

Adaptive Mode matching for advanced LIGO

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DCC LIGO-G050422-00-Z



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LSC meeting, August 16, 2005
LIGO Hanford Observatory

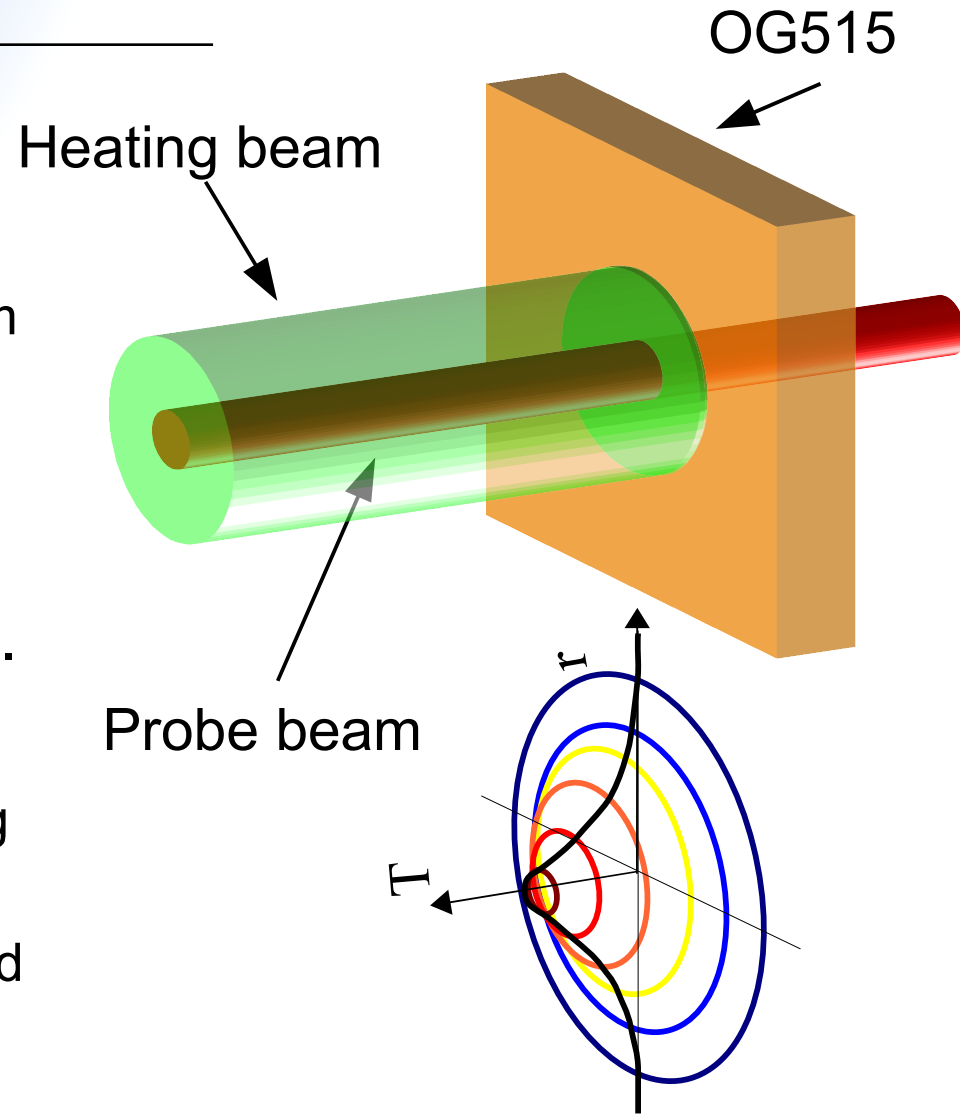
Motivation

Interferometric gravitational wave detectors are basically interferometers with suspended components that are operated in vacuum.

