- Assembly 4 legs into in Solid Works



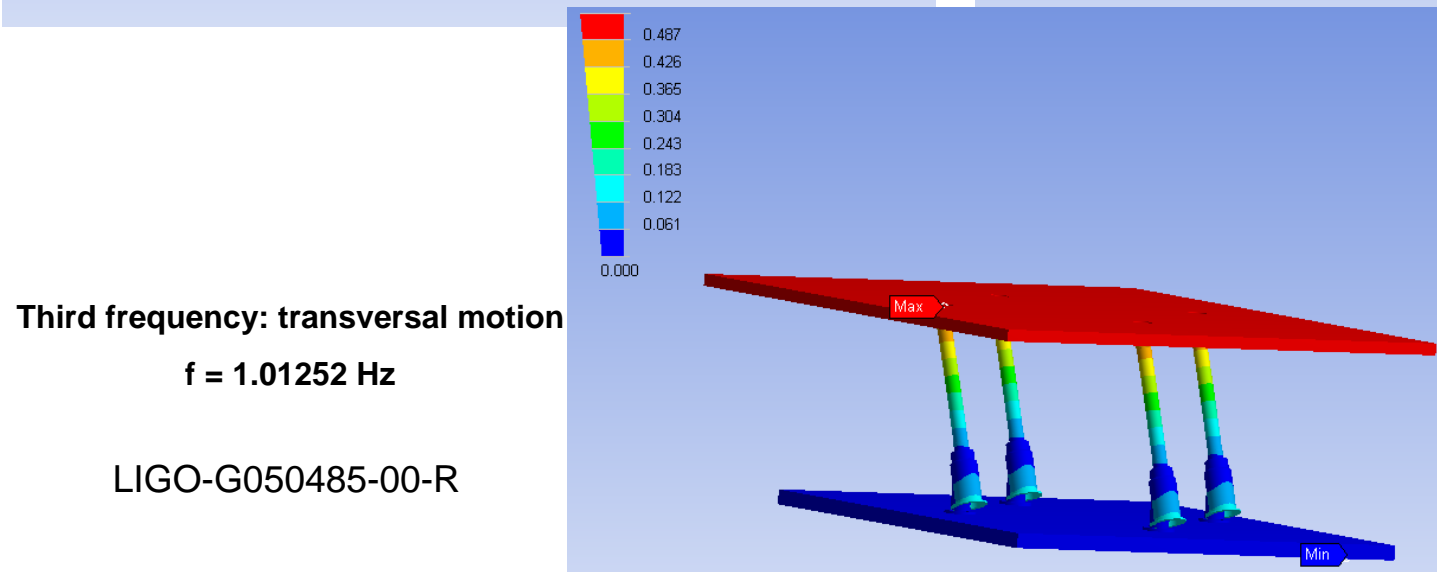
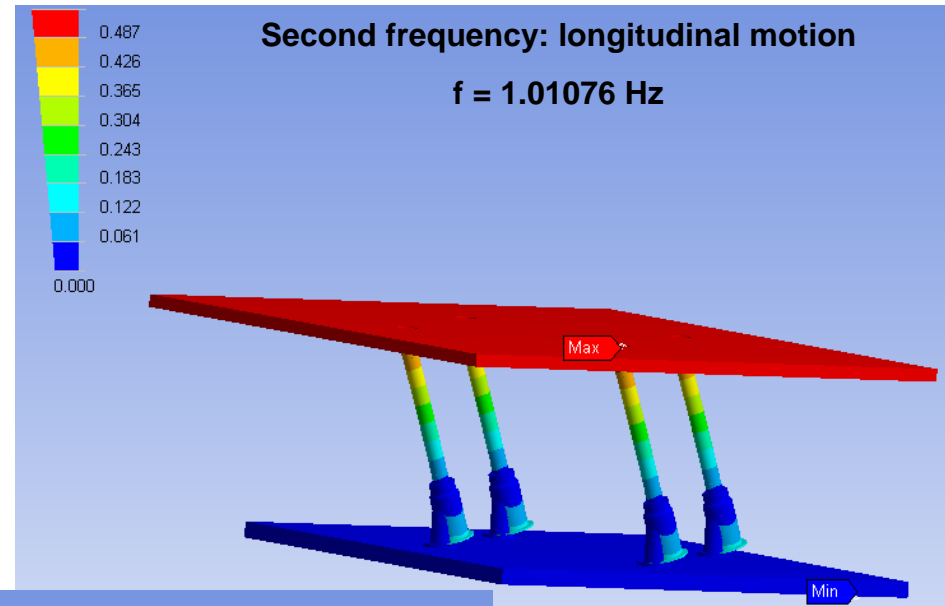
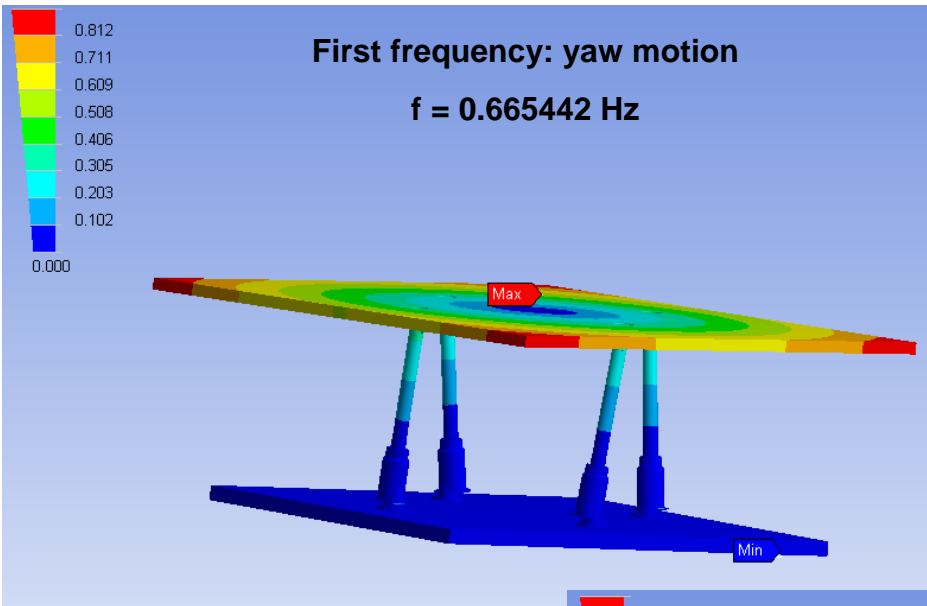
# Fourth Step

