Study of Tim Hayler's simple model of the beam splitter

Justin Greenhalgh, 3 Dec 2006

This model was built to allow exploration of the effect on natural frequency of various beamsplitter model layouts.

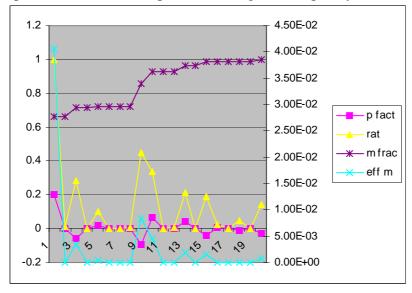
1. Modal mass

I wanted to see if the concept of modal mass could help us to be more quantitative about which modes really matter in terms of controls issues with the seismic platform. The idea is that a mode with very little associated mass does not have a big effect on the controls. This idea was behind the concept of so-called "stay modes", which were thought of as modes involving only the (lightweight) stays. When the "stay modes" were first mooted, the frequencies of the stays fro models being considered at the time were much lower than those of the whole structure, so they were easy to identify. This is not longer the case for structures and stays under consideration.

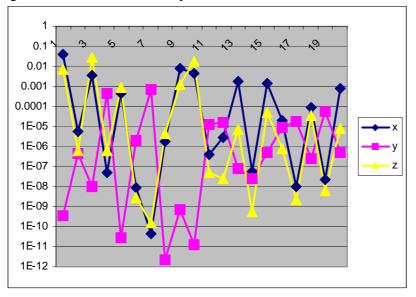
I could not find a way to get ANSYS to tell me "modal mass" per se (as referenced in, eg ANSYS theory chapter 15 eqn 15.97). However, Tim had already arranged for a printout of the modal participation factors like this in the output during solve:

	***** PARTIC	IPATION FACTOR	CALCULATION *****	X DIRECTI	ON	~~~~~
MODE FRACTION	FREQUENCY	PERIOD	PARTIC.FACTOR	RATIO	EFFECTIVE MASS	CUMULATIVE MASS
1	107.339	0.93163E-02	0.20154	1.000000	0.406198E-01	0.659982
2	109.921	0.90974E-02	0.23706E-02	0.011762	0.561957E-05	0.660073
3	117.266	0.85276E-02	-0.57895E-01	0.287260	0.335189E-02	0.714534
4	117.373	0.85199E-02	0.22969E-03	0.001140	0.527592E-07	0.714535
5	120.448	0.83023E-02	0.20979E-01	0.104094	0.440136E-03	0.721686
(etc)						

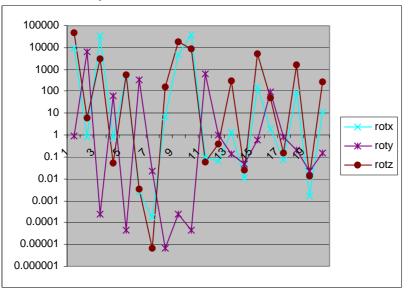
I plotted the various output columns against frequency for the x direction, thus:



And concluded that any of the values "partic. Factor", "ratio", or "effective mass" would show up the important modes. I went for "effective mass" and plotted that against mode number for x,y and z:

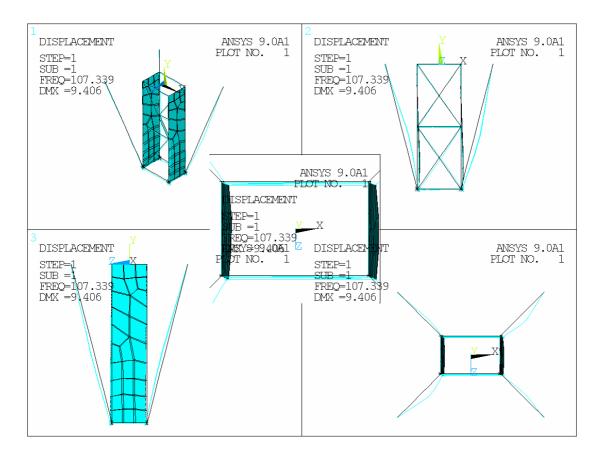


and for rotx, roty, rotz:

