

Atom Interferometers

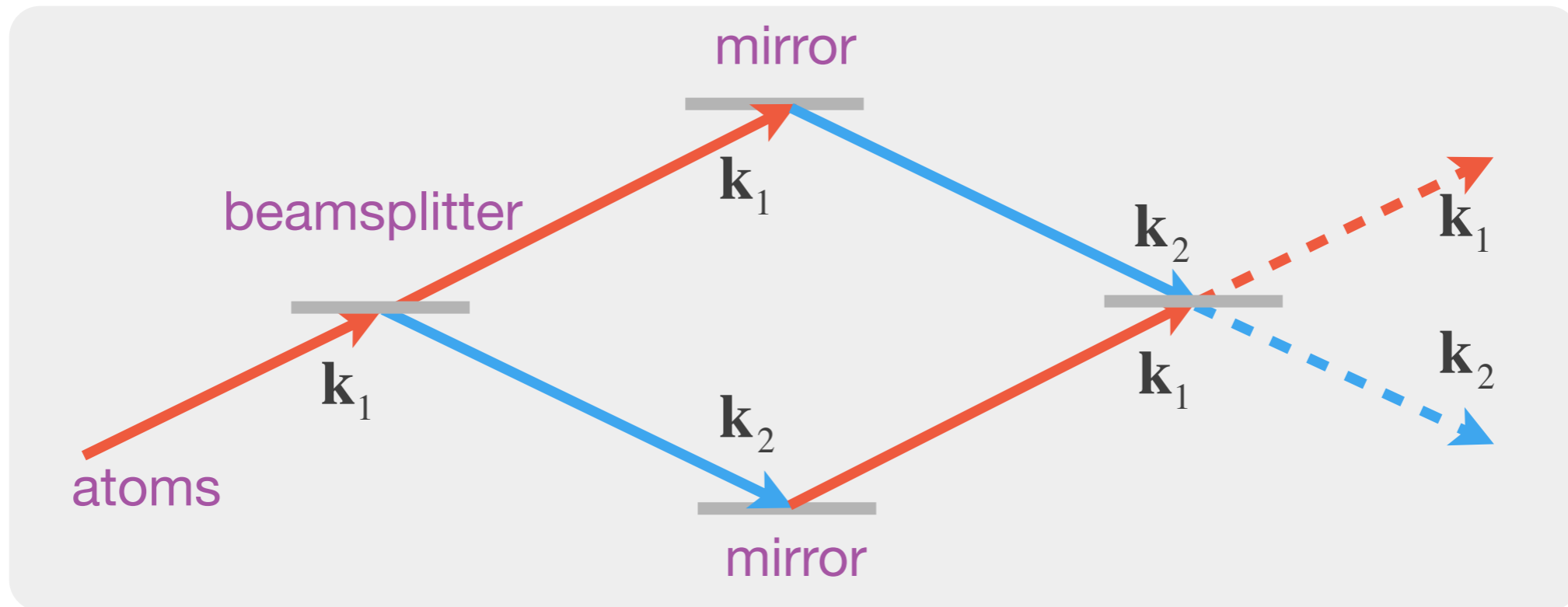
Yanbei Chen

California Institute of Technology

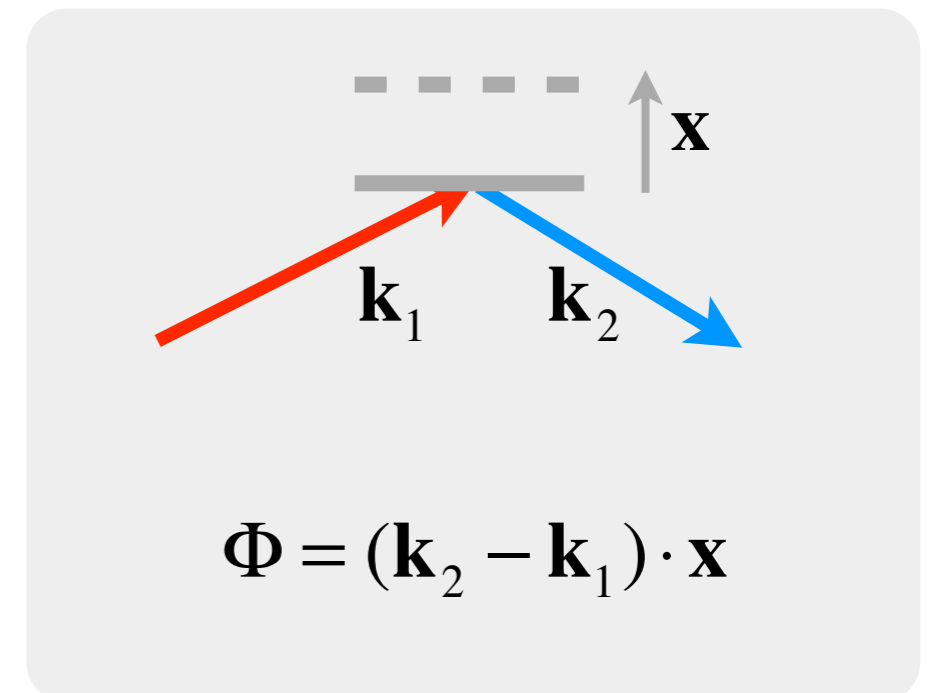
Why Atom Interferometers?

- Not because atoms have short de Broglie wavelength.
- But because atom clouds could be used as test masses for low frequency detection.
- Some recent proposals
 - R. Chiao et al.
 - S. Dimopoulos, P.W. Graham, J.M. Hogan, M.A. Kasevich and S. Rajendran, *Phys. Rev. D* **78**, 122002, (2008).
- Paper on how atom interferometers respond to gravitational waves
 - A. Roura, D.R. Brill, B.L. Hu, C.W. Misner, and W.D. Phillips, *Phys. Rev. D* **73**, 084018 (2006)

How does an atom interferometer work?

