

### FEA Results: BSC ISI Spring, 0-1

large displacement flag enabled in SolidWorks Simulation

Spring material: Maraging 300

|     |       |     |                 |
|-----|-------|-----|-----------------|
| Ex  | 189.6 | GPa | Young's Modulus |
| Gxy | 80    | GPa | Shear Modulus   |
| nu  | 0.3   |     | Poisson's Ratio |

Z axis: in-plane, parallel to Spring's long axis

Y axis: out-of-plane

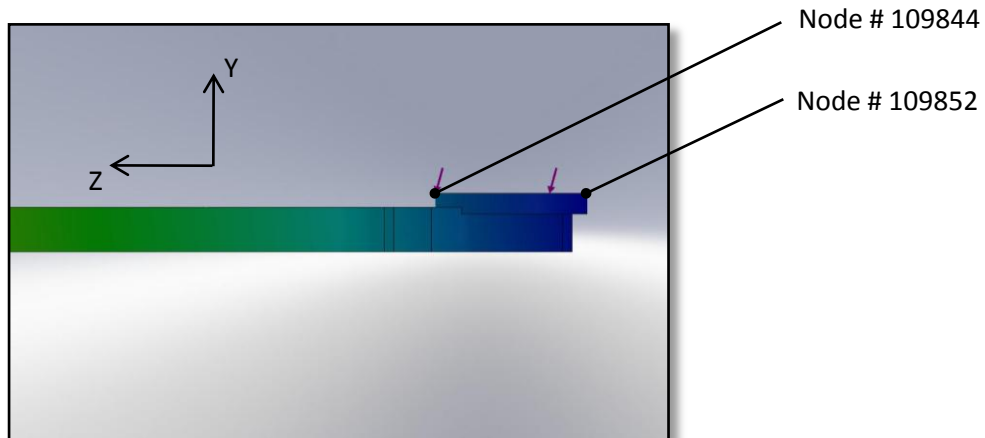
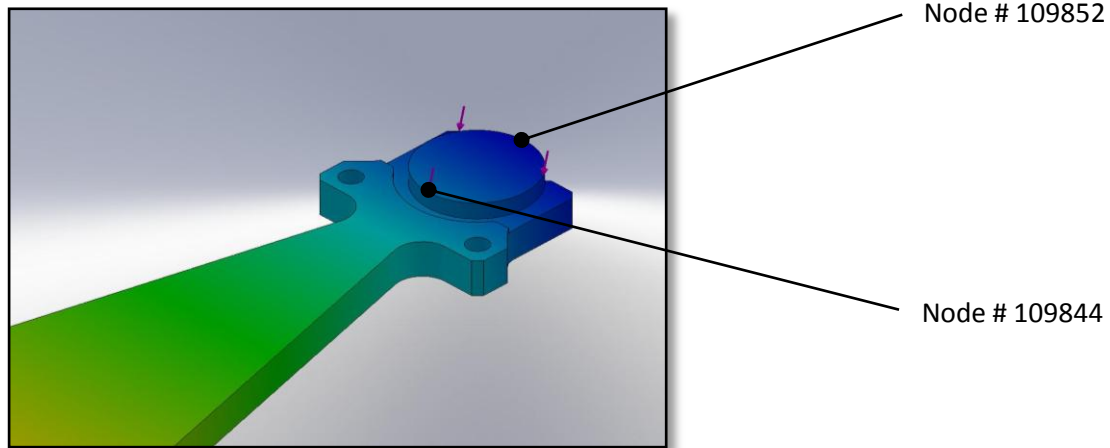
force applied to "Dummy Flexure Mount" mated to top of Spring tip, concentric with the Flexure's axis

Dummy Flexure Mount material... custom very-high-stiffness

|     |          |     |                 |
|-----|----------|-----|-----------------|
| Ex  | 6.89E+04 | GPa | Young's Modulus |
| Gxy | 2.28E+04 | GPa | Shear Modulus   |
| nu  | 0.33     |     | Poisson's Ratio |