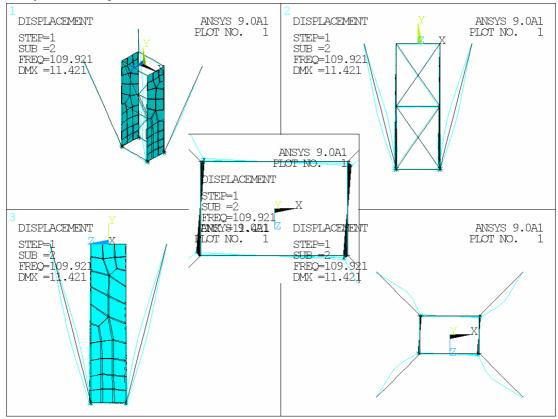


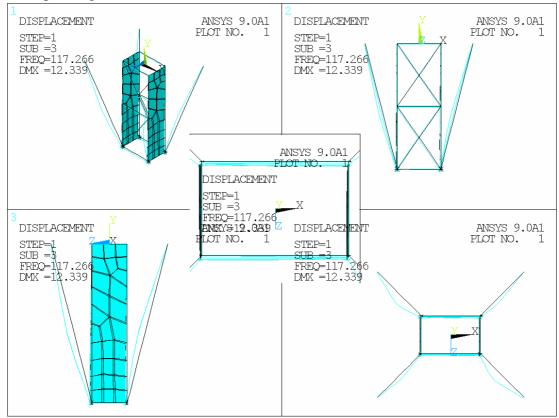
A quick look at the mode shapes for the first few modes suggested that at least the values of the effective mass tie up with the mode shapes. Compare the mode shapes (below) with the charts of effective mass (above). Taking the first three modes:

Mode 1 involves movement at the bottom of the structure mostly in X and a little in Z; this involves rotation about the Z axis (principally) and the X axis (a little):



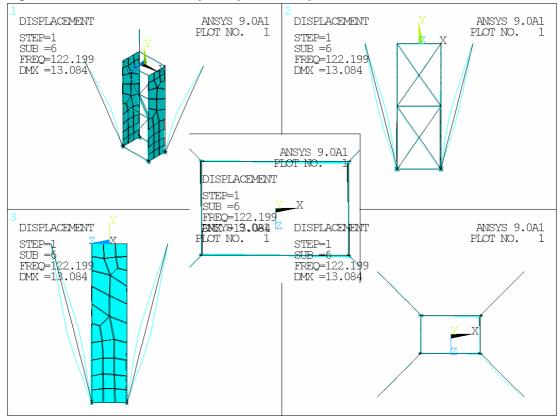
Mode 2 is a twist of the bottom of the structure (ROTY) with little other movement except in the stays:

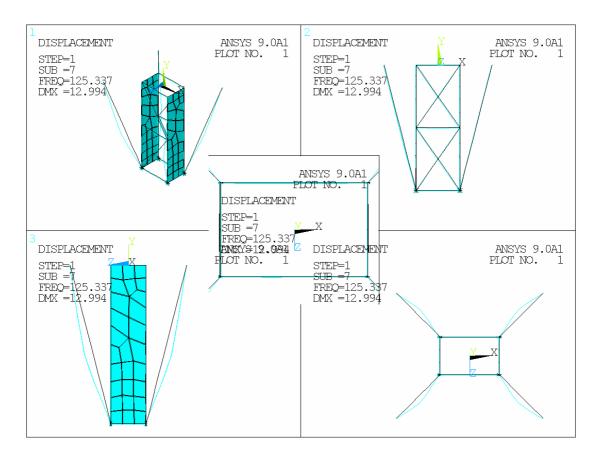




Mode 3 involves movement at the base mostly in Z and a little in X, with the corresponding rotations:

Modes 6 and 7 (from the charts above) have very little effective mass and one might expect to see movement of stays only. Here they are:



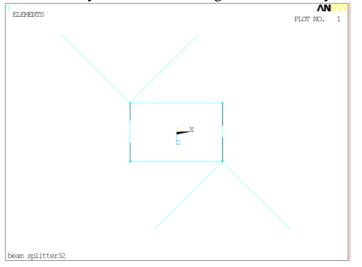


All of which suggests that a study of the effective mass can give a quantitative indication of the "importance" of particular modes – especially if note were taken of the sensitivities of the SEI control system to the various modes. In this case the very first mode has the highest effective mass and so it is unlikely we can ignore it.

2. Configuration of stays – using "folded stays" on the full model

Model 1:

This work follows up an interesting discovery of Ian Wilmut. One would have thought (at least – I would have thought) that a structure with tetrahedral features would be very stiff. So this arrangement of the stays should work well:

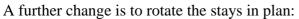


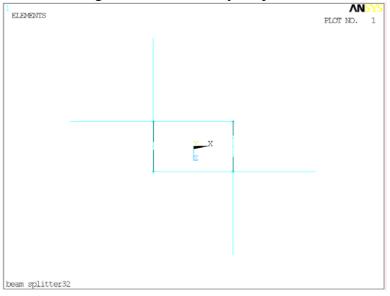
SET	0	ld	New (1)	change %
	1	107.339	. ,	-
	2	109.921	108.6	7 -1%
	3	117.266	109.7	4 -6%
	4	117.373	117.	7 0%
	5	120.448	128.8	8 7%
	6	122.199	129.4	9 6%
	7	125.337	130.5	3 4%
	8	125.916	130.5	7 4%
	9	140.374	133.7	6 -5%
	10	153.983	140.8	9 -9%
	11	164.51	169.0	6 3%
	12	181.426	181.3	9 0%
	13	181.995	181.4	4 0%
	14	183.684	182.9	2 0%
	15	205.189	192.7	1 -6%
	16	207.558	201.8	1 -3%
	17	215.054	215.0	9 0%
	18	219.369	218.4	6 0%
	19	246.881	246.8	2 0%
	20	249.096	249.0	7 0%

The frequencies are

So by and large the ones that don't matter have improved, and the important ones have got worse – but not by a large margin.