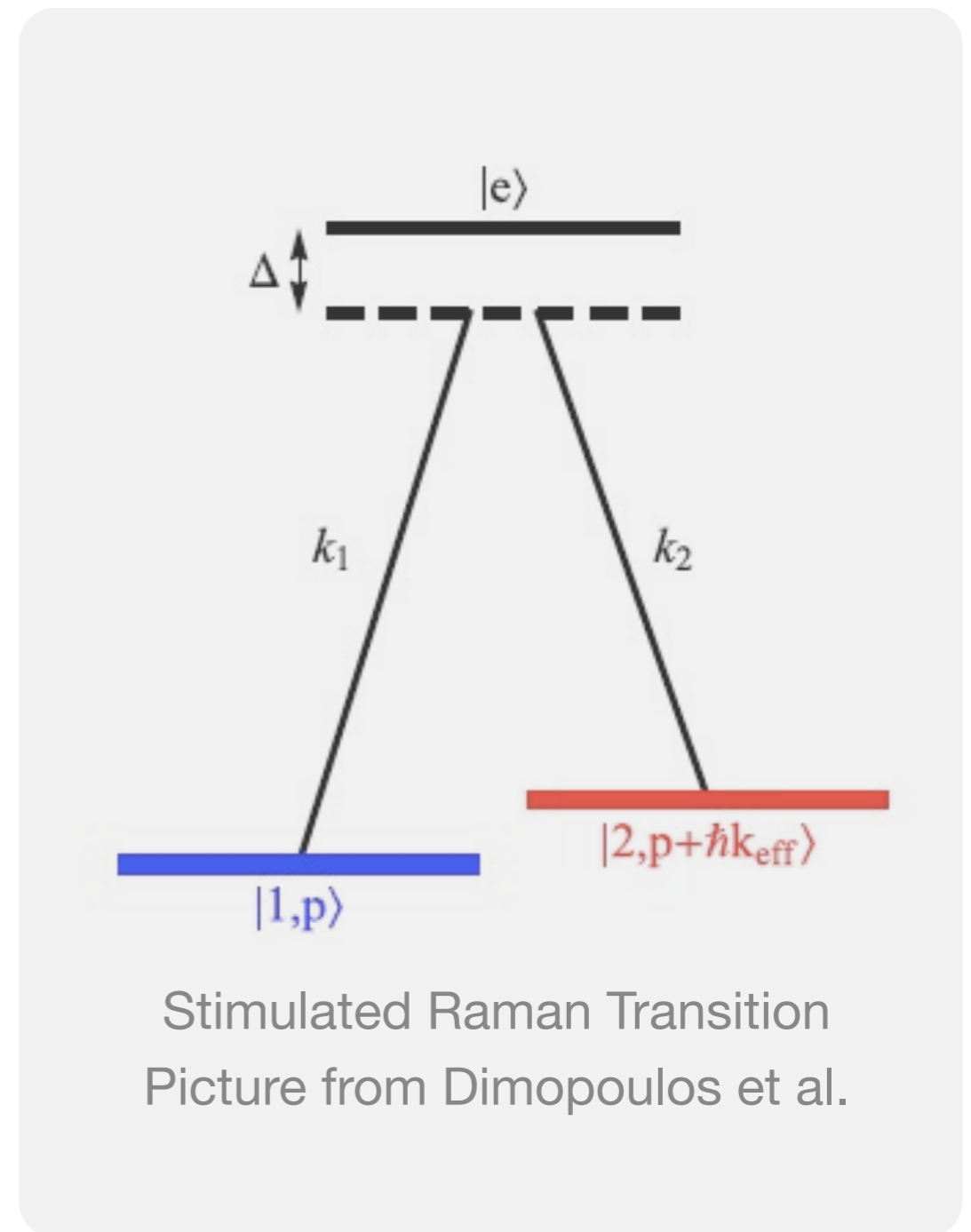
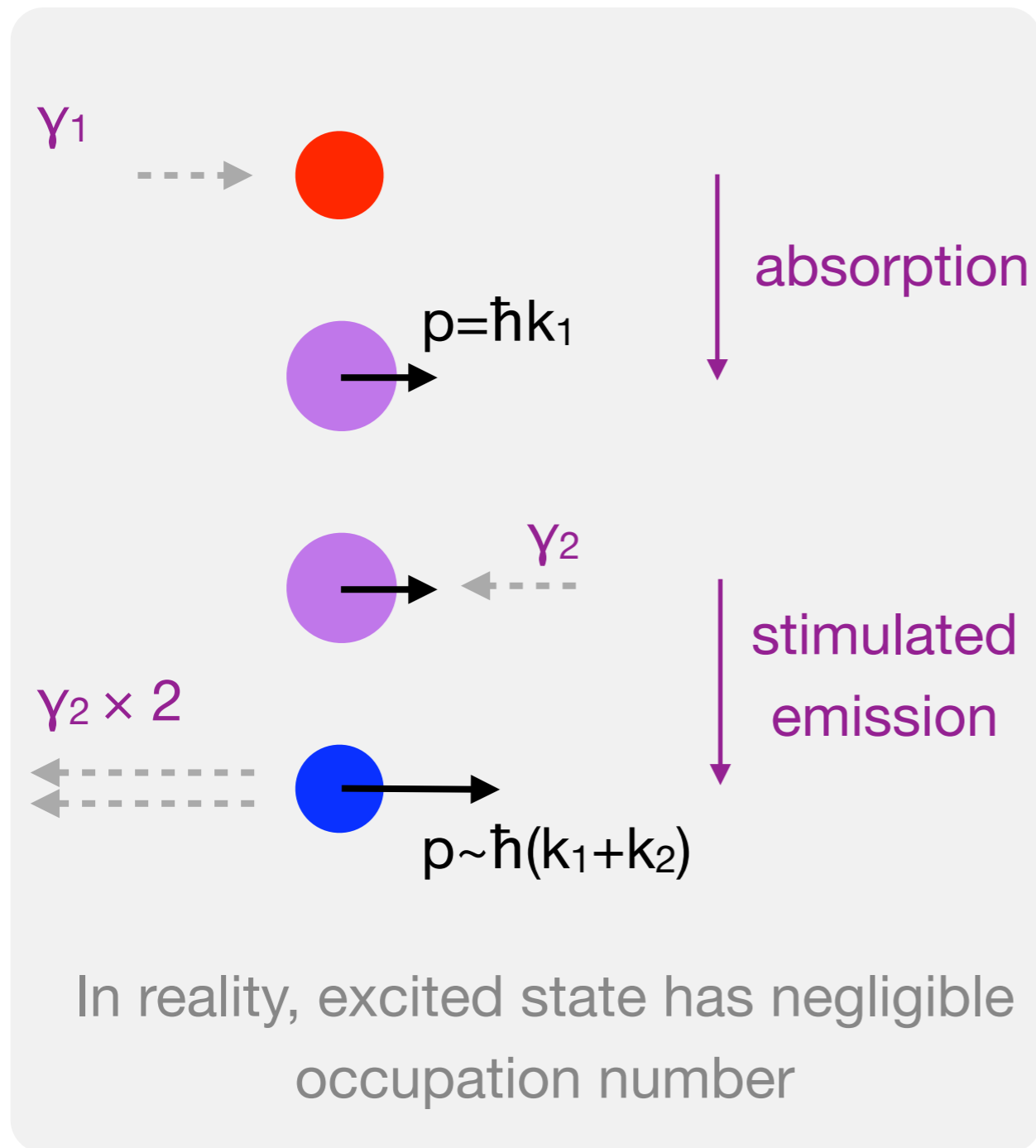


- Similar to optical interferometer
- Phaseshift depends on momentum transfer at mirror
- De Broglie wavelength $\lambda = h/(mv)$ could be small, de Broglie $k = mv/\hbar$ could be high, but it is δk that matters
- How do atom mirrors transfer momentum?



How does an atom mirror work?

- Atoms are deflected by photons, for example **Stimulated Raman Transition**

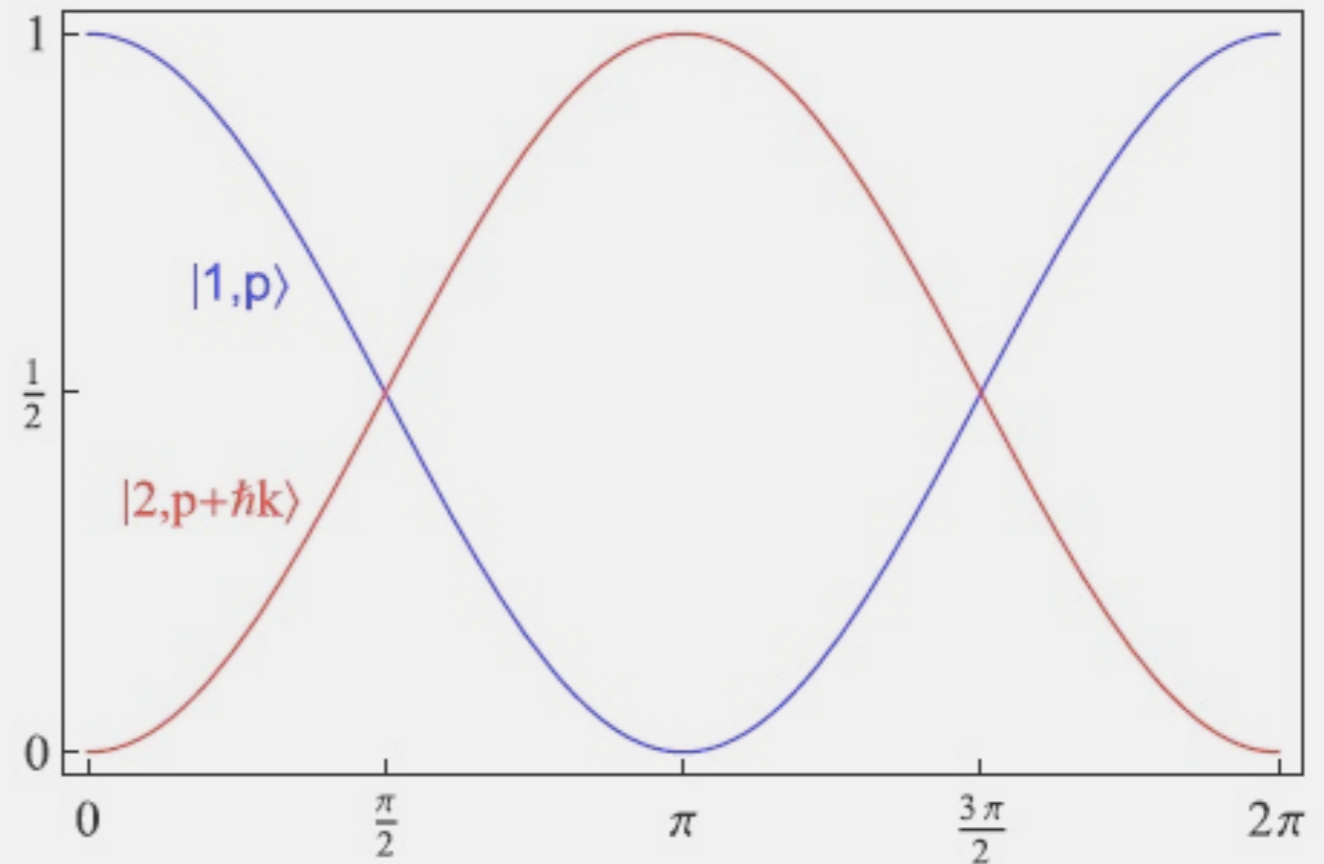


Mirror vs Beamsplitter: Phase of Rabi Oscillation



Rabi oscillation

continuous pumping
with two opposite beams:
atom sloshes between
state 1 and **state 2**



