

CorrPower: a Cross-Correlation Based Algorithm for Triggered and Untriggered Gravitational-Wave Burst Searches

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What is CorrPower?

A new search code for bursts of gravitational waves, looking for excesses of coherent power in multiple detectors.

Three modes of operation:

1. continuous cross-correlation of data from multiple detectors and generation of event triggers associated with an excess of coherent power (the focus of this poster)
2. r-statistic test on burst candidate events → ref: 2004 Class. Quantum Grav. 21 S1695-S1703
3. external trigger search similar to GRB030329 → ref: 2004 Class. Quantum Grav. 21 S1831-S1837

Unification of coherent techniques implemented in the LIGO triggered and un-triggered burst analysis.

Two platforms:

- A. MATLAB standalone (status: running on LSC grid clusters; useful for pipeline development, but non-optimal computational speed)
- B. C++ LIGO Data Monitoring Tool (status: in development; potential for online analysis)

Search Strategy

Cross-correlation of data from a pair of GW detectors.

1. The power of the sum of the two data vectors is: $(\mathbf{a}+\mathbf{b})^2 = \mathbf{a}^2 + \mathbf{b}^2 + 2\mathbf{a}\cdot\mathbf{b}$

$P_{\text{coher}} = \mathbf{a}\cdot\mathbf{b}$ is the coherent power component for the detector pair

2. The angle between data vectors is the quantity used in the r-statistic test

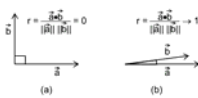
2004 Class. Quantum Grav. 21 S1695-S1703

C_M is the r-statistic confidence for the correlation of a detector pair

For each (i,j) pair of detectors, we build a matrix of P_{coher}^{ij} and C_M^{ij} for several

- A. integration windows (=dimension of the data vectors)
- B. central times

NOTE: P_{coher}^{ij} and C_M^{ij} are maximized over time lags between the two data vectors, up to the light travel distance between detectors + timing resolution



Combine all detector pairs and build network detection statistics for each central-time/integration-window:

$$r\text{-statistic } \Gamma = P_{\text{coher}} / N_{\text{pairs}}$$

$$\text{Coherent Power: } P_c = \sum P_{\text{coher}}^{ij} / N_{\text{pairs}}$$

$$\text{hrss} = \sqrt{P_c}$$

Normalized Excess Power

$$\text{NEP} = (P_c - \mu) / \sigma$$

μ and σ computed separately for each integration length, average over all central times in the analyzed data segment after removal of outliers

Corrgram = 2D pixelization of integration-time versus central-time

The set of integration times and the separation between central times (= overlap between consecutive integration windows) are parameters of the search

- Corrgram pixels with significant statistics are passed to the post-processing:
 - cluster by requiring a minimum separation between events;
 - assign the event the max values of NEP, Γ and hrss_c over the cluster;
 - empirical minimum NEP threshold = 3;
 - empirical minimum Γ threshold = 3;
 - potential for a distributional analysis (compare the distribution of NEP or hrss_c in foreground and background, for a given threshold on Γ);

- The pipeline detection efficiency is determined with MonteCarlo simulations
- The background is estimated introducing an unphysical delay between time series

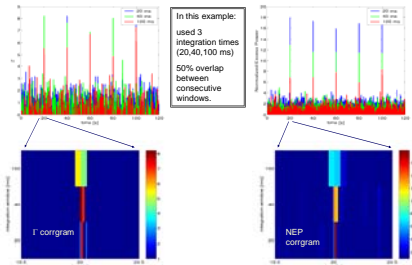
Sample Performance

We show a sample performance of the method using:

- white gaussian noise sampled at 4096 Hz
- 2 or 3 detectors
- Gaussian pulses, with $\tau=1$ ms and different amplitudes

$$h(t) = h_{\text{peak}} e^{-t/\tau} \cos(\omega t)$$

Noise: 2 detectors with white gaussian noise (4096Hz) and same sensitivity
Signal: 1 ms gaussians, $\rho=10$, injected every 20 sec
Analysis segment = 120sec

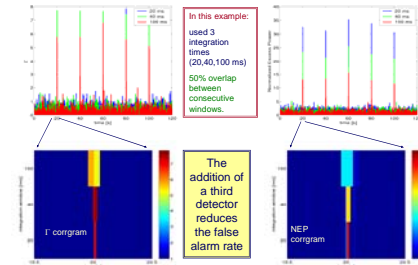


In this example: used 3 integration times (20,40,100 ms) 50% overlap between consecutive windows.

