

Line tracking methods used in LineMon

LIGO-G030615-00-Z

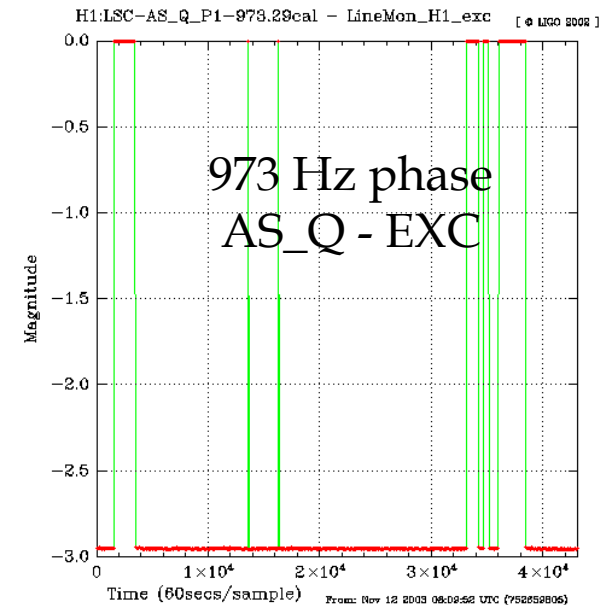
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- **heterodyning**
- **Hann heterodyning**
- **Fourier heterodyning**
- **fast Fourier heterodyning**
- **Wiener heterodyning**



- DMT tool for tracking line noise in LIGO interferometers
 - measures lines (and harmonics) amplitude, phase and frequency.
 - track calibration lines, pulsar injections, violin modes, power lines..
 - measures phase of AS_Q calibration lines with respect to calibration lines in excitation channel
- Output:
 - trend data (amplitude, phase, frequency, SNR)
 - html summary: monitored and detected
- Documentation:
 - LIGO-T010125-01-D
 - available from monitor spi page





- demodulation of data $s(t)$

$$P(t) = s(t) \cdot \sin(2\pi ft)$$

$$Q(t) = s(t) \cdot \cos(2\pi ft)$$

- Low-pass filtering: $\Delta f = 1/T$

$$x = \int_0^T P(t) dt$$

$$y = \int_0^T Q(t) dt$$

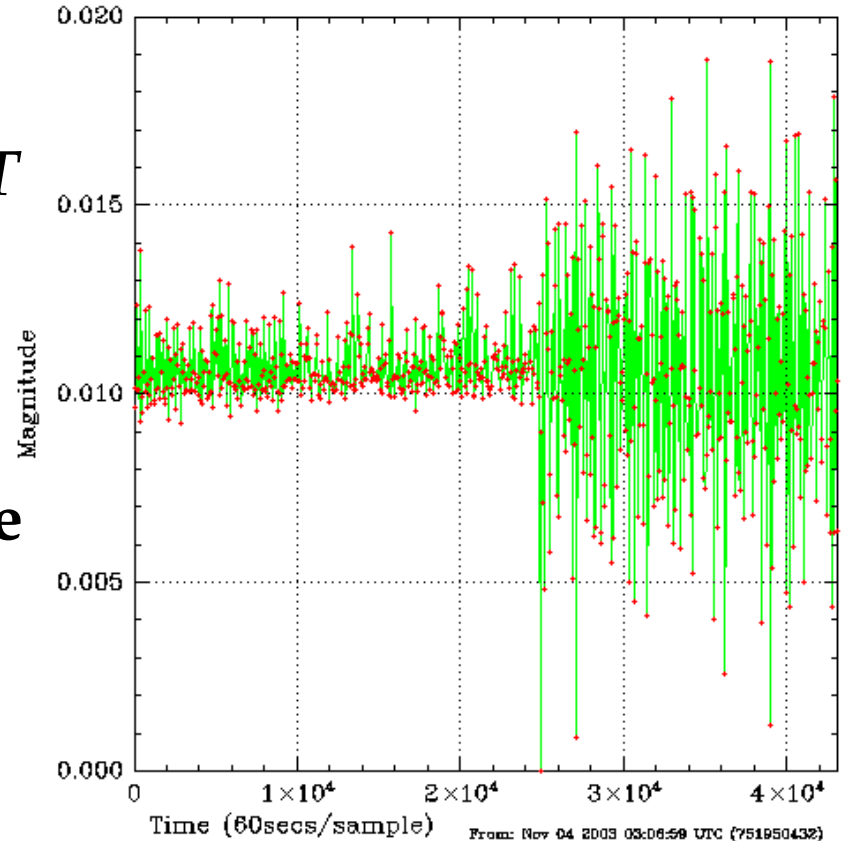
- Line amplitude and phase

$$A = 2\sqrt{x^2 + y^2}$$

$$\varphi = \arctan(x / y)$$

H1 151 Hz calibration line

H1:LSC-AS_Q_A1-151.30cal - LineMon_H1_exc [© LIGO 2003]