(b)

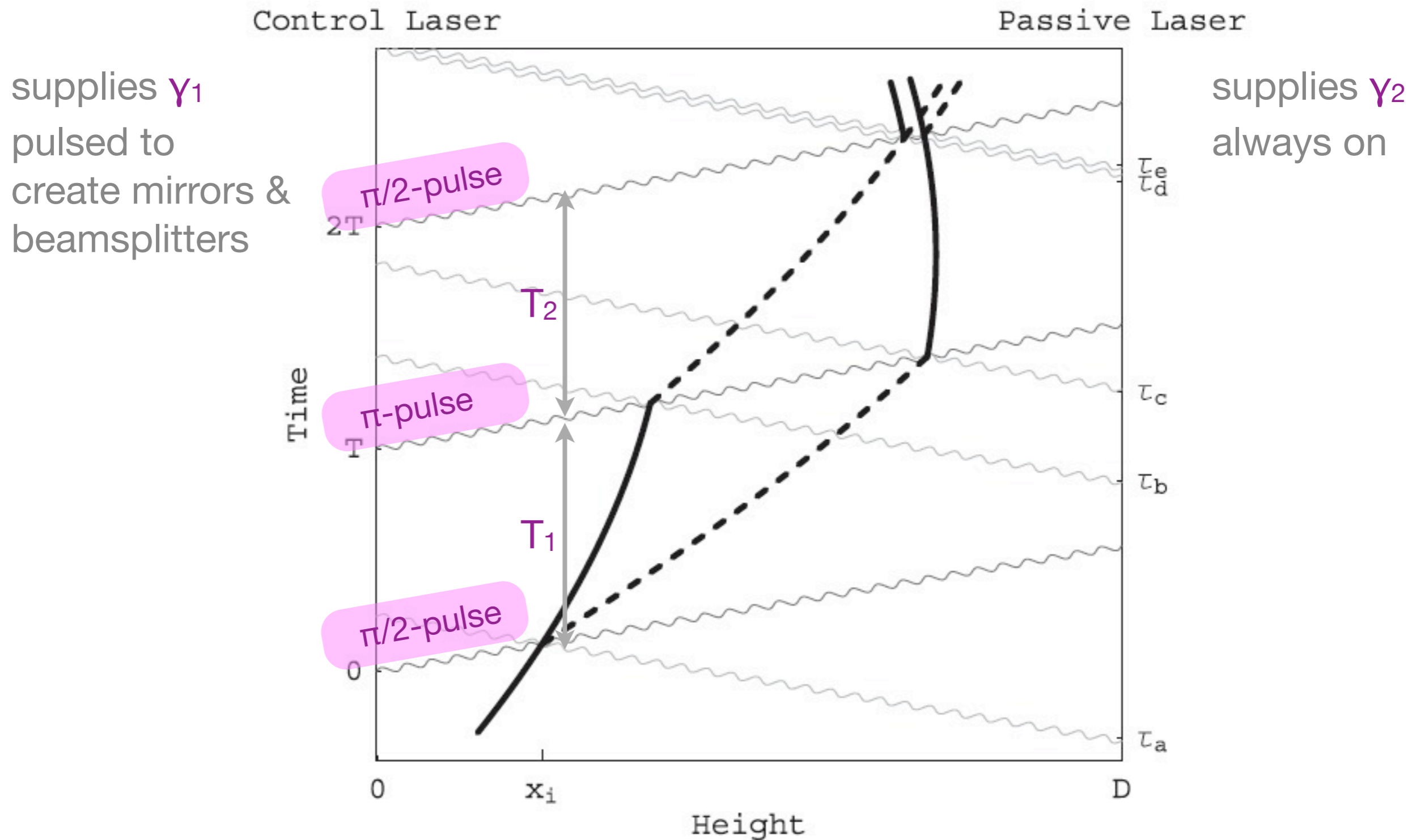
t [$\Omega_{\text{Rabi}}^{-1}$]

Rabi Oscillation

Picture from Dimopoulos et al.

- Depending on phase of the Rabi oscillation, one can make a mirror (π -pulse) or beamsplitter ($\pi/2$ -pulse)

An Atom Interferometer



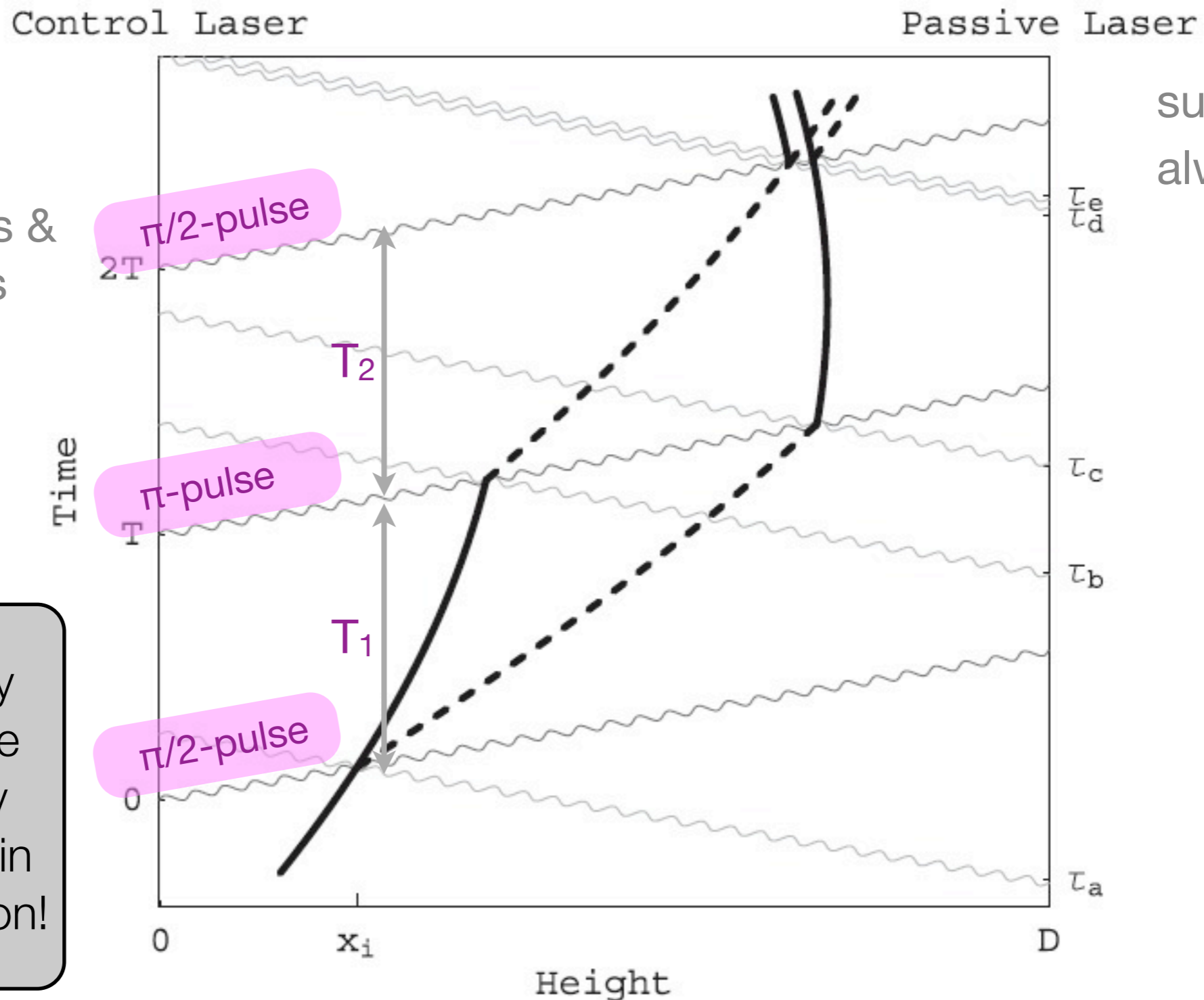
Space-time diagram of a “linear” atom interferometer

Picture from Dimopoulos et al.