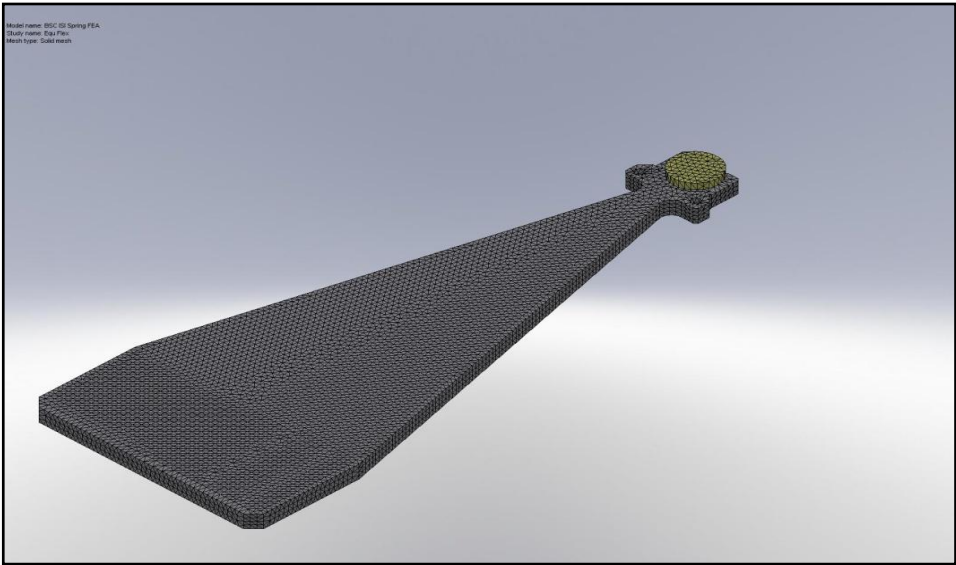
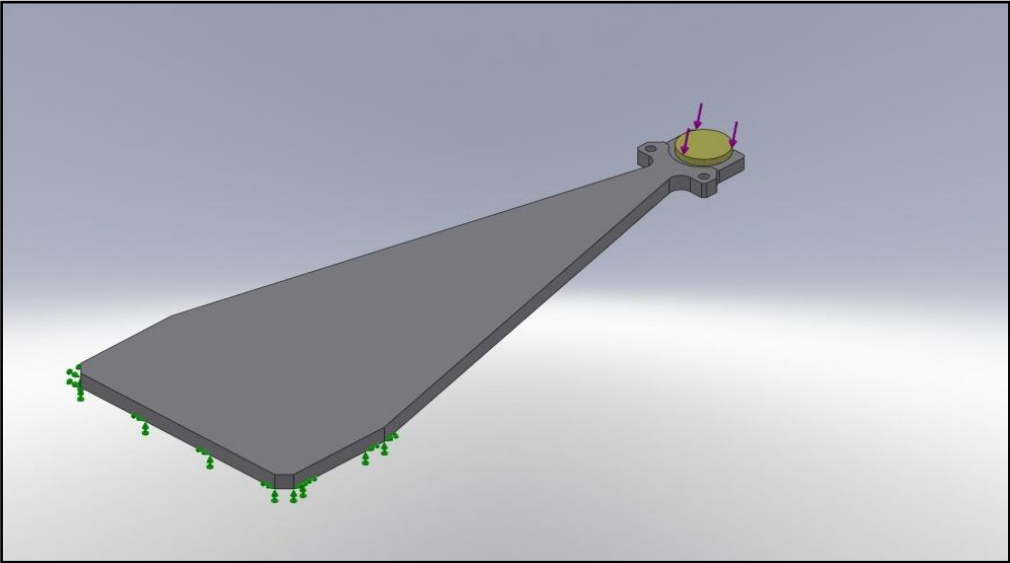
|                   |                                 |                      |  |                |                                       |  |
|-------------------|---------------------------------|----------------------|--|----------------|---------------------------------------|--|
| <b>Study Name</b> |                                 | <b>"Equ Flex"</b>    |  |                |                                       |  |
|                   | Force                           | <b>2750</b> lb       | <i>this is the expected load per 0-1 Spring</i>                    |                |                                       |  |
|                   | Angle of Force, from Tip normal | 13.18 deg            | <i>this value taken from geometry of ASI's curved Spring model</i> |                |                                       |  |
|                   | mesh size                       | 0.175 in             |  |                |                                       |  |
| <i>results:</i>   |                                 |                      |  |                |                                       |  |
|                   | <b>Node Number</b>              | <b>Node Position</b> | <b>Displacement (in)</b>   |                | <b>Tip Angle (Deg)</b>                |  |
|                   | #                               | Z                    | $\Delta Y$   | $\Delta Z$     |                                       |  |
|                   | 109844                          | -16.188              | -1.983   | 5.435E-02      | -                                     |  |
|                   | 109852                          | -17.813              | -2.369   | 1.007E-01      | 13.74                                 |  |
|                   |                                 |                      | <b>resultant displacement</b>                                      | <b>2.18</b> in | <i>referenced to undeformed shape</i> |  |

Displacements are recorded at two points on the infinitely stiff "dummy flexure mount." Typical location of these points (or "nodes") are shown in the following two SolidWorks Simulation screen captures. Knowing the distance between the nodes and the displacements predicted there, we can estimate the angle of the Spring tip when the given load is applied.



| <b>Study Name</b>                         |                | <b>"Equ+ Flex"</b>                           |  |  |  |
|---|----------------|--|--|--|--|
| Force                                     | <b>2800 lb</b> | <b>50 lbs more than the equilibrium load</b> |  |  |  |
| Angle of Force, from Tip normal           | 13.18 deg      |  |  |  |  |
| mesh size                                 | 0.175 in       |  |  |  |  |
| <i>results:</i>                           |                |  |  |  |  |
| Node Number                               | Node Position  | Displacement (in)                            |  | Tip Angle (Deg)                                |  |
| #   | Z              | $\Delta Y$                                   | $\Delta Z$   |  |  |
| 109844                                    | -16.188        | -2.020                                       | 5.837E-02  | -  |  |
| 109852                                    | -17.813        | -2.412                                       | 1.064E-01  | 13.96  |  |
| <b>resultant displacement</b>             |                | <b>0.0403 in</b>                             |  | <i>referenced to "Equ Flex" deformed shape</i> |  |
| <b>linear stiffness, near equilibrium</b> |                | 1241 lb/in                                   | <b>1.24 lb per .001"</b>   |  |  |
|   |                | 4.448 N/lb                                   |  |  |  |
|   |                | 3.94E-05 in/um                               |  |  |  |
|   |                | <b>0.217 N/um</b>                            | <b>Per Blade - for stiffness of entire Stage, multiply by 3x</b> |  |  |