Model 2:



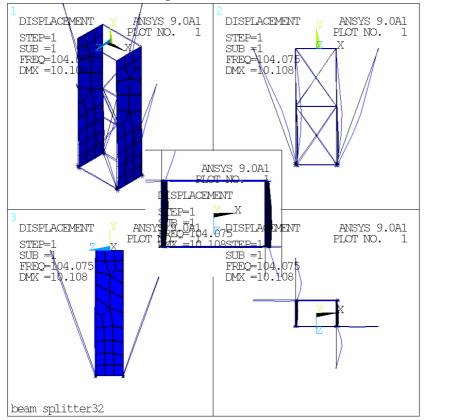


Very little change:

0	ld I	New (1) c	hange % ne	ew(2)
1	107.339	103.78	-3%	104.07
2	109.921	108.67	-1%	108.91
3	117.266	109.74	-6%	110.18
4	117.373	117.7	0%	116.95
	1 2 3	old 1 1 107.339 2 109.921 3 117.266 4 117.373	1107.339103.782109.921108.673117.266109.74	1107.339103.78-3%2109.921108.67-1%3117.266109.74-6%

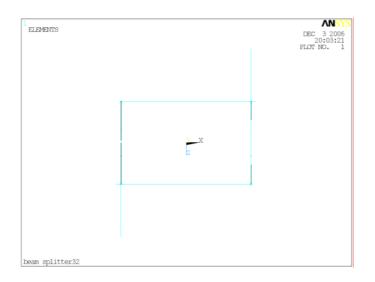
5	120.448	128.88	7%	129.03
6	122.199	129.49	6%	129.52
7	125.337	130.53	4%	130.51
8	125.916	130.57	4%	130.58
9	140.374	133.76	-5%	135.25
10	153.983	140.89	-9%	140.32
11	164.51	169.06	3%	171.18
12	181.426	181.39	0%	181.42
13	181.995	181.44	0%	181.48
14	183.684	182.92	0%	182.87
15	205.189	192.71	-6%	191.84
16	207.558	201.81	-3%	202.4
17	215.054	215.09	0%	215.11
18	219.369	218.46	0%	218.67
19	246.881	246.82	0%	246.85
20	249.096	249.07	0%	249.12

Here's the first mode shape:



Model 3 the "folded stays":

But - and here's the interesting one. Why not move the stays around to use up less footprint (Ian's cunning plan) thus:



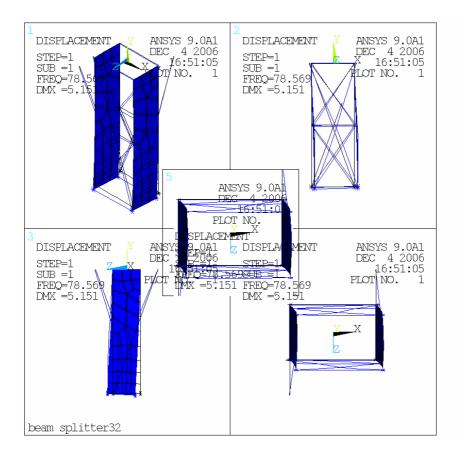
Surely the tripods will be equally effective?

Well, actually, no they aren't:

SET

 0	ld Ne	ew (1) cha	nge % ne	w(2) ne	ew(3)
1	107.339	103.78	-3%	104.07	78.569
2	109.921	108.67	-1%	108.91	106.79
3	117.266	109.74	-6%	110.18	110.86
4	117.373	117.7	0%	116.95	116.78
5	120.448	128.88	7%	129.03	126.19
6	122.199	129.49	6%	129.52	128.85
7	125.337	130.53	4%	130.51	129.56
8	125.916	130.57	4%	130.58	130.59
9	140.374	133.76	-5%	135.25	130.6
10	153.983	140.89	-9%	140.32	137.61
11	164.51	169.06	3%	171.18	157.09
12	181.426	181.39	0%	181.42	179.22
13	181.995	181.44	0%	181.48	181.05
14	183.684	182.92	0%	182.87	181.43
15	205.189	192.71	-6%	191.84	185.43
16	207.558	201.81	-3%	202.4	199.73
17	215.054	215.09	0%	215.11	215.1
18	219.369	218.46	0%	218.67	218.02
19	246.881	246.82	0%	246.85	246.86
20	249.096	249.07	0%	249.12	249

Interestingly, the only big change is in the first mode. Compare its mode shape with that for mode 1 of model 2, above.



There is now significant motion of the structure, in the direction of the short overall footprint (as Ian feared). I don't see why.

What of the effective mass?