An Atom Interferometer

supplies γ_1
pulsed to
create mirrors &
beamsplitters

But δk is only
 $2k_\gamma$, and there
won't be any
improvement in
length resolution!

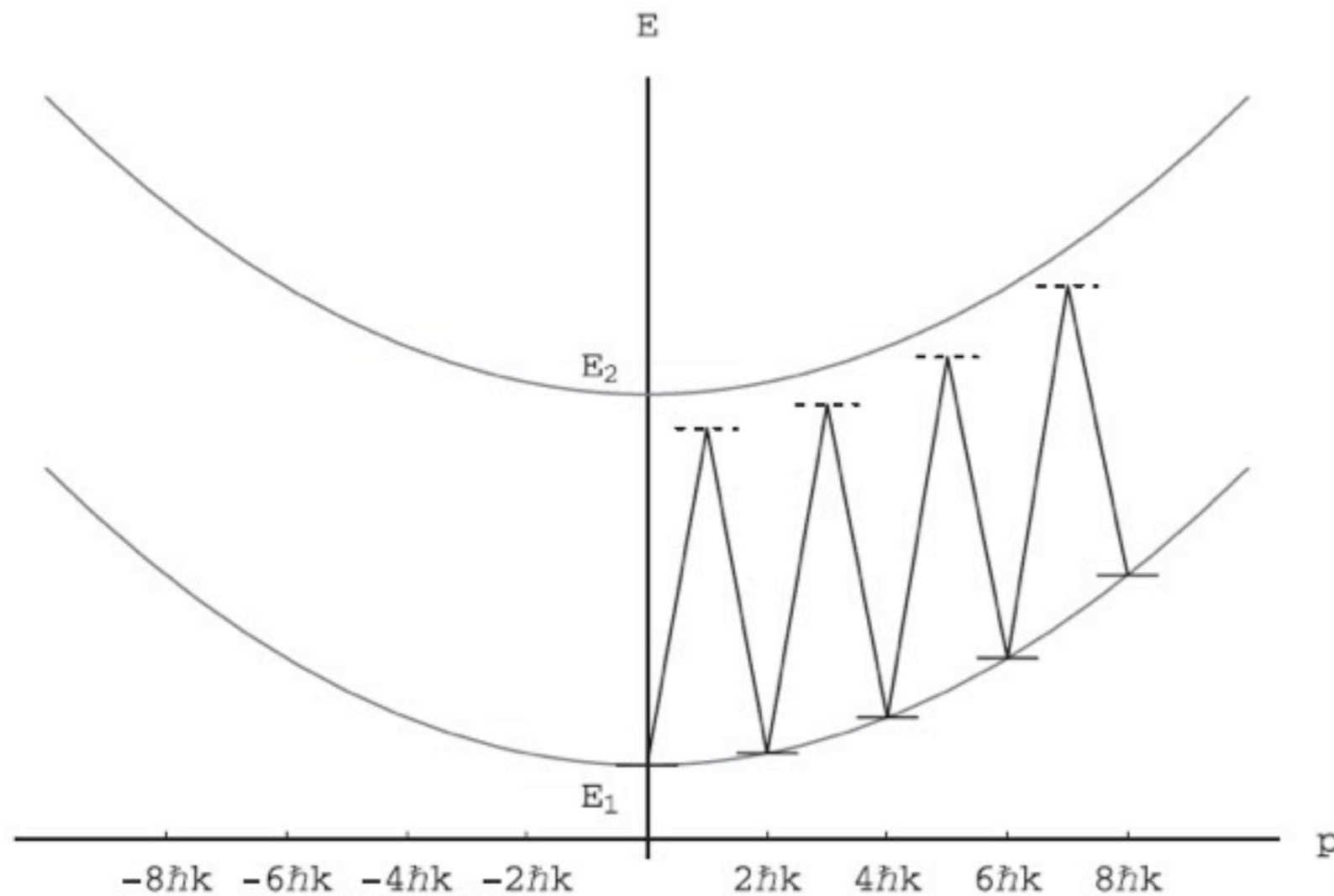


Space-time diagram of a “linear” atom interferometer

Picture from Dimopoulos et al.

Large Momentum Transfer & Atom Squeezing

- It is possible to transfer more momenta, if the transition is Bragg, not Raman



Picture from Dimopoulos et al.

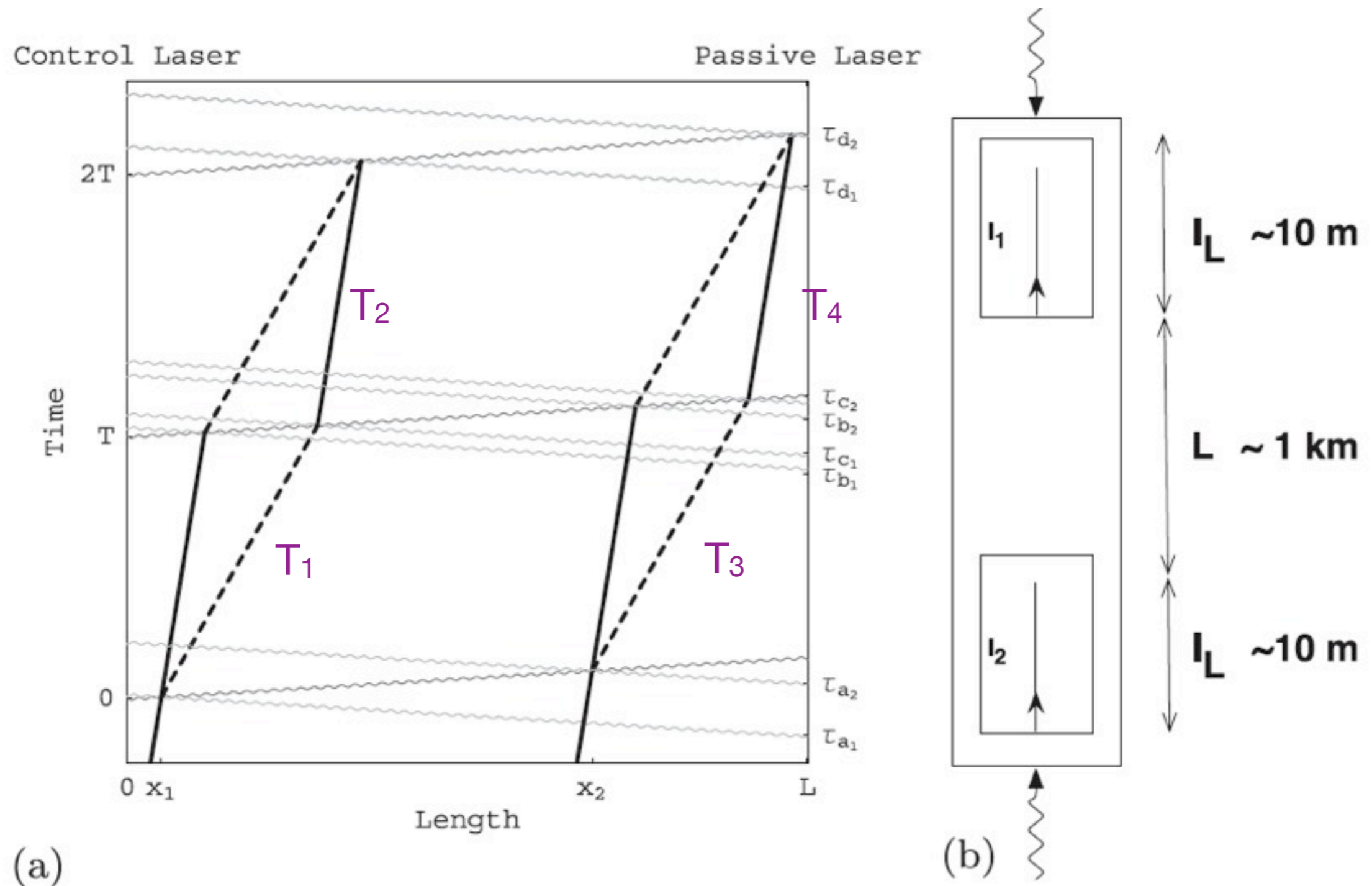
Pulses can be iterated to give N times the momentum
 $N \sim 100 - 1000$ might be realizable

- Roughly equivalent to the use of a cavity with Finesse equal to N , which is not very high.

Why are we still interested in Atom Interferometry?