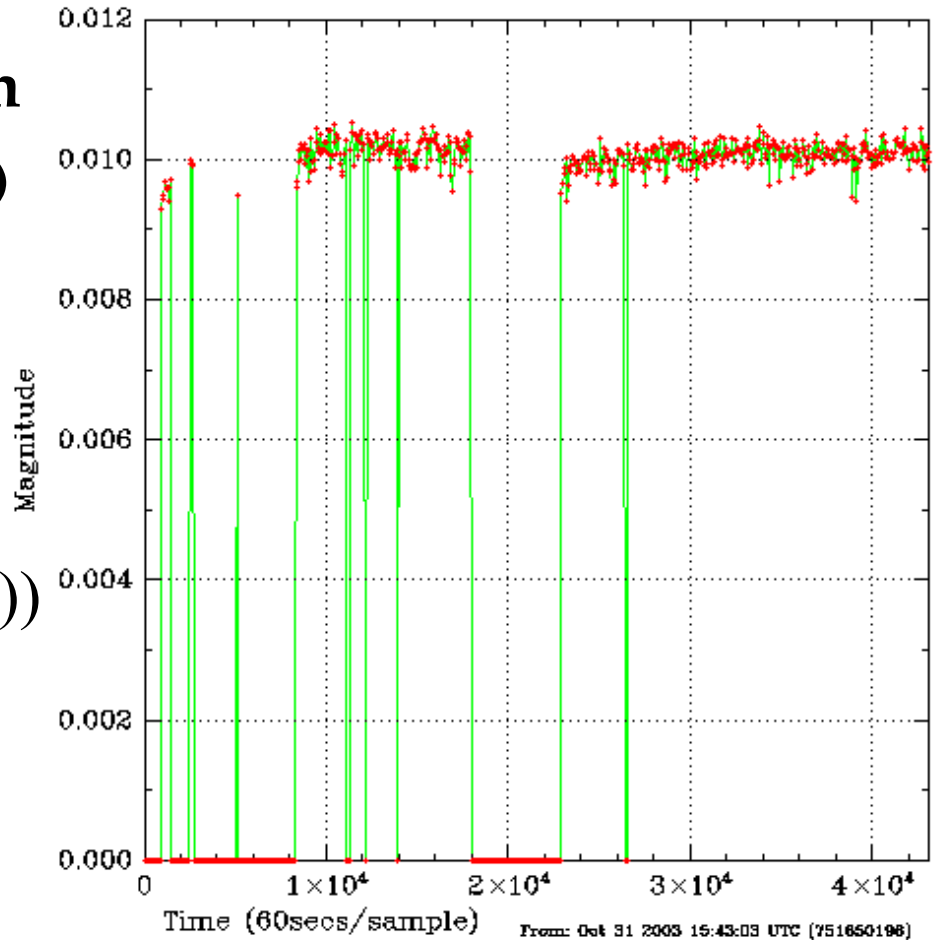
- Before demodulation
apply window to $s(t)$

Hann window

$$s'(t) = s(t) \cdot \left(1 - \cos\left(2\pi \frac{t}{T}\right)\right)$$

H1 151 Hz calibration line

H1:LSC-AS_Q_A1-151.30cal - LineMon_H1_db [© LIGO 2002]





- sampled signal:

$$s(t_i) = n(t_i) + a \sin(2\pi f t_i + \varphi)$$

- f - harmonic signal frequency
- f_s - sampling rate

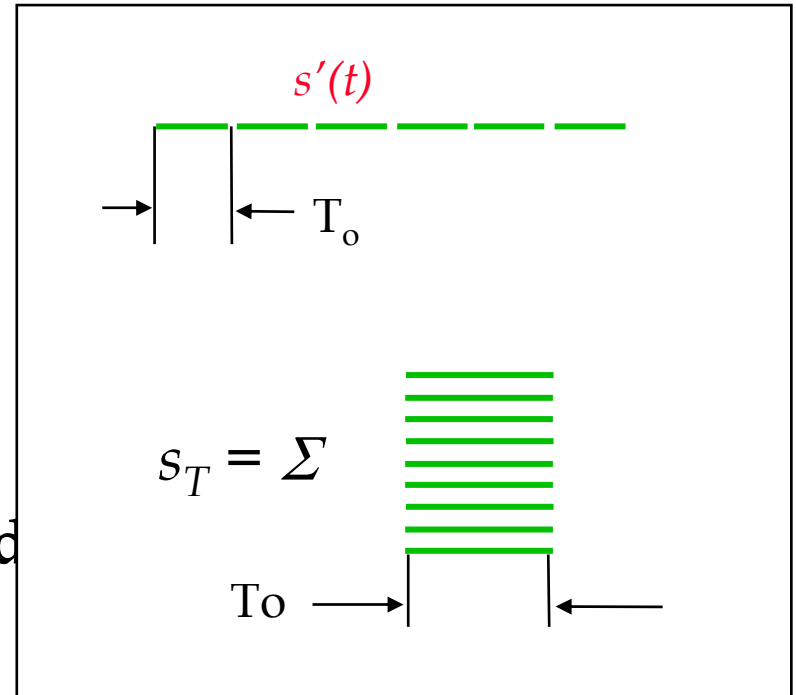
- resample $s(t)$ at frequency

$$f'_s = f \cdot (\text{int}(f_s / f) + 1)$$

- apply $fft \rightarrow x+iy = F_k$ - line Fourier amplitude corresponding to sum of P and Q line quadratures.
- anti-aliasing \rightarrow apply windowed fft
- Good for tracking line harmonics (e.g 60 Hz)