- Objective:
 - Actuator to change the modal parameters of a Gaussian beam without moving parts.
- Requirements:
 - Touch free
 - Vacuum compatible (UHV)
 - Stationary (no movable parts)
- Solution:
 - Telescope with lenses with variable focal lengths

Adjustable lenses

- Use thermal lensing effect
- Use dichroic material
 - high absorption for heating beam
 - low absorption for probe beam
- Schott OG515 is highly transmissive for 1064nm and strongly absorbing for 514 nm.
- Two laser setup
 - Argon-Ion laser provides heating beam to actuate the lens
 - Nd:YAG laser probes the created effect



Calculate temperature profile in substrate

- Solve thermal diffusion equation assuming $\frac{\partial T}{\partial z} = 0$ on the faces and $T(r, z) = T_0$ on the rim (Substrate in heat sink).

$$\nabla^2 T(r, z) = -\frac{2\alpha P}{\pi K w^2} \exp\left(-2\frac{r^2}{w^2}\right) \exp(-\alpha z)$$

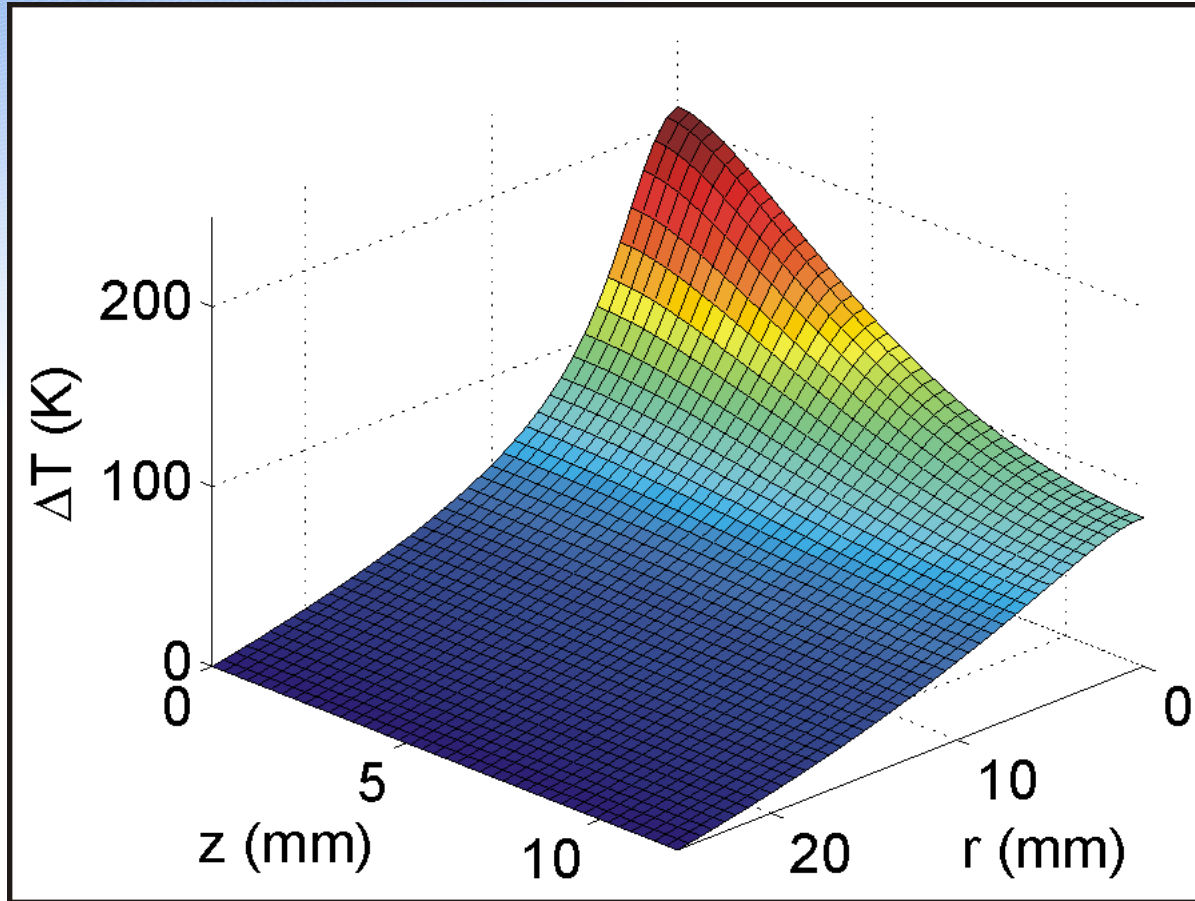
Analytical solution exists:

$$T(r, z) = -\sum_{n=1}^{\infty} \frac{4\alpha P}{\pi K R^2 w^2} \frac{\int_0^R \exp\left(-\frac{2r'^2}{w^2}\right) J_0\left(\frac{k_n r'}{R}\right) r' dr'}{(J_0(k_n))^2} J_0\left(k_n \frac{r}{R}\right) f_n(z) + T_0$$