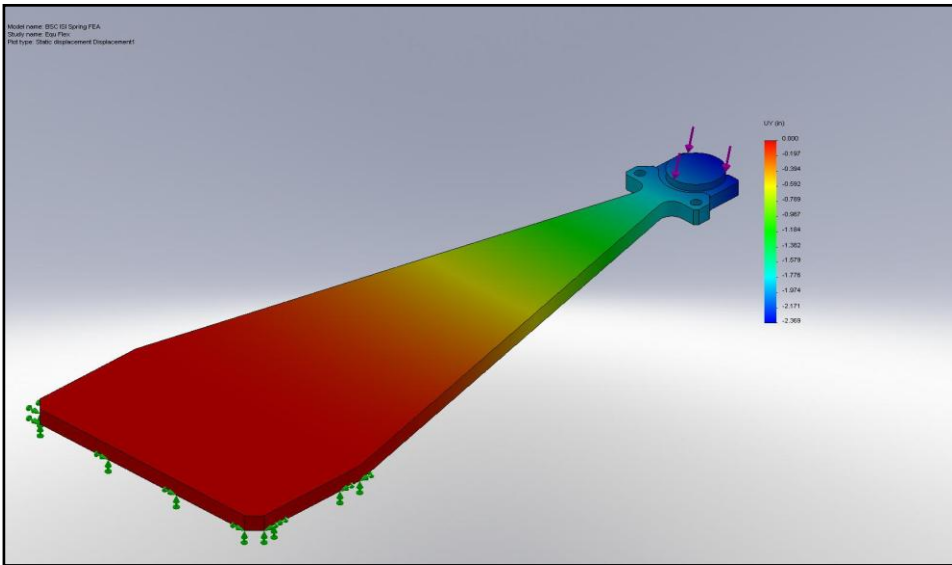
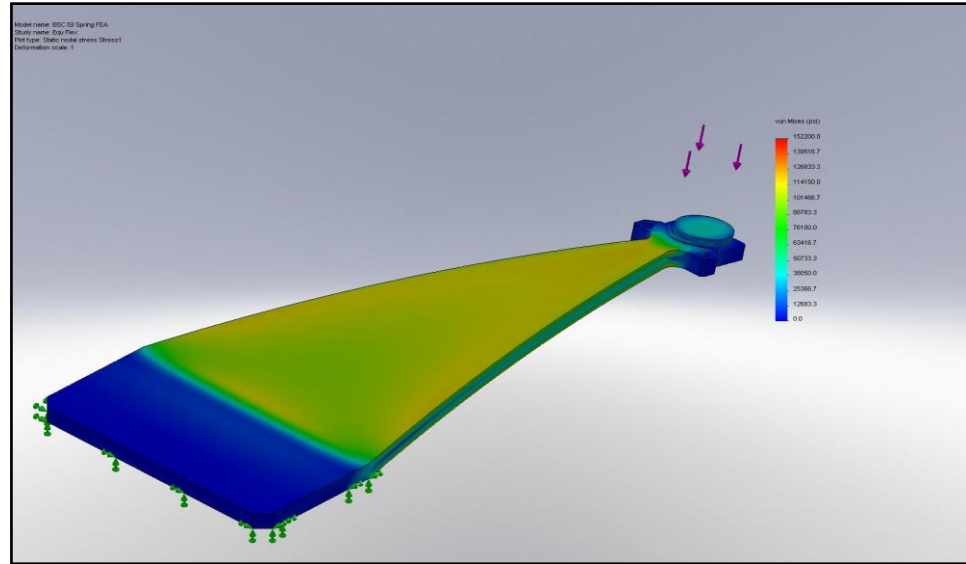
0-1 Spring:  
FEA Setup



0-1 Spring:  
After Meshing

0-1 Spring:  
"Equ Flex" Stress

max value 152200 psi  
min value 0 psi

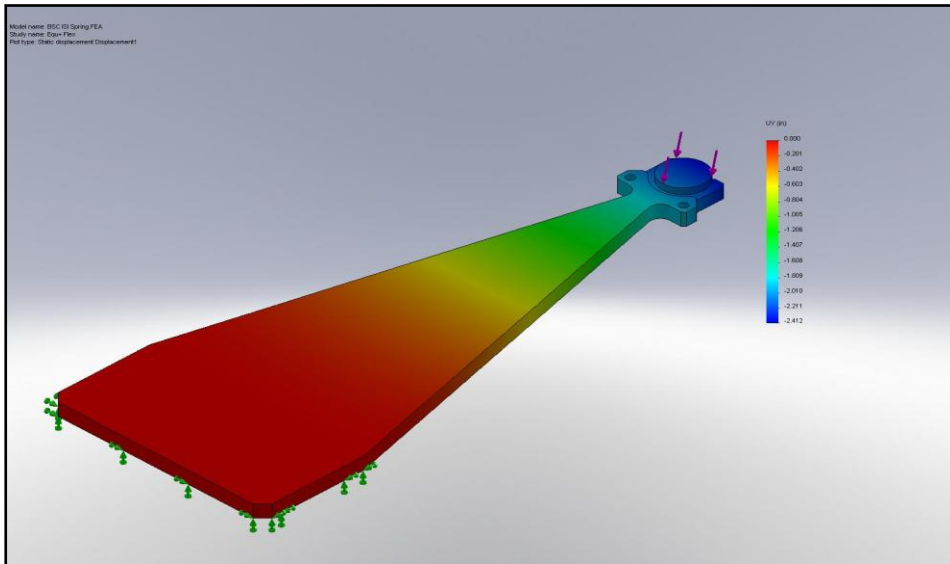
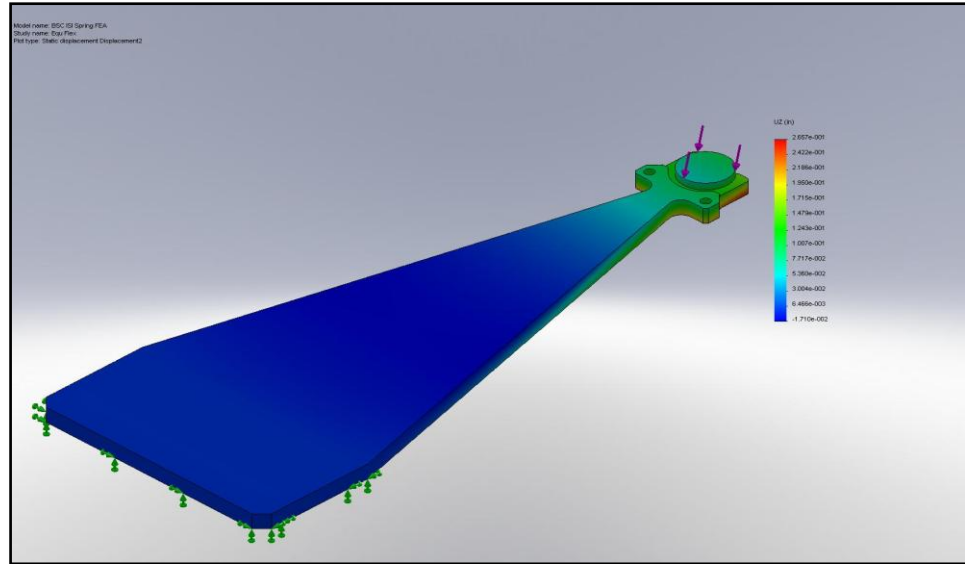