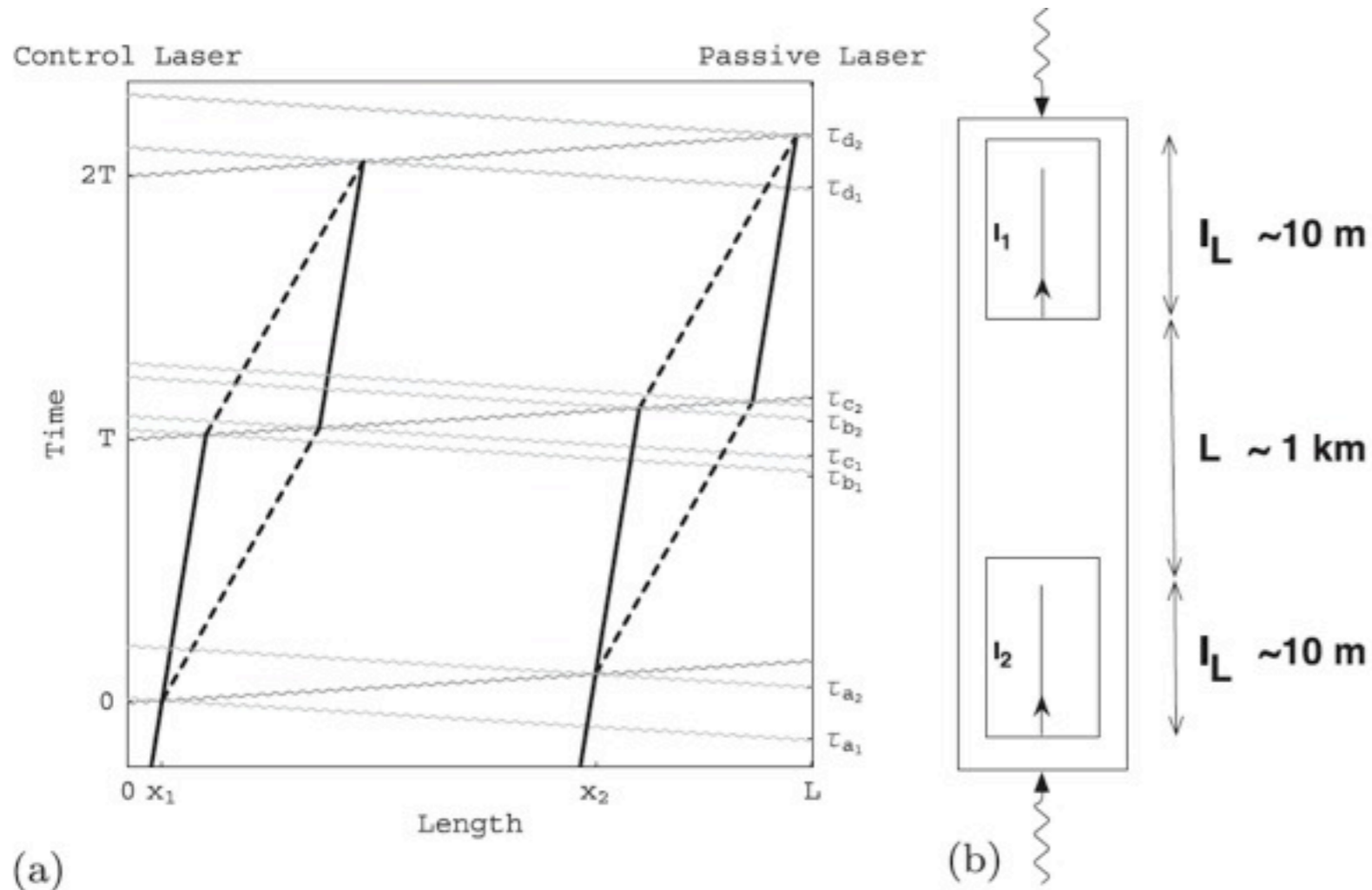
- Atoms might be usable as test masses for low-frequency detectors
 - they do not need to be suspended
 - they do not couple to vibration during flight
- Recent proposal
 - S. Dimopoulos, P.W. Graham, J.M. Hogan, M.A. Kasevich and S. Rajendran, Phys. Rev. D **78**, 122002, (2008).
 - Two versions: terrestrial & space-based

Dimopoulos et al.'s Detector



- Two co-linear atom interferometers sharing the same control and passive light
- Measures delays of laser pulses due to gravitational wave: $(T_4 - T_3) - (T_2 - T_1)$