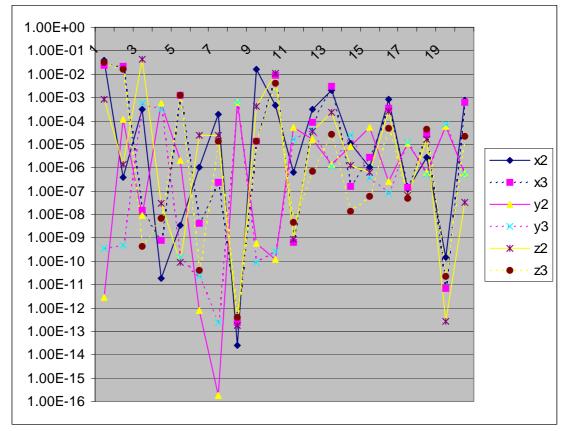
Here are the effective masses for the two models. Model 2 has the protruding stays, model 3 has them folded:

х	:2 x	:З у	′2 y	'3 z	:2 z	:3
1	4.05E-02	2.33E-02	2.87E-12	3.65E-10	8.55E-04	3.06E-02
2	3.70E-07	2.24E-02	1.20E-04	4.51E-10	1.42E-06	1.60E-02
3	3.19E-04	1.42E-08	8.68E-09	5.39E-04	4.22E-02	4.29E-10
4	1.77E-11	7.73E-10	5.76E-04	3.22E-04	2.92E-08	6.74E-09
5	3.50E-09	1.25E-03	2.06E-06	1.46E-10	9.22E-11	1.28E-03
6	1.03E-06	3.96E-09	8.13E-13	2.33E-11	2.44E-05	3.95E-11
7	1.86E-04	2.28E-07	1.89E-16	2.28E-13	2.38E-05	1.32E-05
8	2.58E-14	2.43E-13	6.24E-04	6.27E-04	1.80E-13	3.88E-13
9	1.52E-02	1.31E-05	5.54E-10	8.92E-11	4.03E-04	1.33E-05
10	4.78E-04	8.92E-03	1.23E-10	2.66E-10	1.05E-02	3.92E-03
11	6.42E-07	6.14E-10	5.20E-05	1.66E-05	8.16E-10	4.56E-09
12	3.11E-04	8.84E-05	1.56E-05	4.01E-05	3.40E-05	7.00E-07
13	2.04E-03	2.92E-03	1.41E-06	1.11E-06	2.24E-04	2.58E-05
14	1.12E-05	1.59E-07	7.75E-06	2.32E-05	1.31E-06	1.31E-08
15	1.06E-06	2.77E-06	5.48E-05	4.01E-07	6.00E-07	5.64E-08
16	8.60E-04	3.41E-04	2.67E-07	7.55E-08	2.48E-04	4.75E-05
17	1.17E-07	1.48E-07	1.13E-05	1.16E-05	6.47E-08	4.97E-08
18	2.75E-06	2.73E-05	6.01E-07	5.22E-07	1.57E-05	4.30E-05
19	1.52E-10	6.69E-12	5.65E-05	6.90E-05	2.70E-13	2.29E-11

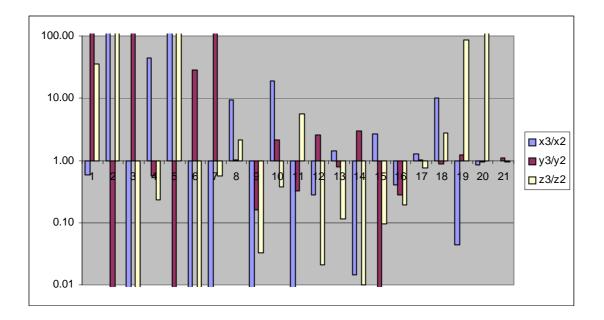
20 7.41E-04 6.19E-04 5.54E-07 5.33E-07 3.32E-08 2.26E-05 6.07E-02 5.99E-02 1.52E-03 1.65E-03 5.46E-02 5.20E-02 So the effective mass in x of the first mode has indeed gone down, but not very dramatically (factor of ~2) and the effective mass in z has gone up.

But – and this is interesting – although the frequencies of the modes above the first seem to match pretty well between models 2 and 3, the effective masses don't.

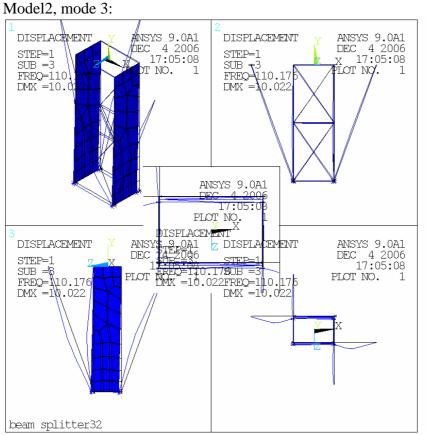
This plot tries to show it, but it's rather hard to follow (and factors of ~two look very small on here):