$$f_n(z) = \frac{1}{\alpha^2 - \left(\frac{k_n}{R}\right)^2} \left\{ \frac{\alpha R}{k_n} \left(\frac{e^{\left(\left(\frac{k_n}{R} - \alpha\right)L\right) - 1} e^{\left(\frac{k_n z}{R}\right)} - e^{\left(-\left(\frac{k_n}{R} + \alpha\right)L\right) - 1} e^{\left(\frac{k_n z}{R}\right)}}{e^{\left(\frac{2k_n L}{R}\right) - 1} - 1} \right) \right\}$$

3D - Temperature profile

- For 4 W heating beam with 3.6 mm radius



Calculated on grid with 460 radial and 1000 axial steps

Evaluating the effects of the temperature profile

- Change of optical path length

$$OPL(r) = \left(\frac{dn}{dT} + \alpha_T(n-1) \right) \int_0^L \Delta T(r, z) dz \quad \text{GRIN lens}$$

- Propagate a Gaussian beam with this OPL

$$\begin{aligned} u(r, z) &= u_{probe}(r, z) \exp(-ik OPL(r)) \\ &= u_{probe}(r, z) \exp\left(-ik \left(OPL(0) + OPL''(0) \frac{r^2}{2} + O(r^4) \right)\right) \end{aligned}$$

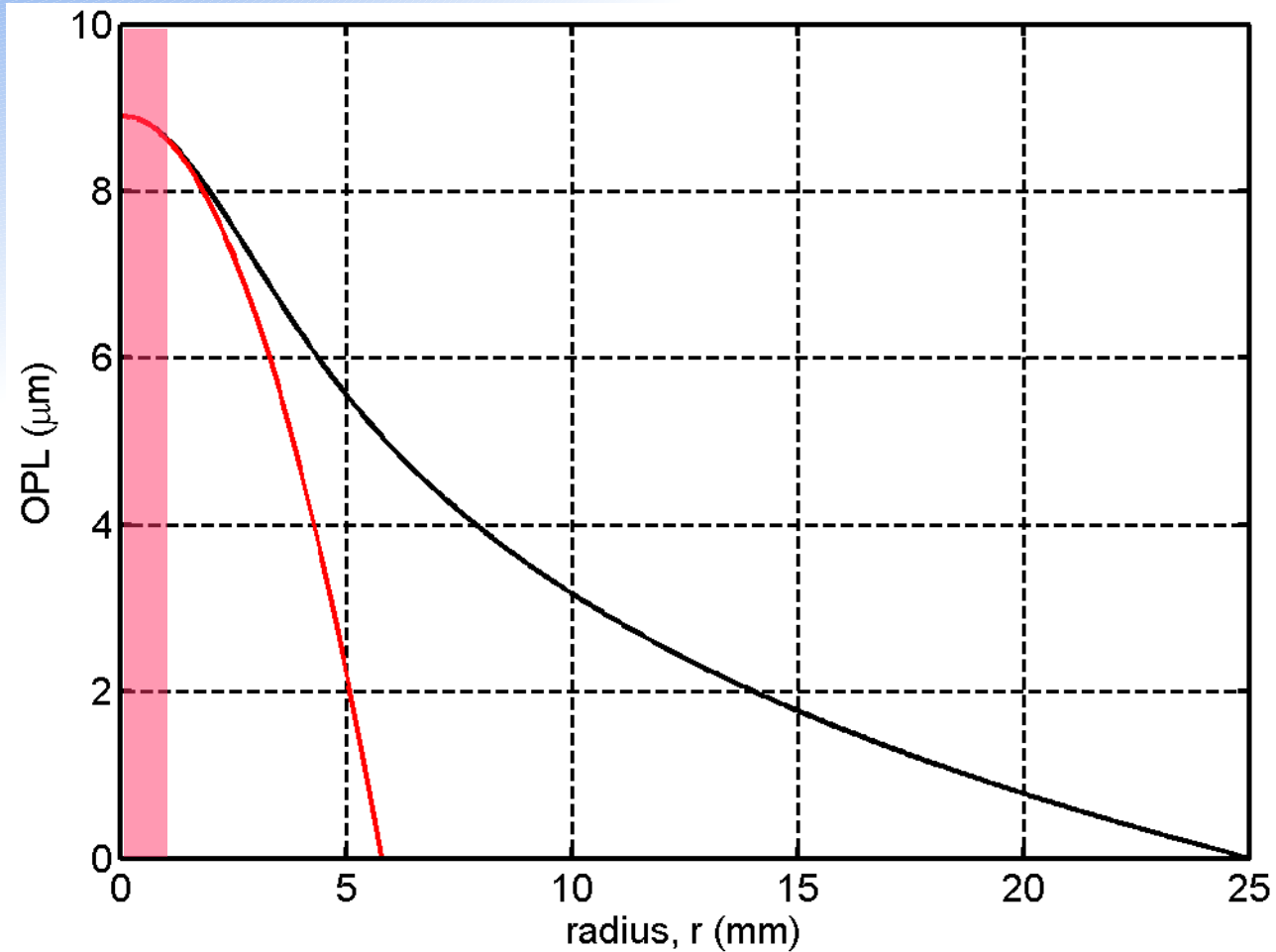
- Compare with propagation through a thin lens