0-1 Spring:  
"Equ Flex"  $\Delta Y$  Results

max value 0 in  
min value -2.369 in

0-1 Spring:  
"Equ Flex"  $\Delta Z$  Results

max value 2.657E-01 in  
min value -1.710E-02 in

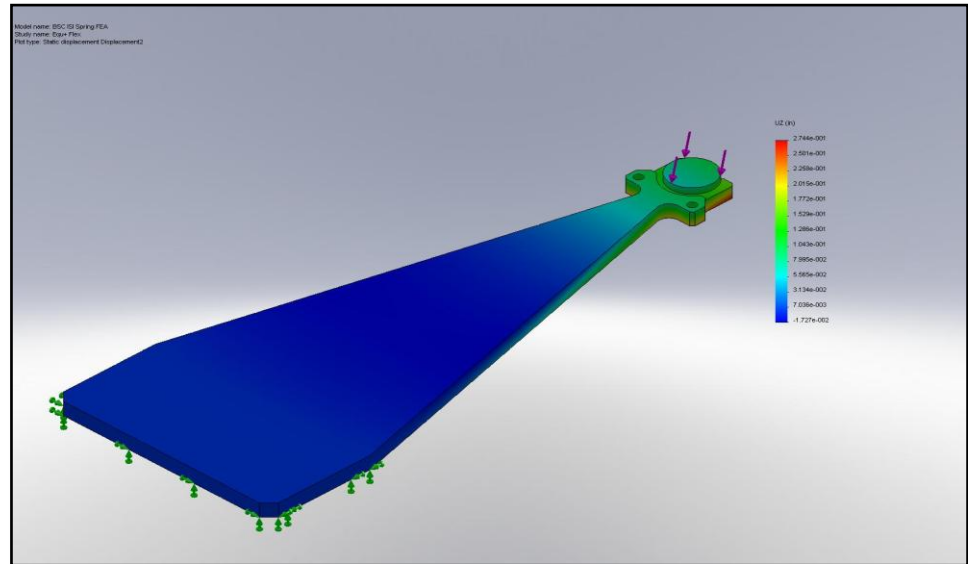


0-1 Spring:  
"Equ+ Flex"  $\Delta Y$  Results

max value 0 in  
min value -2.412 in

0-1 Spring:  
"Equ+ Flex"  $\Delta Z$  Results

max value 2.744E-01 in  
min value -1.727E-02 in



Re-running the "Equ Flex" study for the 0-1 Spring, this time using the slightly larger angle for the force line, as evaluated in the initial study above:

| Study Name                      |               | "Equ Flex"                                      |            |                                       |  |  |
|---------------------------------|---------------|---|------------|---------------------------------------|--|--|
| Force                           | 2750 lb       | <i>this is the expected load per 0-1 Spring</i> |            |                                       |  |  |
| Angle of Force, from Tip normal | 13.74 deg     |   |            |                                       |  |  |
| mesh size                       | 0.175 in      |   |            |                                       |  |  |
| <i>results:</i>                 |               |   |            |                                       |  |  |
| Node Number                     | Node Position | Displacement (in)                               |            | Tip Angle (Deg)                       |  |  |
| #                               | Z             | $\Delta Y$                                      | $\Delta Z$ |                                       |  |  |
| 111011                          | -16.188       | -1.981  | 5.410E-02  | -                                     |  |  |
| 111019                          | -17.813       | -2.366  | 1.003E-01  | 13.71                                 |  |  |
| resultant displacement          |               |   | 2.17 in    | <i>referenced to undeformed shape</i> |  |  |

**conclusion:** no significant effect from re-aligning force line to equilibrium tip angle.

Re-running the "Equ Flex" study for the 0-1 Spring, again. We now use the tip angle evaluated in the above study, and the "correct" value for the Maraging 300's Shear Modulus (Gxy). Also, the mesh density is slightly higher than in all the previous 0-1 Spring FEAs:

| Study Name                      |               | "Equ Flex"                      |            |                                       |  |  |
|---------------------------------|---------------|---------------------------------|------------|---------------------------------------|--|--|
| Force                           | 2750 lb       | <i>Maraging 300 properties:</i> |            |                                       |  |  |
| Angle of Force, from Tip normal | 13.71 deg     | Ex                              | 189.6      | GPa                                   |  |  |
| mesh size                       | 0.150 in      | Gxy                             | 73         | GPa                                   |  |  |
|                                 |               | nu                              | 0.3        |                                       |  |  |
| <i>results:</i>                 |               |                                 |            |                                       |  |  |
| Node Number                     | Node Position | Displacement (in)               |            | Tip Angle (Deg)                       |  |  |
| #                               | Z             | $\Delta Y$                      | $\Delta Z$ |                                       |  |  |
| 176382                          | -16.188       | -1.982                          | 5.423E-02  | -                                     |  |  |
| 176402                          | -17.813       | -2.367                          | 1.005E-01  | 13.71                                 |  |  |
| resultant displacement          |               |                                 | 2.18 in    | <i>referenced to undeformed shape</i> |  |  |

**conclusion:** There is almost no difference between these results and the results listed directly above it. Sensitivity to mesh size and value of Gxy appear to be low enough to give good confidence in the results.



Re-running the "Equ+ Flex" study for the 0-1 Spring, to re-evaluate the Spring's stiffness. We now use the tip angle evaluated in the initial "Equ+ Flex" study, and the correct value for the Maraging 300's Shear Modulus (Gxy):

|                                 |                  |                                 |           |    |   |
|---------------------------------|------------------|---------------------------------|-----------|----|---|
| <b>Study Name</b>               |                  | <b>"Equ+ Flex"</b>              |           |    |   |
| Force                           | <b>2800 lb</b>   | <i>Maraging 300 properties:</i> |           |    |   |
| Angle of Force, from Tip normal | <b>13.90 deg</b> | Ex                              | 189.6     | GP | a |
| mesh size                       | 0.175 in         | Gxy                             | <b>73</b> | GP | a |
|                                 |                  | nu                              | 0.3       |    |   |

results:

| Node Number<br># | Node Position<br>Z | Displacement (in) |            | Tip Angle (Deg) |
|------------------|--------------------|-------------------|------------|-----------------|
|                  |                    | $\Delta Y$        | $\Delta Z$ |                 |
| 111011           | -16.188            | -2.017            | 5.805E-02  | -               |
| 111019           | -17.813            | -2.408            | 1.059E-01  | 13.92           |