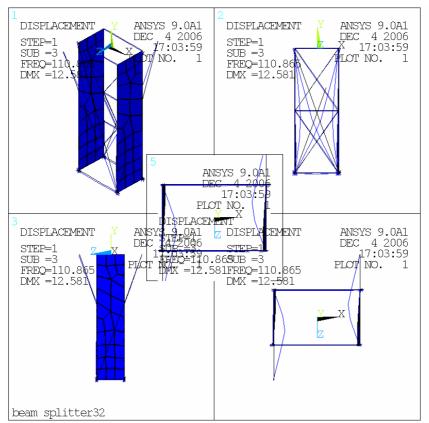
Try showing just the ratios:



Mostly they are very large (or small) ratios. So are the mode shapes the same? Let's take mode 3. frequencies very similar, here are the modes shapes:

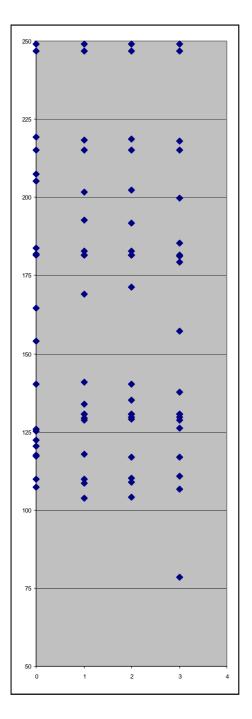


Model3, mode 3:



So, although the frequencies are the same, the mode shapes are rather different. This suggests that the similarities in frequencies is a coincidence between two sorted lists.

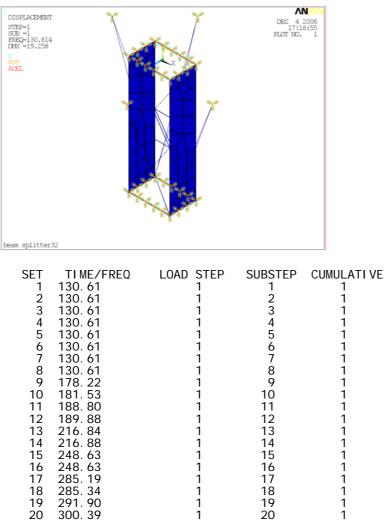
Here is a plot of all the frequencies:



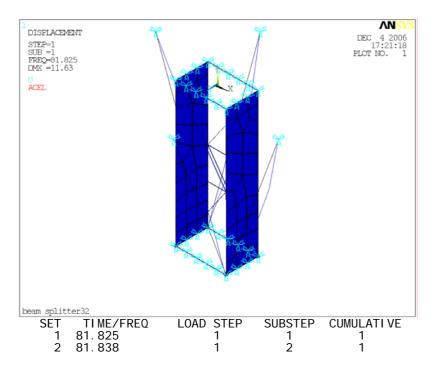
You can see that the frequencies look rather better related between models 1 and 2 than between models 2 and 3. One could try matching mode shapes using the effective mass triples (x, y, z). I have not figured out an elegant way to do this (and doing by eye in the table above does not look easy). The fact remains that model 3 has this very low mode that is not present in model 2.

3. Modes of the stays:

It's probably worth finding out what the modes of the stays themselves are. So run model 2 (any model should do) with the bottom ring nodes fixed:



From which we can conclude that the frequency of a fixed-fixed stay is 130 Hz. Try pinning all constraints, which will leave the stays pinned at the top and somewhat more than pinned (by reason of their connection to the structure) at the bottom:



3 4	83.567 83.574	1	3 4	
5	88.192	1	5	
6	88.192	1	6	
7	88.519	1	7	
8	88.519	1	8	
9	176.01	1	9	
10	179.66	1	10	
11	185.82	1	11	
12	186. 57	1	12	
13	215. 18	1	13	
14	215.26	1	14	
15	247.28	1	15	
16	247.43	1	16	
17	278.20	1	17	
18	280. 79	1	18	
19	284.47	1	19	
20	284.65	1	20	

More like 82 Hz. And with the stays fixed at the top and pinned at the bottom, you get 120 to 130 Hz.

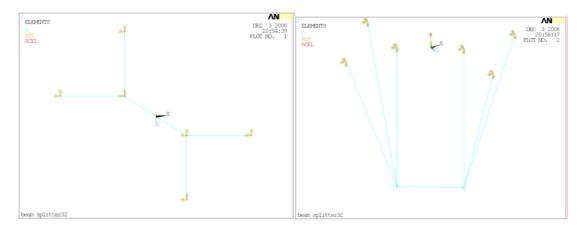
1111111111111

4. Configuration of stays – using "folded stays" on a cut-down model

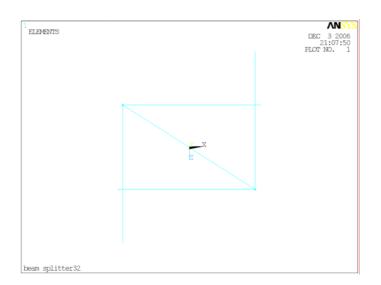
Model 4:

I am still puzzled as to why the folded stays did not work.

Next thing would be to try just the two tripods with a link between them.