$$u(r, z) = u_{probe}(r, z) \exp\left(ik \frac{r^2}{2} \frac{1}{f}\right)$$

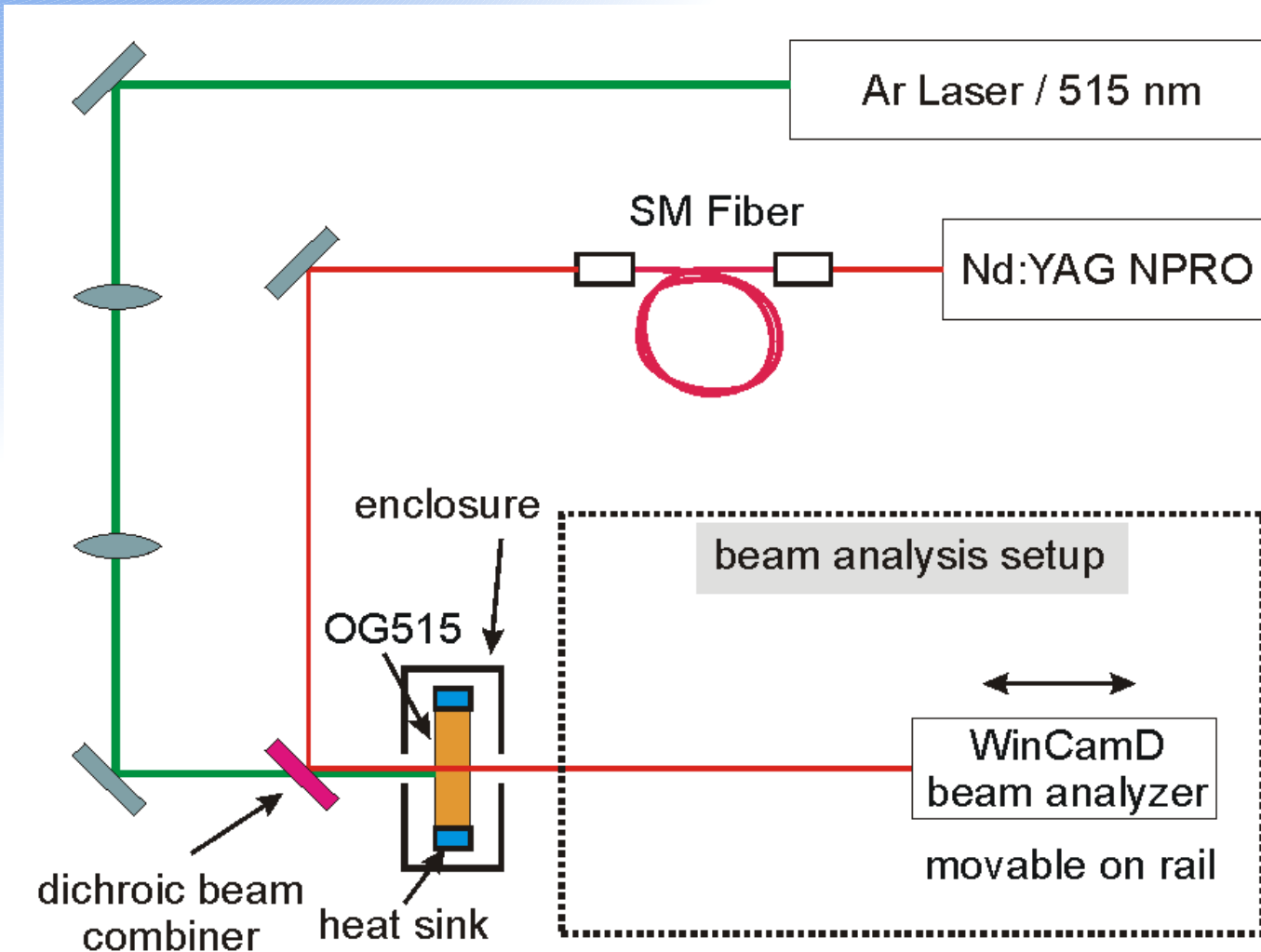
$$\rightarrow f = \frac{-1}{OPL''} \quad \text{focal length}$$