- Solve model and analyze first 20 modes in ANSYS



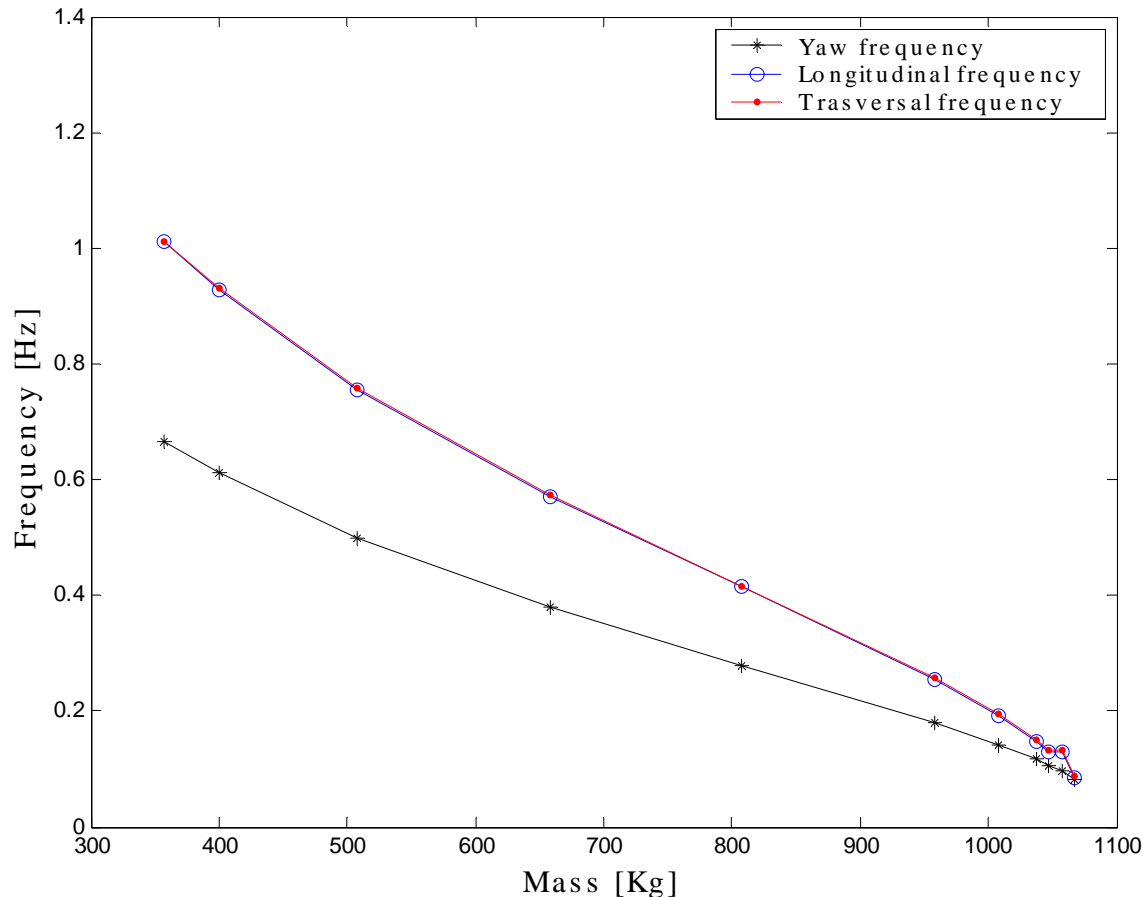


# Table normal modes



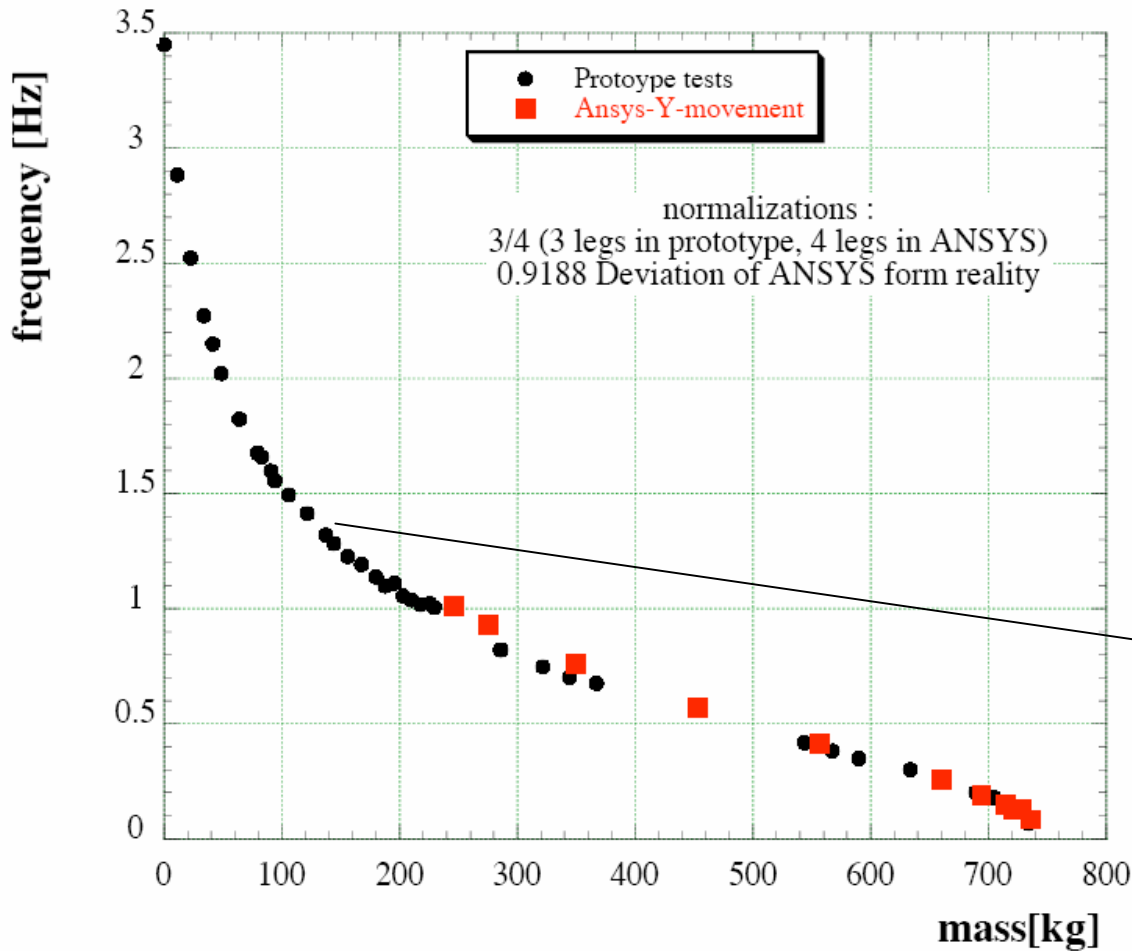
# LIGO Table normal modes (2)

- Frequency vs load: I changed the mass of the table on the top of the 4 legs