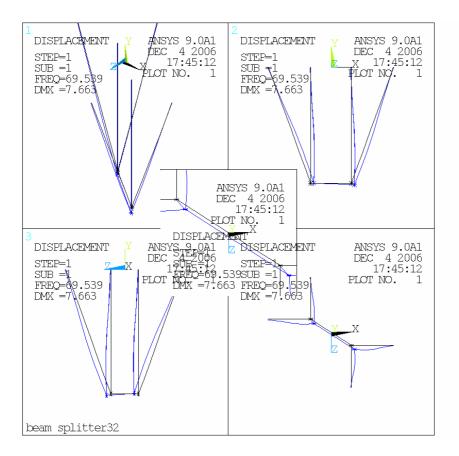
Model 5: And then to try folding the stays as before:

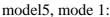


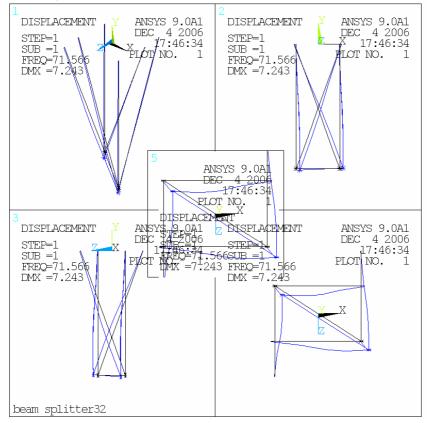
In terms of frequencies, there is very little to choose between the two. This is what I would have expected.

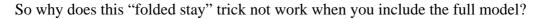
SET	m	odel 4 m	odel 5
	1	69.539	71.566
	2	84.843	84.871
	3	87.43	89.257
	4	99.199	99.177
	5	125.9	125.68
	6	127.98	128.33
	7	131.53	131.44
	8	131.57	131.57
	9	136.37	132.81
	10	136.8	136.79
	11	137.91	137.09
	12	138.38	138.39
	13	144.29	140.07
	14	156.84	156.86
	15	171.24	168.72
	16	338.1	336.78
	17	348.87	349.53
	18	369.73	368.72
	19	380.34	383.43
	20	391.36	388.01

The mode shapes of the lowest frequency look similar: Model4, mode 1:



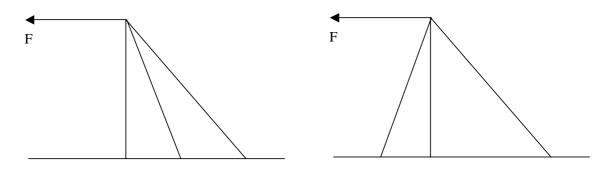






5. Simple test of the folded stay principle

Ian Wilmut suggested a very simple test of the principle. Is the structure on the left as stiff laterally as the structure on the right? This is amenable to solution by hand, and a start at forming the equations suggested that the two will not be equally stiff. However, I decided it would be quicker to demonstrate with a simple FEA model.



Making the vertical member 1m tall, using a cross-section for the members of 50x50x2 SHS, and properties for Al, F = 1N, I found he following results:

For the structure on the left (macro doit6 in appendix)

THE FOLLOWING DEGREE OF FREEDOM RESULTS ARE IN GLOBAL COORDINATES

3 4 5 6 7 8 9 10	-0. 12807E-03 -0. 20549E-04 -0. 69556E-04 0. 0000 -0. 19948E-04 -0. 50345E-04 -0. 87332E-04 0. 0000 -0. 23269E-04	UY 0.0000 3-0.44000E-04 4-0.14667E-04 4-0.29333E-04 0.0000 4 0.48386E-05 4-0.34762E-05 4-0.20791E-04 0.0000 4-0.45805E-05	UZ 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	USUM 0.0000 0.13541E-03 0.25246E-04 0.75489E-04 0.0000 0.20526E-04 0.50464E-04 0.89773E-04 0.0000 0.23715E-04
11 MAXI MUM NODE	-0. 72075E-04 ABSOLUTE VAL	1-0. 22312E-04 LUES	0.0000	0. 75449E-04
	0. 12807E-03-	4	0.0000	0. 13541E-03

For the structure on the right

NODE	UX	UY	UZ	USUM
1	0.0000	0. 0000	0.0000	0.0000
2	-0. 69562E-04	0. 12511E-06	0.0000	0. 69562E-04
3	-0. 11887E-04	0.41702E-07	0.0000	0. 11887E-04
4	-0.39233E-04	0.83405E-07	0.0000	0. 39233E-04
5	0.0000	0.0000	0.0000	0.0000
6	-0. 12461E-04	0.80858E-05	0.0000	0. 14854E-04
7	-0. 28353E-04	0.10498E-04	0.0000	0. 30234E-04
8	-0. 47560E-04	0.75981E-05	0.0000	0. 48164E-04
9	0.0000	0.0000	0.0000	0.0000
10	-0.14068E-04-	-0. 51681E-05	0.0000	0. 14987E-04
11	-0. 39838E-04-	-0. 38231E-05	0.0000	0. 40021E-04
MAXI MUM	ABSOLUTE VALU	JES		
NODE	2	7	0	2
VALUE -	-0.69562E-04 (). 10498E-04	0.0000	0.69562E-04

So the structure on the right is stiffer.

