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**Ear bond area limit for ETM/ITM optics
from consideration of thermal noise**

C. A. Cantley, E. Elliffe, J. Hough, S. Rowan & G. Cagnoli

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California Institute of Technology
LIGO Project – MS 18-34
1200 E. California Blvd.
Pasadena, CA 91125
Phone (626) 395-2129
Fax (626) 304-9834
E-mail: info@ligo.caltech.edu

LIGO Hanford Observatory
P.O. Box 1970
Mail Stop S9-02
Richland WA 99352
Phone 509-372-8106
Fax 509-372-8137

**Institute for Gravitational
Research**
University of Glasgow
Kelvin Building
Glasgow G12 8QQ
Phone: +44 (0)141 330 3340
Fax: +44 (0)141 330 6833
Web: www.physics.gla.ac.uk/gwg

Massachusetts Institute of Technology
LIGO Project – NW17-161
175 Albany St
Cambridge, MA 02139
Phone (617) 253-4824
Fax (617) 253-7014
E-mail: info@ligo.mit.edu

LIGO Livingston Observatory
P.O. Box 940
Livingston, LA 70754
Phone 225-686-3100
Fax 225-686-7189

<http://www.ligo.caltech.edu/>

1 Introduction

The analysis underpinning this document was performed by E. Elliffe at Glasgow in 2004/05. Full details of the analysis and the results obtained will be provided in a paper which is currently in preparation for publication in *Classical and Quantum Gravity*¹.

2 Analysis approach

Finite element calculations were made for prediction of the thermal noise in the test masses of Advanced LIGO associated with the silicate bonds used for silica ear attachment. The analyses were based on the thermal noise analysis technique developed by Levin² and experimental measurements of bond thickness, elastic energy storage and losses^{3 4}. Upper limits were placed on the thermal noise contribution from the bonds as a function of bond area. This provided constraints on the size of the bonds from consideration of the introduction of ‘technical noise’ to the test mass⁵.

A comparison was made of the thermal noise contribution at 10 Hz, 40 Hz and 100 Hz of two and four⁶ 81 nm thick sodium silicate bonds on the sides of a 40 kg Advanced LIGO silica test mass as a function of bond area with a normalized gaussian pressure of 55 mm radius⁷ incident on the front face of the test mass.

The maximum bond areas were evaluated for the thermal noise contribution to be $\leq 10\%$ of the overall intrinsic thermal noise level of the interferometer as specified in the Advanced LIGO Systems Design document⁵.

3 Results

3.1 Limit to bond area

From the analysis the limit to the total bond area on each Advanced LIGO optic was determined to be 7.1cm^2 . This is dictated by the requirement at 100 Hz where, from the Advanced LIGO Systems Design document⁵, the thermal noise for one test mass is $8.0 \times 10^{-21} \text{ m}/\sqrt{\text{Hz}}$. This sets the (technical noise) limit of $8.0 \times 10^{-22} \text{ m}/\sqrt{\text{Hz}}$ for the total bond noise per test mass.

¹ Elliffe, Hough, Rowan & Cagnoli, “*Characterisation of the thermal noise contribution of hydroxide catalysis bonds on 40 kg silica and sapphire test masses in the Advanced LIGO gravitational wave detector*” (in preparation for publication in *Class. Quantum Grav.*)

² Levin Y., *Physics Review D* **57** 659 (1998)

³ Sneddon P. et. al., *Class. Quantum Grav.*, **20** 5025-37 (2003)

⁴ Elliffe E. et. al., *Class. Quantum Grav.*, **22**, 1-11 (2005)

⁵ T010075-00-D, “*Advanced LIGO Systems Design*”, Fritschel et. al..

⁶ When four bonds were modelled the bond pairs on each flat were separated by 30 mm as per proposed ribbon spacing for Advanced LIGO monolithic suspension design.

⁷ Radius value quoted for $1/e$ amplitude of beam.

3.2 Resulting stress levels

From the analysis, the limit to the total bond area on each Advanced LIGO test mass is 7.1cm^2 . The Advanced LIGO test masses are ~ 40 kg each, producing an average stress level of ~ 0.55 MPa on the bonds. The measured breaking stress of sodium silicate bonds (1:6) is typically much larger than this (in range 4.8 MPa to 6.3 MPa)⁸.

4 Conclusions

Simple scaling up from the bonds used in GEO 600 based on the increase of the test masses from 10 kg to 40 kg would require a total bond area per test mass of 24cm^2 to maintain the same level of average stress on the bonds.

The analysis described has shown that the total bond area on each test mass is limited to 7.1cm^2 by consideration of the thermal noise associated with the bonds. However, this is acceptable since the resulting average stress level on the bonds when the test masses are suspended will be several factors lower (at least $\times 8$) than the typical measured breaking stress for these types of sodium silicate bonds (1:6).

⁸ Private communication. Data measured at Caltech by H. Armandula in 2001 on unbaked sodium silicate bonds.