Ground-based version



$l_L \sim 10 \text{ m}$ because atoms drop during the $2T$ interrogation time

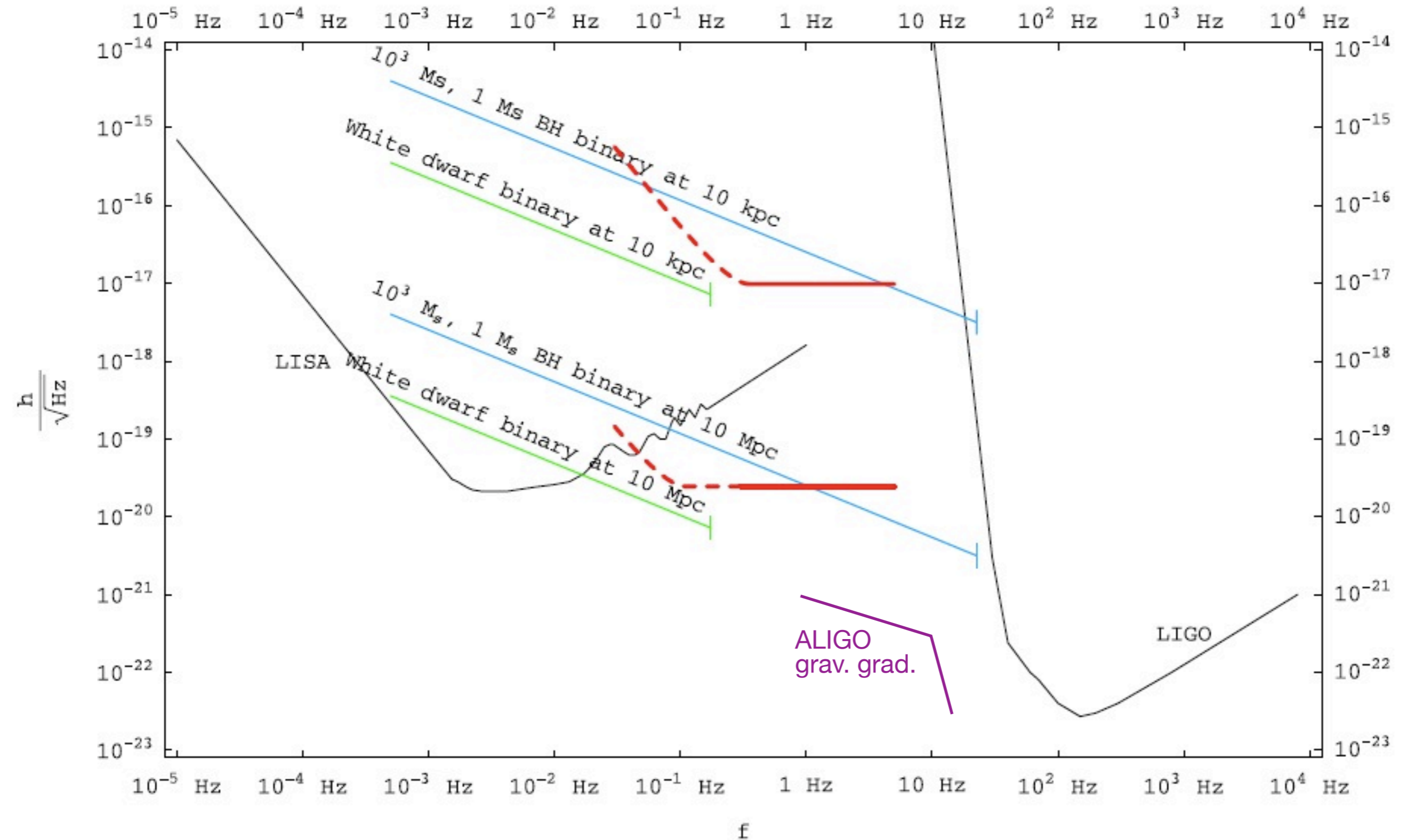
Advanced version $L = 4 \text{ km}$

vacuum 10^{-10} Torr, average collision time 200s

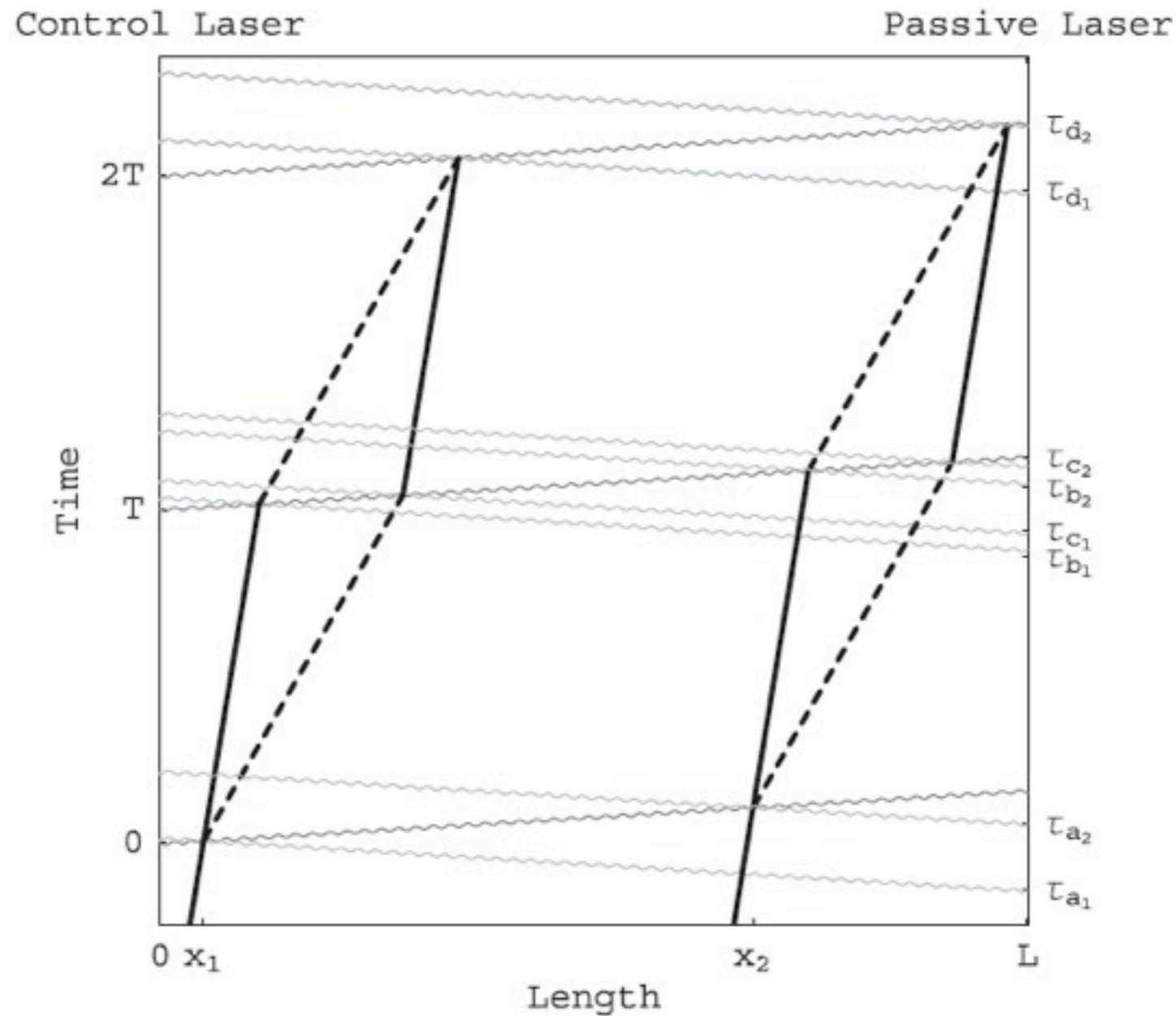
1 W laser waist size 10 cm

- $T \sim 1 \text{ s}$, $k_{\text{eff}} \sim 1.6 \times 10^9$ (with $N \sim 1000$), $n \sim 10^8$, 5 clouds simultaneously, $h \sim 10^{-17} / \text{rtHz}$ at 1 Hz (advanced version is 10x better)

Sensitivity of Ground-Based Version

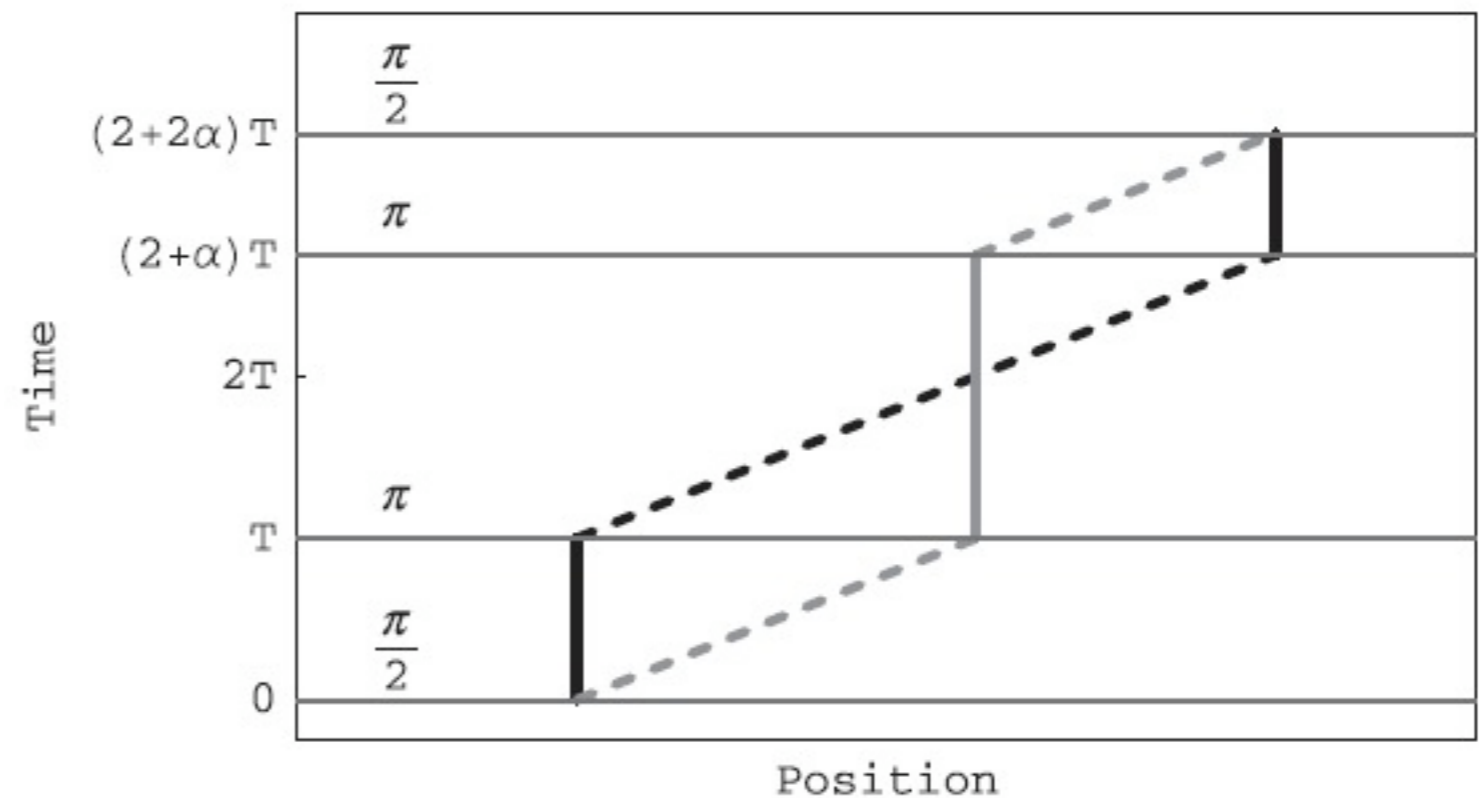
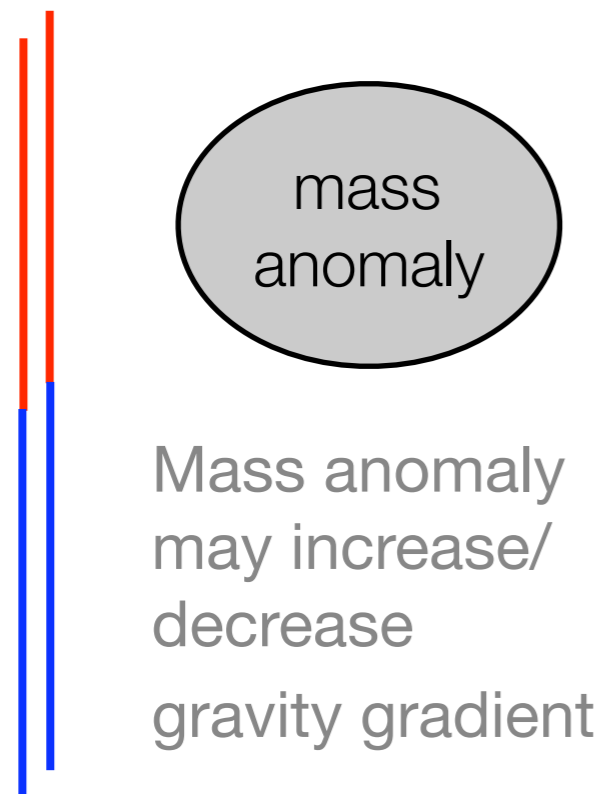