*referenced to "Equ Flex" deformed shape*

|   |                   |  |
|---|-------------------|--|
| <b>resultant displacement</b>             | <b>0.0383 in</b>  |  |
| <i>linear stiffness, near equilibrium</i> | 1306 lb/in        | <b>1.31 lb per .001"</b>   |
|   | 4.448 N/lb        |  |
|   | 3.94E-05 in/um    |  |
|   | <b>0.229 N/um</b> | <i>Per Blade - for stiffness of entire Stage, multiply by 3x</i> |

**conclusion:** We see a small change in the evaluated stiffness.

|  |                      |                          |                                 |                   |  |  |
|--|----------------------|--------------------------|---------------------------------|-------------------|--|--|
| New study named "Equ- Flex," using a force 50 lbs less than the nominal Spring load: |                      |                          |                                 |                   |  |  |
| <b>Study Name</b> "Equ- Flex"  |                      |                          |                                 |                   |  |  |
| Force  | 2700 lb              |                          | <i>Maraging 300 properties:</i> |                   |  |  |
| Angle of Force, from Tip normal  | 13.45 deg            |                          | Ex                              | 189.6             | GPa  |  |
| mesh size  | 0.175 in             |                          | Gxy                             | 73                | GPa  |  |
|  |                      |                          | nu                              | 0.3               |  |  |
| <i>results:</i>  |                      |                          |                                 |                   |  |  |
| <b>Node Number</b>   | <b>Node Position</b> | <b>Displacement (in)</b> |                                 |                   | <b>Tip Angle (Deg)</b>   |  |
| #  | Z                    | $\Delta Y$               | $\Delta Z$                      |                   |  |  |
| 111011   | -16.188              | -1.946                   | 5.031E-02                       | -                 |  |  |
| 111019   | -17.813              | -2.324                   | 9.489E-02                       | 13.45             |  |  |
| <b>resultant displacement</b>  |                      |                          |                                 | <b>0.0398 in</b>  | <i>referenced to "Equ Flex" deformed shape</i>                   |  |
| <b>linear stiffness, near equilibrium</b>  |                      |                          |                                 | 1257 lb/in        | <b>1.26 lb per .001"</b>   |  |
|  |                      |                          |                                 | 4.448 N/lb        |  |  |
|  |                      |                          |                                 | 3.94E-05 in/um    | <b>Per Blade</b> - for stiffness of entire Stage, multiply by 3x |  |
|  |                      |                          |                                 | <b>0.220 N/um</b> |  |  |

**conclusion:** The stiffness calculated in this direction (subtracting from, rather than adding to the nominal force) is very similar to that calculated directly above, adding to our confidence in the previous results.

### FEA Results: BSC ISI Spring, 1-2

large displacement flag enabled in SolidWorks Simulation

Spring material: Maraging 300

|     |       |     |                 |
|-----|-------|-----|-----------------|
| Ex  | 189.6 | GPa | Young's Modulus |
| Gxy | 80    | GPa | Shear Modulus   |
| nu  | 0.3   |     | Poisson's Ratio |

Z axis: in-plane, parallel to Spring's long axis

Y axis: out-of-plane

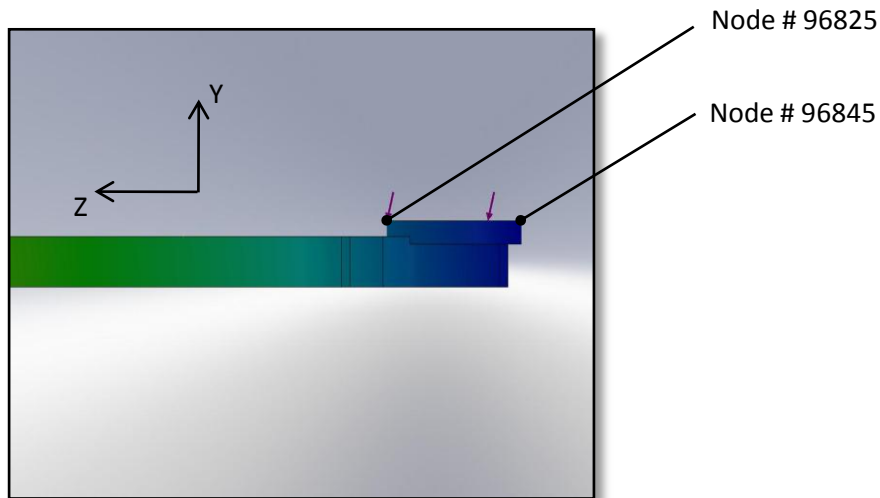
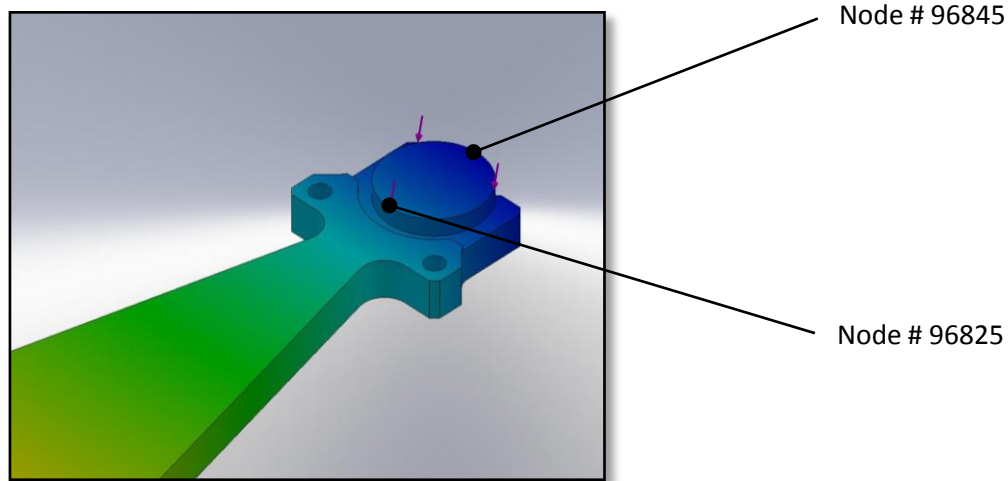
force applied to "Dummy Flexure Mount" mated to top of Spring tip, concentric with the Flexure's axis

