

Developments in test mass and suspension materials for future detectors

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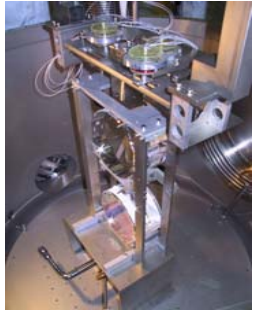
Introduction

- To achieve the desired sensitivities of future long-baseline gravitational wave detectors will require a reduction in thermal noise associated with test masses and their suspensions
- Extend research in the development of low dissipation quasi-monolithic suspensions, acquired through designing suspensions for GEO 600 and Advanced LIGO, to:
 - develop ultra-low thermal noise suspensions for 'GEO-HF' capable of sustaining high optical powers (room temperature)
 - develop ultra-low thermal noise suspensions for EGO and equivalent 3rd generation detections (cryogenic temperatures)



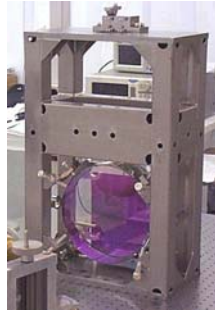
Suspension technology status

current detectors eg:



GEO 600

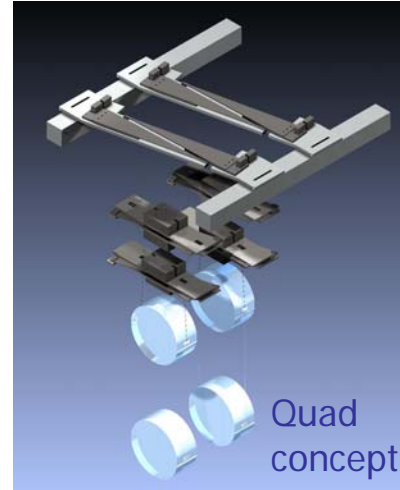
Silica suspension.
Arm length: 600 m.



Initial LIGO
Wire loop.

Arm length: 4 km.

advanced detectors



e.g. Advanced LIGO
Quadruple stage.
Sapphire/silica.
Ribbons/fibres.
Arm length: 4 km.

Quad
concept

being designed

future detectors



e.g. GEO-HF, EGO, others?
Silicon suspension technology.

operational

current research

■ Studies of:

- fabrication of, and dissipation in silicon suspension elements
- intrinsic dissipation in bulk silicon
- fabrication and dissipation of monolithic silicon pendulums

See talk by
Jim Hough



Challenges for future detectors - why silicon ?

#1

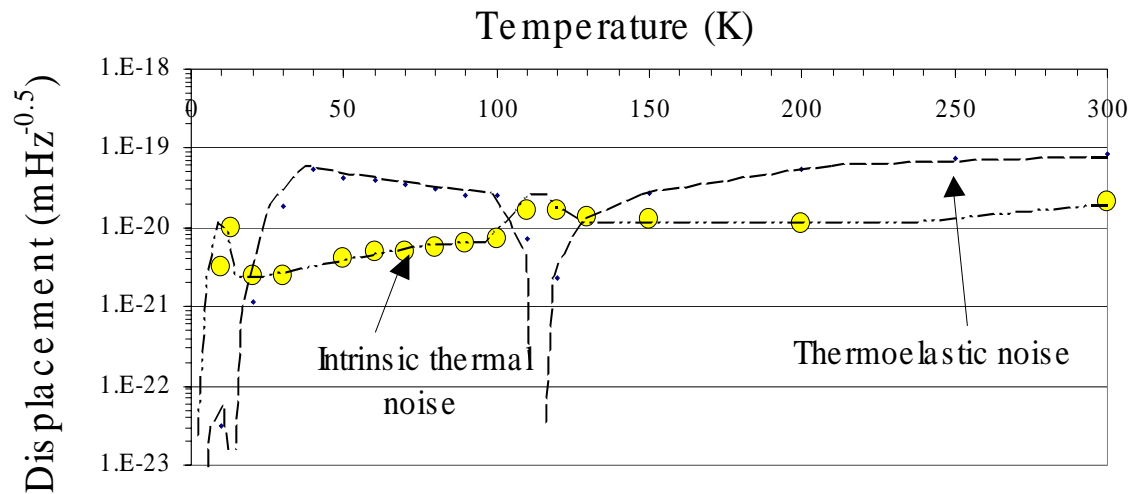
- To improve shot noise limited sensitivity, future detectors may require **higher levels of laser power** than currently used
 - Require mirror substrates capable of sustaining high thermal loads whilst maintaining optical figure
 - Thermally induced deformation of mirror surface is proportional to α/k_{th} [Winkler *et al.*, 1991].
 - α = substrate expansion coefficient
 - k_{th} = substrate thermal conductivity
 - Would like a substrate material for which this figure of merit is minimised
- In addition, further reductions in test mass and suspension thermal noise are required
- Possible material meeting these requirements is **silicon**
- GEO considered silicon mirrors Circa early 90's - at that time purchased substrates polished by Zeiss - but laser/diffractive technology not mature at that time
- Over past few years re-visiting this incorporating recent developments