Noises: vibration & laser phase noise



- Phase noise in control pulse unimportant (except for quantum part which seems small anyway)
- Vibration & Phase noise: phase noise of passive laser are subtracted between times of L/c (short). Requires $\delta x \sim 10^{-15}m$ (for 4 km version) or $10^{-14}m$ (for 1 km version)

Noises: Gravity Gradient



Double loop configuration, cancels g gradient

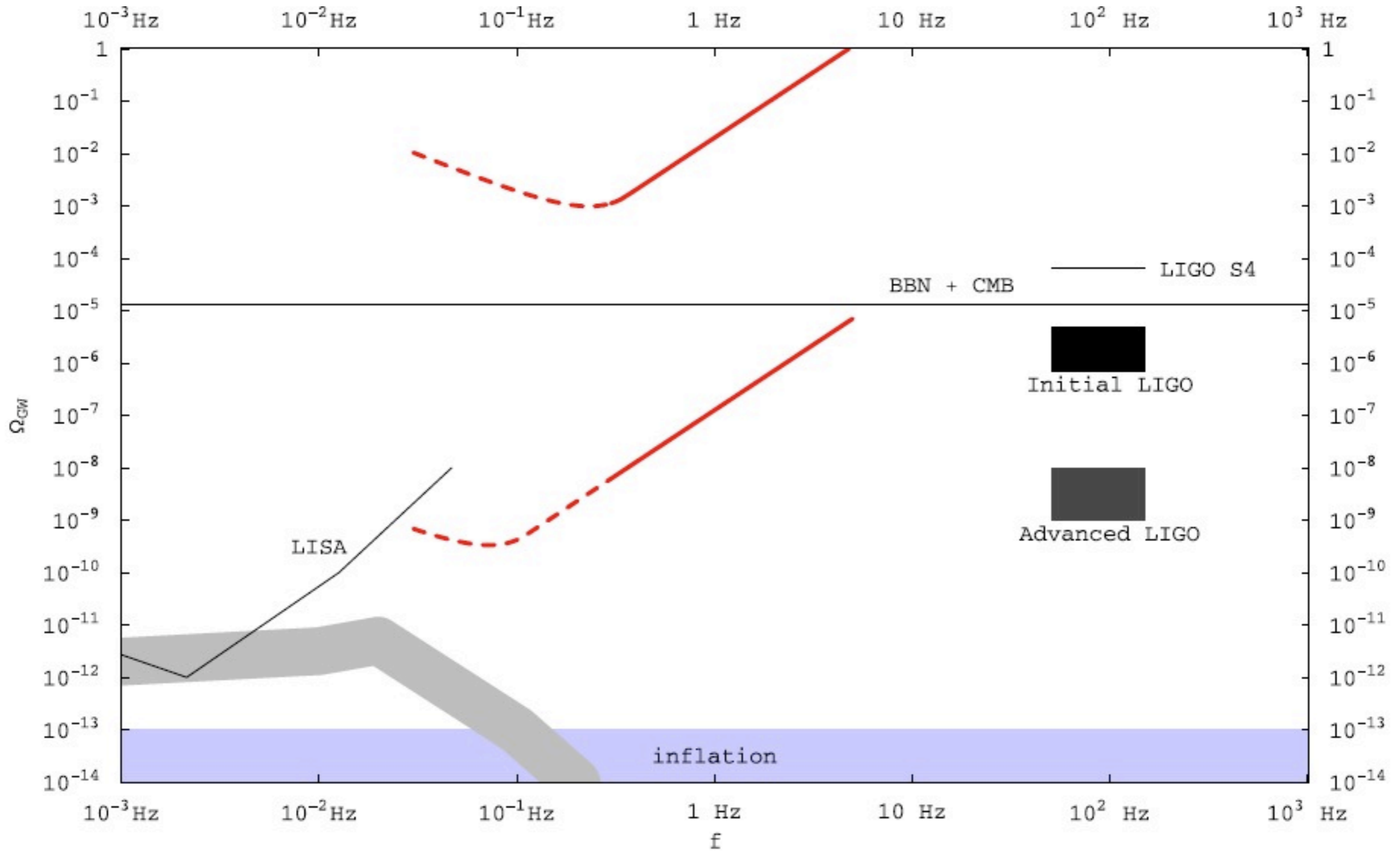
Different paths
sense different g

- **Gravity Gradient:** mostly due to gradient of g --- fluctuations in atoms' path cause difference in g . This sets requirement on the path of atoms, and therefore on the atom trap.
- Tricks can be used to avoid measuring them
 - Add compensation mass
 - Using fancy pulses
- Temporal fluctuations in gravity gradient seems unimportant.

Rotation

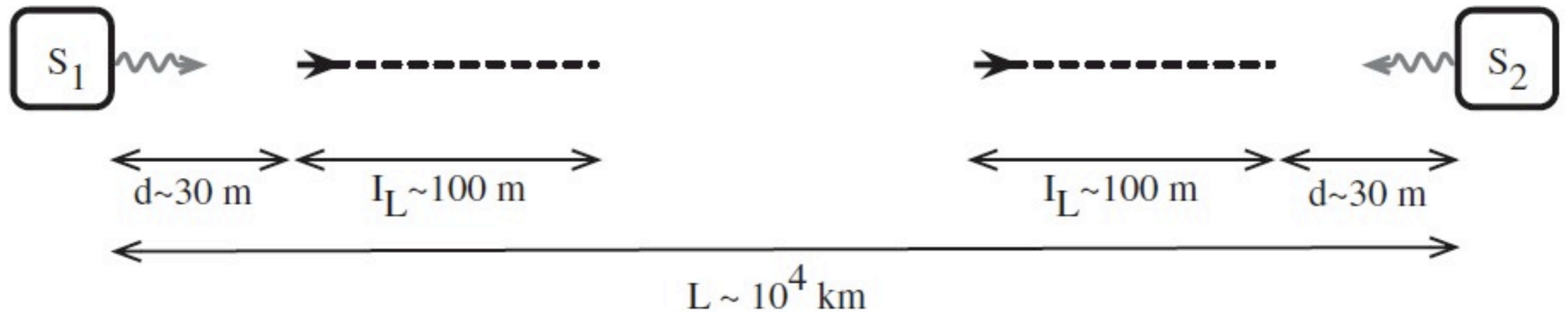
- Coriolis force cause acceleration larger than GW $\delta a = 2\omega_e \delta v$ with $\delta v \sim 10^{-8} \text{m/s}$
 - Can be cancelled if laser axis is not rotating together with earth. Requires accuracy of $\delta\omega < 10^{-9} (\text{rad/s/rHz}) \times (1 \text{ km/L})^{1/2}$
- Laser jittering will cause the atoms to sense different \mathbf{g} , and this requires laser beam to have $\delta\omega < 10^{-9} (\text{rad/s/rHz})$ (for 1 km version)