- Longitudinal and trasversal frequencies are identical
- Zero frequency point is the same for all 3 main modes

# Validation



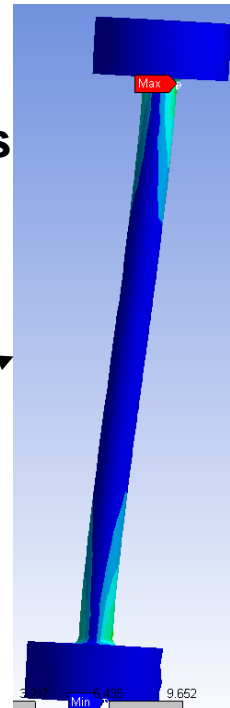
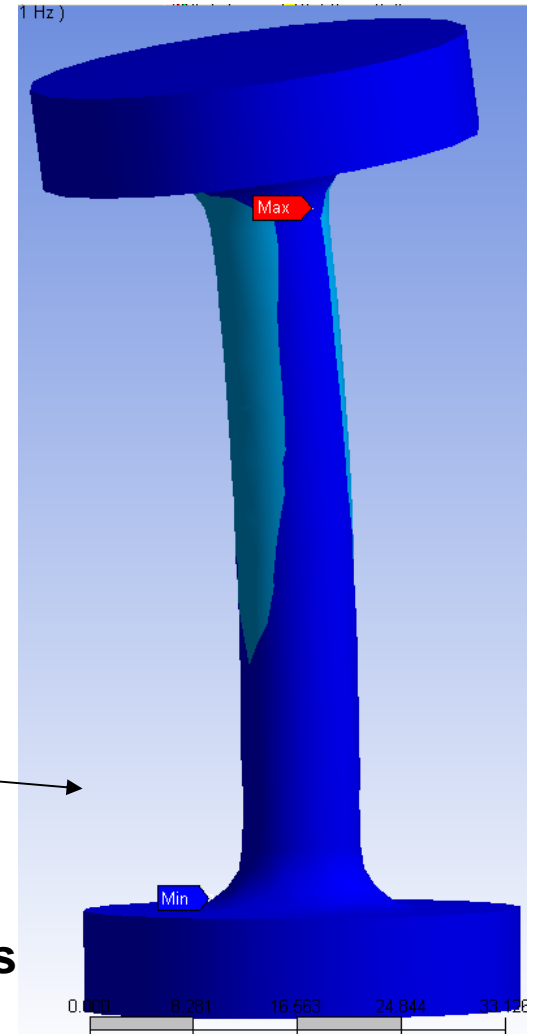
Ansys results are fully validated by the measurement results