Challenges for future detectors - why silicon ?

#2

- Two relevant types of mechanical dissipation:
 - “Intrinsic” dissipation (eg: due to point defects or line dislocations)
 - Thermoelastic dissipation, associated with temperature fluctuations throughout the mass (depends on fundamental material properties)
- Silicon can have low intrinsic dissipation but thermal noise at low frequencies dominated by thermoelastic noise
- Both thermoelastic and intrinsic thermal noise may be reduced by cooling:



Calculated intrinsic thermal and thermoelastic noise @ 10 Hz in a single silicon test mass, sensed with a laser beam of radius ~ 6 cm

- Thermoelastic noise is proportional to α and should vanish at $T \sim 120$ K and ~ 18 K where α tends to zero
- Intrinsic thermal noise exhibits two peaks at similar temperatures
- Silicon may allow significant thermal noise improvements at low temperatures but **material properties need further study**



In more detail

From Braginsky et al:

$$x^2(\omega) = \frac{8}{\sqrt{2\pi}} \alpha^2 (1 + \sigma)^2 \frac{k_b T^2}{\rho C} \frac{a^2}{r_0^3} \frac{1}{\omega^2}$$

(1) Need values for $\alpha(T)$, $C(T)$, $K_{th}(T)$

(2) Formula is valid for $\omega \gg a^2/r_0^2 \sim 1/\tau$

α = coefficient of thermal expansion

σ = Poisson's ratio

ρ = density

C = specific heat capacity

$a^2 = K_{th}/\rho C$: K_{th} = thermal conductivity

r_0 = beam radius at which intensity drops to 1/e

ω = angular frequency

$$x^2(\omega) = \text{Constant} \frac{\alpha^2 T^2}{C} \frac{1}{r_0} \frac{a^2}{r_0^2} \frac{1}{\omega^2}$$

$$= \text{Constant} \frac{\alpha^2 T^2}{C} \frac{1}{r_0} \frac{1}{\omega \tau} \frac{1}{\omega}$$