Dummy Flexure Mount material... custom very-high-stiffness

|     |          |     |                 |
|-----|----------|-----|-----------------|
| Ex  | 6.89E+04 | GPa | Young's Modulus |
| Gxy | 2.28E+04 | GPa | Shear Modulus   |
| nu  | 0.33     |     | Poisson's Ratio |

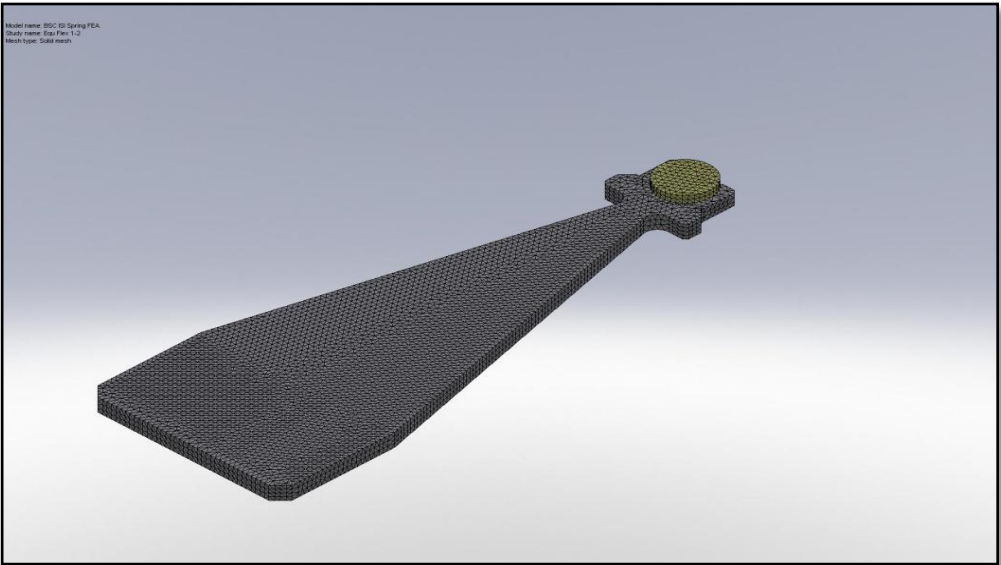
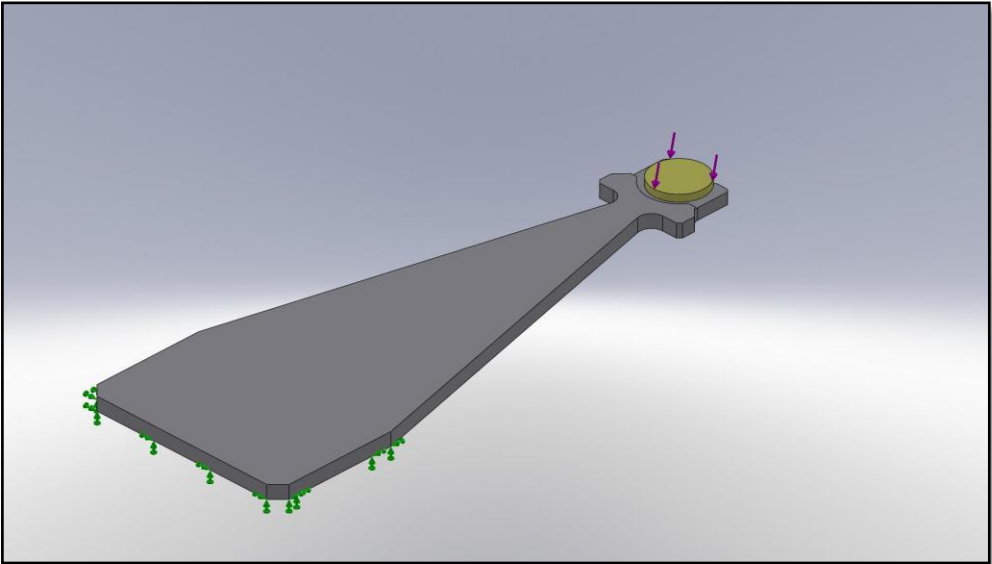
| Study Name               |               | "Equ Flex"   |            |                                       |  |
|--------------------------|---------------|--|------------|---------------------------------------|--|
| Force                    | 2080 lb       | <i>this is the expected load per 1-2 Spring</i>                    |            |                                       |  |
| Angle of Force, from Tip | 11.04 deg     | <i>this value taken from geometry of ASI's curved Spring model</i> |            |                                       |  |
| mesh size                | 0.15 in       |  |            |                                       |  |
| <i>results:</i>          |               |  |            |                                       |  |
| Node Number              | Node Position | Displacement (in)  |            | Tip Angle (Deg)                       |  |
| #                        | Z             | $\Delta Y$   | $\Delta Z$ |                                       |  |
| 96825                    | -11.938       | -1.227   | 1.408E-03  | -                                     |  |
| 96845                    | -13.563       | -1.547   | 3.324E-02  | 11.36                                 |  |
| resultant displacement   |               |  | 1.39 in    | <i>referenced to undeformed shape</i> |  |

Displacements are recorded at two points on the infinitely stiff "dummy flexure mount." Typical location of these points (or "nodes") are shown in the following two SolidWorks Simulation screen captures. Knowing the distance between the nodes and the displacements predicted there, we can estimate the angle of the Spring tip when the given load is applied.