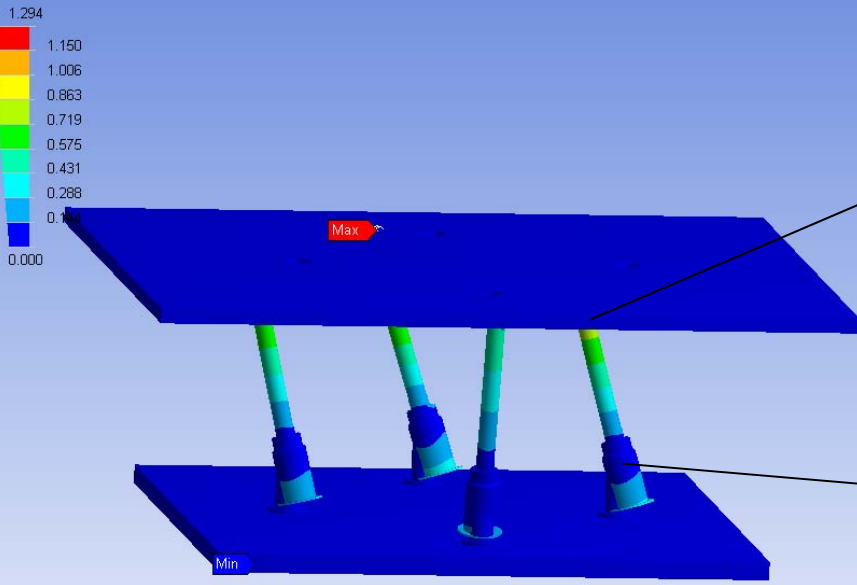
# Rigid leg resonances

- Eight degenerate resonances: each leg has 2 resonances

Small flex joint: S- stress

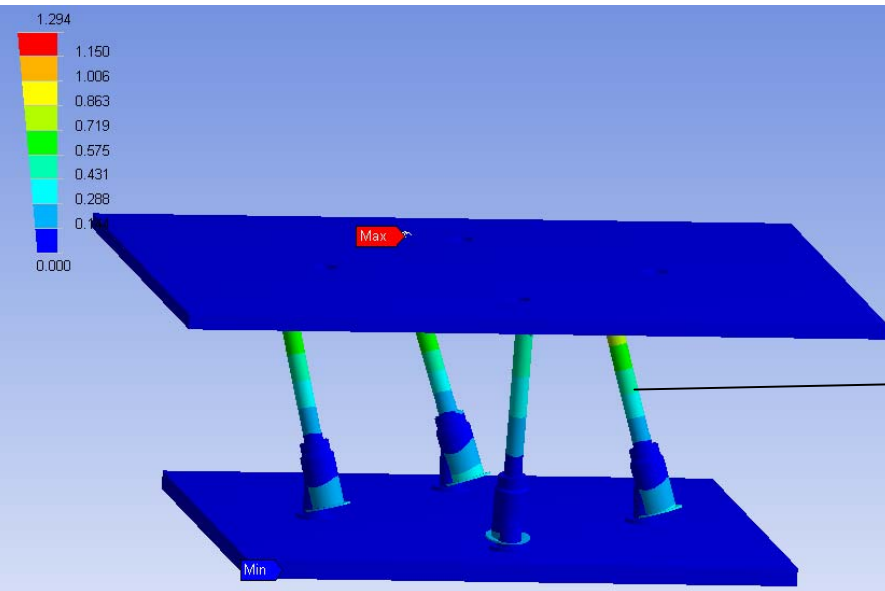


Main flex joint: C- stress

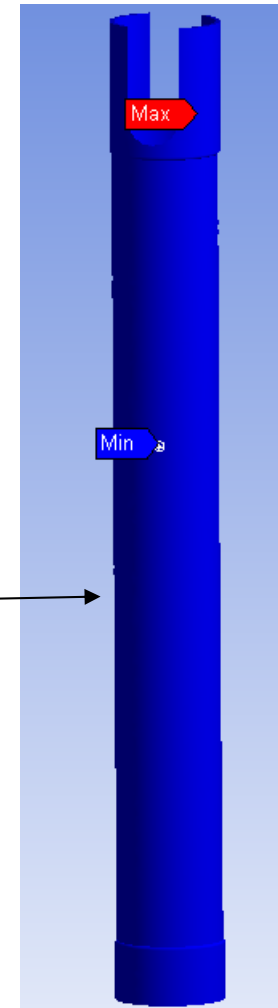


# Rigid leg resonances

- Eight degenerate resonances: each leg has 2 resonances



Leg is not stressed





# LIGO Rigid leg resonances (2)

**Mass of counter weight: 1.212 Kg**

	Resonance frequency with counterweight	Resonance frequency without counterweight
<b>Diameter of small flex joint: 1.5 mm</b>	~110.6 Hz	~122 Hz
<b>Diameter of small flex joint: 3 mm</b>	~178.3 Hz	~235.3 Hz