In the following, the amplitude of the simulated events is expressed as the optimal SNR from matched filtering, computed in the least sensitive detector:

$$\rho = \sqrt{4 \int_{-\infty}^{\infty} |\tilde{h}(\omega)|^2 S_n(\omega) d\omega}$$

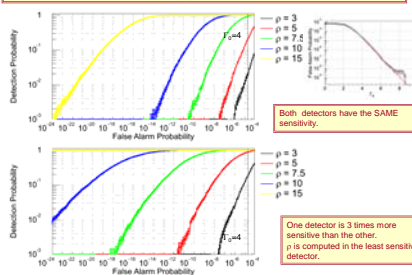
Noise: 3 detectors with white gaussian noise (4096Hz) and same sensitivity
Signal: 1 ms gaussians, $\rho=10$, injected every 20 sec
Analysis segment = 120sec



In this example: used 3 integration times (20,40,100 ms) 50% overlap between consecutive windows.

The addition of a third detector reduces the false alarm rate

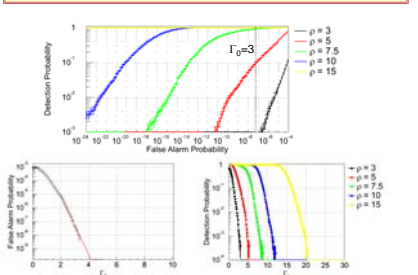
Noise: 2 detectors with white gaussian noise (4096Hz)
Signal: 1 ms gaussians, $\rho=10$, injected every 20 sec. NEP > 3
Parameter on these R.O.C. curves: Γ_c (threshold on Γ)



Both detectors have the SAME sensitivity.

One detector is 3 times more sensitive than the other. ρ is computed in the least sensitive detector.

Noise: 3 detectors with white gaussian noise (4096Hz) and same RMS
Signal: 1 ms gaussians, $\rho=10$, injected every 20 sec. NEP > 3
Parameter on these R.O.C. curves: Γ_c (threshold on Γ)



Challenges of Real Data

- Colored spectrum**
 - This is not problematic with the LIGO-type spectra. A linear-predictor error filter is very effective at whitening real data.
- Non-stationary lines**
 - Known lines can be notched out. Also, the linear-predictor error filter, applied to minute-scale data segments (as in the CorrPower search) reasonably removes lines, but in some instances a post-processing r-statistic test run over small time-scales (seconds) is needed as veto for highly non-stationary lines.
- Broadband transients**
 - Broadband instrumental "glitches" in non-located detectors sometimes appear as correlated events and increase the false rate. A larger Γ_c threshold (6-10) is necessary, for instance, in the S3 analysis (see Yakushin's talk). Background studies are needed to tune the value of Γ_c .
- Environmental correlations affect the false rate in the two Hanford detectors**
 - Acoustic coupling can produce spurious correlations, but an environmental veto is possible for these instances.
- Antenna patterns reduce the detection efficiency**
 - Simulations for the LIGO Hanford-Livingston show the effect is not worse than in incoherent searches. Studies are in progress to evaluate the effect when more detectors are added to the network.

Outlook

- Current status**
 - A MATLAB standalone code is currently running on the LSC grid clusters.
 - With 3 integration windows, data at 4 kHz and 50% overlap between windows, the code runs at 4 x real time on the cluster at LIGO-Caltech.
 - A C++ Data Monitoring Tool (DMT) implementation is in progress.
- Short-term goals**
 - Finalize tuning strategies for the CorrPower pipeline.
 - Analyze S3 and E11 data with CorrPower and the triggers are used for detector characterization (in progress).
 - Use CorrPower in the AURIGA-LIGO (AU1/S3) joint analysis (cross-correlation limited to the LIGO interferometers).
 - Adopt CorrPower in the externally triggered burst search.
- Long-term goals**
 - Promote the DMT version of the code to an online analysis pipeline for LIGO's S5 run.
 - Explore use of CorrPower in joint analysis with other detectors.