| <b>Study Name</b>                         |                | <b>"Equ+ Flex"</b>                           |        |                   |  |            |
|---|----------------|--|--------|-------------------|--|------------|
| Force                                     | <b>2130 lb</b> | <b>50 lbs more than the equilibrium load</b> |        |                   |  |            |
| Angle of Force, from Tip                  | 11.04 deg      |  |        |                   |  |            |
| mesh size                                 | 0.15 in        |  |        |                   |  |            |
| <i>results:</i>                           |                |  |        |                   |  |            |
| Node Number                               | Node Position  | Displacement (in)                            |        | Tip Angle (Deg)   |  |            |
|   |                | #  | Z      |                   |  | $\Delta Y$ |
| 96825                                     | -11.938        |  | -1.257 | 3.509E-03         | -  |            |
| 96845                                     | -13.563        |  | -1.585 | 3.691E-02         | 11.64  |            |
| <b>resultant displacement</b>             |                |  |        | <b>0.0341 in</b>  | <i>referenced to "Equ Flex" deformed shape</i>                   |            |
| <b>linear stiffness, near equilibrium</b> |                |  |        | 1465 lb/in        | <b>1.47 lb per .001"</b>   |            |
|   |                |  |        | 4.448 N/lb        | <b>Per Blade</b> - for stiffness of entire Stage, multiply by 3x |            |
|   |                |  |        | 3.94E-05 in/um    |  |            |
|   |                |  |        | <b>0.257 N/um</b> |  |            |

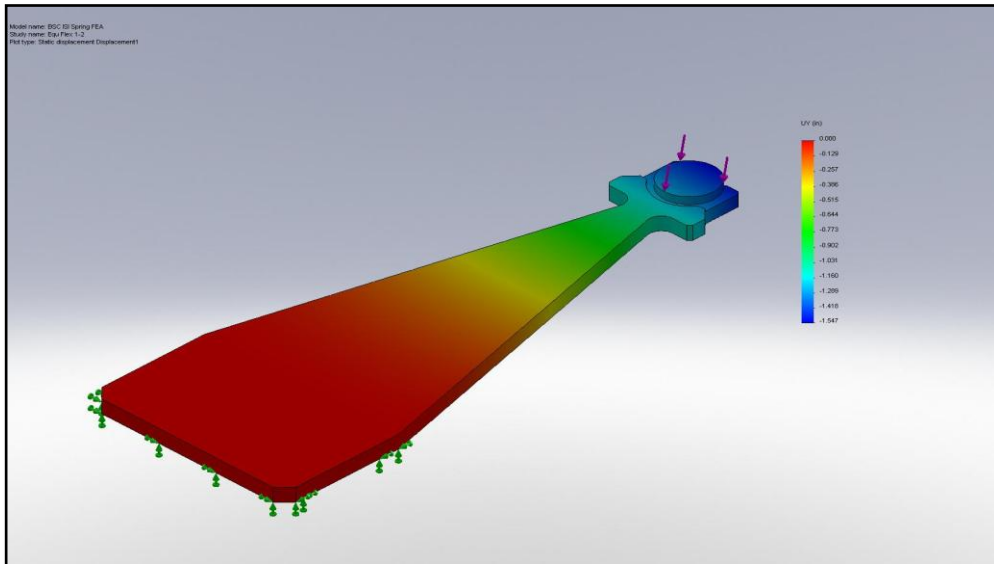
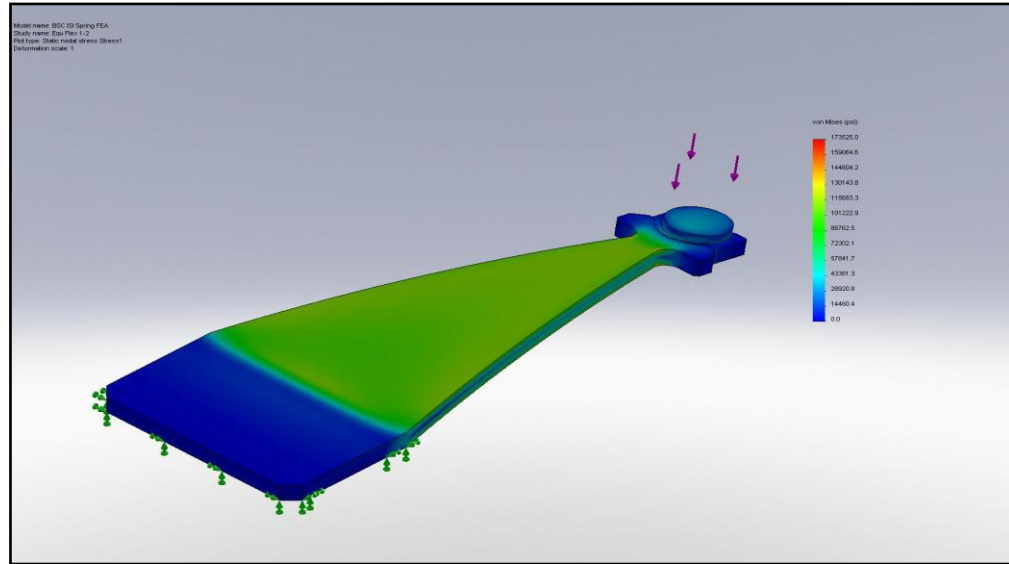
1-2 Spring:  
FEA Setup