# LIGO Rigid leg resonances (2)

Mass of counter weight: 1.212 Kg

	Resonance frequency with counterweight	Resonance frequency without counterweight
Diameter of small flex joint: 1.5 mm	~110.6 Hz	~122 Hz
Diameter of small flex joint: 3 mm	~178.3 Hz	~235.3 Hz

Measurement of prototype: 103 Hz



20% of discrepancy between measurement and Ansys results, within tube tolerances

# LIGO Rigid leg resonances (3)

Mass of counter weight: 1.212 Kg

	Resonance frequency with counterweight	Resonance frequency without counterweight
Diameter of small flex joint: 1.5 mm	~110.6 Hz	~122 Hz
Diameter of small flex joint: 3 mm	~178.3 Hz	~235.3 Hz

Ansysis shows that counter weight doesn't reduce significantly the resonance, that are dangerous. They can be damped



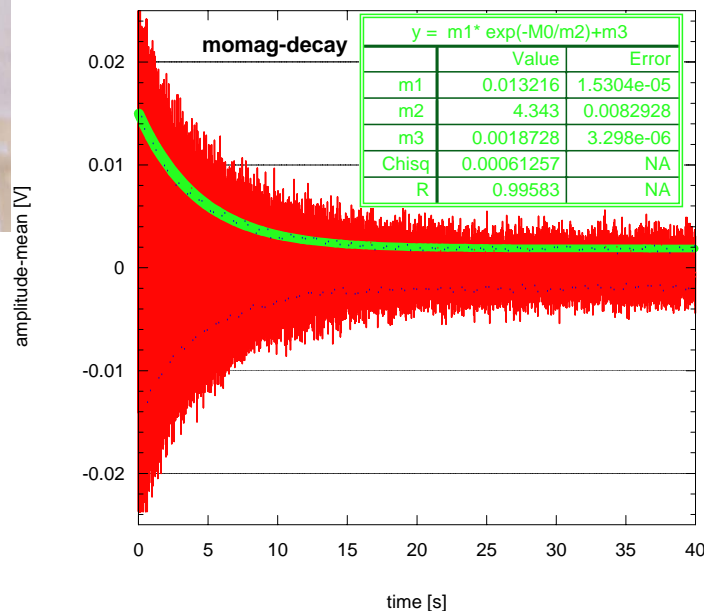