Following classical thermo-elastic damping - more generally

replace $\frac{1}{\omega \tau}$ by $\frac{\omega \tau}{1 + \omega^2 \tau^2}$

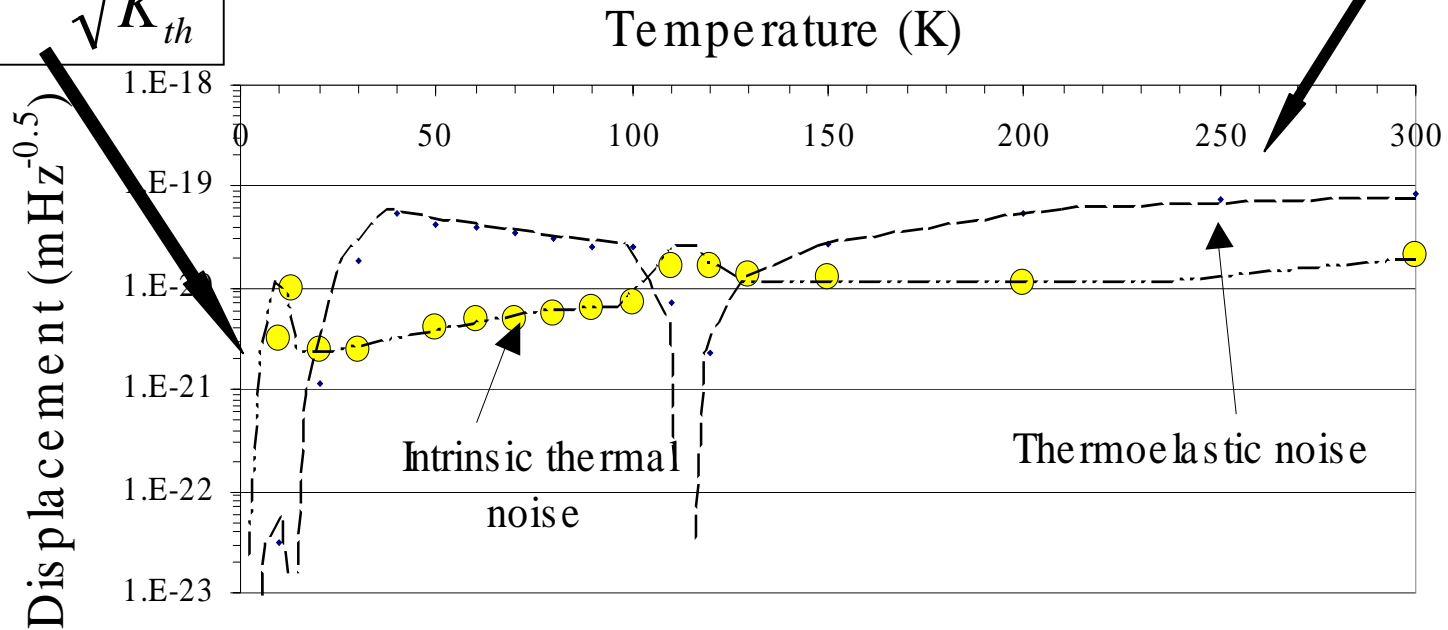


Figures of merit in different regimes

From Braginsky et al:

$$x(\omega) \propto \frac{\alpha T}{\sqrt{K_{th}}}$$

$$x(\omega) \propto \frac{\alpha T \sqrt{K_{th}}}{C} \frac{1}{\omega}$$



Calculated intrinsic thermal and thermoelastic noise @ 10 Hz in a single silicon test mass, sensed with a laser beam of radius ~ 6 cm

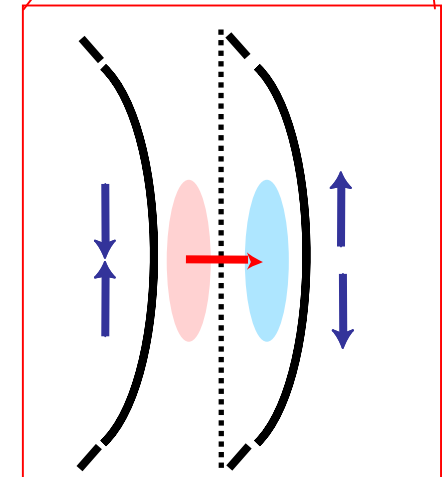
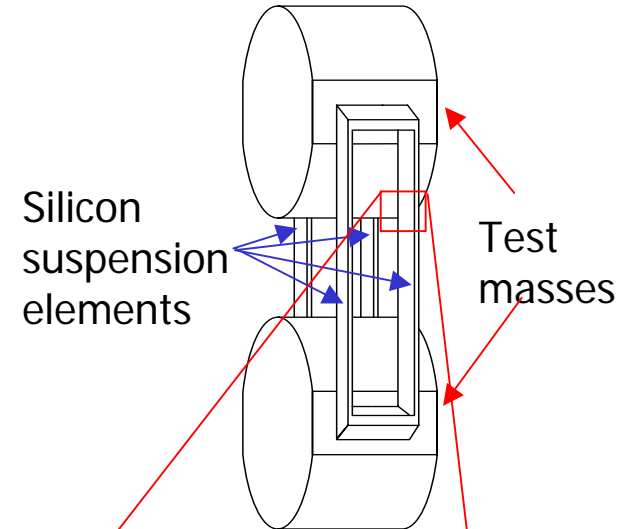
- From Touloukian, K_{th} of silicon can vary significantly, especially at low temperatures, depending on doping

