

# Silicon as a low thermal noise test mass material

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# Research for advanced interferometer suspensions

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- Q measurements in progress of silicon samples
- 2 samples:
  - Dimensions 4 inch diameter x 4 inch long
- Sample (a) un-doped (100) material
- Sample (b) boron doped (111) material
- Measure Q factor of both samples at room temperature
- Results so far : Q of order few x  $10^7$
  
- Most likely suspension limited - work continuing
- Very promising LIGO III material - particularly re: thermo-elastic damping



# Proposed work - materials for test masses/suspensions

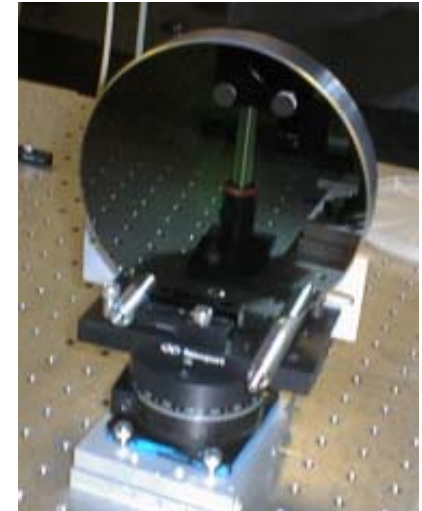
## • Future improvements

- **Thermal noise** from test masses and suspensions important below few 100 Hz
- **Silicon** has various desirable material properties (optical and thermal noise)

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- High thermal conductivity,  $\kappa$
- Available in large pieces (~100kg)
- Can be polished and coated to form high quality dielectric mirrors
- Measurements suggest intrinsic mechanical loss (and **thermo-elastic loss\***) comparable to sapphire at room temperature
- Can be silicate bonded to silica (and by extension to itself)

Coated silicon mirror



- At room temperature, thermo-elastically driven displacement noise forms hard limit to detector sensitivity
- By cooling test masses, expect significant gains in thermal/thermo-elastic noise performance



# Power spectral density of noise due to thermo-elastic damping in a bulk substrate

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$$x^2(\omega) = \frac{8}{\sqrt{2\pi}} \alpha^2 (1 + \sigma)^2 \frac{k_b T^2}{\rho C} \frac{a^2}{r_0^3} \frac{1}{\omega^2}$$

Braginsky et al, Phys. Lett. A

where:

$\alpha$  = coefficient of thermal expansion

$\sigma$  = Poissons ratio

$\rho$  = density

$C$  = specific heat capacity

$a^2 = K_{th}/\rho C$  :  $K_{th}$  = thermal conductivity

$r_0$  = beam radius at which intensity drops to 1/e

$\omega$  = angular frequency

 material  
parameters



# Reduction of “thermo-elastic” noise by cooling

From Braginsky et al

$$x^2(\omega) = \frac{8}{\sqrt{2\pi}} \alpha^2 (1 + \sigma)^2 \frac{k_b T^2}{\rho C} \frac{a^2}{r_0^3} \frac{1}{\omega^2}$$

(1) Need values for  $\alpha(T)$ ,  $C(T)$ ,  $K_{th}(T)$

(2) Formula is valid for  $\omega \gg a^2/r_0^2 \sim 1/\tau$

$$\begin{aligned} x^2(\omega) &= \text{Constant} \frac{\alpha^2 T^2}{C} \frac{1}{r_0} \frac{a^2}{r_0^2} \frac{1}{\omega^2} \\ &= \text{Constant} \frac{\alpha^2 T^2}{C} \frac{1}{r_0} \frac{1}{\omega \tau} \frac{1}{\omega} \end{aligned}$$

Following classical thermo-elastic damping - more generally

replace  $\frac{1}{\omega \tau}$  by  $\frac{\omega \tau}{1 + \omega^2 \tau^2}$

➔ Evaluate  $x^2(\omega)$  as a function of temperature

LIGO-G020163-00-Z



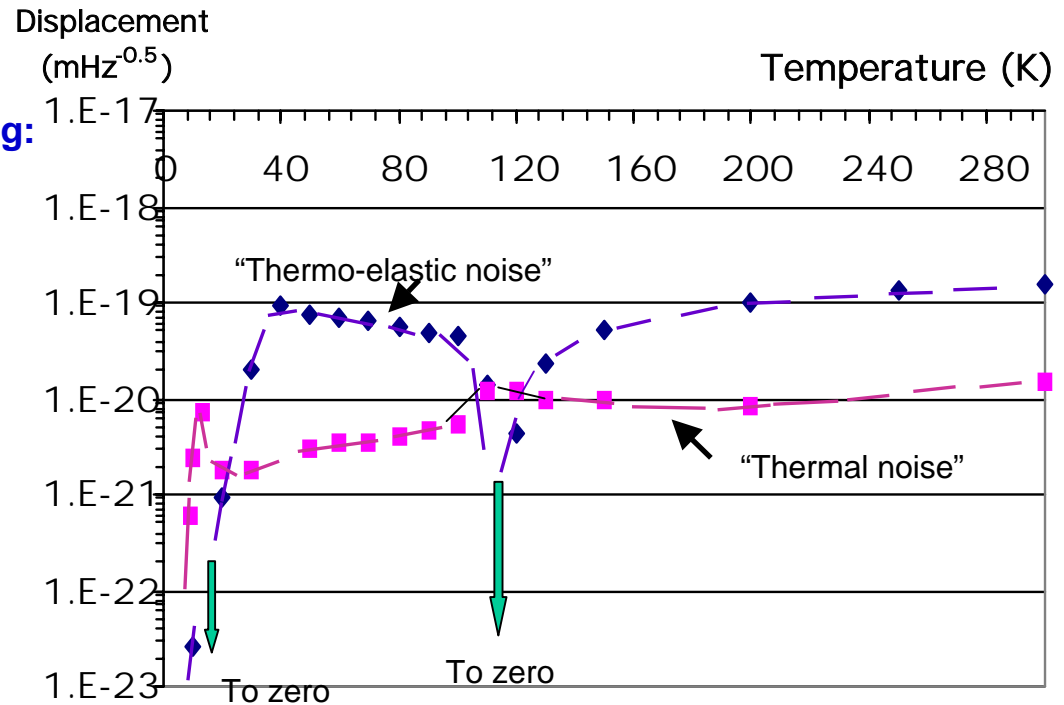
# Proposed work - materials for test masses/suspensions (3)

- Silicon: unique material properties on **cooling**:
  - Intrinsic mechanical loss decreases
  - Two zero's in coefficient thermal expansion,  $\alpha$ , at  $\sim 130\text{K}$  and  $\sim 20\text{K}$

Dual benefits:

- thermal deformation proportional to  $\alpha/\kappa$
- thermo-elastic noise proportional to  $\alpha$

- **both should vanish as  $\alpha$  tends to zero**



“Thermo-elastic” displacement noise and “thermal” noise in a silicon test mass as a function of temperature

- **silicon substrates opens avenues for significant thermal noise improvements at low temperatures** but material properties need further study



# Proposed work - materials for test masses/suspensions

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- Need to investigate, in collaboration with LSC colleagues :
  - **Effects of coatings** on mechanical loss of silicon substrates (room T and cryogenic )
  - **Silicate bonding** to joint silicon suspension elements to the silicon test masses
  - Measurement of **loss factors** associated with the all-silicon silicate bonding
  - Use of **GEO600 detector** for demonstration of silicon technology