# LIGO Solution: Eddy current dampers

Measured and successfully damped in a prototype without counter weight

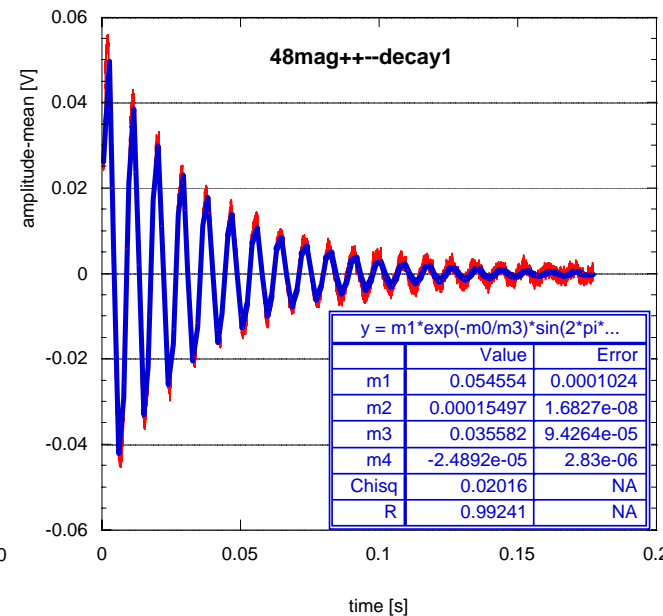
Eddy current dampers



Before installation  $t = 4.3$  s



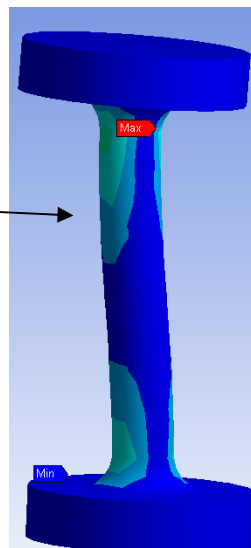
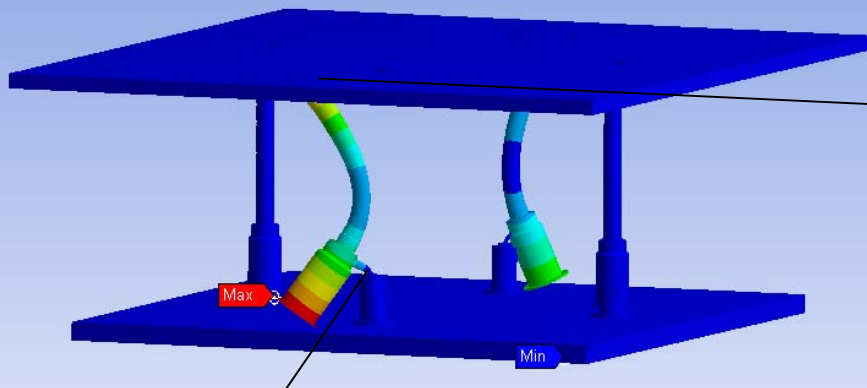
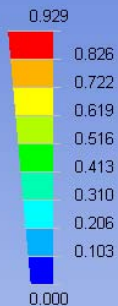
After installation  $t = 35$  ms



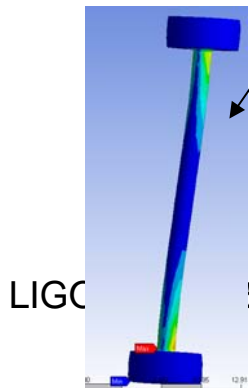
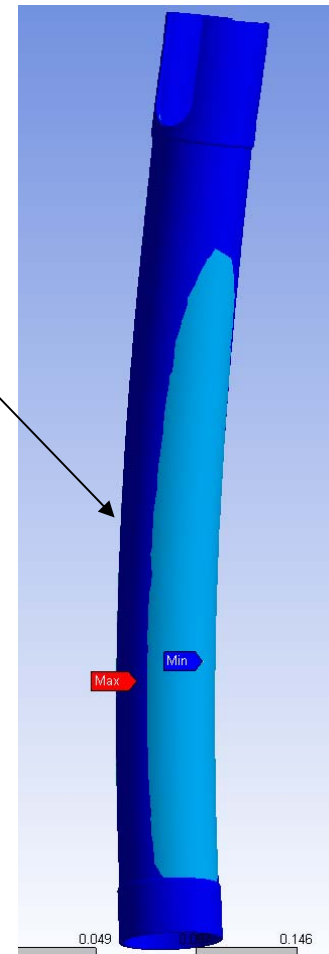
LIGO-G050485-00-R

# Banana leg resonances

Each IP leg has 2 banana resonances



Main flex joint:  
S- stress



Small flex joint: S- stress



# Banana resonances (2)

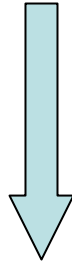
**Mass of counter weight: 1.212 Kg**

	Resonance frequency with counterweight	Resonance frequency without counterweight
<b>Diameter of small flex joint: 1.5 mm</b>	~210.6 Hz	~415 Hz
<b>Diameter of small flex joint: 3 mm</b>	~253.3 Hz	~424 Hz