Sensitivity to Stochastic Background



Ground-based versions

Space-Based Version



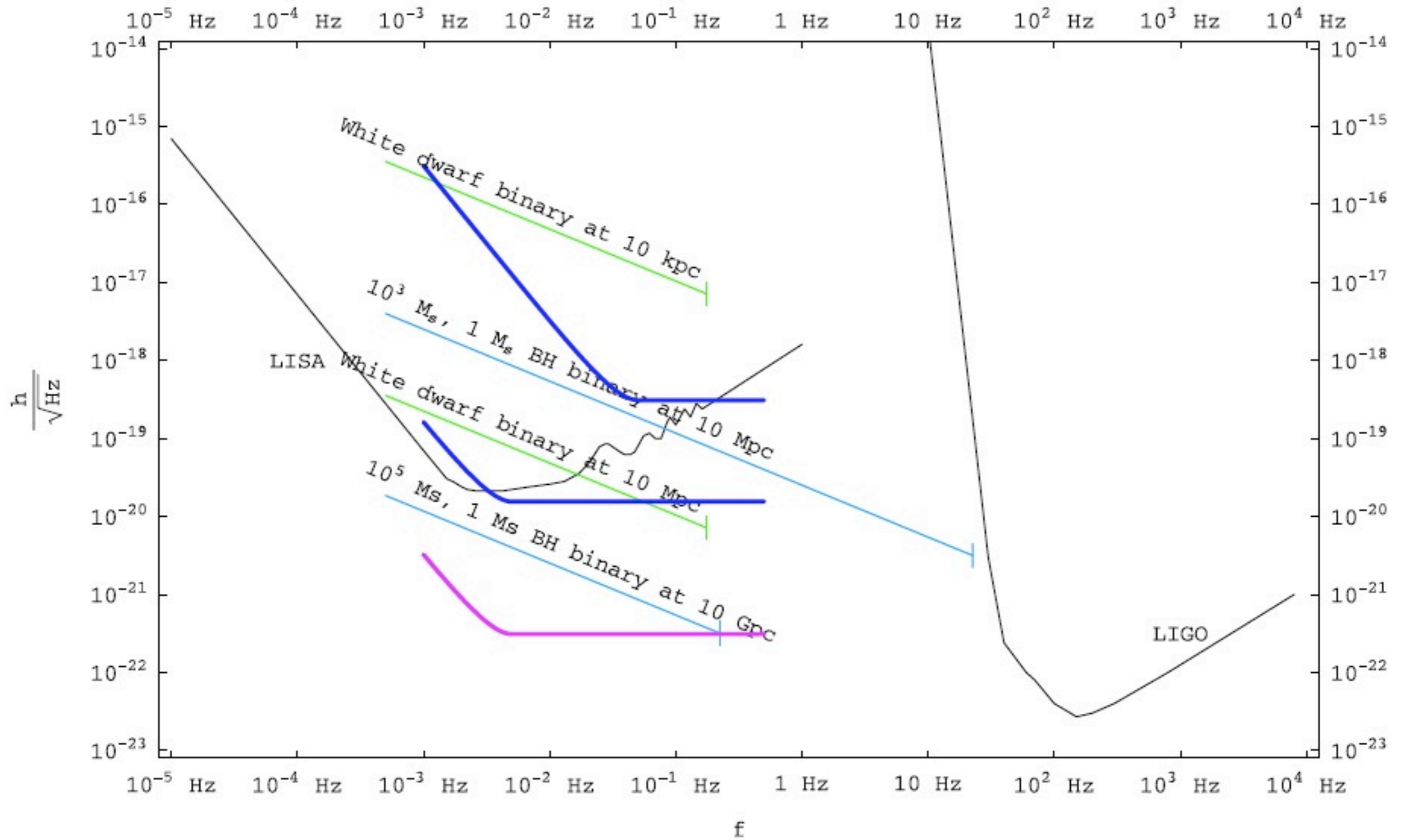
$T \sim 100$ s, aiming at waves below 0.01 Hz
 $d \sim 30$ m to minimize gravity gradient caused by spacecraft
 $l_L \sim 100$ m is the maximum that spacecraft can provide bias B field. For $T \sim 100$ s, this limits k_{eff} to $\sim 10^9$. [$v = \hbar k/m$]
 For 10^3 km version, Laser 1 W waistsize 0.5m

Must be shielded from sunlight, otherwise will only work when it's behind the earth, when photon-atom scattering timescale is longer than T

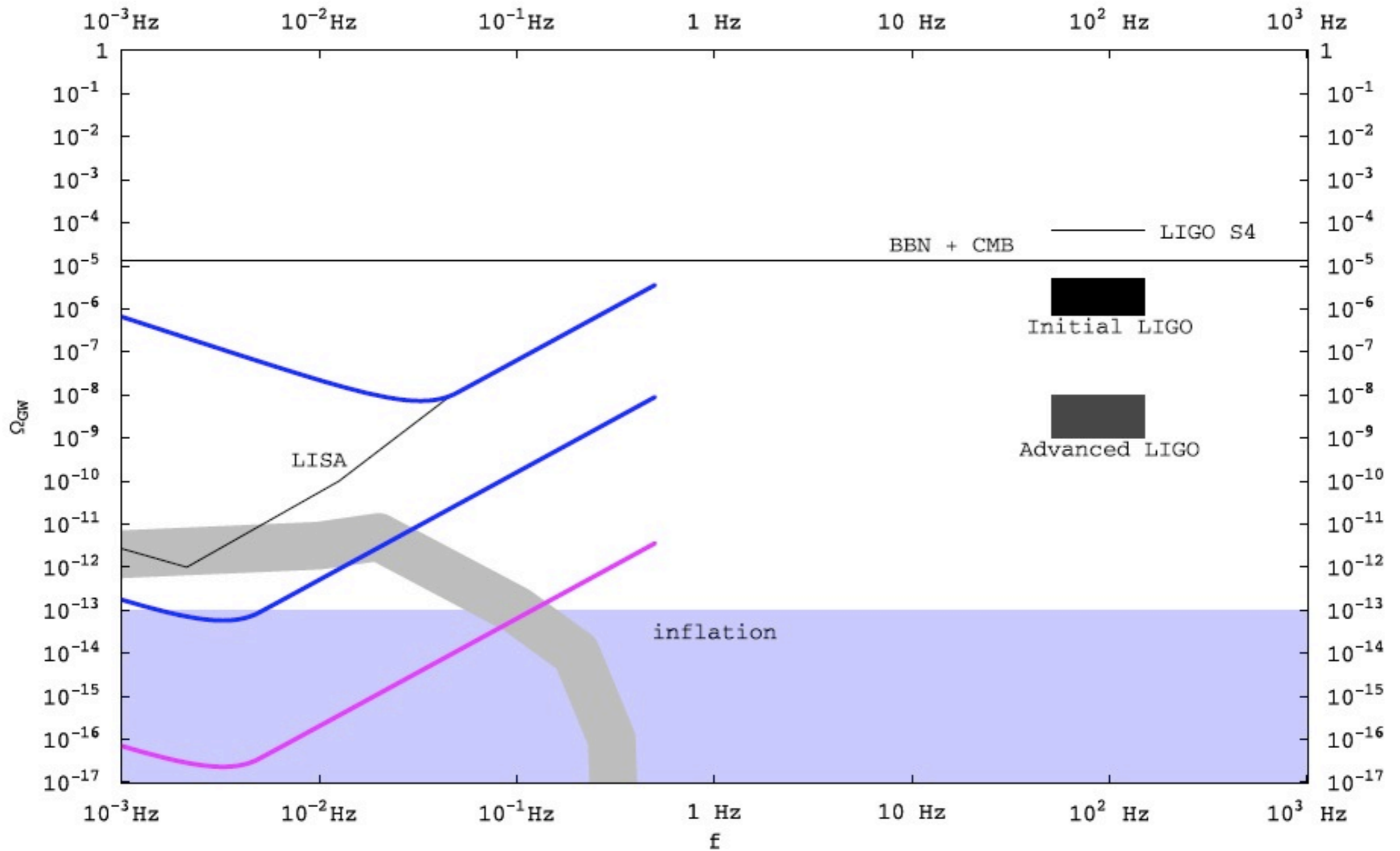
Effect from solar wind considered unimportant

Interplanetary magnetic field can be dealt with

Sensitivity of Space-Based Detector



Sensitivity to Stochastic Background



Space Versions

Comparison with LISA requirements

TABLE II. A comparison between specifications for a three-satellite AGIS configuration that could potentially allow comparable sensitivity to LISA, and the LISA requirements. There are many caveats and details that cannot be captured in a table and are discussed in Secs. V B and V C and in the LISA papers (see e.g. [42,47]).

Attribute	AGIS	LISA
Baseline	10^3 km	5×10^6 km
Satellite control (at $\sim 10^{-2}$ Hz)	$10^4 \frac{\text{nm}}{\sqrt{\text{Hz}}}$	$1 \frac{\text{nm}}{\sqrt{\text{Hz}}}$
Laser frequency control (at $\sim 10^{-2}$ Hz)	$10^4 \frac{\text{Hz}}{\sqrt{\text{Hz}}}$	$1 \frac{\text{Hz}}{\sqrt{\text{Hz}}}$
Rotational control (at $\sim 10^{-2}$ Hz)	$10^{-2} \frac{\text{nrad}}{\sqrt{\text{Hz}}}$	$1 \frac{\text{nrad}}{\sqrt{\text{Hz}}}$
Electromagnetic forces	Atoms neutral, EM forces naturally small, predictable response to measured EM field	Cosmic ray charging of proof mass
Collisions with background gas	Delete atoms, not a noise source	Cause acceleration noise

Photon shot noise does not seem to have been taken into account

Limited by photon shot noise

Discussions?