Dissipation in silicon suspension elements

- Thermoelastic dissipation, $\phi_{th}(\omega)$, is associated with the flexing of **thin suspension elements** [see, eg: Nowick and Berry]

$$\phi_{th}(\omega) = \frac{E\alpha^2 T}{\rho C} \frac{\omega\tau}{1 + \omega^2\tau^2} \quad \tau = \frac{1}{2\rho f_{char}} \quad f_{char} = \frac{\pi K_{th}}{2\rho C t^2}$$

- These provide a convenient means to study:
 - thermoelastic dissipation and its dependence on material properties and temperature
 - other sources of dissipation associated with suspension elements - eg surface effects



Heat flow in a flexing ribbon

Silicon suspension elements

- Initial samples have been fabricated by:
 - machining from bulk pieces of silicon by a commercial vendor



- etching from silicon wafers by collaborators at Stanford University

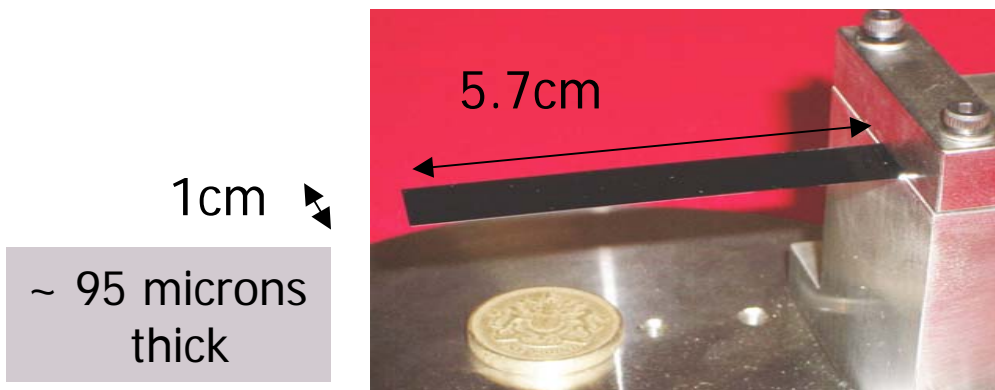


Sample

Rigid clamp

Experimental measurements

- Set of samples fabricated with varying properties and dimensions:
 - 1×10^{-3} Ohm-cm to >100 Ohm-cm
 - ~40 microns thick to ~100's microns thick
- Measurements in progress on first etched sample:



P-type doping (Boron),
Resistivity = 10-20 Ohm-cm

- Resonant modes of samples excited using an electrostatic drive
- Sample displacement monitored using shadow sensor
- Measure rate of decay of the mode amplitudes, from which mechanical dissipation, $\phi(\omega_0)$ can be determined. For any mode of amplitude A , and frequency ω_0 ,

$$A = A_0 e^{-\phi(\omega_0) \frac{\omega_0 t}{2}}$$

Experimental measurements

- Measured dissipation is the sum of dissipation arising from a number of sources:

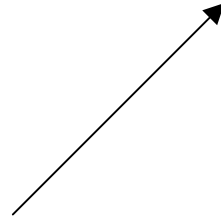
$$\phi_{meas}(\omega) = \phi_{thermoelastic}(\omega) + \phi_{bulk}(\omega) + \phi_{surface}(\omega) + \phi_{gas}(\omega) + \phi_{clamp}(\omega) + \phi_{other}(\omega)$$



calculate from silicon
material properties



measurements of
samples of varying
surface to volume
ratios should allow
estimates