# Banana resonances (3)

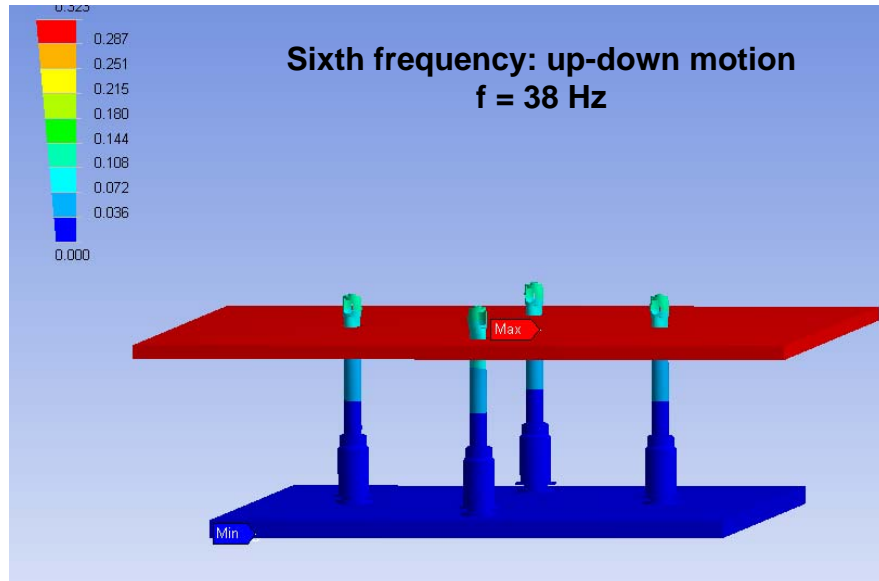
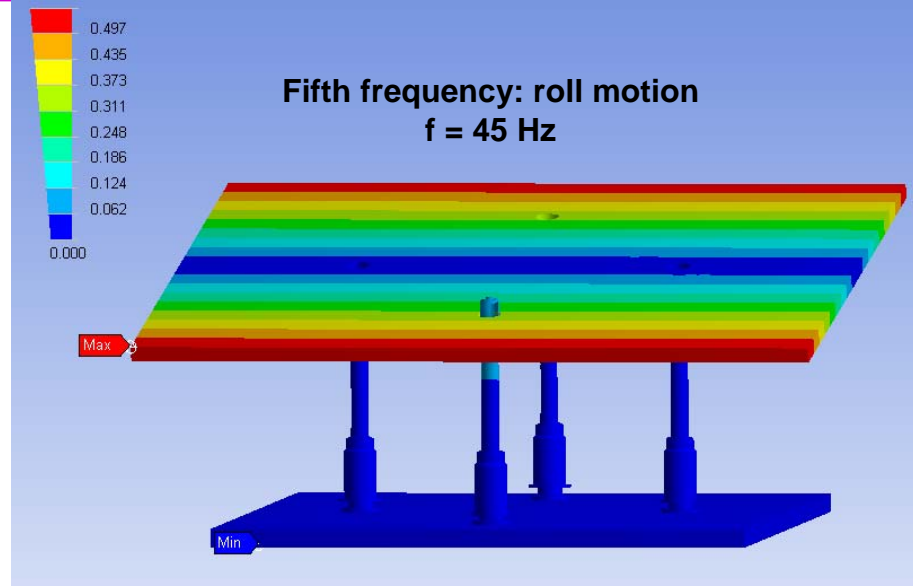
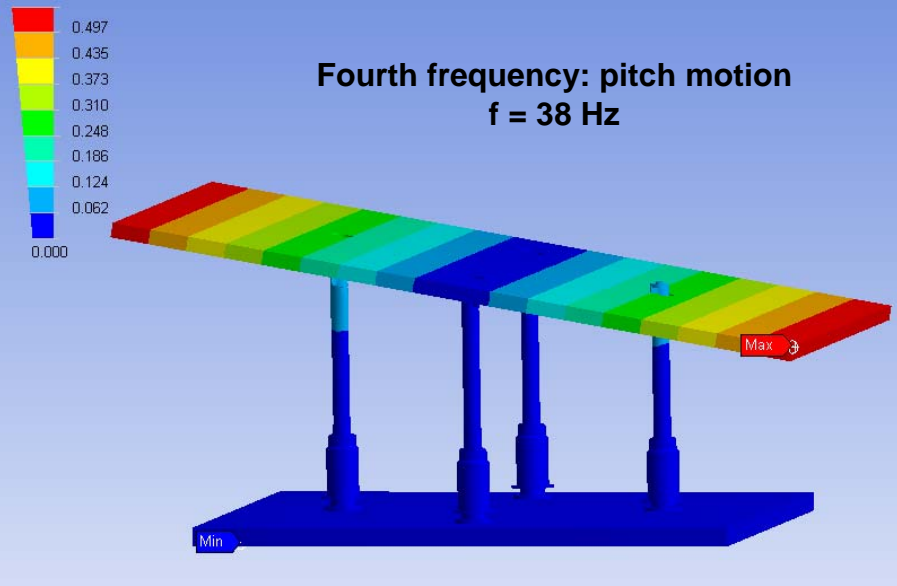
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- Higher frequencies
- Resonances move the head of the leg