1-2 Spring:  
After Meshing

1-2 Spring:  
"Equ Flex" Stress Results

max value 173525 psi  
min value 0 psi

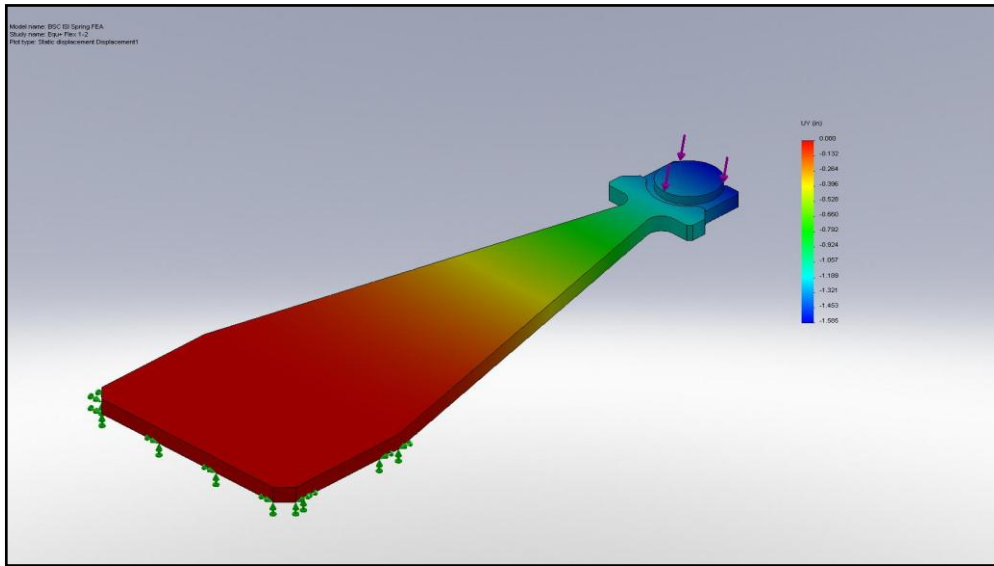
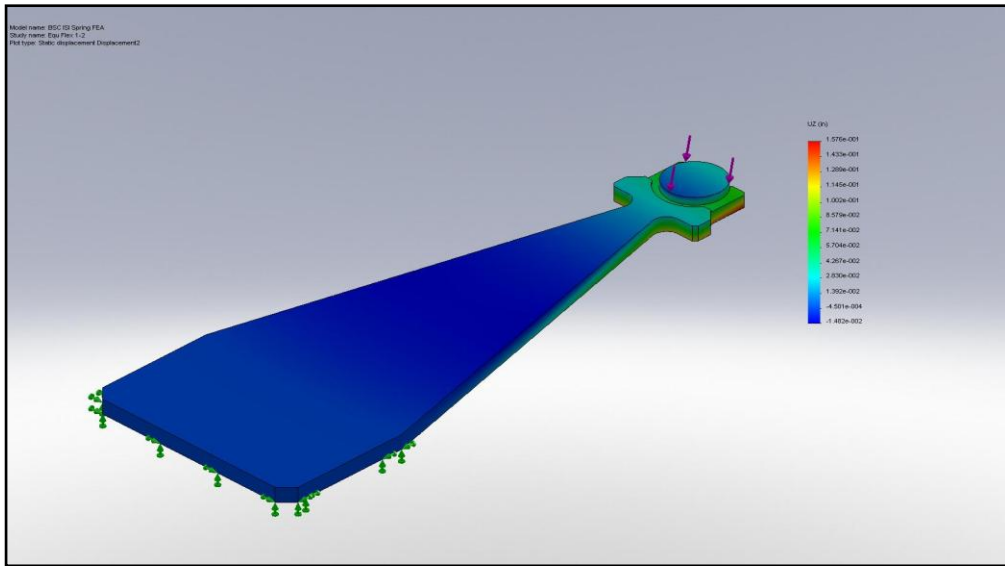


1-2 Spring:  
"Equ Flex" ΔY Results

max value 0 in  
min value -1.547 in

1-2 Spring:  
"Equ Flex"  $\Delta Z$  Results

max value 1.576E-01 in  
min value -1.482E-02 in



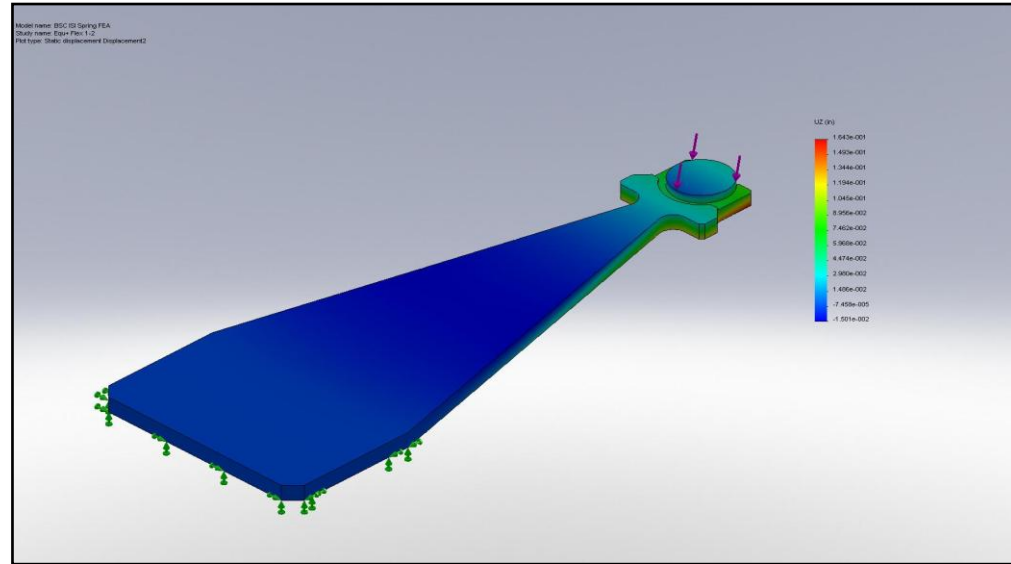
1-2 Spring:  
"Equ+ Flex"  $\Delta Y$  Results

max value 0 in  
min value -1.585 in



1-2 Spring:  
"Equ+ Flex"  $\Delta Z$  Results

max value 1.643E-01 in  
min value -1.501E-02 in



Re-running the "Equ Flex" study for the 1-2 Spring, this time using the correct value for the Shear Modulus (Gxy) and the slightly larger angle for the force line, as evaluated in the initial study above:

|                                 |           |  |       |       |     |
|---------------------------------|-----------|--|-------|-------|-----|
| <b>Study Name</b>               |           | <b>"Equ Flex"</b>                        |       |       |     |
| Force                           | 2080 lb   | <i>Maraging 300 material properties:</i> |       |       |     |
| Angle of Force, from Tip normal | 11.36 deg | Ex                                       | 189.6 | 189.6 | GPa |
| mesh size                       | 0.15 in   | Gxy                                      | 73    | 73    | GPa |
|                                 |           | nu                                       | 0.3   | 0.3   |     |

results:

| Node Number<br># | Node Position<br>Z | Displacement (in) |            | Tip Angle (Deg) |
|------------------|--------------------|-------------------|------------|-----------------|
|                  |                    | $\Delta Y$        | $\Delta Z$ |                 |
| 96825            | -11.938            | -1.227            | 1.367E-03  | -               |
| 96845            | -13.563            | -1.546            | 3.315E-02  | 11.32           |

resultant displacement      1.39 in      *referenced to undeformed shape*

**conclusion:** the minor "corrections" to the model result in almost no change to the results, which is a welcome result.