measurements
in vacuum -
<10⁻⁵ Torr

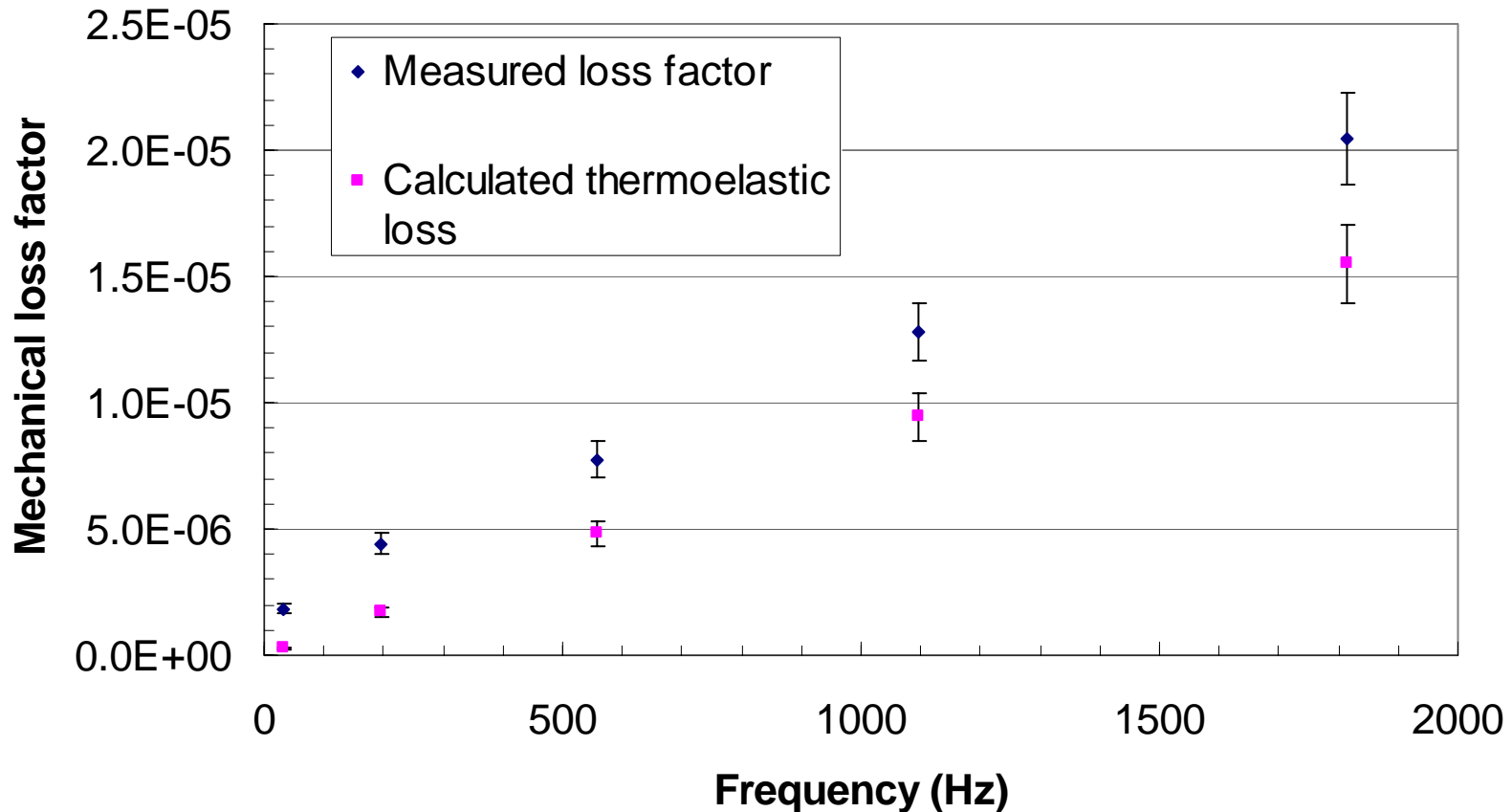


rigid clamp
holding thick
end of sample



Results

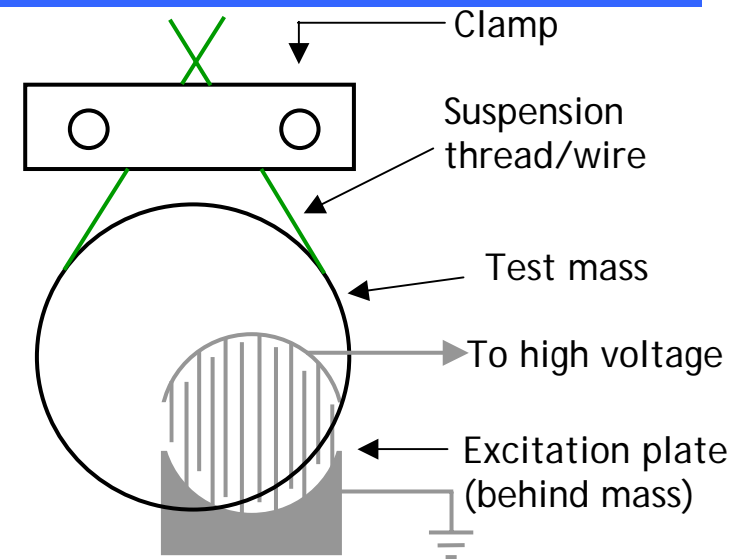
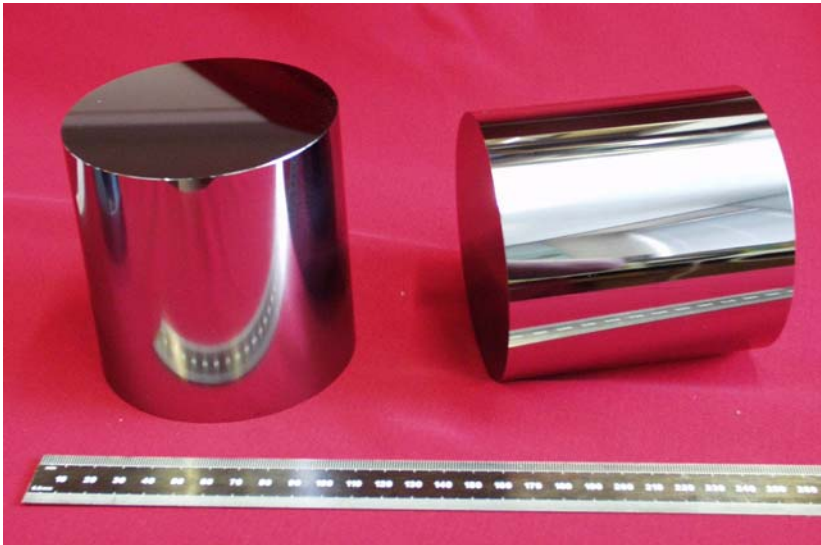
- Measured loss factor for first 5 resonant modes:



- Consistent with mostly thermo-elastic loss - 'excess' loss tbd
- Work ongoing - cryostat commissioned and cooled to 78K

Studies of silicon as a test mass substrate

- Preliminary room T measurements made of mechanical dissipation of bulk silicon samples suspended on silk thread or wire loops
 - Internal resonant modes of the samples excited; decay of mode amplitude measured