6. Macros

6.1 Original macro from Tim Hayler

FINISH

ГПИБП	
/CLE /PREP7	k,9,-(length/2),depth,-(width/2) k,10,(length/2),depth,-(width/2) k,11,-(length/2),depth,(width/2) k,12,(length/2),depth,(width/2)
/title,beam splitter32	
c*** structural members in either beam188 or beam4	1,1,2 1,2,4 1,4,3 1,3,1
c*** length mm c*** Density tonne/mm^3 c*** Mass metric tonne (1 tonne = 1000kg)	1,5,6 1,8,7
mp,ex,1,70e3 mp,prxy,1,0.3 mp,dens,1,2.7e-9	1,9,10 1,10,12 1,12,11 1,11,9
length=550 width=350 depth=-1575	1,1,5 1,2,6 1,4,8 1,3,7
*AFUN,DEG c*** included angle theta	1,5,9 1,6,10 1,8,12 1,7,11
THETA=20 stay=sqrt(((((tan(theta))*depth)**2)/2)	1,2,5 1,5,10
c*** main structure ********************	1,3,8 1,8,11 c*** stays ************************************
k,1,-(length/2),0,-(width/2) k,2,(length/2),0,-(width/2) k,3,-(length/2),0,(width/2) k,4,(length/2),0,(width/2)	kwpave,1 csys,4 K,20,-stay,0,-stay
k,5,-(length/2),depth/2,-(width/2) k,6,(length/2),depth/2,-(width/2) k,7,-(length/2),depth/2,(width/2) k,8,(length/2),depth/2,(width/2)	kwpave,2 csys,4 K,21,stay,0,-stay kwpave,3

csys,4 K,22,-stay,0,stay

kwpave,4 csys,4 K,23,stay,0,stay

1,9,20 1,10,21 1,12,23 1,11,22

a,4,2,6,10,12,8 a,3,1,5,9,11,7

ET,1,BEAM188

C*** section type hollow rectangular ***** sectype,1,beam,hrec, secdata,50,50,5,5,5

c*** section type circular tube ********* sectype,2,beam,ctube, secdata,56,60

ET,2,BEAM4

ET,3,SHELL63

ET,4,MASS21

c*** Real constants for Beam4 **************

C***R,N,AREA,IZZ,IYY,TKZ,TKY

 $c^{***} R4 = 20 \times 20 \times 5mm$ wall thickness $c^{***} R5 = 20 \times 20 \times 2mm$ wall thickness C*** R6 = 30 x 30 x 2mm wall thickness $C^{***} R7 = 40 x 40 x 2mm$ wall thickness $C^{***} R8 = 50 x 50 x 2mm$ wall thickness $c^{***} R9 = 60 \times 60 \times 2mm$ wall thickness $C^{***} R10 = 50 \times 50 \times 4mm$ wall thickness $C^{***} R_{11} = 50 \times 50 \times 50 m$ wall thickness $C^{***} R12 = 50 \times 50 \times 6mm$ wall thickness c^{***} R13 = 60 Dia, 5 mm wal Thk, circular hollow section

R,4,300,12500,12500,20,20 R,5,144,7872,7872,20,20 R,6,224,29419,29419,30,30 R,7,304,73365,73365,40,40 R,8,384,147712,147712,50,50 R,9,464,260459,260459,60,60 R,10,736,261525,261525,50,50 R,11,900,307500,307500,50,50 R,12,1056,347072,347072,50,50 R,13,864,329376,329376,60,60

c*** stays mesh with beam188 ******

MAT,1 TYPE,1 lsel,s,,,23,26 secnum,1 lmesh,all lsel,all c*** main structure mesh with beam188 *****

lsel,u,,,23,26 TYPE,1 secnum,1 lmesh,all lsel,all

c*** alternative mesh with beam4 complete structure ***

c*** Mat,1 c*** type,2 c*** real,11 c*** lmesh,all

c*** side plates mesh ********

R,20,5 real,20 type,3 amesh,all

c*** Additional mass **************** R,30,0.003,0.003,0.003 TYPE,4 real,30 ksel,s,,,9,12 kmesh,all ksel,all c**** constraints ***********