- need to know Fourier amplitude at line frequency
- T_o - k line periods
- $s_T(t)$ - average signal for one line period
- $fft(s_T)$ gives Fourier amplitude for line harmonics
- allows avoid fft of long data sets



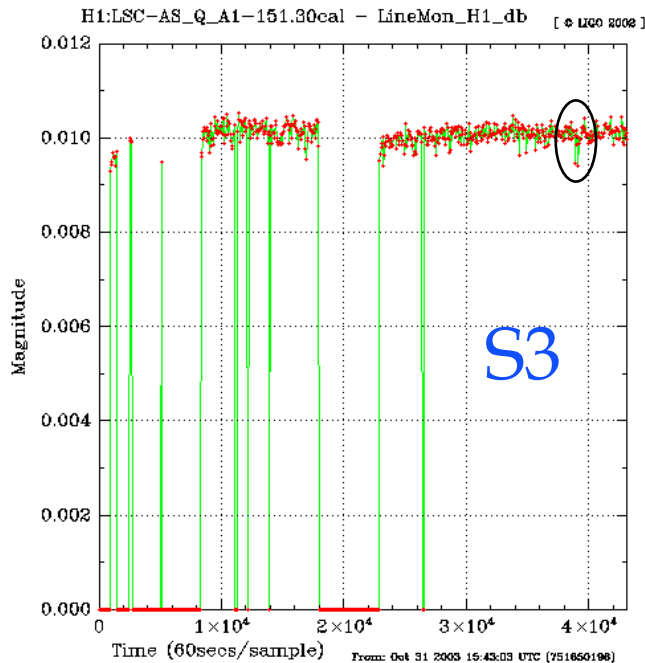


- apply Wiener filter to line Fourier amplitude

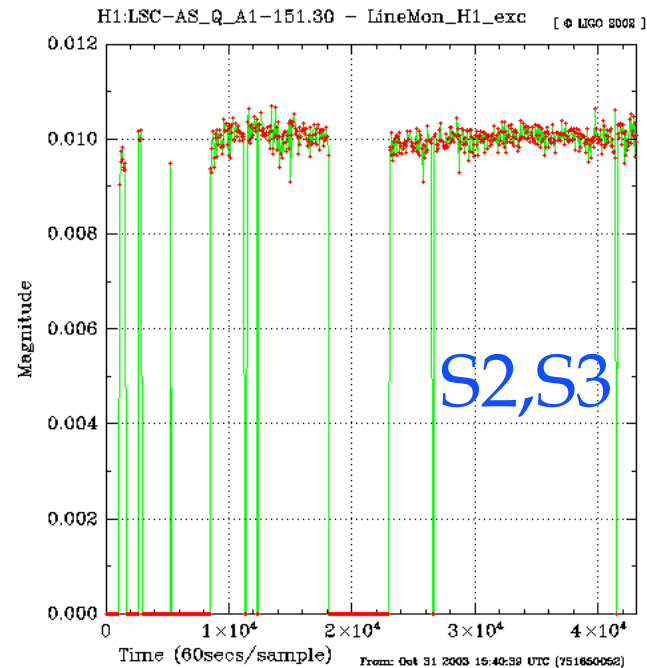
$$F'_k = F_k \cdot \frac{S_L}{S_L + S_N}$$

requires estimation of line (S_L) and noise (S_N) spectral densities

Hann heterodyning



Wiener heterodyning





- straight Heterodyning – implemented, not used
- Hann heterodyning – good for tracking of stable, single lines (pulsar and calibration lines in excitation channel, calibration lines in AS_Q, violin modes). Does not track frequency.
- Fourier heterodyning – not implemented
- fast Fourier heterodyning – can be used for tracking of lines with multiple harmonics and with varying frequency (power lines, violin modes,)
- Wiener heterodyning – tracking of lines with estimation of line SNR. Good for lines with varying amplitude, frequency and phase. Used for setting alarms based on crossing the SNR threshold.



- LineMonitor_exc:
 - AS_Q calibration lines (3x2) – monitored both with Hann and Wiener heterodyning.
 - ETMX-EXC_DAQ: 10 pulsar lines – Hann
 - DARM-EXC_DAQ: 3 calibration lines
- LineMonitor_gws: AS_Q
 - 24 violin modes
 - 10 power lines
- LineMonitor_ioo: IOO-MC_F
 - 7 power lines
- LineMonitor_lsc: MICH_CTRL
 - 7 power lines
- Total: 54 lines per IFO + line statistics in 0-2kHz band
 - speed is a concern
- obsidian: 8 LineMon jobs at 55% CPU load



- Already plenty of methods are implemented
- New, more accurate methods are welcome
- Calibration lines are monitored with two different methods
 - Can easily produce two more $\{\alpha, \beta\}$ samples on-line