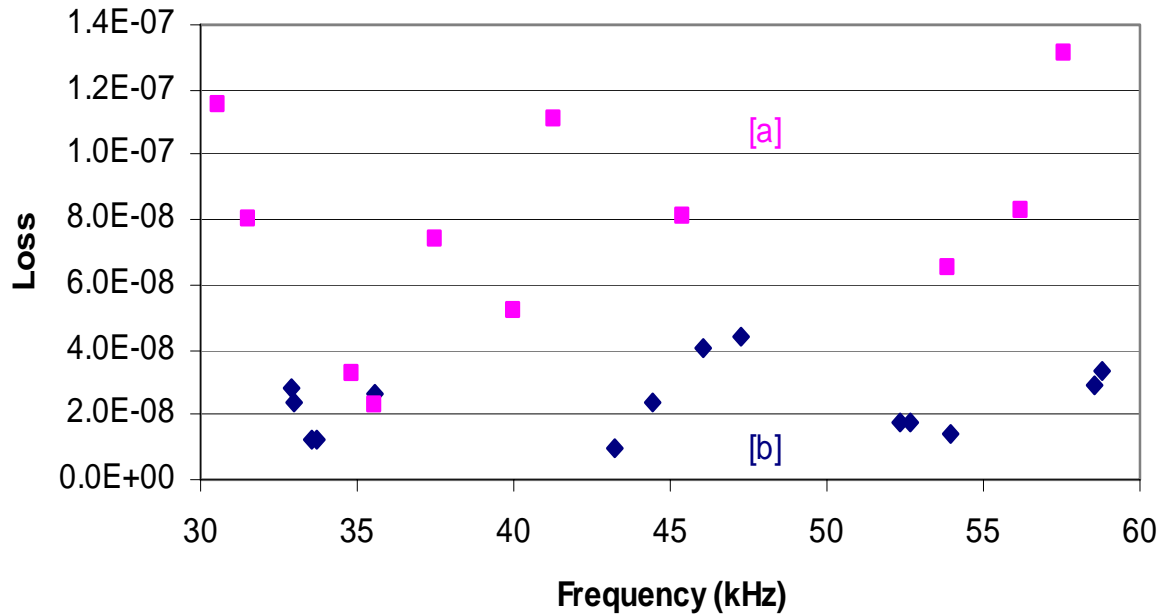


Schematic diagram of front view of suspended test mass.

- Dissipation of two silicon samples of identical geometry, supplied by Stanford, was measured over a range of frequencies.

Results for silicon at room temperature

Measured loss factors for two samples of bulk silicon



Sample [b] typically showed lower dissipation

Sample [a]:
[100] cut, nominally undoped

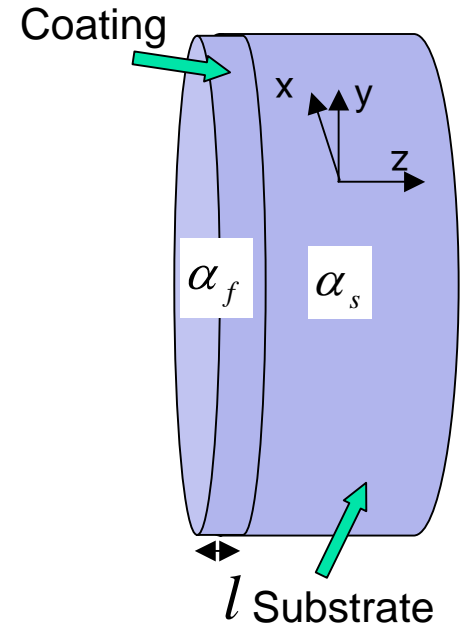
Sample [b]:
[111] cut, boron doped

Reason for difference seen in measured loss factors (eg crystalline orientation of the sample, the dopant, or some other reason) is as yet unknown - under investigation

- Lowest loss obtained so far = $(9.6 \pm 0.3) \times 10^{-9}$
- Comparable with the lowest loss factors measured at room temperature
 - Recall, varying dopant concentrations can vary the thermal conductivity of silicon.
 - This can impact both levels of thermoelastic dissipation and mirror figure distortion under thermal loads - requires further study.

Mechanical dissipation from coatings

- Research with LSC colleagues suggests that adding a typical ion-beam-sputtered (IBS) dielectric mirror coating to a fused silica test mass with a loss of 5×10^{-8} can increase the test mass thermal noise by 13 % or more.
- For future detectors it is vital to reduce, or mitigate the effects of, coating dissipation.
- Potential sources of loss (calculation and expt):
 - Dissipation intrinsic to the coating materials (defects, vacancies etc?)
 - Thermoelastic damping (see Fejer et al, gr-qc/0402034v1 Phys Rev D, resulting from the different thermal and elastic properties of the coating and the substrates



- In both cases resulting thermal noise level depends on relative thermal and elastic properties of coating and substrate
- It follows that the optimum coating for a fused silica or sapphire mass may not be the ideal choice for a silicon mass

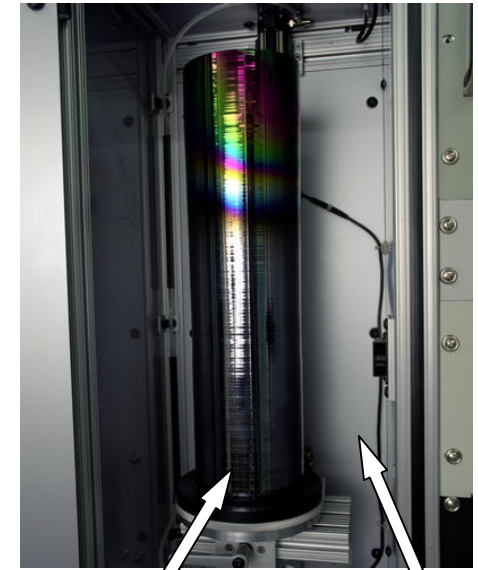
Mechanical dissipation in coatings (cont^d)