Calculated optical path length

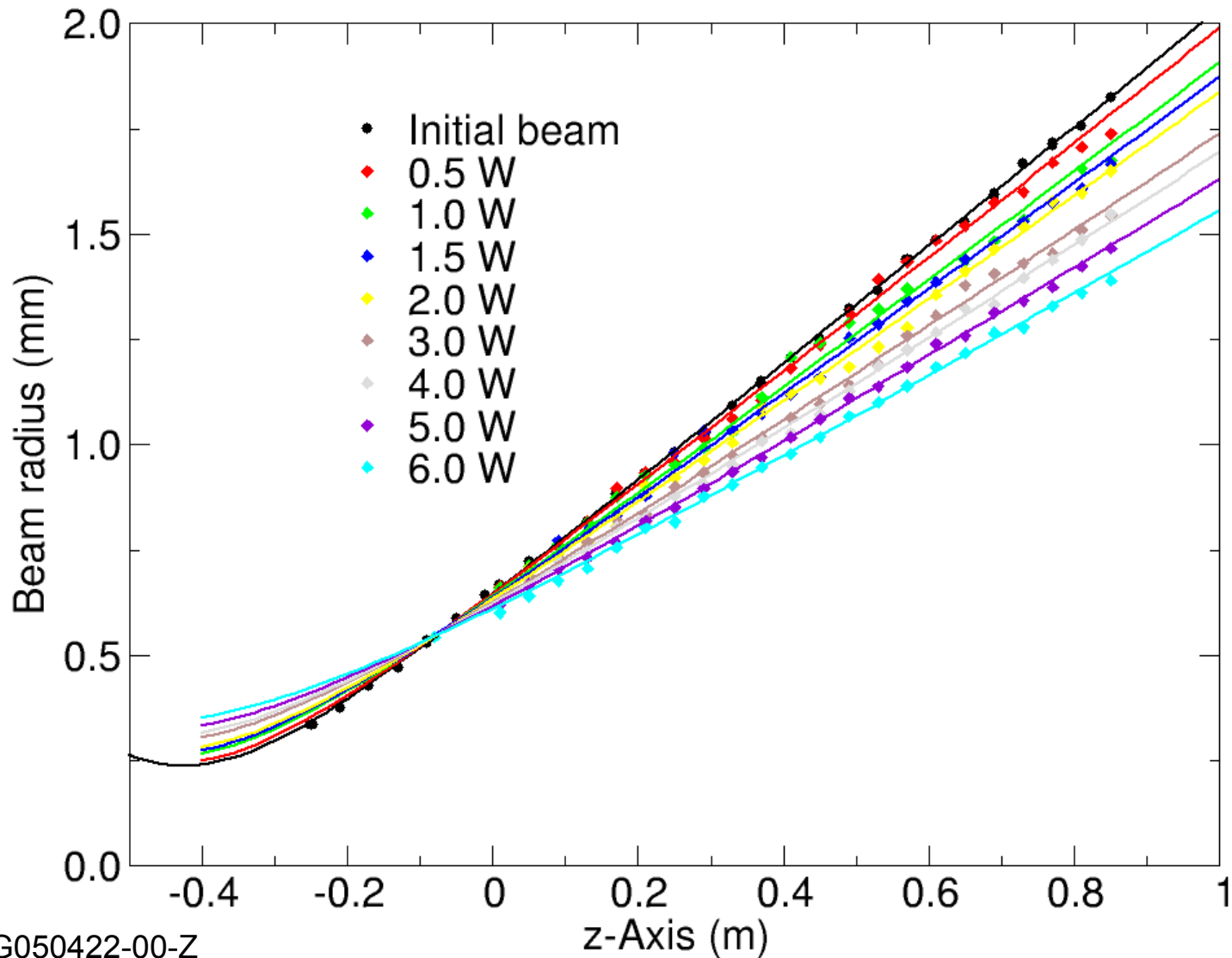
- Comparison with “ideal” thin lens ($f = 1.88$ m)



