

LASER INTERFEROMETER GRAVITATIONAL WAVE OBSERVATORY  
- LIGO -  
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## Calculating the Trend Data

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## 1 SUMMARY

LIGO trend frames are calculated at one-second and one-minute intervals. The one-second trend is stored in one minute long frame files, whereas the one-minute trend is stored in one hour long frame files. Trend channels are denoted by their corresponding channel name extended by a suffix describing the statistical quantity they represent. For each recorded channel the trend data consists of the number of points (“*n*”), the mean value (“*.mean*”), the root-mean-square value (“*.rms*”), the minimum value (“*.min*”) and the maximum value (“*.max*”). Additionally, the standard deviation (“*.stddev*”) can be calculated from the above values as needed.

## 2 ONE-SECOND TREND

Only valid data points are included into calculating the one-second trend. If no valid data points exist within the one second boundary, the one-second trend is invalid for this interval.

### 2.1 CONVENTIONS

The following conventions were chosen (quantities marked by an ‘*x*’ are stored in the frame file, quantities marked by ‘+’ are calculated on-the-fly):

Number of points	$N_s$	x
Data index	$i = 1, 2, 3, \dots N_s$	
Data points	$x_i$	
Mean	$\bar{x}_s$	x
Maximum	$x_s^{\max}$	x
Minimum	$x_s^{\min}$	x
RMS	$x_s^{\text{rms}}$	x
Standard deviation	$\sigma_s$	+

The number of data points within one second interval is equal to the sample rate of the corresponding channel.

## 2.2 FORMULAE

The one-minute trend is calculated as follows:

$$\bar{x}_s = \frac{1}{N_s} \sum_{i=1}^{N_s} x_i$$

$$x_s^{\max} = \max_i \{x_i\}$$

$$x_s^{\min} = \min_i \{x_i\}$$

$$x_s^{\text{rms}} = \sqrt{\frac{1}{N_s} \sum_{i=1}^{N_s} x_i^2}$$

$$\sigma_s = \sqrt{\frac{N_s}{N_s - 1} \left\{ (x_s^{\text{rms}})^2 - (\bar{x}_s)^2 \right\}}$$

## 3 ONE-MINUTE TREND

Only valid one-second trend points are included into calculating the one-minute trend. If no valid one-second trend points exist within the one minute boundary, the one-minute trend is invalid for this interval.

### 3.1 CONVENTIONS

The following conventions were chosen (quantities marked by an ‘x’ are stored in the frame file, quantities marked by ‘+’ are calculated on-the-fly):

Number of points	$N_m$	x
Number of one-second points	$n_m$	
Data index	$i = 1, 2, 3, \dots, n_m$	
One-second data points	$(x_s)_i$	
Mean	$\bar{x}_m$	x
Maximum	$x_m^{\max}$	x

Minimum	$x_m^{\min}$	x
RMS	$x_m^{\text{rms}}$	x
Standard deviation	$\sigma_m$	+

## 3.2 FORMULAE

The one-minute trend is calculated as follows:

$$N_m = \sum_{i=1}^{n_m} (N_s)_i$$

$$\bar{x}_m = \frac{1}{N_m} \sum_{i=1}^{n_m} (N_s)_i (\bar{x}_s)_i$$

$$x_m^{\max} = \max_i \{(x_s)_i\}$$

$$x_m^{\min} = \min_i \{(x_s)_i\}$$

$$x_m^{\text{rms}} = \sqrt{\frac{1}{N_m} \sum_{i=1}^{n_m} (N_s)_i (x_s^{\text{rms}})_i^2}$$

$$\sigma_m = \sqrt{\frac{N_m}{N_m - 1} \left\{ (x_m^{\text{rms}})^2 - (\bar{x}_m)^2 \right\}}$$

Since the minute trend is calculated from the one-second trend, it avoids floating point round-off errors when adding a large number of terms.

## 4 TREND OVER OTHER INTERVALS

A trend which averages over multiple one-second or one-minute points can be calculated ‘on-demand’ using the one-second or the one-minute trend, respectively. For example, a ten-minute trend would average over 10 one-minute trend data points.

## 4.1 CONVENTIONS

The following conventions were chosen (quantities marked by an ‘x’ are stored in the frame file, quantities marked by ‘+’ are calculated on-the-fly):

index denoting new binning	$h$	
Number of points	$N_h$	+
Number of one-minute points/ Number of one-second points	$n_h$	
Data index	$i = 1, 2, 3, \dots, n_h$	
One-minute data points	$(x_h)_i$	
Mean	$\bar{x}_h$	+
Maximum	$x_h^{\max}$	+
Minimum	$x_h^{\min}$	+
RMS	$x_h^{\text{rms}}$	+
Standard deviation	$\sigma_h$	+

## 4.2 FORMULAE

The arbitrary binned trend is calculated as follows:

$$N_h = \sum_{i=1}^{n_h} (N_m)_i$$

$$\bar{x}_h = \frac{1}{N_h} \sum_{i=1}^{n_h} (N_m)_i (\bar{x}_m)_i$$

$$x_h^{\max} = \max_i \{(x_m)_i\}$$

$$x_h^{\min} = \min_i \{(x_m)_i\}$$

$$x_h^{\text{rms}} = \sqrt{\frac{1}{N_h} \sum_{i=1}^{n_h} (N_m)_i (x_m^{\text{rms}})_i^2}$$
$$\sigma_h = \sqrt{\frac{N_h}{N_h - 1} \left\{ (x_h^{\text{rms}})^2 - (\bar{x}_h)^2 \right\}}$$