- Diffractive coatings:
 - If one wants to use silicon as a diffractive optic, either:
 - (a) a diffraction grating can be etched on to the surface of the test mass onto which a coating is applied
(Institute for Applied Optics, University of Jena);
or
 - (b) the test mass can be coated, and a diffraction grating etched into the coating surface
(Lawrence Livermore National Laboratories).
 - Developing collaborations with (a) through colleagues in Hannover, and with (b) through Stanford, to investigate the mechanical dissipation associated with such coatings (room and cryo)
 - Experiments in progress (see talk in configurations session by Alexander Bunkowski) and planned in Glasgow investigating use of diffractive topologies



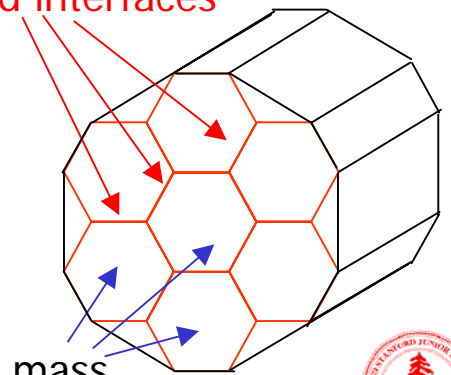
A problem of size

- For 3rd generation detectors, test masses of >50 kg are desirable, to minimise the effects of radiation pressure (see Warren's talk)
- Silicon ingots of 400 mm diameter and 450 kg mass have been manufactured, but are of an aspect ratio which is not optimal for use as a test mass.
- A solution to this could be to use **composite test masses**, where smaller pieces are joined together **without introducing significant excess mechanical dissipation**.
- A composite mass could look something like the schematic shown, the adjoining faces possibly joined by silicate bonding.
- New apparatus in Glasgow is currently being assembled to measure dissipation in larger masses (~40-50kg)



Silicon ingot in growth furnace

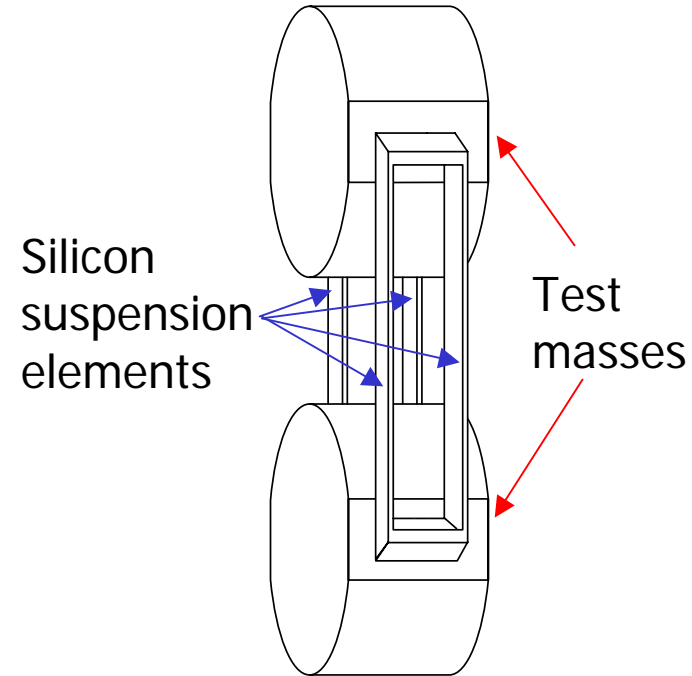
Bonded interfaces



Separate mass segments

Research goals

- Aim to investigate:
 - thermoelastic dissipation as a function of T
 - effect of surface treatment/ fabrication technique on dissipation in thin samples
 - optimal geometry for suspension elements
 - internal dissipation of doped/un-doped bulk silicon as a function of temperature
 - effectiveness of techniques for reducing coating dissipation
 - dissipation due to aspects of test mass design related to use as diffractive optics
 - construction of composite test masses of low dissipation
- Perform a **trade-off** between the use of silicon and other materials



- The overall goal of the programme is to develop low dissipation suspensions suitable for **GEO-HF** and **possible 3rd generation detectors**.