Measurement setup - beam analysis

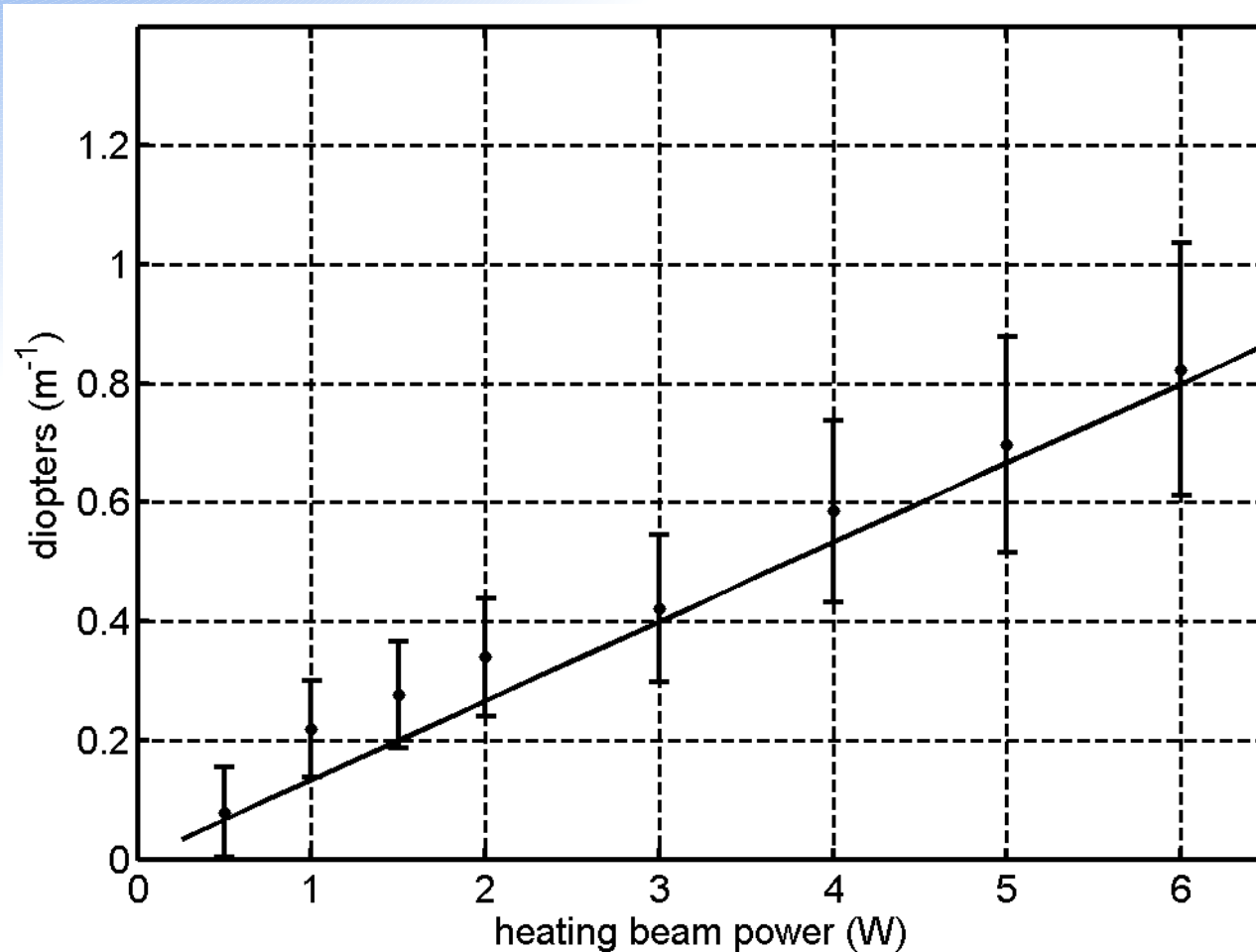


Changes in Gaussian Mode



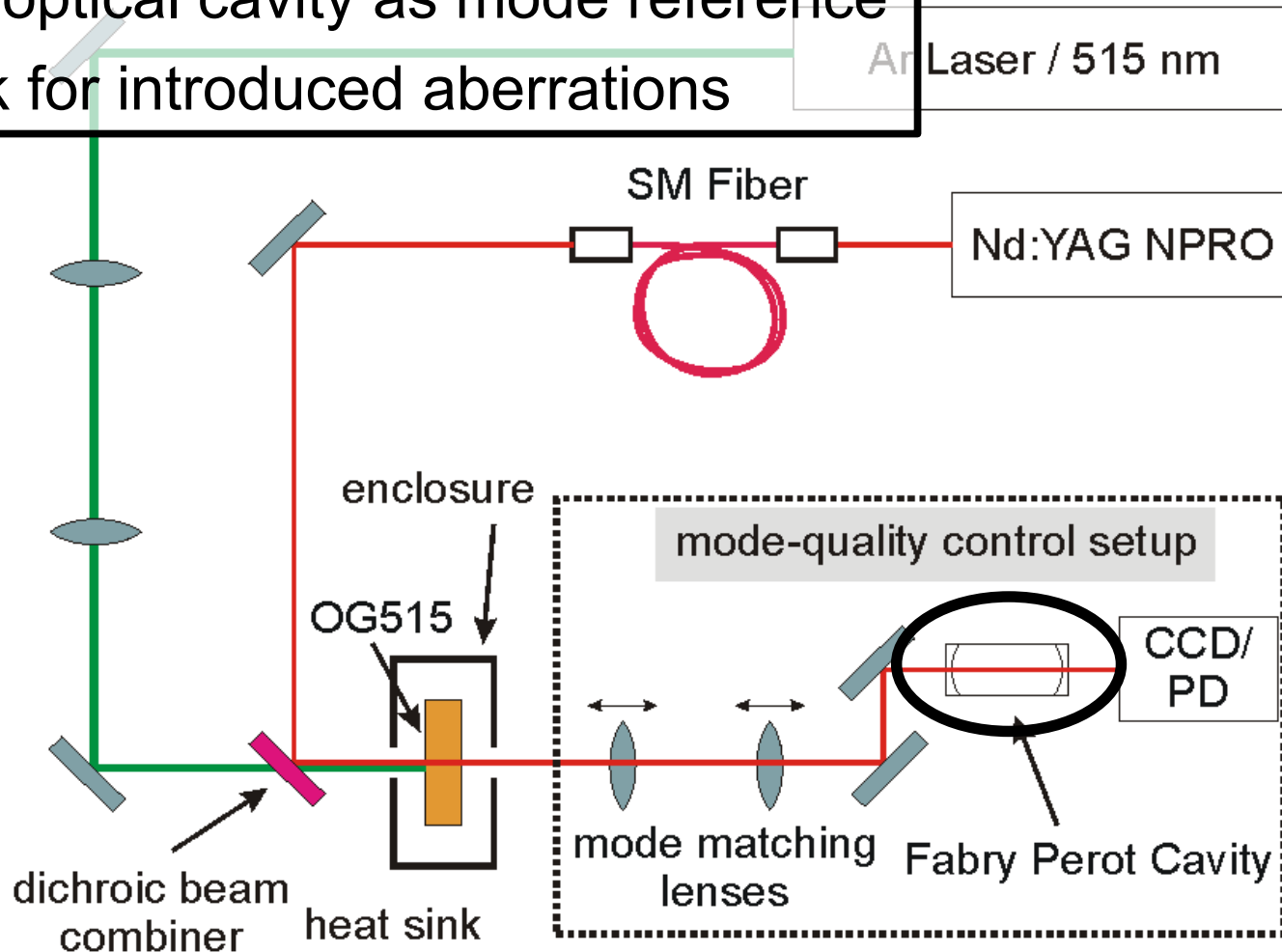
Corresponding focal power changes

- Focal power - diopters

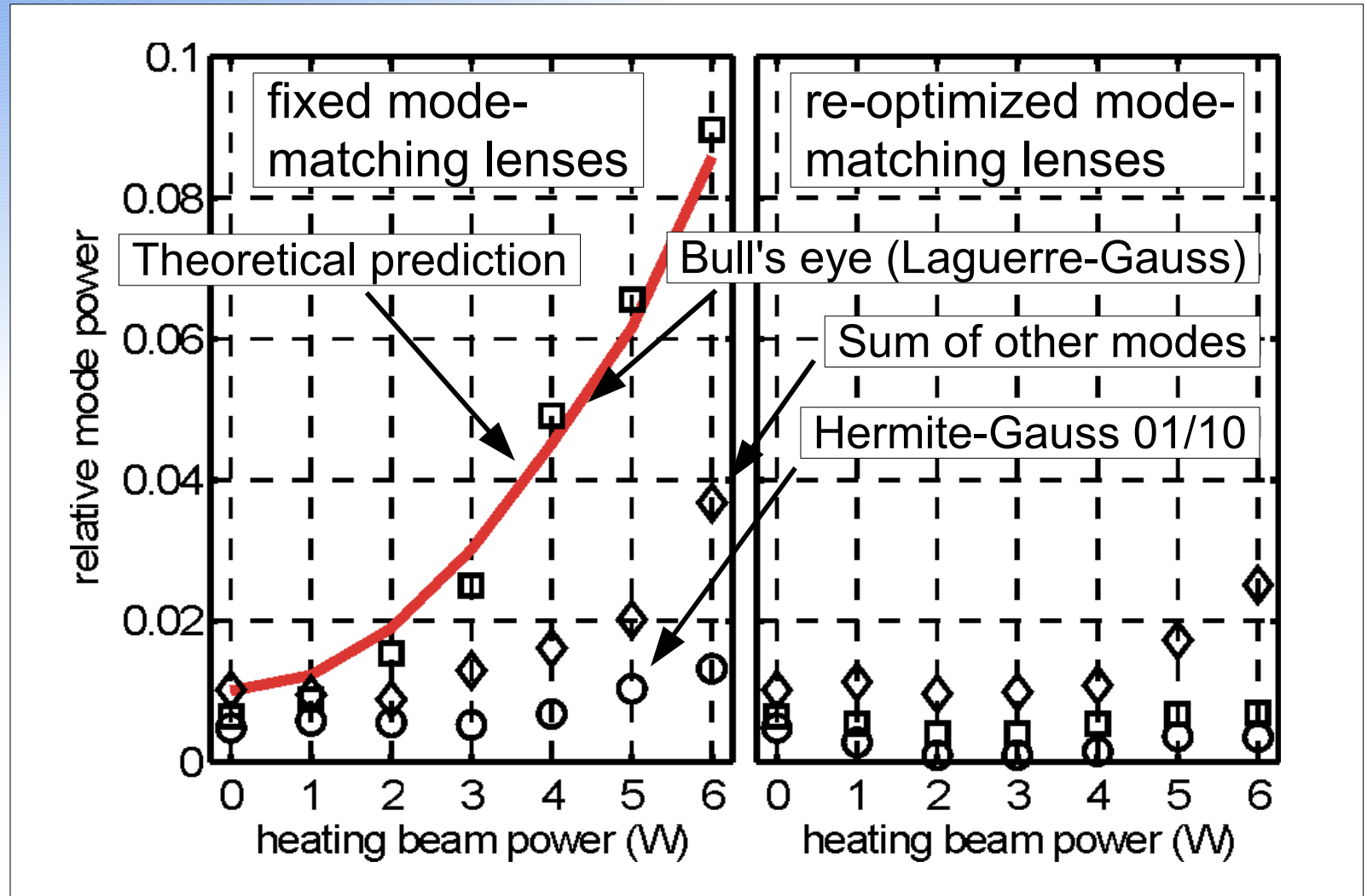


Measurement setup - mode quality

- Use optical cavity as mode reference
- Look for introduced aberrations



Higher order mode content (normalized to TEM₀₀)



Conclusion

- Excellent agreement with theoretical model
- Technique is “touch free” and vacuum compatible
- An aberration free lens can be created if:
 - The amount of heat is kept below the structural limit
 - The ratio of heating beam to probe beam radii is sufficiently large

Future work

- Use different absorbing material
 - CO2 laser and fused silica
- Start beam shaping experiments