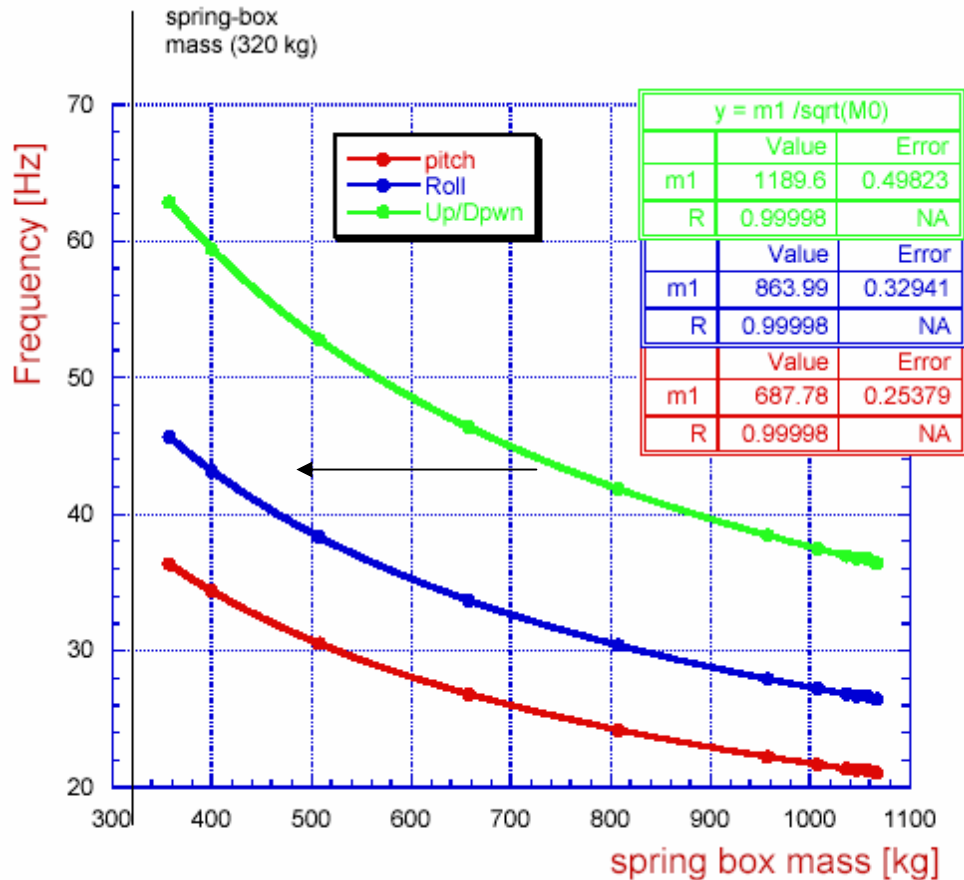
The damper will be even more effective

# Spring box resonances



# LIGO Spring box resonances(2)

Spring box effective mass 320 Kg

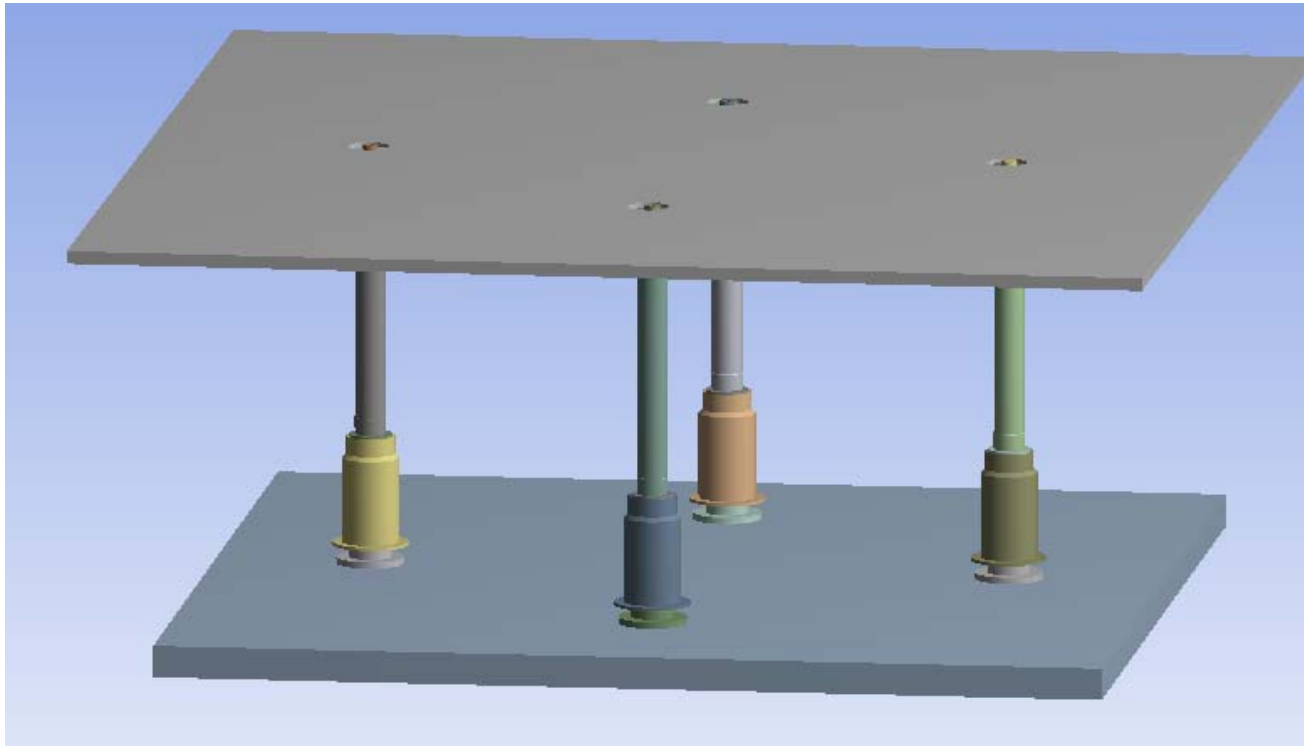


- Leg magnetic dampers may be still effective

- Complementary resonant dampers may be required

# IP Transfer Function

Output: monitor resulting movement



$$TF(f) = \frac{\text{Output}}{\text{Excitation}}$$



Excitation

# IP Transfer Function

- The aim is to determine the counter weight that neutralize the percussion point effect of the legs
- Prototype measurements indicate that the transfer function saturates at 80 dB without counterweight
- A proper counter weight should allow 100 dB attenuation



# Future

- Find a counter weight which allow an attenuation of 100 dB
- Export TF to Sym Mechanic model

# Acknowledgments

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- Riccardo De Salvo and Calum Torrie for their help, encouragements and patience
- Juri Agresti and Virginio Sannibale for answering my quick questions
- Innocenzo Pinto for the opportunity he gave me

# And...

The sun of California...