NSEL,S,LOC,Y,0 D,ALL,ALL NSEL,ALL ACEL,,9810

FINISH /SOLU ANTYPE,STATIC SOLVE

/POST1 /VIEW,1,1,1,1 PLDISP,1

```
FINISH
/SOLU
ANTYPE,MODAL
MODOPT,SUBSP,20
SOLVE
FINISH
```

6.2 Macro "doit4" which builds model 4

FINISH	mp,prxy,1,0.3
/CLE	mp,dens,1,2.7e-9
/PREP7	-
	length=550
/title,beam splitter32	width=350
	depth=-1575
c*** structural members in either	-
beam188 or beam4	
	*AFUN,DEG
c*** length mm	
c*** Density tonne/mm^3	c*** included angle theta
c*** Mass metric tonne (1 tonne =	C
1000kg)	THETA=20
<i>C,</i>	stay=sqrt(((((tan(theta))*depth)**2)/2)
)
	,

mp,ex,1,70e3

c*** main structure kwpave,4 ****** csys,4 !K,23,stay,0,stay k, 1, -(length/2), 0, -(width/2)k,23,jstay,0,0 !k,2,(length/2),0,-(width/2) !k,3,-(length/2),0,(width/2)1,9,20 k,4,(length/2),0,(width/2)1,9,21 1,12,23 k,5,-(length/2),depth/2,-(width/2) 1,12,22 !k,6,(length/2),depth/2,-(width/2) !k,7,-(length/2),depth/2,(width/2)c*** side plates ****** k,8,(length/2),depth/2,(width/2) k,9,-(length/2),depth,-(width/2) !k,10,(length/2),depth,-(width/2)c*** Element types !k,11,-(length/2),depth,(width/2) k,12,(length/2),depth,(width/2) ET,1,BEAM188 !two tripods 1,9,12 C*** section type hollow rectangular ***** 1.1.5 sectype,1,beam,hrec, secdata,50,50,5,5,5,5 1,4,8 c*** section type circular tube ****** 1.5.9 sectype,2,beam,ctube, secdata,56,60 1.8.12 ET,2,BEAM4 c*** stavs ****************** ET,3,SHELL63 jstay = stay*sqrt(2) ET,4,MASS21 kwpave,1 csys.4 !K,20,-stay,0,-stay c*** Real constants for Beam4 ***** K,20,-jstay,0,0 C***R,N,AREA,IZZ,IYY,TKZ,TKY kwpave,1 csys,4 $c^{***} R4 = 20 x 20 x 5mm$ wall !K,21,stay,0,-stay k,21,0,0,-jstay thickness $c^{***} R5 = 20 x 20 x 2mm$ wall kwpave,4 thickness C^{***} R6 = 30 x 30 x 2mm wall csys,4 !K,22,-stay,0,stay thickness $C^{***} R7 = 40 x 40 x 2mm$ wall k,22,0,0,jstay thickness

C*** R8 = 50 x 50 x 2mm wall thickness c*** R9 = 60 x 60 x 2mm wall thickness C*** R10 = 50 x 50 x 4mm wall thickness C*** R11 = 50 x 50 x 5mm wall thickness C*** R12 = 50 x 50 x 6mm wall thickness c*** R13 = 60 Dia, 5 mm wal Thk, circular hollow section

R,4,300,12500,12500,20,20 R,5,144,7872,7872,20,20 R,6,224,29419,29419,30,30 R,7,304,73365,73365,40,40 R,8,384,147712,147712,50,50 R,9,464,260459,260459,60,60 R,10,736,261525,261525,50,50 R,11,900,307500,307500,50,50 R,12,1056,347072,347072,50,50 R,13,864,329376,329376,60,60

c*** stays mesh with beam188 ******

MAT,1 TYPE,1 lsel,s,,,23,26 secnum,1 lmesh,all lsel,all

c*** main structure mesh with beam188 *****

lsel,u,,,23,26 TYPE,1 secnum,1 lmesh,all lsel,all

c*** alternative mesh with beam4 complete structure ***

c*** Mat,1 c*** type,2 c*** real,11 c*** lmesh,all

c*** Additional mass ****************

R,30,0.003,0.003,0.003 TYPE,4 real,30 ksel,s,,,9,12 kmesh,all ksel,all

c**** constraints ************

NSEL,S,LOC,Y,0 D,ALL,ALL NSEL,ALL ACEL,,9810

FINISH /SOLU ANTYPE,STATIC SOLVE

/POST1 /VIEW,1,1,1,1 PLDISP,1

FINISH /SOLU ANTYPE,MODAL MODOPT,SUBSP,20 SOLVE FINISH

Macro "doit6" to make a very simple model 6.3 FINISH /CLE ****** /PREP7 /title,simple model dk,1,all dk,3,all c*** structural members in either dk,4,all beam188 or beam4 fk,2,fx,-1 ! units mm and N (static only) c************ Meshing *********************** mp,ex,1,70e3 mp,prxy,1,0.3 MAT,1 mp,dens,1,2.7e-9 TYPE.1 real.8 length=1000 lmesh,all width=1000 w2 = 500FINISH /SOLU c*** main structure ANTYPE,STATIC ****** **SOLVE** k,1,0,0,0 /POST1 k,2,0,length,0 /VIEW,1,1,1,1 k,3,width,0,0 PLDISP.1 k,4,w2,0,0 !two triangles 1.1.2 1,3,2 1,4,2 c*** Element types ET,1,BEAM3 C***R,N,AREA,IZZ

 $C^{***} R8 = 50 x 50 x 2mm$ wall thickness

R,8,384,147712